

## Electronic Supplementary Information

### Phonon vortices at heavy impurities in two-dimensional materials

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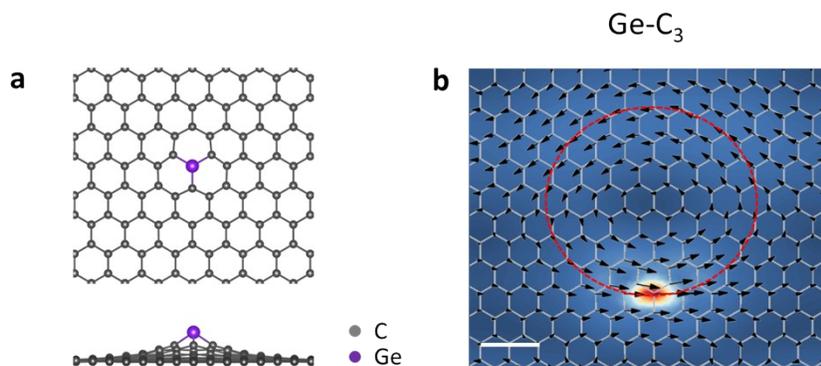


Figure S1. Phonon vortex in  $\text{Ge-C}_3$  -- one C atom is replaced by one Ge atom, *i.e.*, an impurity atom that is larger and heavier than Si. Calculations were performed in a  $12 \times 12$  supercell as in Figure 1d for  $\text{Si-C}_3$  because of the computational cost, but the presence of a vortex is clear.

a) In-plane and side view schematics of the  $\text{Ge-C}_3$  defect showing that the Ge atom buckles by  $2.2 \text{ \AA}$  off the graphene plane, compared with the  $1.8\text{-\AA}$  buckling by Si in  $\text{Si-C}_3$ . b) Atomic displacements around a  $\text{Ge-C}_3$  defect at  $\hbar\omega = 26 \text{ meV}$  showing clearly that Ge generates a larger vortex than Si, as illustrated by the red circle that goes through the Ge site which is much larger than the corresponding red circle of the  $\text{Si-C}_3$ -defect vortex in Fig. 1d. Another notable feature is that the atomic displacements of C atoms forming circles that are concentric with the red circle are pointing in the same direction, in contrast to the  $\text{Si-C}_3$  defect, where the atomic displacements in the two red circles shown in Fig. 1 are in opposite directions. This feature is most likely related to the fact that the wavelength of the pristine-graphene mode that is in resonance with the  $\text{Ge-C}_3$  vortex mode is much longer than in the case of the  $\text{Si-C}_3$  vortex mode. Much larger computational supercells, perhaps even larger than  $24 \times 24$  would be needed to explore these issues further with sufficient accuracy. Scale bar:  $0.5 \text{ nm}$ .