## Nucleation-enhanced condensation and fast shedding

## on self-lubricated silicone organogels

## **Supplementary Information**

Nicolas Lavielle\*, Daniel Beysens and Anne Mongruel

Physique et Mécanique des Milieux Hétérogènes, CNRS, ESPCI, PSL Research University, Sorbonne Université, Sorbonne Paris Cité, 75005 Paris, France

Corresponding author: nicolas.lavielle@espci.fr

## Supplementary note: Calculation of the amplitude constants A and E.

Inspired by references [40] and [42], the calculation of the amplitude constants *A* (condensation) and *E* (evaporation) can be expressed as follows:

$$A = E = \frac{4D(c_{\infty} - c_s)f(\Theta)}{3\rho_w sin\Theta \ G(\Theta)}$$

With:

$$f(\Theta) = \frac{1}{2}(0.00008957 + 0.6333\Theta + 0.116\Theta^2 - 0.08878\Theta^3 + 0.01033\Theta^4)$$

and

$$G(\Theta) = \frac{2 - 3\cos\Theta + \cos\Theta^3}{3\sin\Theta^3}$$

*D* being the diffusion coefficient of water;  $c_{\infty}, c_s$  the concentration of water monomers far and on the drop surface, respectively;  $\rho_w$ , the water density and  $\Theta$ , the dynamic contact angle equal to  $\Theta_a$  (advancing contact angle) in the case of the condensation and to  $\Theta_r$  (receding contact angle) in the case of the evaporation.

As condensation ( / evaporation) experiments on iPDMS, PDMS and Si were performed in the same conditions, the only varying parameter is the geometrical argument (i.e.  $f(\Theta)$ ,  $G(\Theta)$  and  $sin\Theta$ ) and the respective ratios of A and E were calculated and compared to the experimental values:

	PDMS	iPDMS	Si		theo.	exp.
<i>O</i> a (°)	120	105	75	A <sub>iPDMS</sub> /A <sub>PDMS</sub>	1.4	3.8
<b>Ø</b> r (°)	60	105	55	A <sub>iPDMS</sub> /A <sub>Si</sub>	0.6	1.2
A <sub>theo.</sub> (μm²/s)	0.41	0.57	0.97	E <sub>iPDMS</sub> /E <sub>PDMS</sub>	0.5	0.5
<i>E<sub>theo.</sub></i> (μm <sup>2</sup> /s)	1.26	0.57	1.39	E <sub>iPDMS</sub> /E <sub>si</sub>	0.4	0.2

Table 1: Advancing / receding contact angles, theoretical amplitude constants (A for condensation, *E* for evaporation) and comparison between theoretical and experimental amplitude constants ratios for PDMS, iPDMS and Si.



**Supplementary Figure S1: Droplet growth on PDMS horizontal surfaces:** Typical radius evolution of a single droplet on PDMS with time (coalescence events are indicated by red arrows).



Material	t <sub>evap</sub> (s)	<i>Ε</i> (μm²/s)	
iPDMS	1100	324	
PDMS	950	625	
Si	530	1369	

Supplementary Figure S2: Evaporation of a deposited droplet on iPDMS, PDMS and Si surfaces: a) Radius evolution of  $0.5\mu$ L water droplet as function of time ( $t_0$ -t, with  $t_0$  the time of droplet disappearance). b) Time needed for the water droplet to completely evaporate and related values of *E*.



Supplementary Figure S3: Normalized radius distribution of condensed water droplets on horizontal surfaces: Evolution of the number of droplets, *N*, of radius *r*, for (a) PDMS and (b) iPDMS with 5.4 $\mu$ m oil thickness. Normalized size distribution for PDMS and iPDMS with various oil thicknesses at (c) 500 s and (d) 1000 s. (Step of 20  $\mu$ m).

@1000s



**Supplementary Figure S4**: **Microscope images for PDMS, iPDMS (0.25, 0.5 and 1.4um)**: Corresponding threshold images at 1000 s of condensation. The periphery of each droplet is well defined and only a few (2 or 3) drops display a visible wetting ridge for iPDMS 1.4um.



**Supplementary Figure S5**: Microscope image for iPDMS 5.4um at 1000s of condensation: Comparison of the corresponding image analysis with low, medium and high threshold for removing the influence of the wetting ridge in the determination of the drop volumes.