Table S 1 . The NEC of the ground state $\mathrm{B}_{\mathrm{n}} \mathrm{Rb}_{2}(\mathrm{n}=1-12)$ clusters

| Clusters | NEC |  |  |
| :---: | :---: | :---: | :---: |
|  | Rb-1 | $\mathrm{Rb}-2$ | B |
| $\mathrm{B}_{1} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.38} 4 \mathrm{~d}^{0.045} 5 \mathrm{p}^{0.13}$ | $5 \mathrm{~S}^{0.38} 4 \mathrm{~d}^{0.04} 5 \mathrm{p}^{0.13}$ | $2 \mathrm{~S}^{1.90} 2 \mathrm{p}^{2.02}$ |
| $\mathrm{B}_{2} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.06} 4 \mathrm{~d}^{0.04} 5 \mathrm{p}^{0.06}$ | $5 \mathrm{~S}^{0.06} 4 \mathrm{~d}^{0.04} 5 \mathrm{p}^{0.06}$ | $2 \mathrm{~S}^{1.42} 2 \mathrm{p}^{2.42} 3 \mathrm{p}^{0.02}$ |
| $\mathrm{B}_{3} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.11} 4 \mathrm{~d}^{0.025} \mathrm{p}^{0.04}$ | $5 \mathrm{~S}^{0.11} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.04}$ | $2 \mathrm{~S}^{1.11-1.25} 2 \mathrm{p}^{2.30-2.40} 3 \mathrm{~S}^{0.01} 3 \mathrm{p}^{0.01} 3 \mathrm{~d}^{0.01-0.02}$ |
| $\mathrm{B}_{4} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.07} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.02}$ | $5 \mathrm{~S}^{0.07} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.02}$ | $2 \mathrm{~S}^{0.96-1.08} 2 \mathrm{p}^{2.15-2.66} 3 \mathrm{~S}^{0.01} 3 \mathrm{p}^{0.01-0.02} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{5} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.06} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.03}$ | $5 \mathrm{~S}^{0.04} 4 \mathrm{~d}^{0.03} 5 \mathrm{p}^{0.04} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.81-1.20} 2 \mathrm{p}^{1.96-2.77} 3 \mathrm{~S}^{0.01} 3 \mathrm{p}^{0.01-0.02} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{6} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.02} 4 \mathrm{~d}^{0.01} 5 \mathrm{p}^{0.04}$ | $5 \mathrm{~S}^{0.02} 4 \mathrm{~d}^{0.01} 5 \mathrm{p}^{0.04}$ | $2 \mathrm{~S}^{0.86-0.95} 2 \mathrm{p}^{2.38-2.41} 3 \mathrm{p}^{0.01} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{7} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.01} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.03} 5 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.01} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.04} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.51-0.86} 2 \mathrm{p}^{2.28-2.90} 3 \mathrm{p}^{0.01-0.06} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{8} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.01} 5 \mathrm{p}^{0.03} 5 \mathrm{~d}^{0.01} 6 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.01} 5 \mathrm{p}^{0.03} 5 \mathrm{~d}^{0.01} 6 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.49-0.83} 2 \mathrm{p}^{2.35-2.43} 3 \mathrm{p}^{0.01-0.08} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{9} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.01} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.025} \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.01} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.025} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.53-0.86} 2 \mathrm{p}^{2.18-2.59} 3 \mathrm{~S}^{0.01} 3 \mathrm{p}^{0.01-0.05} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{10} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.02} 4 \mathrm{~d}^{0.04} 5 \mathrm{p}^{0.03} 5 \mathrm{~d}^{0.01} 6 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.01} 5 \mathrm{p}^{0.02} 5 \mathrm{~d}^{0.02}$ | $2 \mathrm{~S}^{0.51-0.86} 2 \mathrm{p}^{2.14-2.72} 3 \mathrm{p}^{0.01-0.02} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{11} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.01} 4 \mathrm{~d}^{0.03} 5 \mathrm{p}^{0.025} 5 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.01} 4 \mathrm{~d}^{0.03} 5 \mathrm{p}^{0.025} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.51-0.84} 2 \mathrm{p}^{2.24-2.58} 3 \mathrm{p}^{0.01-0.03} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{12} \mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.02} 4 \mathrm{~d}^{0.03} 5 \mathrm{p}^{0.03} 6 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.01} 5 \mathrm{p}^{0.02} 5 \mathrm{~d}^{0.02} 6 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.50-0.85} 2 \mathrm{p}^{2.23-2.67} 3 \mathrm{p}^{0.01-0.02} 3 \mathrm{~d}^{0.01}$ |

Table S2. The NEC of the ground state $\mathrm{B}_{\mathrm{n}}-\mathrm{Rb}_{2}(\mathrm{n}=1-12)$ clusters

| Clusters | NEC |  |  |
| :---: | :---: | :---: | :---: |
|  | Rb-1 | Rb-2 | B |
| $\mathrm{B}_{1}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.77} 4 \mathrm{~d}^{0.01} 5 \mathrm{p}^{0.18}$ | $5 \mathrm{~S}^{0.77} 4 \mathrm{~d}^{0.01} 5 \mathrm{p}^{0.18}$ | $2 \mathrm{~S}^{1.93} 2 \mathrm{p}^{2.18}$ |
| $\mathrm{B}_{2}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.64} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.11} 5 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.64} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.11} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{1.44} 2 \mathrm{p}^{2.28} 3 \mathrm{p}^{0.02}$ |
| $\mathrm{B}_{3}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.18} 5 \mathrm{p}^{0.16} 5 \mathrm{~d}^{0.03} 6 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.185} 5 \mathrm{p}^{0.16} 5 \mathrm{~d}^{0.03} 6 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{1.02-1.25} 2 \mathrm{p}^{2.54-2.59} 3 \mathrm{p}^{0.01} 3 \mathrm{~d}^{0.02} 4 \mathrm{p}^{0.01}$ |
| $\mathrm{B}_{4}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.40} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.16} 6 \mathrm{~S}^{0.01}$ | $5 \mathrm{~S}^{0.40} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.16} 6 \mathrm{~S}^{0.01}$ | $2 \mathrm{~S}^{0.95-1.08} 2 \mathrm{p}^{2.19-2.64} 3 \mathrm{~S}^{0.01} 3 \mathrm{p}^{0.01-0.02} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{5}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.45} 4 \mathrm{~d}^{0.05} 5 \mathrm{p}^{0.23}$ | $5 S^{0.22} 4 \mathrm{~d}^{0.05} 5 \mathrm{p}^{0.18} 5 \mathrm{p}^{0.01}$ | $2 \mathrm{~S}^{0.84-0.95} 2 \mathrm{p}^{2.27-2.78} 3 \mathrm{~S}^{0.01} 3 \mathrm{p}^{0.01-0.02} 3 \mathrm{~d}^{0.01} 4 \mathrm{p}^{0.01}$ |
| $\mathrm{B}_{6}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.11} 4 \mathrm{~d}^{0.05} 5 \mathrm{p}^{0.02} 5 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.60} 4 \mathrm{~d}^{0.03} 5 \mathrm{p}^{0.23} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.77-0.93} 2 \mathrm{p}^{2.24-2.53} 3 \mathrm{~S}^{0.01} 3 \mathrm{p}^{0.01} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{7}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.01} 5 \mathrm{p}^{0.06} 5 \mathrm{~d}^{0.01} 6 \mathrm{~d}^{0.03}$ | $5 \mathrm{~S}^{0.01} 5 \mathrm{p}^{0.06} 5 \mathrm{~d}^{0.01} 6 \mathrm{~d}^{0.03}$ | $2 \mathrm{~S}^{0.55-0.81} 2 \mathrm{p}^{2.56-2.79} 3 \mathrm{~d}^{0.01} 4 \mathrm{p}^{0.01-0.07}$ |
| $\mathrm{B}_{8}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.68} 4 \mathrm{~d}^{0.04} 5 \mathrm{p}^{0.30} 5 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.01} 4 \mathrm{~d}^{0.02} 5 \mathrm{p}^{0.04} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.55-0.83} 2 \mathrm{p}^{2.32-2.43} 3 \mathrm{p}^{0.01-0.08} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{9}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.03} 4 \mathrm{~d}^{0.03} 5 \mathrm{p}^{0.02} 6 \mathrm{p}^{0.01} 6 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.03} 4 \mathrm{~d}^{0.03} 5 \mathrm{p}^{0.02} 6 \mathrm{p}^{0.01} 6 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.58-1.06} 2 \mathrm{p}^{2.22-2.70} 3 \mathrm{~S}^{0.01} 3 \mathrm{p}^{0.01-0.04} 3 \mathrm{~d}^{0.01-0.02} 4 \mathrm{p}^{0.01}$ |
| $\mathrm{B}_{10}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.53} 4 \mathrm{~d}^{0.03} 5 \mathrm{p}^{0.21}$ | $5 \mathrm{~S}^{0.16} 4 \mathrm{~d}^{0.10} 5 \mathrm{p}^{0.15} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.54-0.85} 2 \mathrm{p}^{2.16-2.64} 3 \mathrm{p}^{0.01-0.02} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{11}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.02} 4 \mathrm{~d}^{0.05} 5 \mathrm{p}^{0.03} 5 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.02} 4 \mathrm{~d}^{0.05} 5 \mathrm{p}^{0.03} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.54-0.83} 2 \mathrm{p}^{2.35-2.59} 3 \mathrm{p}^{0.01-0.03} 3 \mathrm{~d}^{0.01}$ |
| $\mathrm{B}_{12}-\mathrm{Rb}_{2}$ | $5 \mathrm{~S}^{0.02} 4 \mathrm{~d}^{0.05} 5 \mathrm{p}^{0.04} 5 \mathrm{~d}^{0.01}$ | $5 \mathrm{~S}^{0.02} 4 \mathrm{~d}^{0.05} 5 \mathrm{p}^{0.04} 5 \mathrm{~d}^{0.01}$ | $2 \mathrm{~S}^{0.64-0.87} 2 \mathrm{p}^{2.23-2.52} 3 \mathrm{p}^{0.01-0.033} 3 \mathrm{~d}^{0.01}$ |

