

Supplementary Information (SI) File

Formation of pyramidal structures through mixing gold and platinum atoms: The $\text{Au}_x\text{Pt}_y^{2+}$ clusters with $x + y = 10$

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- ii) Adaptive natural density partitioning (AdNDP) analysis of the $\text{Au}_x\text{Pt}_y^{2+}$ clusters with $x + y = 10$ at B3PW91/ cc-pVTZ-PP theory level (Figures S3-S14).
- iii) Calculated density of states (DOS) of the $\text{Au}_x\text{Pt}_y^{2+}$ ($x + y = 10$) at B3PW91/aug-cc-pVTZ-PP theory level (Figure S15).
- iv) Optimized geometrical shapes and Cartesian coordinates of the lowest-lying $\text{Au}_x\text{Pt}_y^{2+}$ ($x + y = 10$) isomers calculated at B3PW91/ aug-cc-pVTZ-PP method (Table S1).

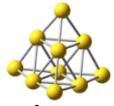
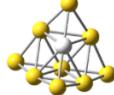
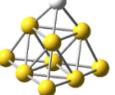
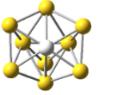
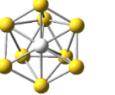
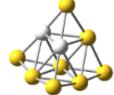
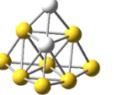
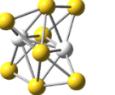
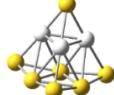
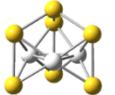
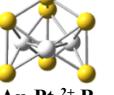
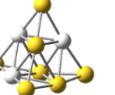
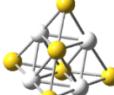
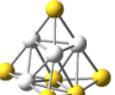
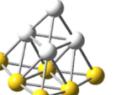
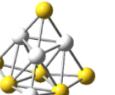
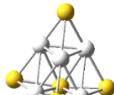
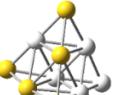
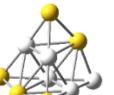
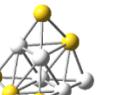
Method	Structures			
	 Au_{10}^{2+} (singlet)			
	 $\text{Au}_8\text{Pt}_2^{2+}.\text{A}$	 $\text{Au}_9\text{Pt}_2^{2+}.\text{B}$	 $\text{Au}_9\text{Pt}_2^{2+}.\text{C}$	 $\text{Au}_9\text{Pt}_2^{2+}.\text{D}$
B3PW91	0.00 (doublet)	0.42 (doublet)	0.42 (doublet)	0.47 (doublet)
TPSSh	0.00 (doublet)	0.42 (doublet)	0.37 (doublet)	0.30 (doublet)
BP86	0.00 (doublet)	0.31 (doublet)	0.48 (doublet)	0.49 (doublet)
revTPSS	0.00 (doublet)	0.37 (doublet)	0.35 (doublet)	0.26 (doublet)
	 $\text{Au}_8\text{Pt}_2^{2+}.\text{A}$	 $\text{Au}_8\text{Pt}_2^{2+}.\text{A}$	 $\text{Au}_8\text{Pt}_2^{2+}.\text{B}$	 $\text{Au}_8\text{Pt}_2^{2+}.\text{D}$
B3PW91	0.00 (triplet)	0.07 (singlet)	0.17 (triplet)	0.18 (singlet)
TPSSh	0.00 (triplet)	0.11 (singlet)	0.16 (triplet)	0.20 (triplet)
BP86	0.00 (triplet)	0.10 (singlet)	0.15 (triplet)	0.13 (triplet)
revTPSS	0.00 (triplet)	0.12 (singlet)	0.15 (triplet)	0.24 (triplet)
	 $\text{Au}_7\text{Pt}_3^{2+}.\text{A}$	 $\text{Au}_7\text{Pt}_3^{2+}.\text{B}$	 $\text{Au}_7\text{Pt}_3^{2+}.\text{B}$	 $\text{Au}_7\text{Pt}_3^{2+}.\text{C}$
B3PW91	0.00 (quartet)		0.52 (quartet)	0.52 (quartet)
TPSSh	0.00 (quartet)	0.22 (doublet)	0.49 (quartet)	0.44 (quartet)
BP86	0.00 (quartet)	0.16 (doublet)	0.37 (quartet)	0.39 (quartet)
revTPSS	0.00 (quartet)		0.42 (quartet)	0.38 (quartet)
	 $\text{Au}_6\text{Pt}_4^{2+}.\text{A}$	 $\text{Au}_6\text{Pt}_4^{2+}.\text{B}$	 $\text{Au}_6\text{Pt}_4^{2+}.\text{C}$	 $\text{Au}_6\text{Pt}_4^{2+}.\text{D}$
B3PW91	0.00 (quintet)	0.17 (quintet)	0.34 (quintet)	0.46 (quintet)
TPSSh	0.00 (quintet)	0.17 (quintet)	0.26 (quintet)	0.44 (quintet)
BP86	0.00 (quintet)	0.17 (quintet)	0.04 (quintet)	0.25 (quintet)
revTPSS	0.00 (quintet)	0.16 (quintet)	0.09 (quintet)	0.33 (quintet)
	 $\text{Au}_5\text{Pt}_5^{2+}.\text{A}$	 $\text{Au}_5\text{Pt}_5^{2+}.\text{B}$	 $\text{Au}_5\text{Pt}_5^{2+}.\text{C}$	 $\text{Au}_5\text{Pt}_5^{2+}.\text{C}$
B3PW91	0.00 (sextet)	0.11 (sextet)	0.15 (quartet)	0.17 (sextet)
TPSSh	0.00 (sextet)	0.14 (sextet)	0.13 (quartet)	0.15 (sextet)
BP86	0.03 (sextet)	0.05 (sextet)	0.00 (quartet)	0.05 (sextet)
revTPSS	0.00 (sextet)	0.02 (sextet)	0.03 (quartet)	0.08 (sextet)
CCSD(T) (*)	0.00 (sextet)	0.13 (sextet)		

Figure S1. Structures, relative energies (eV), and spin states (in bracket) of the most stable isomers of $\text{Au}_x\text{Pt}_y^{2+}$ with $x + y = 10$ and $y = 0 - 5$ using B3PW91, TPSSh, BP86 and revTPSS/ aug-cc-pVTZ-PP + ZPE computations. (*) is calculated at CCSD(T)/ cc-pVDZ-PP method. Yellow ball = Au and white ball = Pt.

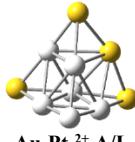
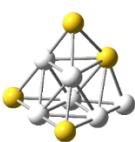
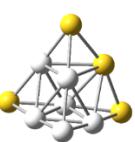
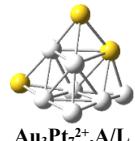
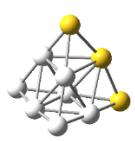
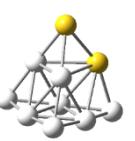
Method	Structures			
				
$\text{Au}_4\text{Pt}_6^{2+}.\text{A/L}$	0.00 (septet)	0.27 (septet)	0.48 (quintet)	0.61 (quintet)
B3PW91	0.00 (septet)	0.28 (septet)	0.20 (quintet)	0.55 (quintet)
TPSSh	0.00 (septet)	0.22 (septet)	0.12 (quintet)	0.25 (quintet)
BP86	0.00 (septet)	0.26 (septet)	0.17 (quintet)	0.55 (quintet)
revTPSS	0.00 (septet)	0.26 (septet)	0.17 (quintet)	0.55 (quintet)
				
$\text{Au}_3\text{Pt}_7^{2+}.\text{A/L}$	0.00 (octet) 0.10 (sextet) 0.28 (quartet)	0.11 (octet)	0.00 (nonet) 0.36 (septet)	0.56 (nonet) 0.64 (septet)
B3PW91	0.00 (octet) 0.10 (sextet) 0.28 (quartet)	0.00 (sextet) 0.05 (octet)	0.00 (nonet) 0.35 (septet)	0.59 (nonet) 0.56 (septet)
TPSSh	0.01 (octet)	0.00 (sextet)	0.00 (nonet)	0.08 (quintet)
BP86	0.09 (sextet) 0.10 (octet)	0.00 (sextet) 0.04 (octet)	0.00 (nonet)	0.16 (septet)
revTPSS	0.10 (octet) 0.13 (sextet) 0.28 (quartet)	0.00 (sextet) 0.06 (octet)	0.00 (nonet) 0.28 (septet)	0.26 (quintet) 0.42 (nonet)
				
$\text{AuPt}_9^{2+}.\text{A}$	0.00 (10-et) 0.14 (octet) 0.17 (sextet)	0.80 (quartet)	0.00 (11-et) 0.10 (nonet) 0.30 (septet)	
B3PW91	0.00 (10-et) 0.14 (octet) 0.17 (sextet)	0.80 (quartet)	0.00 (11-et) 0.10 (nonet) 0.30 (septet)	
TPSSh	0.00 (10-et) 0.07 (octet) 0.12 (sextet)	0.62 (quartet)	0.00 (11-et) 0.07 (nonet) 0.04 (septet)	
BP86	0.00 (octet) 0.05 (sextet) 0.11 (10-et)	0.13 (quartet)	0.00 (septet) 0.00 (quintet) 0.30 (nonet) 0.30 (11-et)	
revTPSS	0.07 (10-et) 0.00 (octet) 0.07 (sextet)	0.29 (quartet)	0.40 (11-et) 0.26 (nonet) 0.00 (septet)	

Figure S2. Structures, relative energies (eV), and spin states (in bracket) of the most stable isomers of $\text{Au}_x\text{Pt}_y^{2+}$ with $x + y = 10$ and $y = 6 - 10$ using B3PW91, TPSSh, BP86 and revTPSS/aug-cc-pVTZ-PP + ZPE computations. Yellow ball = Au and white ball = Pt.

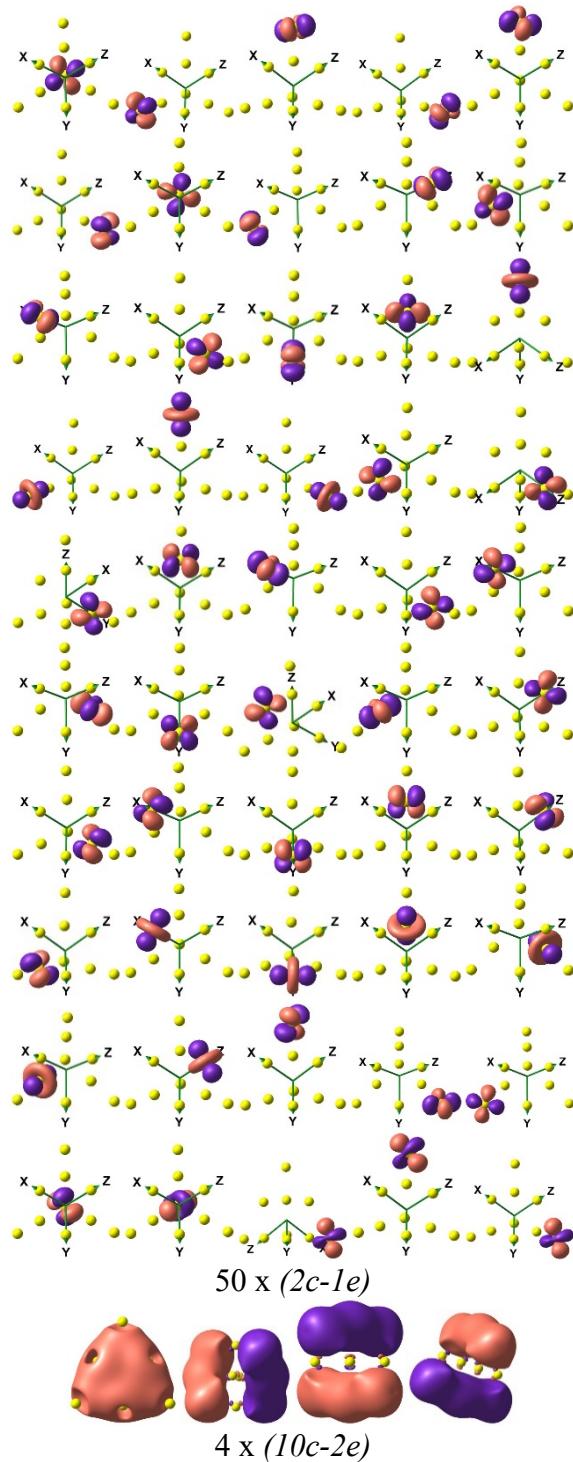


Figure S3: AdNDP analysis showing multi-center bonds in the Au_{10}^{2+} cluster at singlet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

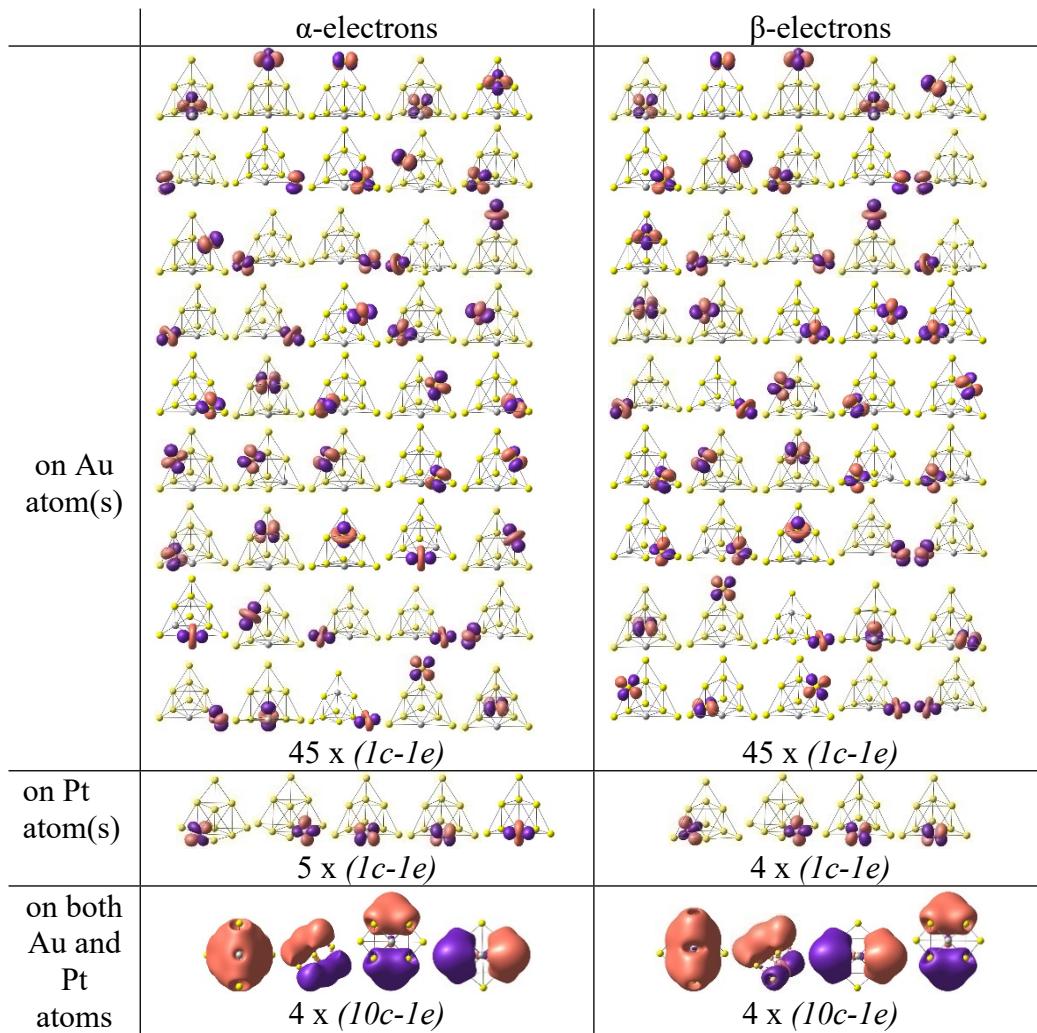


Figure S4: AdNDP analysis showing multi-center bonds in the $\text{Au}_9\text{Pt}^{2+}\cdot\text{A}$ cluster at doublet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

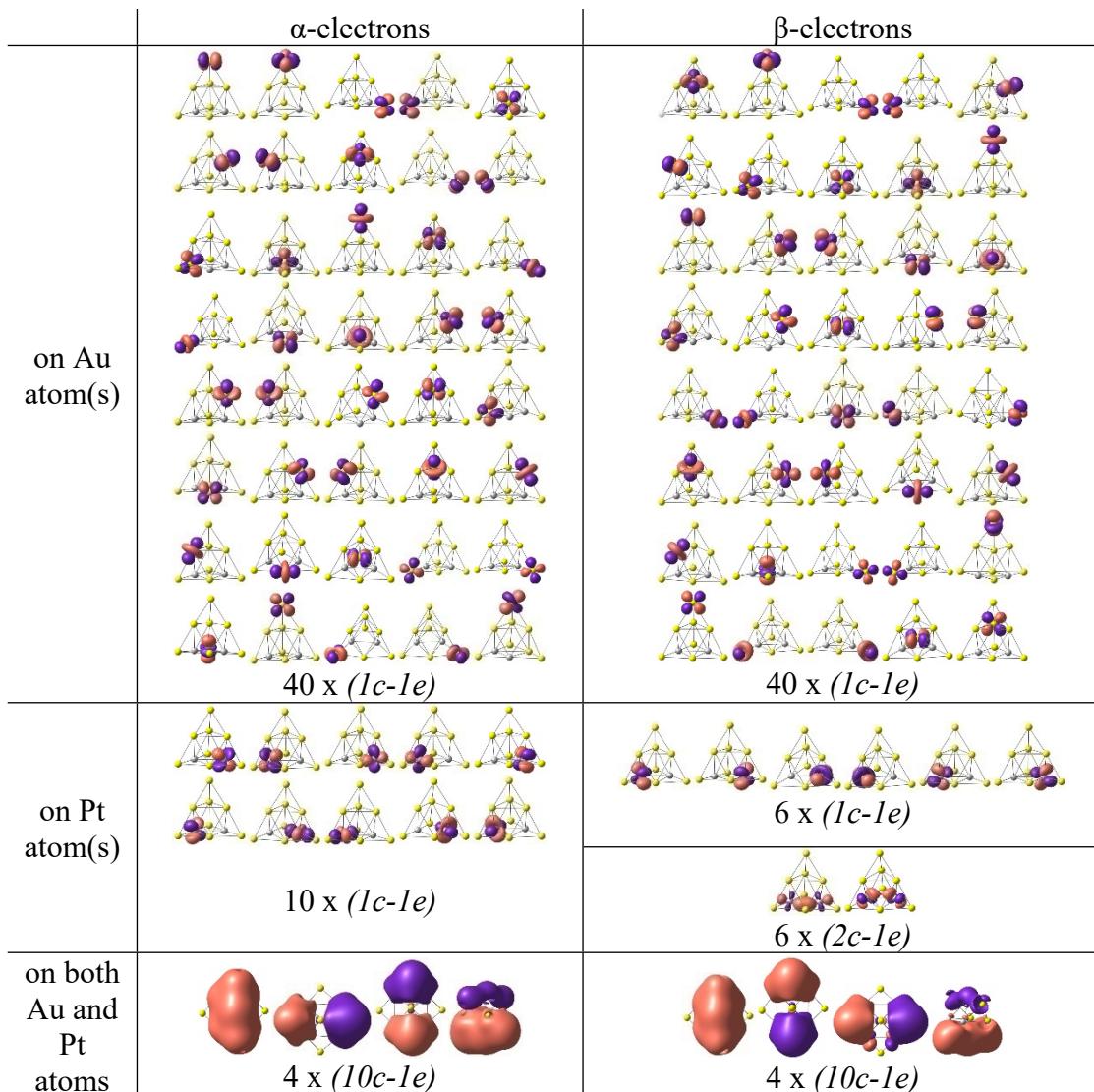


Figure S5: AdNDP analysis showing multi-center bonds in the $\text{Au}_8\text{Pt}_2^{2+}\cdot\text{A}$ cluster at triplet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

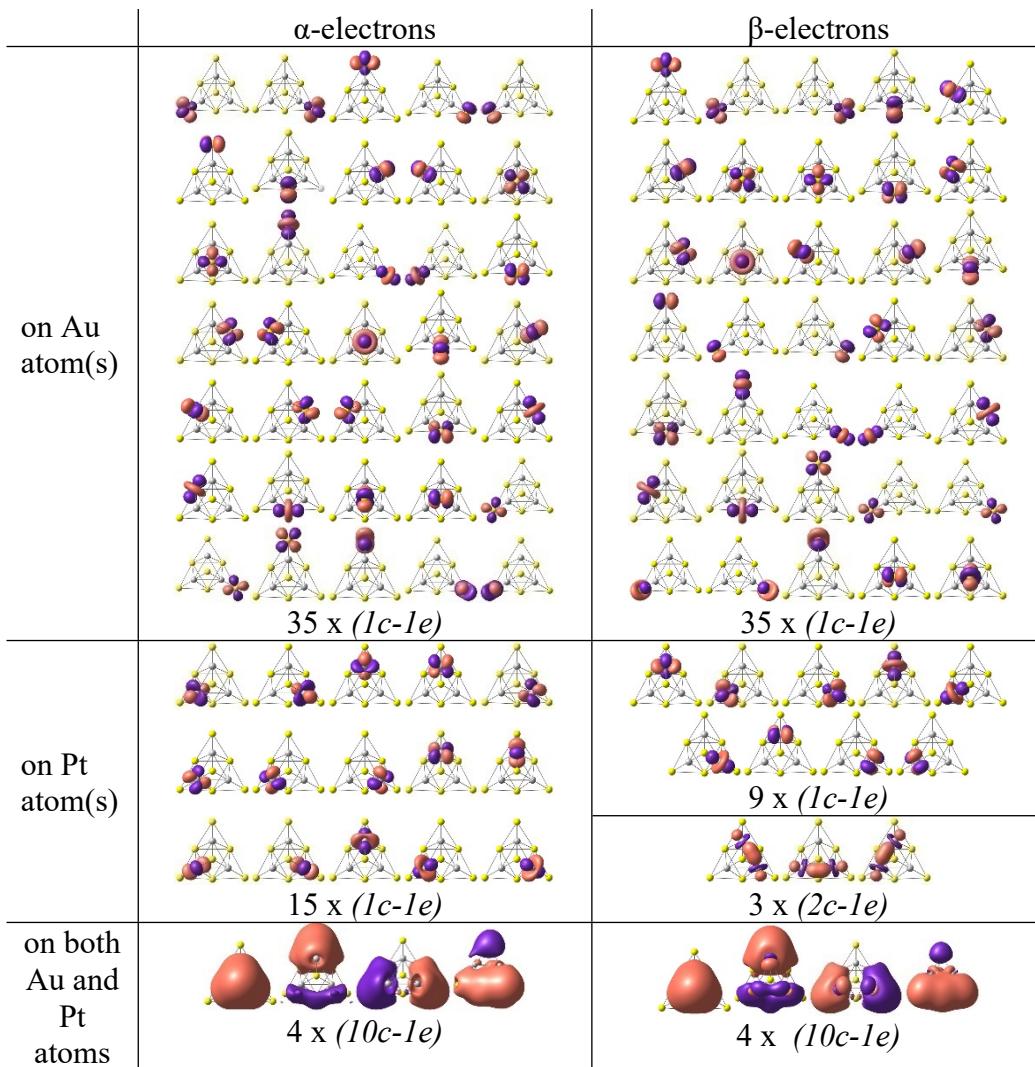


Figure S6: AdNDP analysis showing multi-center bonds in the $\text{Au}_7\text{Pt}_3^{2+}.\text{A}$ cluster at quartet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

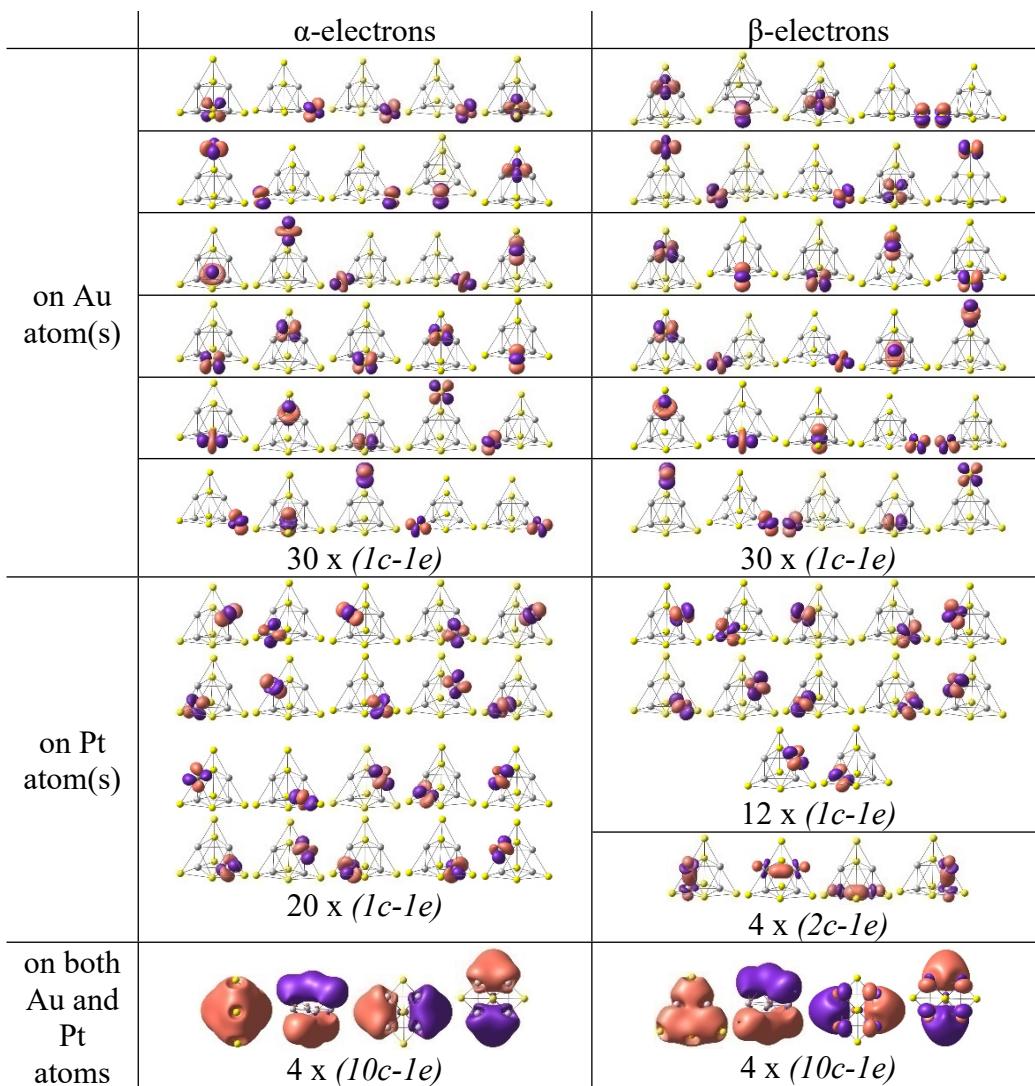


Figure S7: AdNDP analysis showing multi-center bonds in the $\text{Au}_6\text{Pt}_4^{2+}.\text{A}$ cluster at quintet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

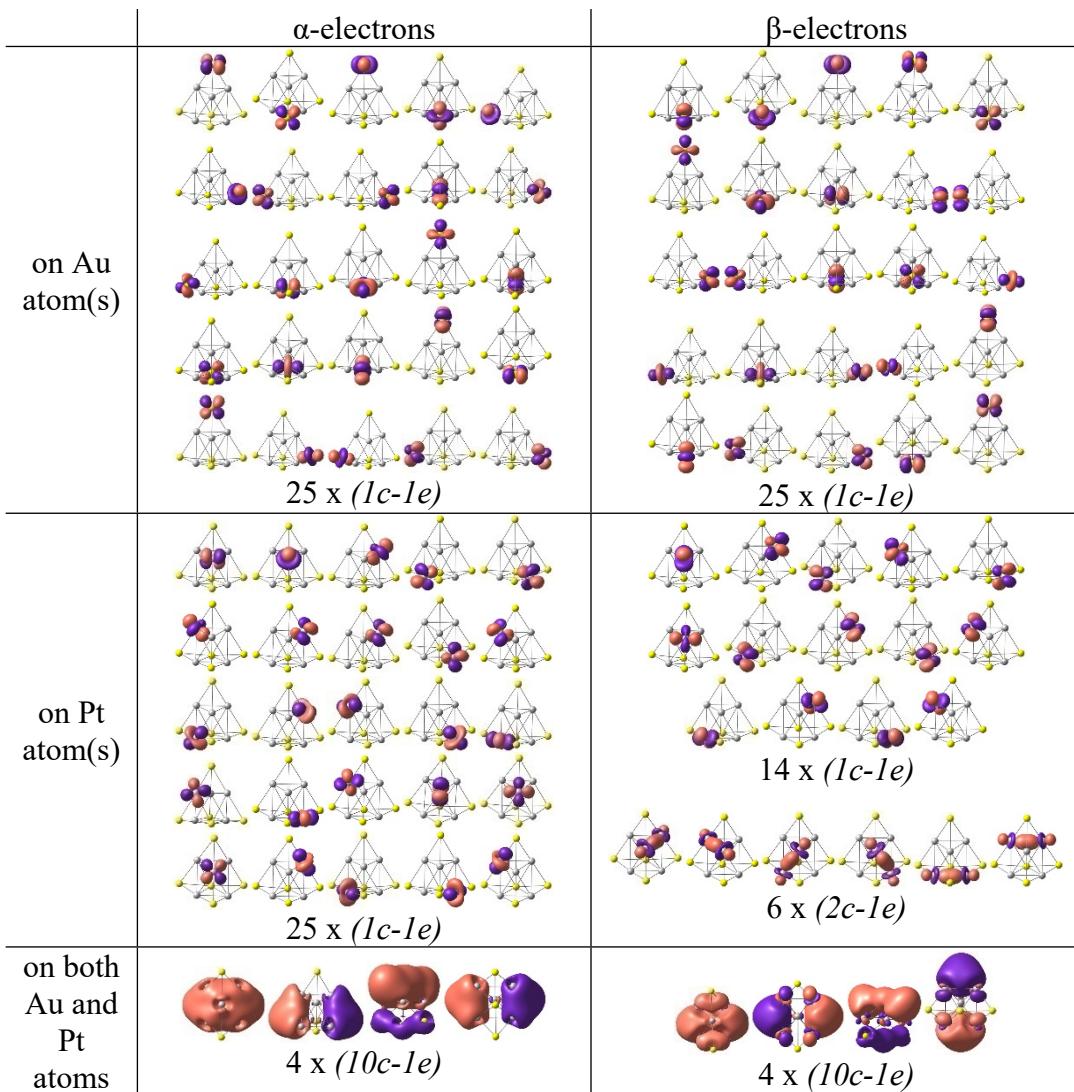


Figure S8: AdNDP analysis showing muti-center bonds in the $\text{Au}_5\text{Pt}_5^{2+}\cdot\text{A}$ cluster at sextet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

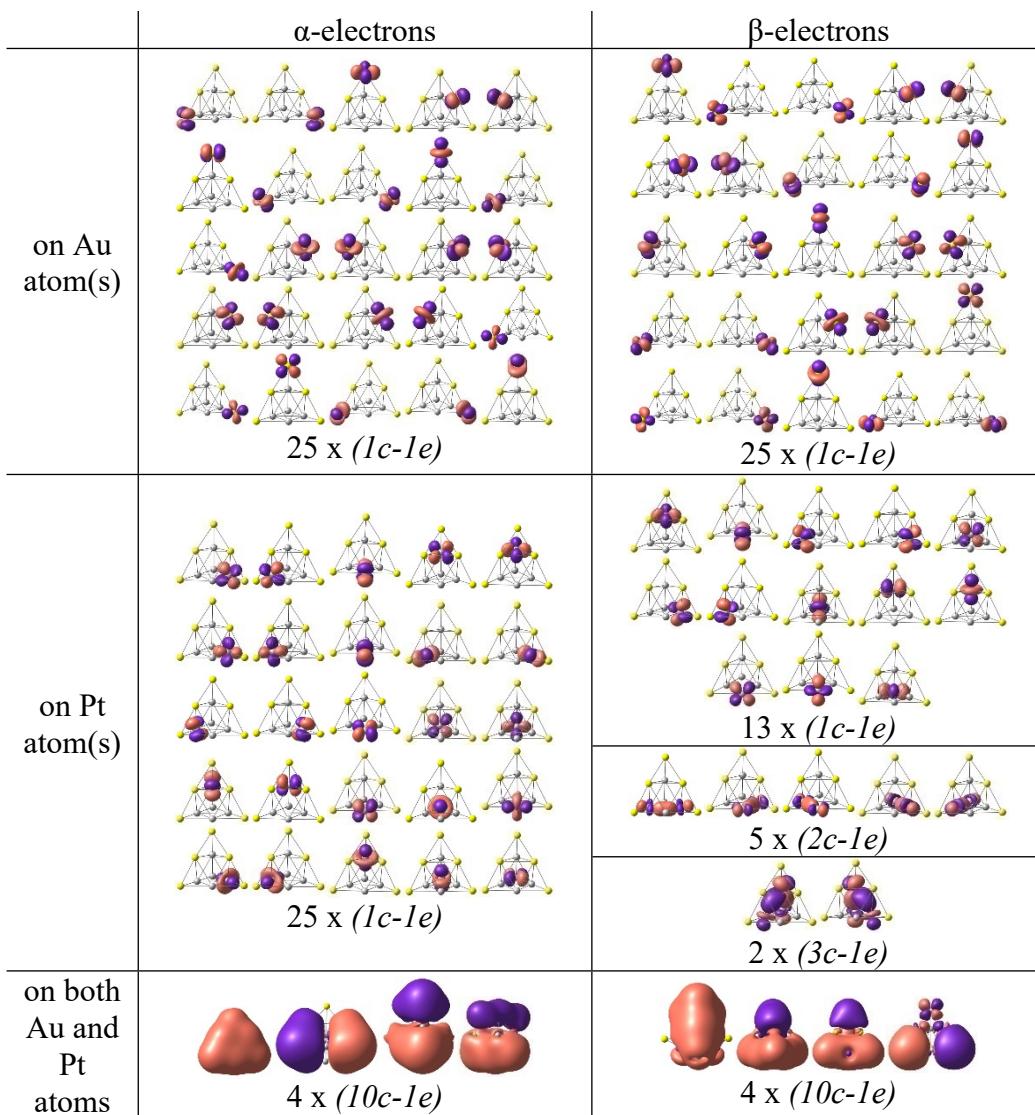


Figure S9: AdNDP analysis showing multi-center bonds in the $\text{Au}_5\text{Pt}_5^{2+}.\text{B}$ cluster at sextet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

| α -electrons | β -electrons

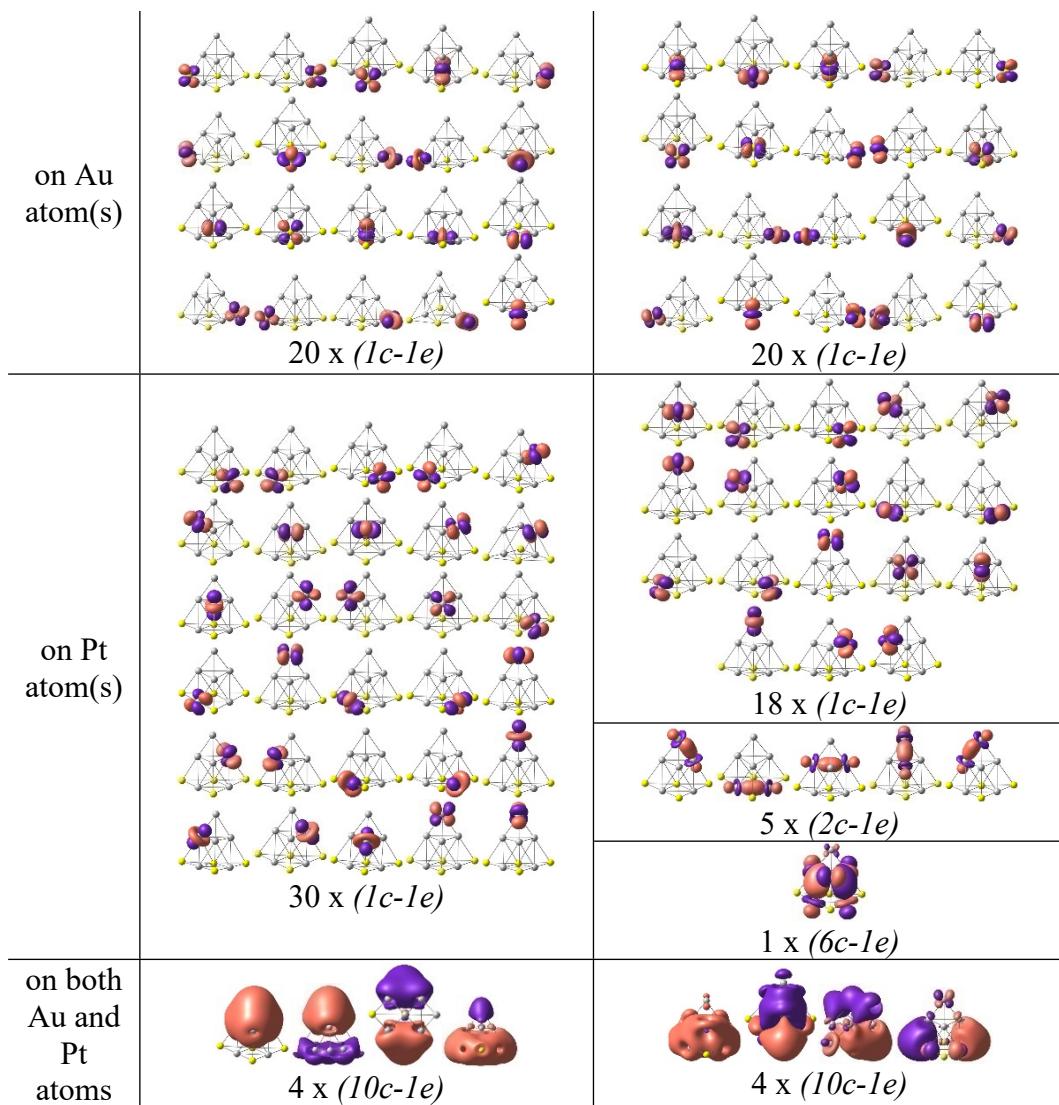


Figure S10: AdNDP analysis showing multi-center bonds in the $\text{Au}_4\text{Pt}_6^{2+}.\text{A}$ cluster at septet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

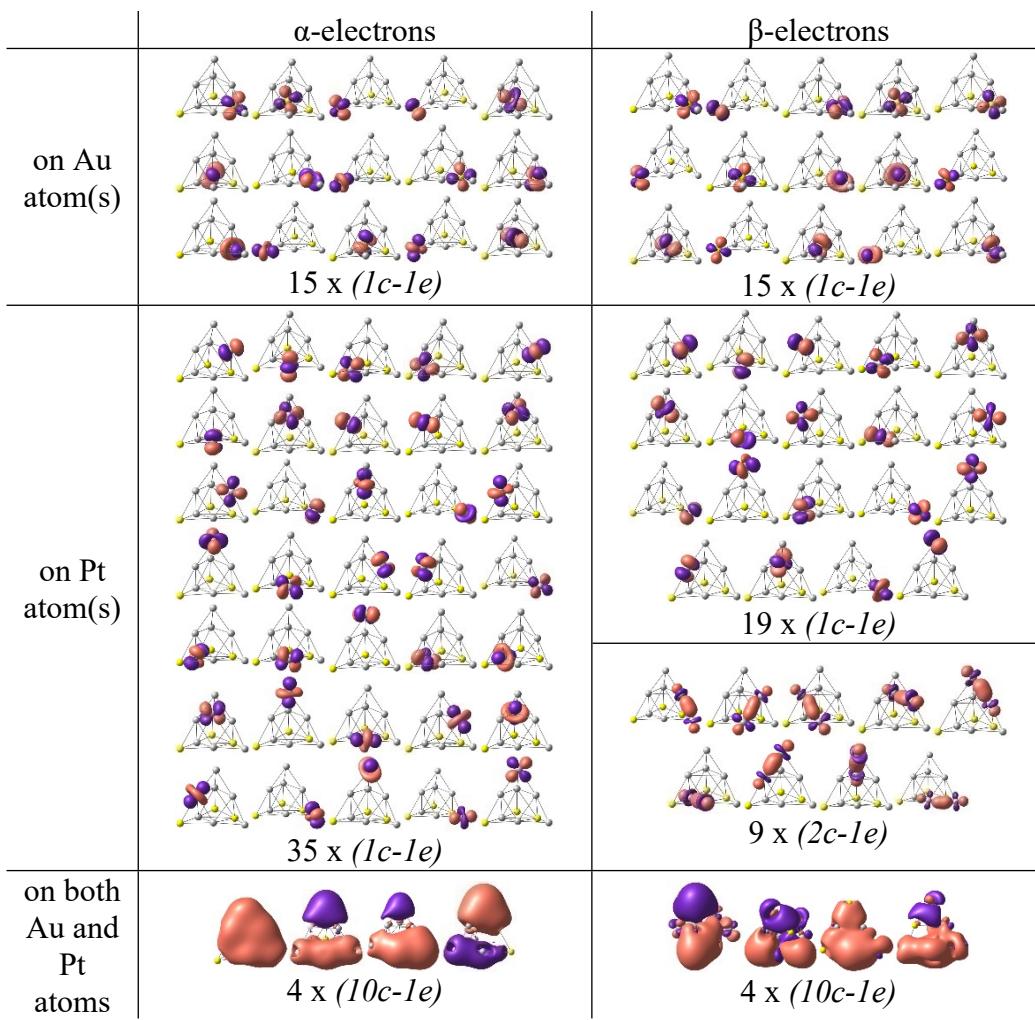


Figure S11: AdNDP analysis showing multi-center bonds in the $\text{Au}_3\text{Pt}_7^{2+}.\text{A}$ cluster at octet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

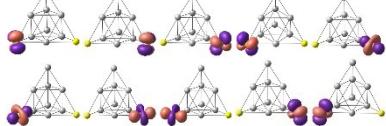
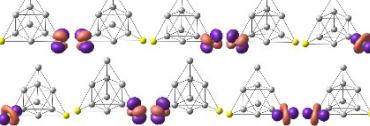
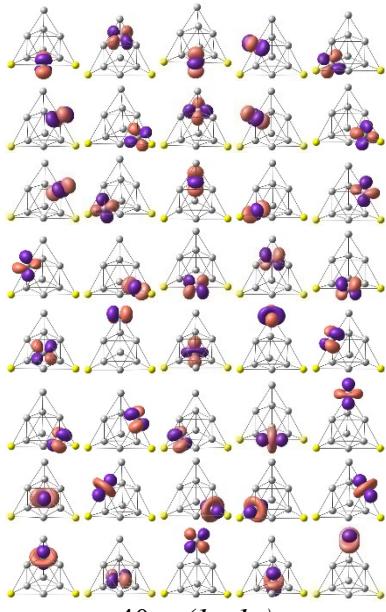
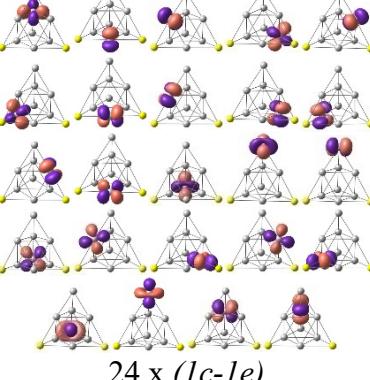
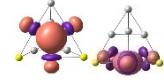
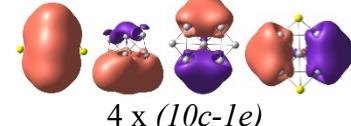
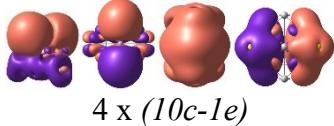
	α -electrons	β -electrons
on Au atom(s)	 $10 \times (1c-1e)$	 $10 \times (1c-1e)$
on Pt atom(s)	 $40 \times (1c-1e)$	 $24 \times (1c-1e)$  $6 \times (2c-1e)$  $2 \times (3c-1e)$
on both Au and Pt atoms	 $4 \times (10c-1e)$	 $4 \times (10c-1e)$

Figure S12: AdNDP analysis showing multi-center bonds in the $\text{Au}_2\text{Pt}_8^{2+}.\text{A}$ cluster at nonet state, calculated at B3PW91/ cc-pVTZ-PP theory level.

	α -electrons	β -electrons
on Au atom(s)	 $5 \times (1c-1e)$	 $5 \times (1c-1e)$
on Pt atom(s)	 $24 \times (1c-1e)$	 $12 \times (2c-1e)$
on both Au and Pt atoms	 $4 \times (10c-1e)$	 $4 \times (10c-1e)$

Figure S13: AdNDP analysis showing multi-center bonds in the $\text{AuPt}_9^{2+}.\text{A}$ cluster at 10-et state, calculated at B3PW91/ cc-pVTZ-PP theory level.

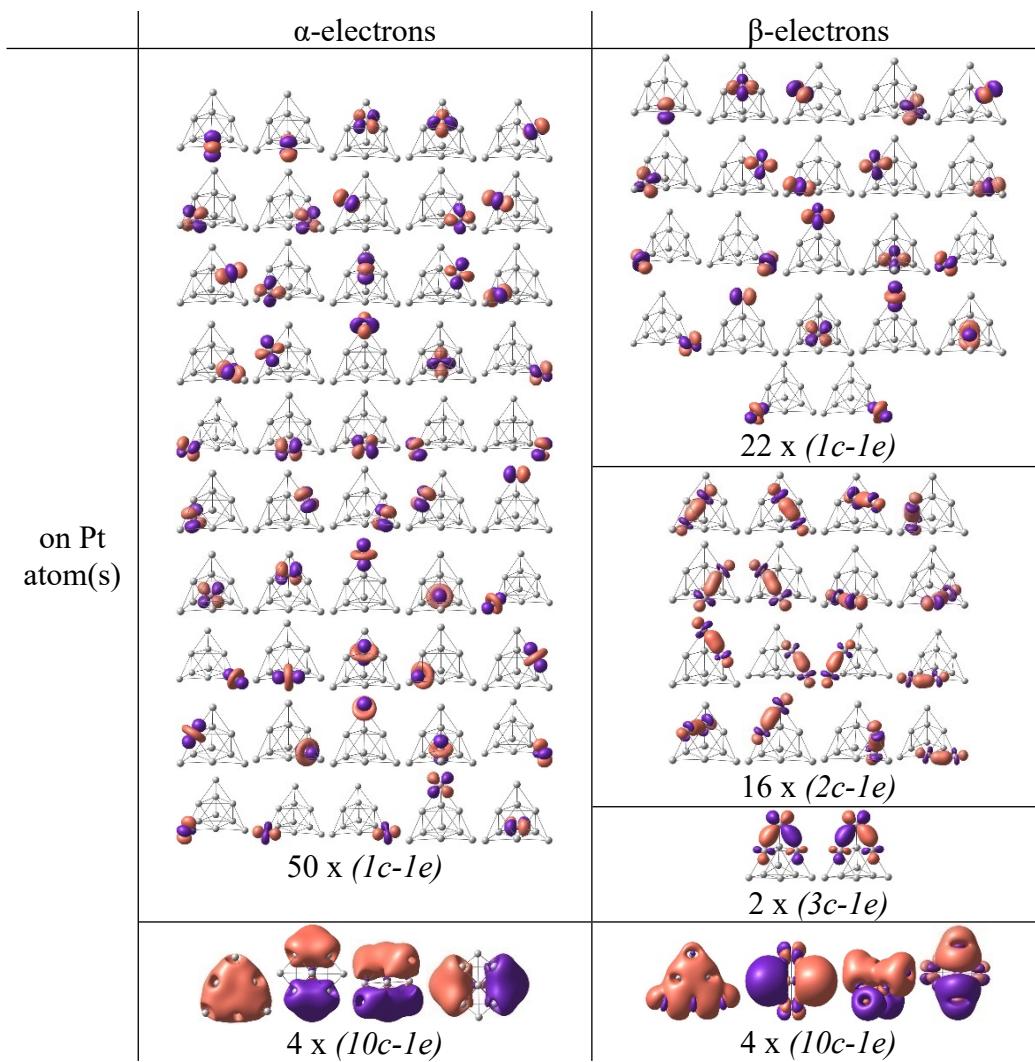
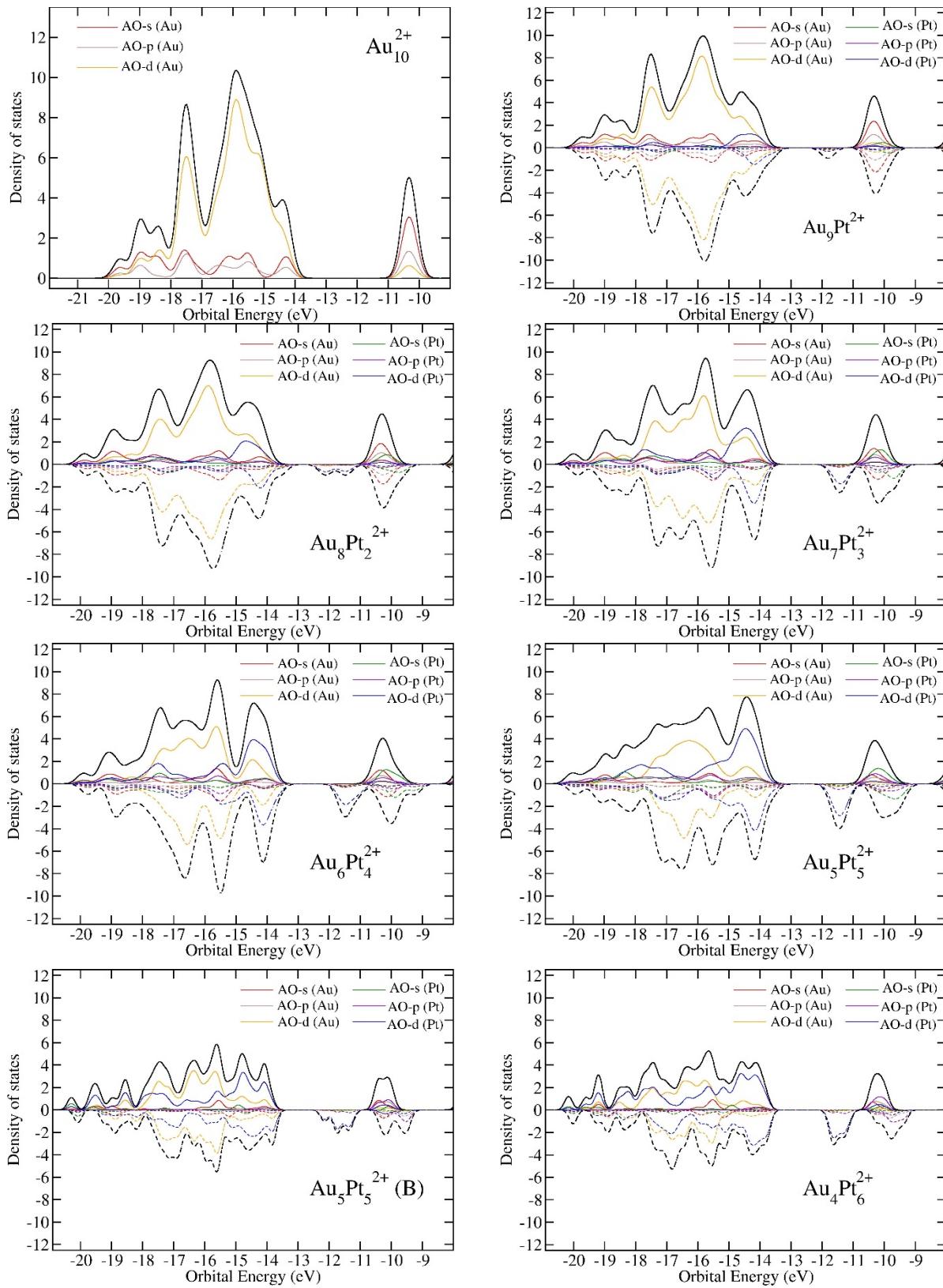


Figure S14: AdNDP analysis showing multi-center bonds in the $\text{Pt}_{10}^{2+}\cdot\text{A}$ cluster at 11-et state, calculated at B3PW91/ cc-pVTZ-PP theory level.



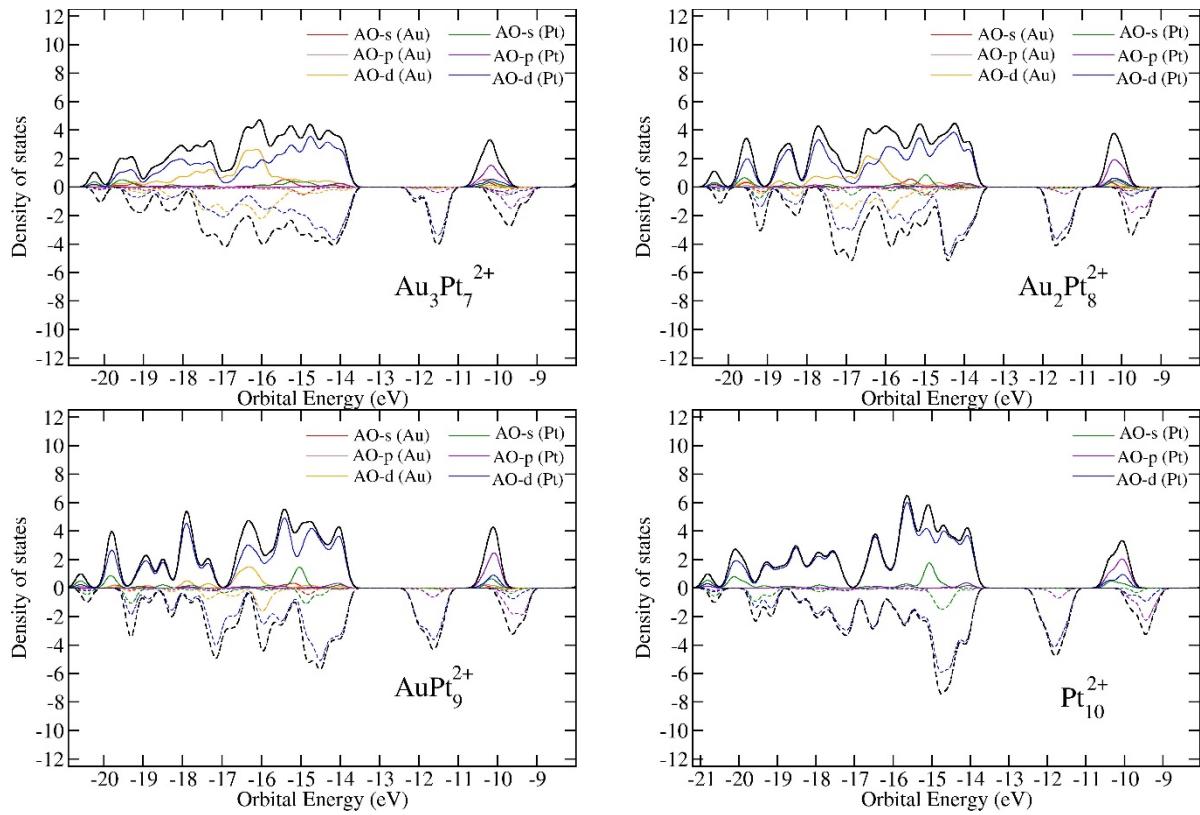
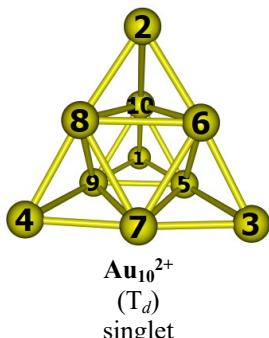
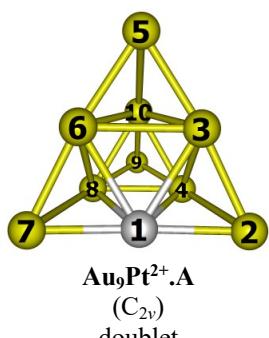
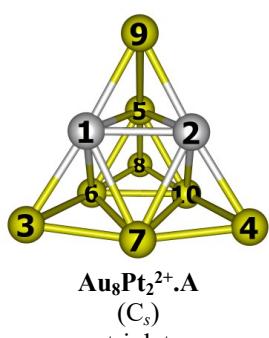
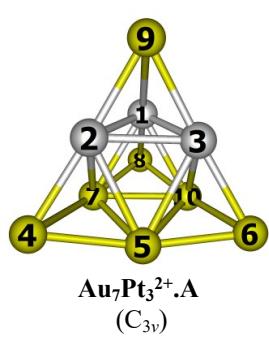
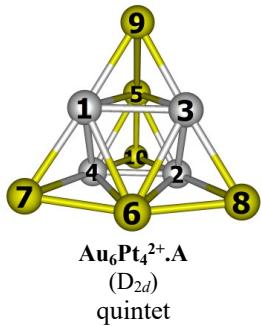


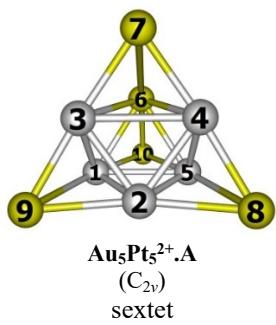
Figure S15: Calculated density of states (DOS) of $\text{Au}_x\text{Pt}_y^{2+}$ ($x+y=10$) at B3PW91/aug-cc-pVTZ-PP level. Positive and negative DOS represent spin-up and spin-down electrons, respectively.

Table S1: Optimized geometrical shapes and Cartesian coordinates of the lowest-lying $\text{Au}_x\text{Pt}_y^{2+}$ ($x + y = 10$) isomers calculated at B3PW91/aug-cc-pVTZ-PP method.

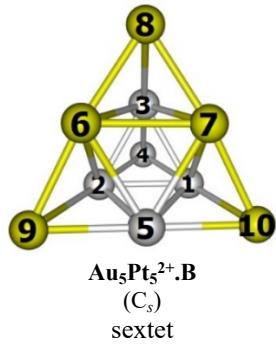
Isomer	Coordinates		
 Au_{10}^{2+} (T_d) singlet	Au -1.90919614 1.90919614 1.90919614 Au 1.90919614 -1.90919614 1.90919614 Au 1.90919614 1.90919614 -1.90919614 Au -1.90919614 -1.90919614 -1.90919614 Au -0.00000000 2.02642215 0.00000000 Au 2.02642215 -0.00000000 0.00000000 Au -0.00000000 0.00000000 -2.02642215 Au 0.00000000 -2.02642215 -0.00000000 Au -2.02642215 0.00000000 0.00000000 Au 0.00000000 -0.00000000 2.02642215		
 $\text{Au}_9\text{Pt}_2^{2+}\cdot\text{A}$ (C_{2v}) doublet	Pt 0.00000000 -0.00000000 -1.90497415 Au 0.00000000 2.63733420 -1.95262215 Au 1.45503911 1.44306111 -0.00612800 Au -1.45503911 1.44306111 -0.00612800 Au 2.70442921 -0.00000000 1.90662515 Au 1.45503911 -1.44306111 -0.00612800 Au 0.00000000 -2.63733420 -1.95262215 Au -1.45503911 -1.44306111 -0.00612800 Au -2.70442921 0.00000000 1.90662515 Au -0.00000000 0.00000000 1.99736915		
 $\text{Au}_8\text{Pt}_2^{2+}\cdot\text{A}$ (C_s) triplet	Pt 1.14144281 0.81770330 1.25838410 Pt 1.14144281 0.81770330 -1.25838410 Au 1.14144281 -1.44589787 2.68187220 Au 1.14144281 -1.44589787 -2.68187220 Au -1.15710836 1.63808536 0.00000000 Au -1.18545936 -0.86639583 1.42614911 Au 1.16466782 -1.76958090 0.00000000 Au -3.31907953 -0.02144677 0.00000000 Au 1.14556481 3.16282448 0.00000000 Au -1.18545936 -0.86639583 -1.42614911		
 $\text{Au}_7\text{Pt}_3^{2+}\cdot\text{A}$ (C_{3v}) quartet	Pt 1.29498210 -0.74765806 1.14725809 Pt -0.00000009 1.49531657 1.14725809 Pt -1.29498201 -0.74765822 1.14725809 Au 0.00000000 3.10231624 -0.99291807 Au -1.44459311 0.83403606 -1.25428709 Au -2.68668459 -1.55115797 -0.99291807 Au 1.44459289 0.83403645 -1.25428709 Au 2.68668459 -1.55115797 -0.99291807 Au 0.00000000 0.00000010 3.34340826 Au 0.00000022 -1.66807222 -1.25428709		



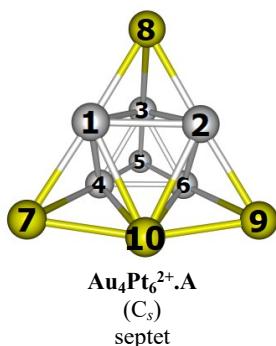
Pt	1.29483810	1.29483810	0.00000000
Pt	-1.29483810	-1.29483810	0.00000000
Pt	-1.29483810	1.29483810	0.00000000
Pt	1.29483810	-1.29483810	0.00000000
Au	0.00000000	0.00000000	2.26016317
Au	0.00000000	0.00000000	-2.26016317
Au	2.66886321	0.00000000	-1.87859514
Au	-2.66886321	0.00000000	1.87859514
Au	0.00000000	2.66886321	1.87859514
Au	0.00000000	-2.66886321	-1.87859514



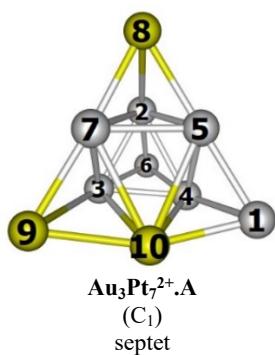
Pt	-1.52136112	1.29029010	-0.01516100
Pt	0.00000000	0.00000000	-1.65814813
Pt	-1.52136112	-1.29029010	-0.01516100
Pt	1.52136112	-1.29029010	-0.01516100
Pt	1.52136112	1.29029010	-0.01516100
Au	0.00000000	0.00000000	2.09950616
Au	-0.00000000	-2.66868620	1.69694013
Au	2.83403722	-0.00000000	-1.89817514
Au	-2.83403722	0.00000000	-1.89817514
Au	0.00000000	2.66868620	1.69694013



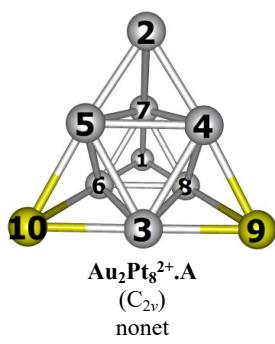
Pt	0.01264400	1.39250311	1.29322510
Pt	0.01264400	1.39250311	-1.29322510
Pt	-1.88017814	0.09212801	0.00000000
Pt	-1.79734514	2.65057320	-0.00000000
Pt	1.86005114	0.10289601	-0.00000000
Au	0.01264400	-1.52859812	-1.44141611
Au	0.01264400	-1.52859812	1.44141611
Au	-2.00763016	-2.60502820	0.00000000
Au	1.87591914	0.05144700	-2.67775920
Au	1.87591914	0.05144700	2.67775920



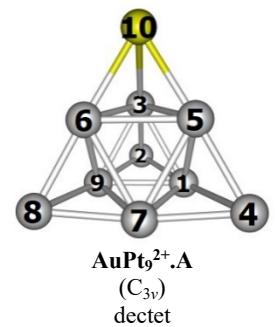
Pt	1.08191108	-0.79568106	1.29798410
Pt	1.08191108	-0.79568106	-1.29798410
Pt	1.14878909	1.62064913	0.00000000
Pt	-1.06880508	0.85748406	1.31265310
Pt	-0.93999007	3.02964323	0.00000000
Pt	-1.06880508	0.85748406	-1.31265310
Au	-1.06880508	-1.47201911	2.67873320
Au	3.26846125	-0.05480600	0.00000000
Au	-1.06880508	-1.47201911	-2.67873320
Au	-1.36288810	-1.71462513	-0.00000000



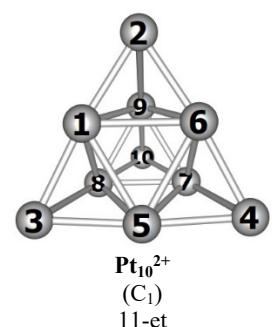
Pt	1.64118924	-1.49645925	-2.20534308
Pt	-1.81442278	-0.56948653	0.68856613
Pt	0.45863957	0.30807548	1.83011522
Pt	0.82764889	-1.71002417	0.17787910
Pt	-0.60946049	-0.42474314	-1.65762304
Pt	-0.49050561	-2.01063842	2.31353526
Pt	-0.65384360	1.72928908	-0.20001093
Au	-2.92398788	0.90690707	-1.25724001
Au	1.52805878	2.63519622	1.00440916
Au	2.02857306	0.57904839	-0.68229897



Pt	0.00000000	2.55494218	1.82919213
Pt	-0.00000000	-2.55494218	1.82919213
Pt	-0.00000000	-0.00000000	-1.89513314
Pt	1.34354210	-1.39648710	0.03267100
Pt	-1.34354210	-1.39648710	0.03267100
Pt	-1.34354210	1.39648710	0.03267100
Pt	0.00000000	0.00000000	1.91763214
Pt	1.34354210	1.39648710	0.03267100
Au	2.62910219	-0.00000000	-1.88166114
Au	-2.62910219	0.00000000	-1.88166114



Pt	1.30834417	0.75537292	-1.18750708
Pt	-0.00000010	2.96050021	-1.01376208
Pt	-0.00000005	1.56040611	1.09768408
Pt	2.56386844	-1.48025002	-1.01376208
Pt	1.35135136	-0.78020301	1.09768408
Pt	-1.35135130	-0.78020310	1.09768408
Pt	0.00000005	-1.51074575	-1.18750708
Pt	-2.56386834	-1.48025020	-1.01376208
Pt	-1.30834422	0.75537283	-1.18750708
Au	0.00000000	0.00000000	3.26884623



Pt	0.00000000	0.00000000	-1.72233712
Pt	0.00000000	2.53834418	-1.89170114
Pt	-0.00000000	-2.53834418	-1.89170114
Pt	-2.59671018	0.00000000	1.71971012
Pt	-1.30402909	-1.48296211	0.06612600
Pt	-1.30402909	1.48296211	0.06612600
Pt	0.00000000	0.00000000	1.80181613
Pt	1.30402909	-1.48296211	0.06612600
Pt	1.30402909	1.48296211	0.06612600
Pt	2.59671018	-0.00000000	1.71971012