

# New RM734-like Fluid Ferroelectrics Enabled through a Simplified Protecting Group Free Synthesis

## Supplemental Information

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## 1 Experimental Methods

### 1.1. Chemical Synthesis

Chemicals were purchased from commercial suppliers (Fluorochem, Merck) and used as received. Solvents were purchased from Merck and used without further purification. Reactions were performed in standard laboratory glassware at ambient temperature and atmosphere and were monitored by TLC with an appropriate eluent and visualised with 254 nm light. Chromatographic purification was performed using a Combiflash NextGen 300+ System (Teledyne Isco) with a silica gel stationary phase and a hexane/ethyl acetate gradient as the mobile phase, with detection made in the 200-800 nm range. Chromatographed materials were subjected to re-crystallisation from an appropriate solvent system.

### 1.2 Chemical Characterisation Methods

The structures of intermediates and final products were determined using <sup>1</sup>H, <sup>13</sup>C{<sup>1</sup>H}, and, where appropriate, <sup>19</sup>F NMR spectroscopy. NMR was performed using a Bruker Avance III HDNMR spectrometer operating at 400 MHz, 100.5 MHz or 376.4 MHz (<sup>1</sup>H, <sup>13</sup>C{<sup>1</sup>H} and <sup>19</sup>F, respectively).

### 1.3 Mesophase Characterisation

Characterisation of the translational properties of compounds **1-11** were determined by differential scanning calorimetry (DSC) using a TA instruments Q200 heat flux calorimeter with a liquid nitrogen cooling system for temperature control. Samples were measured under a nitrogen atmosphere with 20 °C min<sup>-1</sup> heating and cooling rates. The transition temperatures

and enthalpy values reported are averages obtained for duplicate runs and normally extracted from heating traces. Phase identification by polarised optical microscopy (POM) was performed using a Leica DM 2700 P polarised optical microscope equipped with a Linkam TMS 92 heating stage. Samples were studied sandwiched between two untreated glass coverslips.

#### 1.4 Simulation Setup and Analysis

Fully atomistic molecular dynamics (MD) simulations were performed in Gromacs 2019, [1–7] with parameters modelled using the General Amber Force Field (GAFF). [8] Atomic charges were determined using the RESP method [9] for geometry optimised at the B3LYP/6-31G(d) level of DFT [10,11] using the Gaussian G16 revision c01 software package. [12] Topologies were generated using AmberTools 16 [13,14] and converted into Gromacs readable format with Acpye. [15]

We initially constructed a low density lattice of 600 molecules of **10** with random positional and orientational order. Following energy minimization by the steepest decent method we performed short (5 ns) equilibration simulations in the NVE and NVT (T = 600 K) ensembles. We then performed a short ‘compression’ simulation (25 ns) at 600K with an isotropic barostat (P = 100 Bar) to compress the simulation to a liquid like density (~ 1.1 g cm<sup>3</sup>). We then obtained a *polar* nematic configuration by applying a static electric field (1 V nm<sup>-1</sup>) along the x-axis of the isotropic starting configuration for a total of 100 ns at 413 K and 1 Bar; this configuration was used as a starting point for subsequent simulations. Production MD simulations were performed without the biasing field and employed an anisotropic barostat (pressure of 1 Bar), at temperatures of 413 – 513 K in 10 K increments for a further 250 ns, unless otherwise noted.

Simulations employed periodic boundary conditions in xyz. Bonds lengths were constrained to their equilibrium values with the LINCS algorithm [16]. During production MD simulations the system pressure was maintained at 1 Bar using an isotropic Parrinello-Raham barostat. [17,18] Compressibilities in xyz dimensions were set to 4.5e-5, with the off-diagonal compressibilities were set to zero to ensure the simulation box remained rectangular. Simulation temperature was controlled with a Nosé–Hoover thermostat. [19,20] Long-range electrostatic interactions were calculated using the Particle Mesh Ewald method with a cut-off value of 1.2 nm. A van der Waals cut-off of 1.2 nm was used. MD trajectories were visualised using PyMOL 4.5. Q-tensor analysis was performed using MDTraj 1.9.8. [21] Cylindrical distribution functions (CDF) were computed using the *cylindr* code. [22] Simulation densities, dipole moments and volumes were obtained with the *gmx energy* program, with dipole and volume being used to compute spontaneous polarisation.

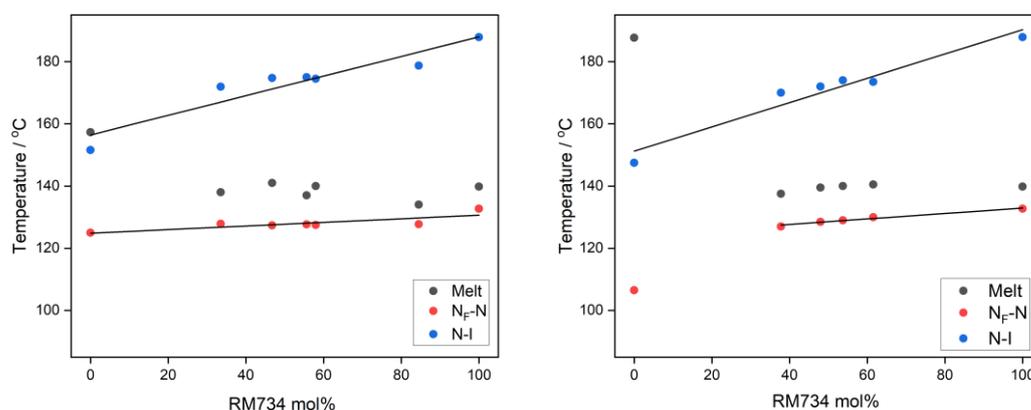
We calculate the second-rank orientational order parameter  $\langle P_2 \rangle$  via the Q-tensor according to equation (1);

$$Q_{\alpha\beta} = \frac{1}{N} \sum_{m=1}^N \frac{3a_{m\alpha}a_{m\beta} - \delta_{\alpha\beta}}{2} \quad (1)$$

where N is the number of monomers, m is the monomer number within a given simulation,  $\alpha$  and  $\beta$  represent the Cartesian x, y and z axes, delta is the Kronecker delta, *a* is a vector that describes the molecular long axis, which is computed for each monomer as the eigenvector associated with the smallest eigenvalue of the inertia tensor. The director at each frame was defined as the eigenvector associated with the largest eigenvalue of the ordering tensor. The order parameter  $\langle P_2 \rangle$  corresponds to the largest eigenvalue of  $Q_{\alpha\beta}$ , and the biaxial order

parameter  $\langle B \rangle$  corresponds to the difference between the two smallest eigenvalues. The polar order parameter,  $\langle P1 \rangle$ , was calculated as the total dipole moment of the simulation box over the sum of the individual molecular dipoles. The polarization,  $P$ , was calculated from the total dipole of the box over the volume.

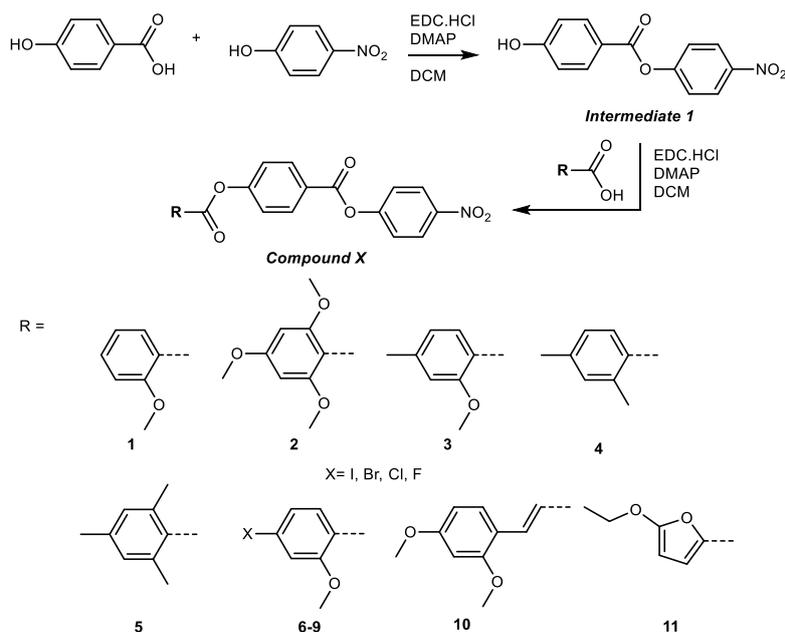
## 2 Supplemental Results



**SIFig. 1** Phase diagram for the mixture of compound **3** (left) and compound **6** (right) with RM734.

## 3 Chemical synthesis

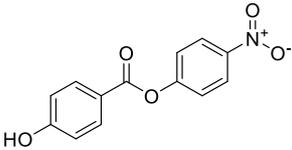
Compounds **1-11** were synthesised as outlined in SIScheme 1.



**SIScheme 1:** Synthesis of the RM734 derivatives, Compounds **1-11**.

## 2.1 Synthesis of 4-nitrophenyl 4-hydroxybenzoate (Intermediate 1)

A round bottomed flask was charged with 4-nitro phenol (10.0 g, 0.072 mol, 1 eqv.), 4-hydroxy benzoic acid (9.83 g, 0.072 mol, 1.0 eqv), EDC.HCl (20.7 g, 0. 108 mol, 1.5 eqv.) and DMAP (2 mol%). Dichloromethane was added (conc. ~ 0.1 M) and the suspension stirred until complete consumption of the phenol as judged by TLC. The volatiles were removed in vacuo and the crude material was subjected to flash chromatography over silica gel with a gradient of hexane/EtOAc. Intermediate 1 was then recrystallized from EtOH and dried under reduced pressure overnight to give the reported yield.

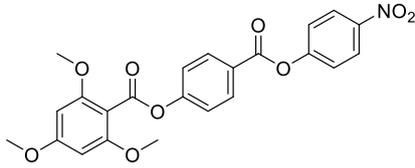
 Intermediate 1	
White powder	10.8 g, 58 %
R <sub>f</sub> (EtOAc): 0.68	
<sup>1</sup> H NMR (400 MHz, DMSO-d <sub>6</sub> ) (δ)	10.64 (s, 1H, Ar-OH), 8.33 (d, J = 8.9 Hz 2H, Ar-H), 8.01 (d, J = 8.1 Hz, 2H, Ar-H), 7.57 (d, J = 8.9 Hz, 2H, Ar-H), 6.94 (dd, J = 8.1, Hz, 2H, Ar-H).
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, DMSO-d <sub>6</sub> ) (δ)	164.10, 163.57, 156.26, 145.40, 132.99, 126.63, 123.80, 119.03, 116.18.

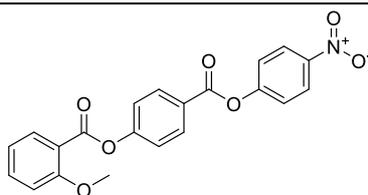
## 2.2 Synthesis of Compounds 1-11

A round bottomed flask was charged with 4-nitrophenyl 4-hydroxybenzoate (1 eqv.), the appropriate carboxylic acid (1.5 eqv), EDC.HCl (1.5 eqv.) and DMAP (2 mol%). Dichloromethane was added (conc. ~ 0.1 M) and the suspension stirred until complete consumption of the phenol as judged by TLC. The volatiles were removed in vacuo and the crude material was subjected to flash chromatography over silica gel with a gradient of hexane/DCM. The materials were subsequently recrystallized from EtOH before being dried under reduced pressure to give the reported yields. The quantities and masses of the reagents used are given in SITable 1.

**SITable 1:** Quantities and masses of the reagents used in the synthesis of Compounds 1-11.

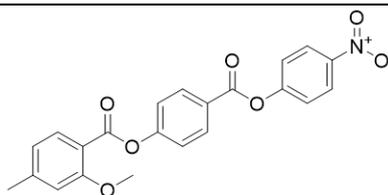
Compound	Benzoic acid used	Quantity of benzoic acid		Quantity of 4-nitrophenyl 4-hydroxybenzoate		Quantity of EDC.HCl		Quantity of DMAP	
		mg	mmol	mg	mmol	mg	mmol	mg	mmol
1	2,4,6-Trimethoxybenzoic acid	123	0.58	100	0.38	111	0.58	0.9	0.01
2	2-Methoxybenzoic Acid	88	0.58	100	0.38	111	0.58	0.9	0.01
3	2-Methoxy-4-methylbenzoic acid	96	0.58	100	0.38	111	0.58	0.9	0.01
4	2,4-Dimethylbenzoic acid	87	0.58	100	0.38	111	0.58	0.9	0.01
5	2,4,6-Trimethylbenzoic acid	95	0.58	100	0.38	111	0.58	0.9	0.01
6	4-Iodo-2-methoxybenzoic acid	161	0.58	100	0.38	111	0.58	0.9	0.01
7	4-Bromo-2-methoxybenzoic acid	134	0.58	100	0.38	111	0.58	0.9	0.01
8	4-Chloro-2-methoxybenzoic acid	108	0.58	100	0.38	111	0.58	0.9	0.01
9	4-Fluoro-2-methoxybenzoic acid	99	0.58	100	0.38	111	0.58	0.9	0.01
10	3-(2,4-Dimethoxyphenyl)acrylic acid	121	0.58	100	0.38	111	0.58	0.9	0.01
11	5-ethoxy-2-furoic acid	45	0.29	50	0.19	56	0.29	0.5	0.01

 <p>Compound 1</p>			
Appearance	White needles	135 mg, 78 %	
Melting Point	181.9 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.19
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.34 (d, J = 9.0 Hz, 2H, Ar-H), 8.25 (d, J = 8.8 Hz, 2H, Ar-H), 7.46 – 7.39 (m, 6H, Ar-H), 3.89 (s, 6H, 2x Ar-O-CH <sub>3</sub> (positions 2 & 6)), 3.86 (s, 3H, Ar-O-CH <sub>3</sub> (position 4)).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	168.51, 164.58, 163.01, 162.11, 156.08, 155.90, 155.04, 145.47, 131.95, 125.87, 125.82, 125.31, 122.67, 122.43, 104.42, 56.15, 55.55		



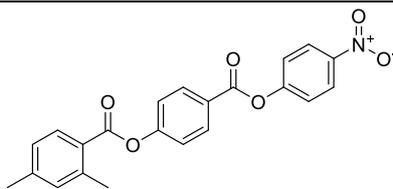
Compound 2

Appearance	White powder	105 mg, 88 %	
Melting Point	136.4 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.58
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	10.53 (s, 1H, Ar-H), 8.35 (d J = 9.1 Hz, 2H, Ar-H), 8.30 (d, J = 8.8 Hz, 2H, Ar-H), 7.98 (d, J = 8.8 Hz, 1H, Ar-H), 7.48 – 7.35 (m, 4H, Ar-H), 6.61 – 6.49 (m, 2H, Ar-H), 3.88 (s, 3H, Ar-O-CH <sub>3</sub> ).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	163.59, 163.49, 160.22, 155.80, 155.68, 145.48, 134.93, 132.39, 131.97, 125.85, 125.32, 122.67, 122.44, 120.32, 118.20, 112.30, 56.09.		



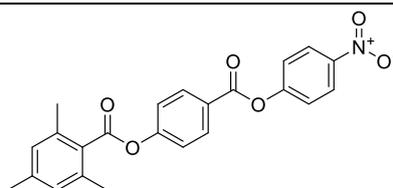
Compound 3

Appearance	White Powder	108 mg, 70 %	
Melting Point	157.3 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.18
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.34 (d, J = 9.2 Hz, 2H, Ar-H), 8.26 (dd, J = 8.8 Hz, 2H, Ar-H), 7.98 (d, J = 7.8 Hz, 1H, Ar-H), 7.46 – 7.37 (m, 4H, Ar-H), 6.92 – 6.83 (m, 2H, Ar-H), 3.95 (s, 3H, Ar-O-CH <sub>3</sub> ), 2.45 (s, 3H, Ar-CH <sub>3</sub> ).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	163.62, 163.31, 160.49, 155.92, 155.70, 146.36, 145.47, 132.54, 131.92, 125.70, 125.31, 122.67, 122.49, 121.19, 115.12, 113.01, 56.02, 22.15.		



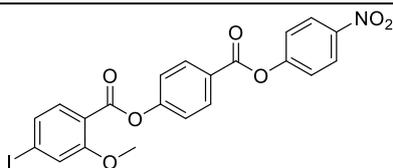
Compound 4

Appearance	White powder	107 mg, 72 %	
Melting Point	151.1 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.48
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.34 (d, J = 9.0 Hz, 2H, Ar-H), 8.28 (dd, J = 8.8 Hz, 2H, Ar-H), 8.10 (d, J = 8.4 Hz, 1H, Ar-H), 7.42 (m, 4H, Ar-H), 7.20 – 7.11 (m, 2H, Ar-H), 2.66 (s, 3H, Ar-CH <sub>3</sub> (position 2)), 2.42 (s, 3H, Ar-CH <sub>3</sub> (position 4)).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	165.44, 163.57, 155.84, 155.67, 145.49, 144.11, 141.96, 132.98, 132.02, 131.53, 126.83, 125.86, 125.32, 124.81, 122.66, 122.48, 22.03, 21.56.		



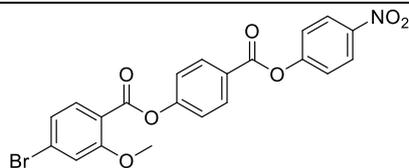
Compound 5

Appearance	White powder	120 mg, 78 %	
Melting Point	137.8 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.39
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.34 (d, J = 9.1 Hz, 2H, Ar-H), 8.29 (dd, J = 8.7 Hz, 2H, Ar-H), 7.50 – 7.38 (m, 4H, Ar-H), 6.95 (m, 2H, Ar-H), 2.47 (s, 6H, 2x Ar-CH <sub>3</sub> (positions 2 & 6)), 2.34 (s, 3H Ar-CH <sub>3</sub> (positions 4)).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	167.61, 163.47, 155.62, 155.46, 145.51, 140.56, 135.91, 132.14, 129.15, 128.87, 126.15, 125.33, 122.66, 122.15, 21.24, 20.16.		



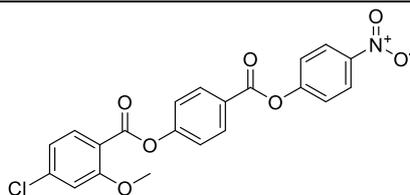
Compound 6

Appearance	White powder	158 mg, 81 %	
Melting Point	187.7 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.34
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.34 (d J = 9.2 Hz, 2H, Ar-H), 8.30 – 8.24 (m, 2H, Ar-H), 7.74 (d, J = 8.2 Hz, 1H, Ar-H), 7.46 – 7.37 (m, 6H, Ar-H), 3.96 (s, 3H, Ar-O-CH <sub>3</sub> ).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	163.53, 163.01, 160.12, 155.65, 155.55, 145.50, 133.30, 132.00, 129.79, 126.01, 125.33, 122.65, 122.35, 121.97, 117.77, 101.86, 56.43.		



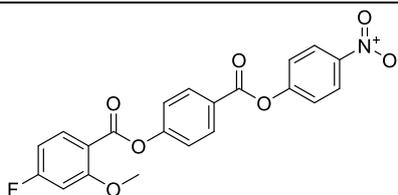
Compound 7

Appearance	White powder	133 mg, 74 %	
Melting Point	180.0 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.28
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.34 (d J = 9.2 Hz, 2H, Ar-H), 8.27 (d, J = 8.9 Hz, 2H, Ar-H), 7.93 (d, J = 8.8 Hz, 1H, Ar-H), 7.42 (m, 4H, Ar-H), 7.25 – 7.21 (m, 2H, Ar-H), 3.97 (s, 3H, Ar-O-CH <sub>3</sub> ).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	163.53, 162.80, 160.63, 155.65, 155.55, 145.50, 133.51, 132.00, 129.41, 126.01, 125.33, 123.68, 122.65, 122.35, 117.10, 116.01, 56.44.		



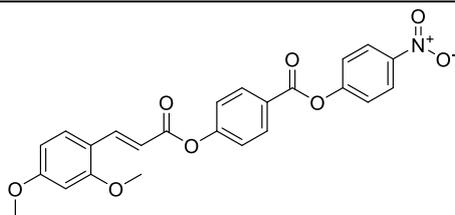
Compound 8

Appearance	White powder	135 mg, 83 %	
Melting Point	173.6 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.22
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.33 (d J = 9.1 Hz, 2H, Ar-H), 8.27 (d, J = 8.8 Hz, 2H, Ar-H), 8.04 – 7.98 (m, 1H, Ar-H), 7.46 – 7.36 (m, 4H, Ar-H), 7.10 – 7.02 (m, 2H, Ar-H), 3.96 (s, 3H, Ar-O-CH <sub>3</sub> ).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	163.52, 162.66, 160.83, 155.65, 155.57, 145.49, 141.02, 133.50, 131.99, 125.99, 125.32, 122.65, 122.37, 120.68, 116.62, 113.04, 56.41.		



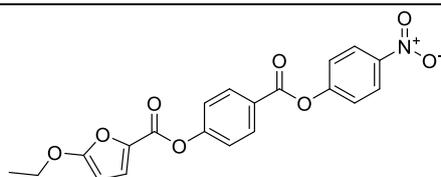
Compound 9

Appearance	White powder	106 mg, 68 %	
Melting Point	172.0 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.39
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.33 (d J = 9.2 Hz, 2H, Ar-H), 8.27 (dd, J = 8.9 Hz, 2H, Ar-H), 8.15 – 8.08 (m, 1H, Ar-H), 7.47 – 7.37 (m, 4H, Ar-H), 6.82 – 6.73 (m, 2H, Ar-H), 3.96 (s, 3H, Ar-O-CH <sub>3</sub> ).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	168.26, 165.73, 163.55, 162.51 (d, J = 2.9 Hz), 155.65, 145.48, 134.74, 131.98, 125.92, 125.32, 122.66, 122.41, 114.28 (d, J = 2.9 Hz), 107.59, 100.53, 100.28, 56.40.		
<sup>19</sup> F NMR (376 MHz, CDCl <sub>3</sub> ) (δ)	100.97 (m, 1F, Ar-F).		



Compound 10

Appearance	White powder	147 mg, 86 %	
Melting Point	173.2 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.53
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.33 (d, J = 9.2 Hz, 2H, Ar-H), 8.25 (d, J = 9.0 Hz, 2H, Ar-H), 8.12 (d, J = 16.0 Hz, 1H, Ar-CH=CH-COO), 7.51 (d, J = 8.5 Hz, 1H, Ar-H), 7.42 (d, J = 9.2 Hz, 2H, Ar-H), 7.36 (d, J = 8.8 Hz, 2H, Ar-H), 6.64 (d, J = 16.0 Hz, 1H, Ar-CH=CH-COO), 6.58 – 6.52 (m, 1H, Ar-H), 6.49 (d, J = 2.4 Hz, 1H, Ar-H), 3.91 (s, 3H, Ar-O-CH <sub>3</sub> (position 2)), 3.87 (s, 3H, Ar-O-CH <sub>3</sub> (position 4)).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	165.63, 163.60, 163.43, 160.35, 155.95, 155.71, 145.45, 143.12, 131.94, 131.21, 125.58, 125.30, 122.66, 122.29, 116.17, 114.16, 105.53, 98.49, 55.56.		



Compound 11

Appearance	White platelets	100 mg, 66 %	
Melting Point	191.4 °C	R <sub>f</sub> (DCM:Hex [7:3])	0.48
<sup>1</sup> H NMR (400 MHz, CDCl <sub>3</sub> ) (δ)	8.34 (d, J = 9.1 Hz, 2H, Ar-H), 8.25 (d, J = 8.9 Hz, 2H, Ar-H), 7.46 – 7.35 (m, 6H, Ar-H), 5.45 (d, J = 3.7 Hz, 2H, Furan Ar-H), 4.29 (q, J = 7.1 Hz, 3H, Furan Ar-O-CH <sub>2</sub> -CH <sub>3</sub> ), 1.48 (t, J = 7.1 Hz, 3H Furan Ar-O-CH <sub>2</sub> -CH <sub>3</sub> ).		
<sup>13</sup> C{ <sup>1</sup> H} NMR (101 MHz, CDCl <sub>3</sub> ) (δ)	163.53, 163.23, 155.66, 155.24, 149.07, 145.01, 133.05, 132.00, 125.83, 125.32, 124.34, 122.65, 122.19, 85.00, 67.51, 14.49.		

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