

## Supplementary data

### Exploitation of Mixed-Valency Chemistry for Designing Monolayer with Double Ferroelectricity and Triferroic Couplings

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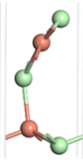
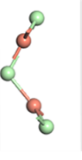
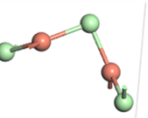
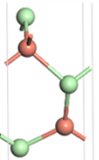
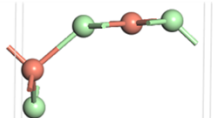
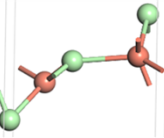
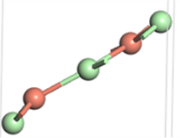
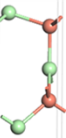
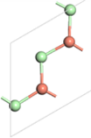
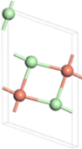
				
0	0.032	0.035	0.055	0.055
				
0.060	0.0624	0.082	0.092	0.269

Figure S1. A series of low-energy 2D  $\text{Cu}_2\text{Cl}_3$  structures obtained in the extensive structural search using the Calypso code, and their relative energies (in eV/f.u. compared with the ground state).

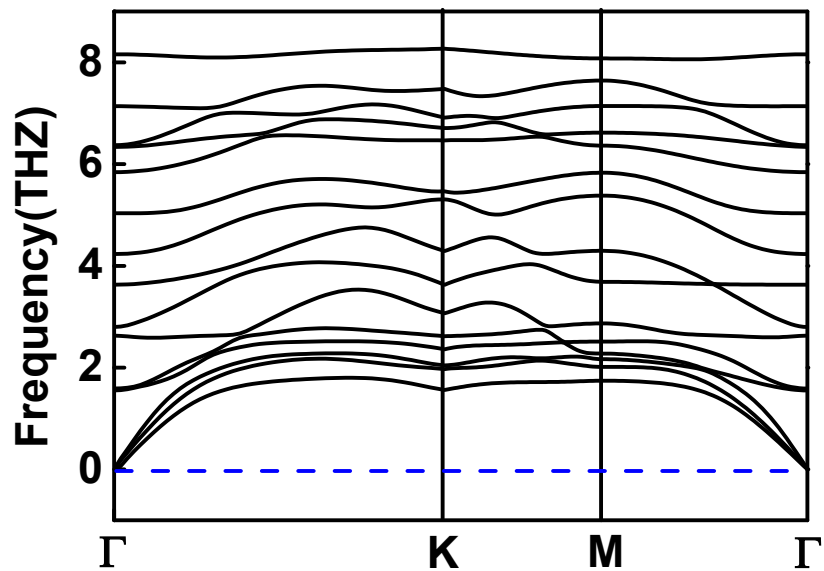


Figure S2. Phonon dispersion of  $\text{Cu}_2\text{Cl}_3$  monolayer.

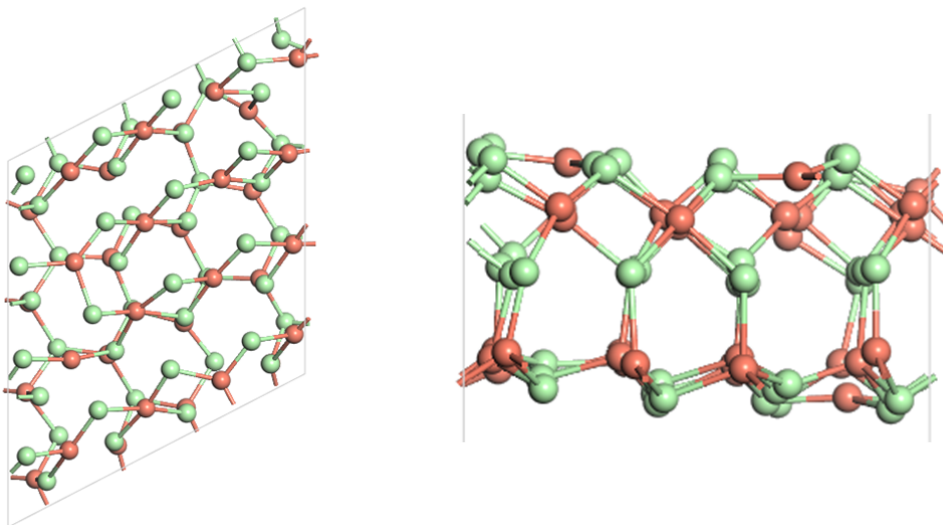


Figure S3. Snapshot of  $\text{Cu}_2\text{Cl}_3$  monolayer after AIMD simulation in the canonical ensemble at 373K for 15 ps.

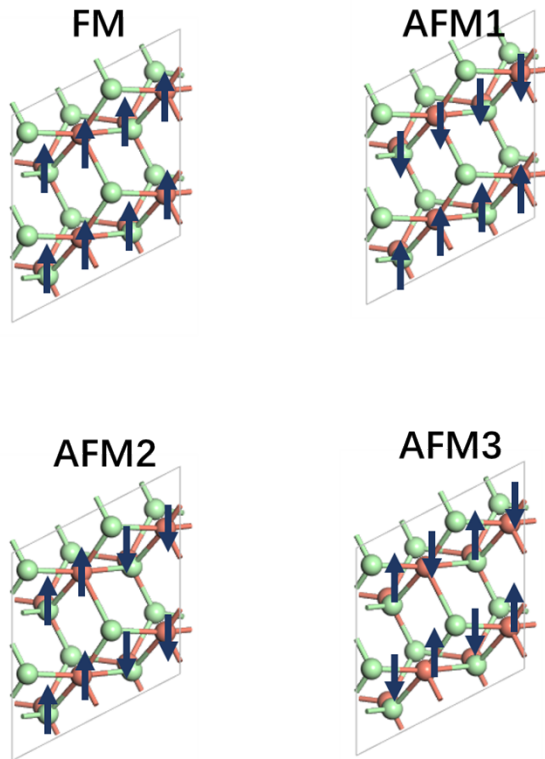


Figure S4. Different spin configurations for  $\text{Cu}_2\text{Cl}_3$  monolayer, where AFM1, AFM2, AFM3 are respectively 38, 36 and 38 meV higher in energy compared with the FM ground state.