## **Supporting Information**

# Obtaining Giant Rashba-Dresselhaus Spin Splitting in Two-Dimensional Chiral

### **Metal-Organic Frameworks**

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#### **Reduction of reducible representation:**

To compute the characters for the full rotation group, we use the formula 1:

$$\chi^{j}(\alpha) = \frac{\sin((j+1/2)\theta)}{\sin(\theta/2)} \quad (S1)$$

where  $\chi$  is the character of the reducible representation  $\Gamma$ ,  $\theta$  is the rotation angle.

For j = 1/2, 3/2 and 5/2 states, we have:

$$\chi^{1/2}(\theta) = \frac{\sin(\theta)}{\sin(\theta/2)}$$

$$\chi^{3/2}(\theta) = \frac{\sin(2\theta)}{\sin(\theta/2)}$$

$$\chi^{5/2}(\theta) = \frac{\sin(3\theta)}{\sin(\theta/2)}$$
(S2)

#### *C*<sub>2</sub> double group (Table S5):

For the  $E, \bar{E}, C_2, \bar{E}C_2$  symmetry operations of the  $C_2$  double group, the corresponding rotation angle  $\theta$  is 0,  $2\pi, \pi$ ,  $-\pi$ . Substitute into Eq. S2 to get:

$C_2^D$	Ε	$\overline{E}$	$C_2$	$\overline{EC}_2$
$\Gamma^{1/2}$	2	-2	0	0
$\Gamma^{3/2}$	4	-4	0	0
$\Gamma^{5/2}$	6	-6	0	0

Reducible representations can be transformed into direct sums of irreducible representations. The following formula can calculate the number of occurrences of the *i*-th irreducible representation:

$$a_i = \frac{1}{h} \sum_{\hat{R}}^n \chi_i(\hat{R})^* \chi_{\Gamma}(\hat{R})$$
(S3)

where *h* is the order of the group,  $\hat{R}$  is the symmetry operation,  $\chi_i$  is the character of the matrix corresponding to irreducible representation  $\Gamma_i$ , and  $\chi_{\Gamma}$  is the character of the matrix corresponding to reducible representation  $\Gamma$ .

From Eq. S3, Reducible representations  $\Gamma$  is reduced to:

 $\Gamma^{1/2} = \Gamma_3 \oplus \Gamma_4$ 

$$\Gamma^{3/2} = 2\Gamma_3 \oplus 2\Gamma_4 \tag{S4}$$

 $\Gamma^{5/2} = 3\Gamma_3 \oplus 3\Gamma_4$ 

 $D_4$  double group (Table S6):

For the  $E, \bar{E}, C_4, \bar{E}C_4, C_2, \bar{E}C_2$  symmetry operations of the  $D_4$  double group, the corresponding rotation angle  $\theta$  is  $0, 2\pi, \pi/4, -\pi/4, \pi, -\pi$ . Substitute into Eq. S2 to get:

$D_4^D$	Ε	Ē	$2C_{4}$	$2^{\overline{E}C_4}$	$C_2, \overline{E}C_2$	2 <i>C</i> ′ <sub>2</sub> , 2 <i>ĒC</i> ′ <sub>2</sub>	2 <i>C</i> " <sub>2</sub> , 2 <i>ĒC</i> " <sub>2</sub>
$\Gamma^{1/2}$	2	-2	$\sqrt{2}$	- $\sqrt{2}$	0	0	0
$\Gamma^{3/2}$	4	-4	0	0	0	0	0
$\Gamma^{5/2}$	6	-6	- $\sqrt{2}$	$\sqrt{2}$	0	0	0

Similarly, according to Eq. S3, we can reduce the reducible representation to:

$$\Gamma^{1/2} = \Gamma_6$$

$$\Gamma^{3/2} = \Gamma_6 \oplus \Gamma_7 \tag{S5}$$
$$\Gamma^{5/2} = \Gamma_6 \oplus 2\Gamma_7$$

In the case of free atoms, if electron spin is not considered, the effective Hamiltonian symmetry group for the system is the full rotation group O(3), and the *l*-state degeneracy is given by 2(2l + 1). When the spin-orbit coupling is further considered, the effective Hamiltonian symmetry group is the SU(2) group, and the atomic state of the *l*-state will be divided into two energy levels ( $j = l \pm 1/2$ ), each with a degeneracy degree of 2j+1. When this free atom is placed in a surrounding crystal environment with point group symmetry, the Hamiltonian symmetry is reduced to that of the point group symmetry in the environment due to the interaction between the electron and its surroundings. At this time, the original degenerate energy level with a degeneracy of 2j+1 will be further split, and the electronic state will be labeled with an irreducible representation of the point group.

In Fig. 4b, we only consider the *p*-state for the conduction band, which corresponds to l = 1. This state is split into two energy levels, j = 1/2 and 3/2. When the atomic state is placed in a surrounding crystal environment with  $C_2$ double point group symmetry,  $\Gamma^{1/2}$  and  $\Gamma^{3/2}$  can be reduced to  $\Gamma_3 \oplus \Gamma_4$  and  $2\Gamma_3 \oplus 2\Gamma_4$  (Eq. S4) respectively. It is worth mentioning that for the j = 3/2 state (with quadruple degeneracy), it will be decomposed into two  $\Gamma_3 \oplus \Gamma_4$ , which is not fully plotted in Fig. 4b. Regarding the valence band, we only consider the *d*-state (l = 2), which is split into two energy levels, j = 3/2 and 5/2, and the corresponding  $\Gamma^{3/2}$  and  $\Gamma^{5/2}$  can be reduced to  $2\Gamma_3 \oplus 2\Gamma_4$  and  $3\Gamma_3 \oplus 3\Gamma_4$  (Eq. S4). Likewise, the j = 5/2 state (with six-fold degeneracy) and the j = 3/2 state (with quadruple degeneracy), are not fully plotted in Fig. 4b.

In Fig. 4d, we focus on the *p*-state (l = 1) at the conduction band. This state is split into two energy levels j = 1/2and 3/2. In a crystal environment with  $D_4$  double point group symmetry,  $\Gamma^{1/2}$  and  $\Gamma^{3/2}$  can be reduced to  $\Gamma_6$  and  $\Gamma_6 \oplus \Gamma_7$ (Eq. S5) respectively. Regarding the valence band, we only consider the *d*-state (l = 2). This state is divided into two energy levels j = 3/2 and 5/2, and the corresponding  $\Gamma^{3/2}$  and  $\Gamma^{5/2}$  can be reduced to  $\Gamma_6 \oplus \Gamma_7$  and  $\Gamma_6 \oplus 2\Gamma_7$  (Eq. S5) respectively.

#### Basis functions of the double-valued representations:

When the SOC effect is included, the spin-up and down states will be entangled together to form a two-component spinor. Therefore, it is necessary to use the projection operator under the double-valued representations to obtain the basis of the irreducible representations.

To compute the basis functions of the double-valued representations, the projection operator for irreducible representations (IR) can be used:

$$\mathcal{P}^{\Gamma_i} = \frac{l_{\Gamma_i}}{h} \sum_{\hat{R}} \chi_{\Gamma_i}(\hat{R})^* \mathcal{P}_R \mathcal{P}_S \#(S6)$$

where  ${}^{\iota}\Gamma_{i}$  is the dimension of the irreducible representation  $\Gamma_{i}$ , h is the order of the group,  ${}^{\chi}\Gamma_{i}$  is the character of the irreducible representation,  $\hat{R}$  is the symmetry operation,  ${}^{p}R$  and  ${}^{p}s$  correspond to the representation matrices of orbit and spin respectively.<sup>2</sup>

#### Take the D<sub>4</sub> double group as an example: (Table S6)

First, find the spin  $\frac{1}{2}$  *p*-orbital basis of  $\Gamma_6$  IR:

$$\mathcal{P}^{\Gamma_{6}} \begin{bmatrix} p_{x} \\ p_{y} \\ p_{z} \end{bmatrix} \otimes \begin{bmatrix} \uparrow \\ \downarrow \end{bmatrix} = \frac{1}{4} \begin{bmatrix} p_{x}^{\uparrow} \\ p_{y}^{\downarrow} \\ p_{y}^{\uparrow} \\ p_{z}^{\uparrow} \\ p_{z}^{\downarrow} \end{bmatrix} + \frac{1}{4} \begin{bmatrix} ip_{y}^{\uparrow} \\ -ip_{y}^{\downarrow} \\ ip_{x}^{\downarrow} \\ p_{z}^{\uparrow} \\ p_{z}^{\downarrow} \end{bmatrix} \# (S7)$$

From Eq. S7, we find two doubly-degenerate basis of  $\Gamma_6$  IR are:  $\left\{\frac{1}{\sqrt{2}}(p_x + ip_y)\uparrow, \frac{1}{\sqrt{2}}(p_x - ip_y)\downarrow\right\}, \{p_z\uparrow, p_z\downarrow\}$ 

Second, find the spin  $\overline{2}$  *p*-orbital basis of  $\Gamma_7$  IR:

$$\mathcal{P}^{\Gamma_{7}} \begin{bmatrix} p_{x} \\ p_{y} \\ p_{z} \end{bmatrix} \otimes \begin{bmatrix} \uparrow \\ \downarrow \end{bmatrix} = \frac{1}{4} \begin{bmatrix} p_{x}^{\uparrow} \\ p_{y}^{\downarrow} \\ p_{y}^{\downarrow} \\ p_{z}^{\uparrow} \\ p_{z}^{\downarrow} \end{bmatrix} + \frac{1}{4} \begin{bmatrix} -ip_{y}^{\uparrow} \\ ip_{y}^{\downarrow} \\ ip_{x}^{\uparrow} \\ -ip_{x}^{\downarrow} \\ -p_{z}^{\uparrow} \\ -p_{z}^{\downarrow} \end{bmatrix} \# (S8)$$

From Eq. S8, we find one doubly-degenerate basis of  $\Gamma_7$  IR are:  $\left\{\frac{1}{\sqrt{2}}(p_x + ip_y)\uparrow, \frac{1}{\sqrt{2}}(p_x - ip_y)\downarrow\right\}$ 

Third, find the spin  $\overline{2}$  *d*-orbital basis of  $\Gamma_6$  IR:

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$$\mathcal{P}^{\Gamma_{6}}\begin{bmatrix} d_{z^{2}} \\ d_{xz} \\ d_{yz} \\ d_{x^{2}-y^{2}} \\ d_{xy} \end{bmatrix} \otimes \begin{bmatrix} \uparrow \\ \downarrow \end{bmatrix} = \frac{1}{2} \begin{bmatrix} d_{z^{2}} \\ d_{z^{2}} \downarrow \\ (d_{xz} - id_{yz})\uparrow \\ (d_{yz} - id_{xz})\uparrow \\ (d_{yz} + id_{xz})\downarrow \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} \#(S9)$$

From Eq. S9, we find two doubly-degenerate basis of  $\Gamma_6$  IR are:  $\{d_{z^2}\uparrow, d_{z^2}\downarrow\}$ ,  $\left\{\frac{1}{\sqrt{2}}(d_{xz}+id_{yz})\uparrow,\frac{1}{\sqrt{2}}(d_{xz}-id_{yz})\downarrow\right\}$ 

Last, find the spin  $\frac{1}{2}$  *d*-orbital basis of  $\Gamma_7$  IR:

$$\mathcal{P}^{\Gamma_{7}}\begin{bmatrix} d_{z^{2}}\\ d_{xz}\\ d_{yz}\\ d_{yz}\\ d_{xy} \end{bmatrix} \otimes \begin{bmatrix} \uparrow \\ \downarrow \end{bmatrix} = \frac{1}{4} \begin{bmatrix} 0\\ (d_{xz} - id_{yz})\uparrow\\ (d_{yz} + id_{xz})\uparrow\\ (d_{yz} - id_{xz})\downarrow\\ d_{x^{2} - y^{2}\uparrow}\\ d_{x^{2} - y^{2}\downarrow}\\ 2d_{xy}\uparrow\\ 2d_{xy}\downarrow \end{bmatrix} \#(S10)$$

From Eq. S10, we find three doubly-degenerate basis of  $\Gamma_7$  IR are:  $\left\{\frac{1}{\sqrt{2}}(d_{xz} + id_{yz})\uparrow, \frac{1}{\sqrt{2}}(d_{xz} - id_{yz})\downarrow\right\}$  $\left\{d_{x^2-y^2}^{\uparrow,d}d_{x^2-y^2}^{\downarrow}\right\}$ ,  $\left\{d_{xy}^{\uparrow,d}d_{xy}^{\downarrow}\right\}$ 

Note S2. A possible route for the experimental synthesis

Here, we provide a possible route for the experimental synthesis of 2D chiral MOFs  $OsH_2(bipyridine_X_Y)$ , where bipyridine\_X\_Y represents a series of axially chiral ligands 4,4'-bipyridines.<sup>3</sup>

MOF nanosheets can be synthesized via the bottom-up method.<sup>4</sup> The bottom-up method aims to synthesize MOF nanosheets using metals and organic precursors directly. In this process, the vertical directional growth is restricted while the lateral direction is not affected. The corresponding methods include interfacial synthesis,<sup>5</sup> three-layer synthesis,<sup>6</sup> surfactant-assisted synthesis,<sup>7</sup> modulated synthesis,<sup>8</sup> and sonication synthesis, etc.<sup>9</sup>

For our OsH<sub>2</sub>(bipyridine\_X\_Y) nanosheets, first, the laser-ablated Os atoms and H<sub>2</sub> react in pure H<sub>2</sub> and solid neon/argon matrixes. Osmium atom reactions with hydrogen in excess neon/argon produce OsH<sub>2</sub> molecule.<sup>10</sup>

Next, the bipyridine\_X\_Y molecules and the  $OsH_2$  are transferred onto an appropriate substrate (e.g., Si wafer)<sup>11</sup> by molecular layer deposition (MLD).<sup>12</sup> The bipyridine\_X\_Y molecules will form coordination complexes with the  $OsH_2$  molecule. By adjusting the temperature, the metal-ligand ratio can be precisely controlled.<sup>13</sup>

Finally, after an annealing process under strict humidity control conditions, self-assembly takes place on the surface of the substrate to form the target MOF OsH<sub>2</sub>(bipyridine\_X\_Y) with a specific structure.<sup>14,15</sup>



Fig. S1. Phonon spectra of OsH<sub>2</sub>(bipyridine\_CN) computed with (a)  $2 \times 2 \times 1$ , and (b)  $3 \times 3 \times 1$  supercells, respectively. The calculation shows that the maximum imaginary frequency is reduced from 1.16 cm<sup>-1</sup> with a  $2 \times 2 \times 1$  supercell to 0.78 cm<sup>-1</sup> with a  $3 \times 3 \times 1$  supercell. These unphysically small imaginary frequencies are caused by size and boundary effects, and a similar phenomenon has also been observed in other reported MOFs [*J. Am. Chem. Soc.*, 2023, **145**, 7869–7878; *Nano Lett.*, 2022, **22**, 1573–1579; *J. Am. Chem. Soc.*, 2023, **145**, 2485–2491]. These small imaginary frequencies can theoretically be eliminated in larger supercells. Nevertheless, using supercells larger than  $3 \times 3 \times 1$  significantly increases the computing resources; hence, we only calculate phonon spectra with  $3 \times 3 \times 1$  supercells.



Fig. S2. The total potential energy fluctuations of  $OsH_2$ (bipyridine\_CN) during ab initio molecular dynamics simulations using a  $2 \times 2 \times 1$  supercell at 600K.



Fig. S3. HSE06+SOC band structure of 2D OsH<sub>2</sub>(bipyridine\_CN).



Fig. S4. (a) Possible path and energy barrier for the transition from structure **RR** to **RS** and **RS** to **SS**. (b) Different chirality of ligands in the structure of OsH<sub>2</sub>(bipyridine\_CN). Band structures calculated with (c) PBE+SOC of OsH<sub>2</sub>(bipyridine\_CN). The spin texture of (d) upper and lower Rashba bands in the VB of OsH<sub>2</sub>(bipyridine\_CN).



Fig. S5. R-D band splitting and spin texture schematic diagram: (a) three-dimensional view. (b) two-dimensional view,  $\Delta E$  is the energy difference between the energies of the peak and the degenerate energy at the high symmetry point, and  $k_0$  is the momentum offset between the peak and the high symmetry point. (c) spin texture characteristic of the Rashba splitting (R-type) and (d) the Dresselhaus splitting (D-type) in the  $k_x$ - $k_y$  plane, in which  $E_+$  ( $E_-$ ) denotes the upper (lower) branch, meanwhile the red (blue) color represents the positive (negative) spin component  $s_y$ .

Table S1.	Parameters	of CMOFs	materials	being	calculated	in	Step I	: material	type,	space	group,	band	gap
$F^{PBE} + SOC$	2												

$\Delta g$ , and $\Delta E$ in the valence band or conduction band (CB) at the	e l'point.	
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Material	Non-magnetic semiconductor	Space group	$E^{PBE + SOC}_{g}$ (eV)	$\Delta E (\mathrm{meV})$
SrCl <sub>2</sub> (bipyridine_I)	Yes	C2	2.19	0.35
YCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
ZrCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
NbCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
MoCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
TcCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
RuCl <sub>2</sub> (bipyridine_I)	Yes	<i>C</i> 2	1.45	0.50
RhCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
PdCl <sub>2</sub> (bipyridine_I)	Yes	<i>C</i> 2	0.74	0.02(CB)
AgCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
CdCl <sub>2</sub> (bipyridine_I)	Yes	C2	2.53	0.15
SnCl <sub>2</sub> (bipyridine_I)	Yes	<i>C</i> 2	0.99	0.01
BaCl <sub>2</sub> (bipyridine_I)	Yes	C2	1.85	0.02
HfCl <sub>2</sub> (bipyridine_I)	Metal	-	-	-
TaCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
WCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
ReCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
OsCl <sub>2</sub> (bipyridine_I)	Yes	<i>C</i> 2	1.2	3.20
IrCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
PtCl <sub>2</sub> (bipyridine_I)	Yes	<i>C</i> 2	0.42	0.35(CB)

AuCl <sub>2</sub> (bipyridine_I)	Magnetic	-	-	-
HgCl <sub>2</sub> (bipyridine_I)	Yes	<i>C</i> 2	2.45	0.05
PbCl <sub>2</sub> (bipyridine_I)	Yes	<i>C</i> 2	1.54	0.10

**Table S2.** Parameters of CMOFs materials being calculated in Step II: space group, band gap  $E^{PBE + SOC}$ , the symmetry at  $\Gamma$  in the VB and CB,  $\Delta E$ , and the R-D coupling constant  $\alpha$  in the valence band at the  $\Gamma$  point.

5 5		1 0			1
Material	Space group	$E^{PBE + SOC}_{g}$ (eV)	Same symmetry	$\Delta E ({\rm meV})$	α (eVÅ)
OsI <sub>2</sub> (bipyridine_I)	<i>C</i> 2	1.46	No	2.6	0.05
OsBr <sub>2</sub> (bipyridine_I)	<i>C</i> 2	1.34	No	0.8	0.05
OsCl <sub>2</sub> (bipyridine_I)	<i>C</i> 2	1.20	No	3.2	0.12
OsF <sub>2</sub> (bipyridine_I)	<i>C</i> 2	0.64	Yes	11.5	0.38
Os(CN) <sub>2</sub> (bipyridine_I)	<i>C</i> 2	1.30	Yes	34.9	0.48
OsH <sub>2</sub> (bipyridine_I)	<i>C</i> 2	0.88	Yes	43.5	0.73

**Table S3.** Parameters of CMOFs materials being calculated in Step III: space group, band gap  $E^{PBE + SOC}_{g}$ , the symmetry at  $\Gamma$  in the VB and CB,  $\Delta E$ , and the R-D coupling constant  $\alpha$  in the valence band at the  $\Gamma$  point.

Material	Space group	$E^{PBE + SOC}_{g}$ (eV)	Same symmetry	$\Delta E (\mathrm{meV})$	α (eVÅ)
OsH <sub>2</sub> (bipyridine_CH <sub>3</sub> _I)	<i>P</i> 1	1.20	Yes	3.9	0.17
OsH <sub>2</sub> (bipyridine_CH <sub>3</sub> _NH <sub>2</sub> )	<i>P</i> 1	1.10	Yes	16.6	0.42
OsH <sub>2</sub> (bipyridine_NH <sub>2</sub> )	<i>C</i> 2	0.92	Yes	39.7	0.80
OsH <sub>2</sub> (bipyridine_I)	<i>C</i> 2	0.88	Yes	43.5	0.73
OsH <sub>2</sub> (bipyridine_Br)	<i>C</i> 2	0.84	Yes	59.8	0.87
OsH <sub>2</sub> (bipyridine_CH <sub>3</sub> )	<i>C</i> 2	0.83	Yes	61.8	0.90
OsH <sub>2</sub> (bipyridine_CF <sub>3</sub> )	<i>C</i> 2	0.82	Yes	51.2	0.80
OsH <sub>2</sub> (bipyridine_Cl)	<i>C</i> 2	0.81	Yes	71.0	0.98
OsH <sub>2</sub> (bipyridine_OH)	<i>C</i> 2	0.72	Yes	80.9	1.26
OsH <sub>2</sub> (bipyridine_F)	<i>C</i> 2	0.63	No	82.1	1.32
OsH <sub>2</sub> (bipyridine_CCH)	<i>C</i> 2	0.65	Yes	94.0	1.33
OsH <sub>2</sub> (bipyridine_H)	P422	0.52	No	88.5	1.33
OsH <sub>2</sub> (bipyridine_CN)	<i>C</i> 2	0.60	Yes	97.2	1.37

**Table S4.** Parameters of CMOFs materials being calculated: material type,  $\Delta E$ , and the R-D coupling constant  $\alpha$  in the valence band at the  $\Gamma$  point.

Material	Non-magnetic semiconductor	$\Delta E (\mathrm{meV})$	α (eVÅ)
RuCl <sub>2</sub> (bipyridine_I)	Yes	0.5	0.04
RuH <sub>2</sub> (bipyridine_CN)	Yes	14.8	0.59

**Table S5.** Character table for the single and double group representatives of  $C_2$  point group and the corresponding basis functions, given for the high symmetry k point  $\Gamma$  in  $C_2$  Brillouin zone.

<i>C</i> <sub>2</sub>	Е	<i>C</i> <sub>2</sub>	Linear functions rotations	Quadratic functions
A	1	1	$z, R_z$	$x^2, y^2, z^2, xy$

В	1	-1	$x, y, R_x, R_y$	yz, xz
$C_2^D$	Ε	$\overline{E}$	$C_2$	$\overline{EC}_2$
$\Gamma_1$	1	1	1	1
$\Gamma_2$	1	1	-1	-1
$\Gamma_3$	1	-1	i	-i
$\Gamma_4$	1	-1	-i	i

**Table S6.** Character table for the single and double group representatives of  $D_4$  point group and the corresponding basis functions, given for the high symmetry k point  $\Gamma$  in P422 Brillouin zone.

$D_4$	Ε	$2C_{4}$	<i>C</i> <sub>2</sub>	2 <i>C</i> ′ <sub>2</sub>	2 <i>C</i> ″ <sub>2</sub>	Linear functions rotations	Quadratic functions
$A_1$	1	1	1	1	1		$x^{2+}y^{2}, z^{2}$
$A_2$	1	1	1	-1	-1	$z, R_z$	Ζ
$B_1$	1	-1	1	1	-1		$x^2 - y^2$
<i>B</i> <sub>2</sub>	1	-1	1	-1	1		xy
E	2	0	-2	0	0	$(x, y) (R_x, R_y)$	(xz, yz)
$D_4^D$	Ε	$\overline{E}$	$2C_{4}$	$2^{\overline{E}C_4}$	$C_2, \overline{E}C_2$	2 <i>C</i> ′ <sub>2</sub> , 2 <i>ĒC</i> ′ <sub>2</sub>	2 <i>C</i> " <sub>2</sub> , 2 <i>ĒC</i> " <sub>2</sub>
$\Gamma_1$	1	1	1	1	1	1	1
$\Gamma_2$	1	1	1	1	1	-1	-1
$\Gamma_3$	1	1	-1	-1	1	1	-1
$\Gamma_4$	1	1	-1	-1	1	-1	1
Γ <sub>5</sub>	2	2	0	0	-2	0	0
$\Gamma_6$	2	-2	$\sqrt{2}$	- $\sqrt{2}$	0	0	0
Γ <sub>7</sub>	2	-2	- $\sqrt{2}$	$\sqrt{2}$	0	0	0

Table S7. The proportion of heavy elements in the valence band.

Material	Os	Ι
OsI <sub>2</sub> (bipyridine_I)	0.43	0.16
OsBr <sub>2</sub> (bipyridine_I)	0.50	0.003
OsCl <sub>2</sub> (bipyridine_I)	0.54	0.002
OsF <sub>2</sub> (bipyridine_I)	0.55	0.004
Os(CN) <sub>2</sub> (bipyridine_I)	0.58	0.002
OsH <sub>2</sub> (bipyridine_I)	0.65	0.003

**Table S8.** Effects of strong field ligands on R-D spin splitting. Here  $E^{PBE + SOC}_{g}$  is the band gap,  $\Delta E$  is the R-D energy of spin splitting, and  $\alpha$  is the R-D coupling constant.

°P'	spinning, and a is the relief of apping constants					
	Material	$E^{PBE + SOC}_{g}$ (eV)	$\Delta E ({\rm meV})$	$\alpha$ (eVÅ)		
-	Os(NCS) <sub>2</sub> (bipyridine_I)	1.56	8.9	0.11		
	Os(NO <sub>2</sub> ) <sub>2</sub> (bipyridine_I)	1.69	13.0	0.28		
	Os(PH <sub>3</sub> ) <sub>2</sub> (bipyridine_I)	Metal	-	-		
	Os(CN) <sub>2</sub> (bipyridine_I)	1.30	34.9	0.48		
	Os(CO) <sub>2</sub> (bipyridine_I)	Metal	-	-		

The spectrochemical sequence for these strong field ligands is  $NCS^- < NO_2^- < PH_3 < CN^- < CO$ . The

calculation results show that the energy of spin splitting increases as the ligand field strength increases (see Table S8). Unfortunately, when the ligands are neutral molecules ( $PH_3$  and CO), the system is metallic and does not meet our conditions.

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