## Supplementary Information



Fig. S1 The total reaction probabilities for the total angular momentum $J_{\mathrm{tot}}=0,10,15$, $20,25,30,40,60$, and 80 for the initial ground rovibrational state as a function of collision energy.


Fig. S2 Product HF vibrational state-resolved ICS as a function of collision energy calculated with $9 J_{\text {tot }}(0,10,15,20,25,30,40,60,80)$, in comparison with those calculated with only $5 J_{\text {tot }}(0,20,40,60,80)$.


Fig. S3 Normalized HF vibrational populations as a function of collision energy for the title reaction, in comparison with the QCT results in Ref 45.


Fig. S4 3-dimensional representation of the correlated ICS of the product pair of $\mathrm{HF}\left(v^{\prime}\right)$ and $\mathrm{CD}_{3}\left(v_{2}\right)$ at the collision energy of 0.121 eV .


Fig. S5 3-dimensional representation of the correlated ICS of the product pair of $\mathrm{HF}\left(v^{\prime}\right)$ and $\mathrm{CD}_{3}\left(v_{2}\right)$ at the collision energy of $0.0145 \mathrm{eV}, 0.1 \mathrm{eV}, 0.2 \mathrm{eV}$ and 0.3 eV , that the sum of correlated HF vibration populations for each $\mathrm{CD}_{3}$ state at a given $\mathrm{E}_{\mathbf{c}}$ are scaled to unity.

Table S1. Energy disposal (in eV) into $\mathrm{HF}\left(v^{\prime}\right)+\mathrm{CD}_{3}\left(v_{2}\right)$ products when HF vibrationally excited from $v^{\prime}=0$ to 3 .

| HF state | $v^{\prime}=0$ | $v^{\prime}=1$ | $v^{\prime}=2$ | $v^{\prime}=3$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{E}_{\mathrm{HF}}\left(v^{\prime}\right)$ | 0 | 0.491 | 0.96 | 1.409 |
| $\mathrm{E}_{\mathrm{c}}=0.0145 \mathrm{eV}$ |  |  |  |  |
| $<\mathrm{E}_{v 2}>\mathrm{CD}^{2}$ | 0.399 | 0.298 | 0.2 | - |
| $<\mathrm{E}_{v 2}>\mathrm{CD}^{2}+\mathrm{E}_{\mathrm{HF}}\left(v^{\prime}\right)$ | 0.399 | 0.789 | 1.16 | - |
| $\mathrm{E}_{\mathrm{c}}=0.1 \mathrm{eV}$ |  |  |  |  |
| $<\mathrm{E}_{v 2}>\mathrm{CD} 3$ | 0.368 | 0.276 | 0.171 | - |
| $<\mathrm{E}_{v 2}>\mathrm{CD}^{2}+\mathrm{E}_{\mathrm{HF}}\left(v^{\prime}\right)$ | 0.368 | 0.767 | 1.132 | - |
| $\mathrm{E}_{\mathrm{c}}=0.2 \mathrm{eV}$ |  |  |  |  |
| $<\mathrm{E}_{v 2}>\mathrm{CD} 3$ | 0.364 | 0.263 | 0.153 | 0.036 |
| $<\mathrm{E}_{v 2}>\mathrm{CD} 3+\mathrm{E}_{\mathrm{HF}}\left(v^{\prime}\right)$ | 0.364 | 0.754 | 1.114 | 1.445 |
| $\mathrm{E}_{\mathrm{c}}=0.3 \mathrm{eV}$ |  |  |  |  |
| $<\mathrm{E}_{v 2}>\mathrm{CD} 3$ | 0.359 | 0.25 | 0.143 | 0.049 |
| $<\mathrm{E}_{v 2}>\mathrm{CD} 3+\mathrm{E}_{\mathrm{HF}}\left(v^{\prime}\right)$ | 0.359 | 0.741 | 1.104 | 1.458 |

Table S2. Energy disposal (in eV ) into $\mathrm{HF}\left(v^{\prime}\right)+\mathrm{CD}_{3}\left(v_{2}\right)$ products when $\mathrm{CD}_{3}$ vibrationally excited from $v_{2}=0$ to 9 .

| $\mathrm{CD}_{3}$ state | $v_{2}=0$ | $v_{2}=1$ | $v_{2}=2$ | $v_{2}=3$ | $v_{2}=4$ | $v_{2}=5$ | $v_{2}=6$ | $v_{2}=7$ | $v_{2}=8$ | $v_{2}=9$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{E}_{\mathrm{CD} 3}\left(v_{2}\right)$ | 0 | 0.056 | 0.119 | 0.186 | 0.257 | 0.331 | 0.407 | 0.486 | 0.567 | 0.649 |
| $\mathrm{E}_{\mathrm{c}}=0.0145 \mathrm{eV}$ |  |  |  |  |  |  |  |  |  |  |
| $<\mathrm{E}_{v}>_{\mathrm{HF}}$ | 0.956 | 0.947 | 0.935 | 0.929 | 0.917 | 0.919 | 0.892 | 0.469 | 0.465 | 0.471 |
| $<\mathrm{E}_{v}>_{\mathrm{HF}}+\mathrm{E}_{\mathrm{CD} 3}\left(v_{2}\right)$ | 0.956 | 1.004 | 1.054 | 1.115 | 1.174 | 1.25 | 1.3 | 0.955 | 1.031 | 1.12 |
| $\mathrm{E}_{\mathrm{c}}=0.1 \mathrm{eV}$ |  |  |  |  |  |  |  |  |  |  |
| $<\mathrm{E}_{v}>_{\mathrm{HF}}$ | 1.328 | 0.937 | 0.929 | 0.908 | 0.879 | 0.827 | 0.755 | 0.583 | 0.443 | 0.416 |
| $<\mathrm{E}_{v}>_{\mathrm{HF}}+\mathrm{E}_{\mathrm{CD} 3}\left(v_{2}\right)$ | 1.328 | 0.993 | 1.048 | 1.095 | 1.136 | 1.158 | 1.162 | 1.069 | 1.01 | 1.065 |
| $\mathrm{E}_{\mathrm{c}}=0.2 \mathrm{eV}$ |  |  |  |  |  |  |  |  |  |  |
| $<\mathrm{E}_{v}>_{\mathrm{HF}}$ | 1.27 | 1.198 | 0.971 | 0.873 | 0.808 | 0.715 | 0.616 | 0.542 | 0.509 | 0.324 |
| $<\mathrm{E}_{v}>_{\mathrm{HF}}+\mathrm{E}_{\mathrm{CD} 3}\left(v_{2}\right)$ | 1.27 | 1.254 | 1.09 | 1.059 | 1.065 | 1.046 | 1.023 | 1.028 | 1.076 | 0.973 |
| $\mathrm{E}_{\mathrm{c}}=0.3 \mathrm{eV}$ |  |  |  |  |  |  |  |  |  |  |
| $<\mathrm{E}_{v}>_{\mathrm{HF}}$ | 1.23 | 1.143 | 1 | 0.864 | 0.745 | 0.657 | 0.549 | 0.477 | 0.462 | 0.292 |
| $<\mathrm{E}_{v}>_{\mathrm{HF}}+\mathrm{E}_{\mathrm{CD} 3}\left(v_{2}\right)$ | 1.23 | 1.199 | 1.119 | 1.05 | 1.003 | 0.989 | 0.956 | 0.963 | 1.029 | 0.941 |

## A. Numerical parameters

The numerical parameters used in reactant Jacobi coordinates are as following: A total number of 280 sine basis functions covering a range from 3.0 to 19.8 bohrs were used for $R$ with 140 grid points in the interaction region. For the $r$ dimension, 100 basis functions were used in the range of [1.0,11.0] bohrs in the interaction region, while 6 basis functions were used in the asymptotic region. The number of basis functions for the umbrella motion was 16 . The rotational basis functions were constrained by the parameters, $J_{\max }=204, l_{\max }=180, j_{\max }=24$. The center of the prepared Gaussian wave packet was located at $R_{0}=18.0$ bohrs, with the width of $\delta=0.2 \mathrm{bohr}$, and the central energy of $E_{0}=0.15 \mathrm{eV}$. For total angular momentum $J_{\mathrm{tot}}=0$, we propagated the wave packets for 150,000 a.u. of time with a time step of 10 to converge the reaction probabilities. The absorption potential on the $r$ coordinate for the MRPD calculation takes the form

$$
V_{p}(r)=C\left(\frac{r-r^{0}}{\Delta r}\right)^{n},
$$

with $r^{0}=9.0$ a.u., $\Delta r=2.0$ a.u., $C=0.04$, and $n=1.5$. To minimize the computational cost, the coordinate transformation is carried out at every 8 propagation time steps. Continuous propagation in the product Jacobi coordinates only involves a total number of 300 sine functions for the translational coordinate in a range of $[3.0,21.0]$ bohrs and 7 vibrational basis functions for HF bond. The number of basis functions for the umbrella motion was 11 . The rotational basis functions were constrained by the parameters, $J_{\max }^{\prime}=54, l_{\text {max }}^{\prime}=30$, and $j_{\max }^{\prime}=24$. A dividing surface is placed at $R^{\prime}=15.5$ bohr to extract $S$ matrix elements. The number of $K^{\prime}$-blocks included in the product calculation increases with the total angular momentum, from 1 for $J_{\text {tot }}=0$, up to 6 for $J_{\text {tot }}=80$.

