

Supplementary Information

Machine Learning-based Screening of Mn-PNP Catalysts for CO₂ Reduction Reaction Using Region-wise Ligand-encoded Feature Matrix

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A. Gaussian full references

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B. DFT calculated descriptors for all the 44 catalysts.

Table S1. DFT calculated $\Delta\Delta G^\ddagger$ and ΔG^\ddagger values for all the 44 catalysts. All the values are in eV.

SL No.	L ₁	L ₂	L ₃	$\Delta\Delta G^{\ddagger RN}$	$\Delta\Delta G^{\ddagger N}$	$\Delta\Delta G^{\ddagger M}$	$\Delta G^{\ddagger TS1}$	$\Delta G^{\ddagger TS2}$	$\Delta G^{\ddagger TS3}$
1	Me	Me	H	0.58	1.70	2.04	0.35	1.04	-0.01
2	Ph	Ph	H	0.65	1.75	2.08	0.41	1.05	-0.08
3	Ph	H	H	0.53	1.86	2.19	0.18	1.17	0.07
4	Pr	Me	H	0.57	1.71	2.04	0.36	0.85	-0.09
5	^t Bu	Et	H	0.46	1.60	1.93	0.24	0.98	0.06
6	ⁱ Pr	OMe	H	0.82	1.84	2.26	0.47	1.04	-0.02
7	Et	CF ₃	H	1.18	1.72	2.18	0.29	1.05	0.66
8	H	H	Me	0.55	1.79	2.13	0.24	1.08	-0.02
9	H	Pr	Me	0.55	1.76	2.09	0.27	1.05	0.17
10	H	Et	Me	0.56	1.78	2.11	0.11	1.07	0.07
11	Me	ⁱ Pr	Me	0.41	1.70	2.03	0.20	0.99	0.01
12	ⁱ Pr	Et	Me	0.40	1.68	2.01	0.18	0.96	-0.06
13	OEt	Et	Me	0.64	1.94	2.28	0.41	1.03	-0.07
14	OEt	ⁱ Pr	Me	1.01	1.97	2.30	0.15	1.06	0.00
15	CF ₃	ⁱ Pr	Me	0.70	1.89	2.23	0.36	1.20	0.15
16	Ph	Ph	Et	0.52	1.71	2.05	0.26	1.03	-0.08
17	H	^t Bu	Et	0.75	1.63	1.97	0.51	0.91	-0.03
18	OMe	Me	Et	0.55	1.83	2.16	0.22	1.14	0.05
19	Pr	Et	Et	0.47	1.65	1.98	0.25	0.96	0.02
20	OMe	Pr	Et	0.63	1.73	2.15	0.25	0.92	0.00
21	Ph	CF ₃	Et	1.06	1.77	2.10	0.43	1.14	0.54
22	CF ₃	Pr	Et	0.98	1.90	2.24	0.44	1.21	0.49
23	ⁱ Pr	H	Pr	0.54	1.77	2.10	0.33	1.04	-0.04
24	OEt	Me	Pr	0.56	1.83	2.16	0.25	1.07	-0.03
25	Et	Ph	Pr	0.53	1.64	1.97	0.30	0.99	-0.10
26	OMe	Et	Pr	0.59	1.86	2.19	0.29	1.05	0.01
27	OEt	Pr	Pr	0.72	2.16	2.14	0.34	0.97	-0.06
28	CF ₃	H	Pr	0.93	1.93	2.26	0.51	1.16	0.14
29	CF ₃	OEt	Pr	0.80	2.15	2.49	0.49	1.23	0.35
30	^t Bu	^t Bu	ⁱ Pr	0.94	1.43	1.76	0.68	0.61	0.35
31	ⁱ Pr	ⁱ Pr	ⁱ Pr	0.69	1.38	1.71	0.33	0.70	0.27
32	H	OEt	ⁱ Pr	0.70	1.99	2.32	0.46	1.12	-0.02
33	Et	Me	ⁱ Pr	0.50	1.70	2.03	0.23	1.00	0.12
34	Ph	ⁱ Pr	ⁱ Pr	0.60	1.54	1.87	0.29	0.94	-0.05
35	^t Bu	Pr	ⁱ Pr	0.65	1.70	2.03	0.07	1.01	0.38
36	OMe	OEt	ⁱ Pr	0.59	1.79	2.12	0.32	1.13	-0.01
37	CF ₃	H	ⁱ Pr	0.76	2.06	2.39	0.30	1.30	0.13
38	OMe	OMe	^t Bu	0.72	2.01	2.34	0.50	1.20	0.03

39	Ph	H	'Bu	0.56	1.89	2.22	0.33	1.22	-0.01
40	Me	Ph	'Bu	0.43	1.68	2.01	0.20	1.02	0.02
41	Ph	Pr	'Bu	0.42	1.59	1.92	0.20	0.93	-0.02
42	'Bu	OMe	'Bu	0.72	1.92	2.17	0.47	1.03	-0.03
43	CF₃	Me	'Bu	0.76	1.96	2.30	0.27	1.11	0.13
44	OMe	CF₃	'Bu	1.01	1.93	2.26	0.55	1.23	0.35

C. Optimized hyperparameters values.

Table S2. Optimized values of the hyperparameters for the best fitted ML algorithms for all the considered descriptors.

Descriptors	ML Models	Optimized hyperparameters for best fitted models
$\Delta\Delta G^{\ddagger RN}$	XGBR	n_estimators: 100, min_child_weight: 3, max_depth: 5, learning_rate: 0.05, booster: gbtree, base_score: 0.5
$\Delta\Delta G^{\ddagger N}$	GBR	n_estimators: 100, min_samples_split: 10, min_samples_leaf: 3, max_depth: 10, learning_rate: 0.2
$\Delta\Delta G^{\ddagger M}$	XGBR	n_estimators: 1500, min_child_weight: 4, learning_rate: 0.1, booster: gbtree, max_depth: 15, base_score: 1
$\Delta G^{\ddagger TS1}$	XGBR	n_estimators: 100, min_child_weight: 2, learning_rate: 0.05, booster: gbtree, max_depth: 15, base_score: 0.25
$\Delta G^{\ddagger TS2}$	GBR	n_estimators: 100, min_samples_split: 10, min_samples_leaf: 3, max_depth: 10, learning_rate: 0.5
$\Delta G^{\ddagger TS3}$	GBR	n_estimators: 900, min_samples_split: 5, min_samples_leaf: 5, max_depth: 3, learning_rate: 0.1

D. Performance analysis of ML models

Table S3. Performance analysis (RMSE) of all the considered ML models for all the descriptors. All the values are in eV.

Algorithm	Error	$\Delta\Delta G^{\ddagger\text{RN}}$	$\Delta\Delta G^{\ddagger\text{N}}$	$\Delta\Delta G^{\ddagger\text{M}}$	$\Delta G^{\ddagger\text{TS1}}$	$\Delta G^{\ddagger\text{TS2}}$	$\Delta G^{\ddagger\text{TS3}}$
Linear Regression	Train (RMSE)	0.08	0.09	0.07	0.09	0.06	0.10
	Test (RMSE)	0.21	0.11	0.13	0.10	0.12	0.16
KRR	Train (RMSE)	0.12	0.09	0.07	0.09	0.01	0.11
	Test (RMSE)	0.15	0.10	0.13	0.09	0.11	0.10
RFR	Train (RMSE)	0.14	0.09	0.07	0.11	0.07	0.13
	Test (RMSE)	0.13	0.13	0.13	0.10	0.11	0.08
GBR	Train (RMSE)	0.11	0.01	0.13×10^{-4}	0.07	0.01	0.01
	Test (RMSE)	0.15	0.09	0.12	0.08	0.10	0.08
XGBR	Train (RMSE)	0.08	0.87×10^{-4}	0.03	0.04	0.02	0.09
	Test (RMSE)	0.14	0.10	0.12	0.07	0.11	0.09

E. Best fitted ML models for TS1, TS2 and TS3 and their performance analysis.

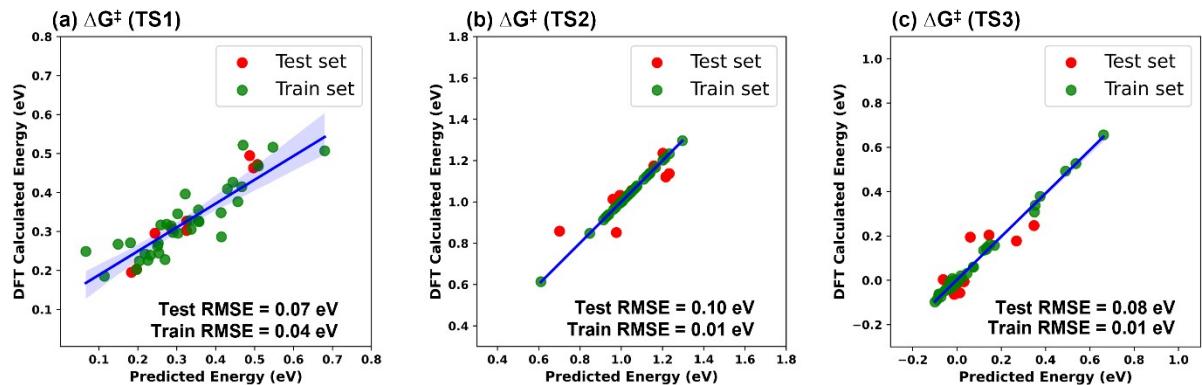


Fig. S1 Plot of DFT calculated vs ML predicted activation barriers of the transition states: (a) TS1, (b) TS2 and (c) TS3. All the energy values are in eV.

F. Cross-Validation (CV) analysis for best fitted machine learning models.

An evaluation method called Cross-Validation is used in machine learning to determine whether the model is stable and efficient enough when trained on the subset of input data sets and tested on the unseen set of datasets. Here, we used the k-fold cross validation method. The data sample is split into ‘k’ number of smaller samples, and in our case, k is 5 and the data sets is split into 5-fold (CV_i, i = 1, 2, 3, 4 and 5) sub-datasets (train and test). First, for example, CV₂₋₅ subsets are considered for training, and the CV₁ subset is left for the validation of the trained model. This process is repeated four more times with different subsets for the validation of the trained model. Cross-validation reduces the chances of overfitting and increases the generalizability of the parameters used in the machine learning model. Fig. S2 shows the concept of a 5-fold cross-validation loop. The root-mean-square error (RMSE) of each iteration and the mean of the RMSE for the total 5 iterations are computed.

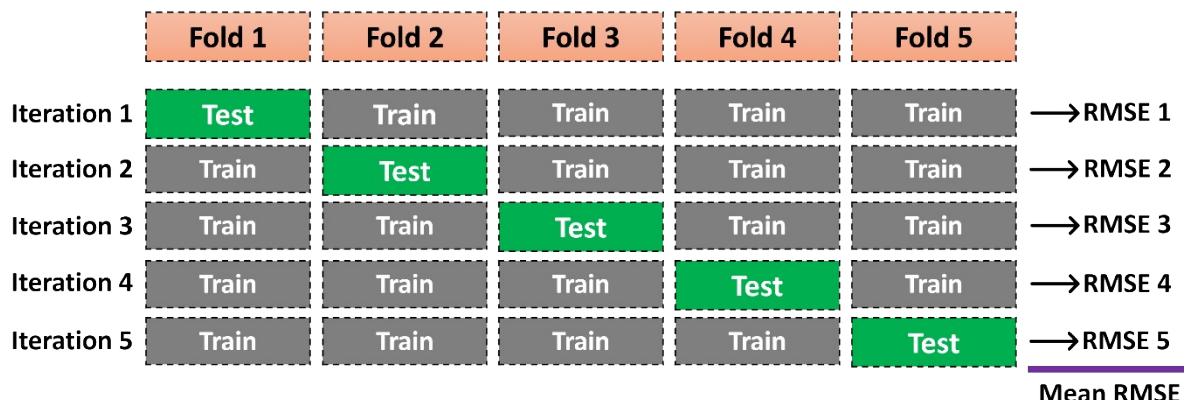


Fig. S2 The scheme explaining of k-fold (k = 5) Cross-Validation (CV) method.

Table S4. Root-Mean-Square Error (RMSE) Score for each fold (CV_i) of the 5-Fold CV using best fitted ML models for descriptors. Here, Avg. is the Mean RMSE of all the CV. All the values are in eV.

Data sets	Method	CV1	CV2	CV3	CV4	CV5	Avg.
$\Delta\Delta G^{\ddagger\text{RN}}$	XGBR	0.14	0.17	0.21	0.15	0.11	0.16
$\Delta\Delta G^{\ddagger\text{N}}$	GBR	0.10	0.17	0.10	0.11	0.13	0.12
$\Delta\Delta G^{\ddagger\text{M}}$	XGBR	0.15	0.10	0.16	0.12	0.12	0.13
$\Delta G^{\ddagger\text{TS1}}$	XGBR	0.10	0.17	0.12	0.10	0.11	0.12

$\Delta G^{\ddagger TS2}$	GBR	0.09	0.13	0.11	0.08	0.13	0.11
$\Delta G^{\ddagger TS3}$	GBR	0.15	0.10	0.09	0.11	0.15	0.12

G. ML predicted descriptors values for all the 286 catalysts

Table S5. ML predicted $\Delta\Delta G^\ddagger$ and ΔG^\ddagger values for all the 286 catalysts. All the values are in eV.

SL No.	L1	L2	L3	$\Delta\Delta G^{\ddagger RN}$	$\Delta\Delta G^{\ddagger N}$	$\Delta\Delta G^{\ddagger M}$	$\Delta G^{\ddagger TS1}$	$\Delta G^{\ddagger TS2}$	$\Delta G^{\ddagger TS3}$
45	H	H	H	0.68	1.82	2.16	0.35	1.13	0.10
46	Et	Et	H	0.57	1.65	2.01	0.26	1.01	0.07
47	tBu	tBu	H	0.75	1.66	1.97	0.50	0.93	0.05
48	Pr	Pr	H	0.67	1.66	2.04	0.28	0.92	0.02
49	iPr	iPr	H	0.74	1.68	2.01	0.40	0.99	0.02
50	OMe	OMe	H	0.75	1.89	2.28	0.46	1.11	0.03
51	OEt	OEt	H	0.78	1.97	2.29	0.48	1.09	-0.02
52	Me	H	H	0.57	1.80	2.12	0.28	1.11	0.00
53	Et	H	H	0.56	1.81	2.13	0.22	1.11	0.13
54	tBu	H	H	0.68	1.73	2.06	0.48	0.99	0.08
55	iPr	H	H	0.67	1.78	2.15	0.33	1.08	0.06
56	Pr	H	H	0.63	1.78	2.12	0.25	1.04	0.10
57	OMe	H	H	0.68	1.89	2.25	0.38	1.13	0.07
58	OEt	H	H	0.71	2.02	2.31	0.38	1.14	0.02
59	Ph	Me	H	0.54	1.71	2.00	0.33	1.04	-0.07
60	Et	Me	H	0.53	1.66	2.04	0.26	1.00	-0.03
61	tBu	Me	H	0.56	1.64	1.94	0.37	0.91	-0.03
62	iPr	Me	H	0.56	1.70	2.00	0.33	0.97	-0.03
63	OMe	Me	H	0.57	1.86	2.19	0.35	1.12	-0.02
64	OEt	Me	H	0.58	1.88	2.22	0.36	1.08	-0.07
65	Et	Ph	H	0.57	1.69	2.02	0.28	1.01	-0.06
66	tBu	Ph	H	0.63	1.68	1.98	0.40	0.96	-0.05
67	iPr	Ph	H	0.63	1.71	2.03	0.31	1.01	-0.15
68	Pr	Ph	H	0.55	1.61	1.96	0.26	0.94	-0.08
69	OMe	Ph	H	0.63	1.89	2.23	0.37	1.12	-0.08
70	OEt	Ph	H	0.68	1.98	2.26	0.38	1.09	-0.15
71	iPr	Et	H	0.56	1.66	1.99	0.25	0.97	0.00
72	Pr	Et	H	0.53	1.61	2.02	0.25	0.94	0.03
73	OMe	Et	H	0.57	1.87	2.23	0.25	1.06	0.04
74	OEt	Et	H	0.64	1.96	2.27	0.33	1.05	-0.01
75	iPr	tBu	H	0.75	1.66	1.95	0.49	0.94	0.05
76	Pr	tBu	H	0.67	1.66	2.03	0.25	0.89	0.03
77	OMe	tBu	H	0.75	1.83	2.16	0.49	0.96	0.01

78	OEt	tBu	H	0.79	1.94	2.20	0.50	0.97	0.00
79	Pr	iPr	H	0.67	1.68	2.01	0.27	0.92	-0.02
80	OEt	iPr	H	0.79	1.97	2.28	0.40	1.05	0.02
81	OMe	Pr	H	0.68	1.80	2.20	0.28	0.99	-0.02
82	OEt	Pr	H	0.70	2.04	2.21	0.30	0.98	-0.06
83	OEt	OMe	H	0.76	1.96	2.30	0.48	1.12	-0.05
84	CF ₃	CF ₃	H	0.96	1.82	2.23	0.48	1.15	0.56
85	CF ₃	H	H	0.91	1.90	2.25	0.43	1.19	0.41
86	CF ₃	Me	H	0.80	1.92	2.29	0.38	1.13	0.37
87	CF ₃	Ph	H	0.96	1.78	2.15	0.43	1.14	0.57
88	CF ₃	tBu	H	0.96	1.81	2.17	0.50	1.14	0.49
89	CF ₃	iPr	H	0.96	1.85	2.20	0.46	1.15	0.43
90	CF ₃	Pr	H	0.91	1.87	2.29	0.34	1.15	0.50
91	CF ₃	OMe	H	0.95	1.85	2.23	0.47	1.18	0.54
92	CF ₃	OEt	H	0.97	2.03	2.44	0.50	1.18	0.54
93	Me	Me	Me	0.49	1.68	2.04	0.22	1.03	0.00
94	Ph	Ph	Me	0.57	1.70	2.07	0.32	1.05	-0.10
95	Et	Et	Me	0.52	1.66	2.01	0.27	1.00	0.01
96	tBu	tBu	Me	0.72	1.65	1.95	0.36	0.93	0.01
97	Pr	Pr	Me	0.59	1.68	2.03	0.22	0.93	0.09
98	iPr	iPr	Me	0.59	1.70	2.02	0.18	0.99	-0.02
99	OMe	OMe	Me	0.67	1.91	2.27	0.28	1.11	-0.01
100	OEt	OEt	Me	0.79	1.96	2.29	0.34	1.09	-0.06
101	Me	H	Me	0.49	1.76	2.10	0.20	1.08	-0.01
102	Ph	H	Me	0.53	1.82	2.17	0.16	1.11	-0.04
103	tBu	H	Me	0.64	1.70	2.02	0.32	0.95	0.00
104	iPr	H	Me	0.52	1.78	2.14	0.15	1.04	-0.01
105	OMe	H	Me	0.60	1.88	2.23	0.22	1.10	0.00
106	OEt	H	Me	0.72	2.00	2.29	0.21	1.10	-0.05
107	Ph	Me	Me	0.49	1.67	2.01	0.22	1.04	-0.04
108	Et	Me	Me	0.49	1.67	2.06	0.21	1.01	-0.01
109	tBu	Me	Me	0.53	1.62	1.93	0.25	0.92	0.00
110	Pr	Me	Me	0.48	1.73	2.04	0.22	0.91	0.06
111	OMe	Me	Me	0.50	1.87	2.20	0.22	1.13	0.02
112	OEt	Me	Me	0.59	1.87	2.23	0.24	1.08	-0.04
113	Et	Ph	Me	0.51	1.67	2.02	0.28	1.00	-0.12
114	tBu	Ph	Me	0.62	1.64	1.97	0.36	0.95	-0.10
115	iPr	Ph	Me	0.50	1.71	2.05	0.18	1.01	-0.20
116	Pr	Ph	Me	0.50	1.60	1.94	0.22	0.95	-0.02
117	OMe	Ph	Me	0.58	1.89	2.23	0.28	1.12	-0.12
118	OEt	Ph	Me	0.69	1.97	2.27	0.34	1.09	-0.19
119	tBu	Et	Me	0.57	1.60	1.92	0.26	0.92	0.01
120	Pr	Et	Me	0.48	1.64	2.02	0.22	0.95	0.09
121	OMe	Et	Me	0.53	1.89	2.22	0.22	1.07	-0.01
122	iPr	tBu	Me	0.72	1.67	1.96	0.28	0.94	0.02
123	Pr	tBu	Me	0.64	1.68	2.01	0.19	0.91	0.10

124	OMe	^t Bu	Me	0.71	1.85	2.15	0.32	0.97	-0.04
125	OEt	^t Bu	Me	0.80	1.93	2.19	0.37	0.97	-0.04
126	Pr	ⁱ Pr	Me	0.52	1.71	2.04	0.19	0.93	0.06
127	OMe	ⁱ Pr	Me	0.61	1.86	2.26	0.22	1.05	-0.05
128	OMe	Pr	Me	0.60	1.83	2.19	0.22	0.99	0.06
129	OEt	Pr	Me	0.70	2.06	2.22	0.25	0.99	0.02
130	OEt	OMe	Me	0.77	1.95	2.29	0.31	1.13	-0.08
131	CF ₃	CF ₃	Me	0.93	1.85	2.23	0.41	1.17	0.29
132	CF ₃	H	Me	0.88	1.90	2.26	0.32	1.16	0.15
133	CF ₃	Me	Me	0.78	1.95	2.29	0.30	1.16	0.13
134	CF ₃	Ph	Me	0.93	1.78	2.15	0.42	1.16	0.31
135	CF ₃	^t Bu	Me	0.97	1.84	2.15	0.44	1.17	0.23
136	CF ₃	Et	Me	0.93	1.77	2.19	0.31	1.14	0.37
137	CF ₃	Pr	Me	0.89	1.91	2.29	0.30	1.18	0.37
138	CF ₃	OMe	Me	0.94	1.88	2.25	0.36	1.19	0.28
139	CF ₃	OEt	Me	0.97	2.05	2.46	0.42	1.20	0.29
140	H	H	Et	0.64	1.73	2.08	0.35	1.08	-0.01
141	Me	Me	Et	0.53	1.67	2.00	0.23	1.02	0.02
142	Et	Et	Et	0.53	1.67	1.98	0.23	0.99	0.02
143	^t Bu	^t Bu	Et	0.75	1.63	1.91	0.48	0.91	0.03
144	Pr	Pr	Et	0.64	1.66	1.98	0.30	0.93	0.04
145	ⁱ Pr	ⁱ Pr	Et	0.63	1.69	1.95	0.34	0.97	0.01
146	OMe	OMe	Et	0.71	1.82	2.21	0.37	1.11	0.02
147	OEt	OEt	Et	0.77	1.94	2.24	0.41	1.07	-0.04
148	Me	H	Et	0.54	1.73	2.06	0.21	1.09	-0.04
149	Ph	H	Et	0.55	1.78	2.12	0.22	1.11	-0.06
150	Et	H	Et	0.52	1.75	2.07	0.22	1.08	0.01
151	ⁱ Pr	H	Et	0.57	1.74	2.07	0.32	1.04	-0.03
152	Pr	H	Et	0.62	1.71	2.05	0.30	1.03	0.07
153	OMe	H	Et	0.65	1.81	2.17	0.36	1.12	-0.03
154	OEt	H	Et	0.72	1.97	2.23	0.37	1.10	-0.09
155	Ph	Me	Et	0.51	1.66	2.00	0.22	1.03	-0.02
156	Et	Me	Et	0.50	1.66	2.02	0.23	1.00	-0.01
157	^t Bu	Me	Et	0.58	1.60	1.90	0.30	0.91	0.02
158	Pr	Me	Et	0.54	1.70	2.00	0.25	0.91	0.01
159	ⁱ Pr	Me	Et	0.46	1.69	1.98	0.24	0.97	0.04
160	OEt	Me	Et	0.59	1.89	2.19	0.26	1.07	-0.02
161	Et	Ph	Et	0.53	1.68	2.01	0.24	1.00	-0.11
162	^t Bu	Ph	Et	0.63	1.63	1.93	0.38	0.93	-0.07
163	ⁱ Pr	Ph	Et	0.51	1.71	2.00	0.26	0.99	-0.16
164	Pr	Ph	Et	0.52	1.59	1.92	0.28	0.95	-0.07
165	OMe	Ph	Et	0.59	1.81	2.19	0.27	1.12	-0.09
166	OEt	Ph	Et	0.67	1.97	2.22	0.31	1.07	-0.17
167	^t Bu	Et	Et	0.58	1.60	1.90	0.28	0.92	0.01
168	ⁱ Pr	Et	Et	0.45	1.68	1.95	0.25	0.96	-0.04
169	OMe	Et	Et	0.54	1.82	2.18	0.23	1.06	0.00

170	OEt	Et	Et	0.64	1.94	2.23	0.29	1.04	-0.06
171	iPr	tBu	Et	0.75	1.66	1.90	0.47	0.91	0.05
172	Pr	tBu	Et	0.69	1.65	1.98	0.29	0.90	0.05
173	OMe	tBu	Et	0.75	1.76	2.09	0.47	0.96	-0.01
174	OEt	tBu	Et	0.79	1.91	2.15	0.50	0.95	-0.02
175	Pr	iPr	Et	0.57	1.70	1.97	0.30	0.92	0.01
176	OMe	iPr	Et	0.64	1.79	2.19	0.36	1.05	-0.02
177	OEt	iPr	Et	0.78	1.94	2.22	0.35	1.03	0.01
178	OEt	Pr	Et	0.70	2.01	2.17	0.32	0.98	-0.04
179	OEt	OMe	Et	0.75	1.93	2.23	0.41	1.12	-0.06
180	CF ₃	CF ₃	Et	0.93	1.84	2.18	0.47	1.15	0.49
181	CF ₃	H	Et	0.89	1.89	2.20	0.44	1.17	0.30
182	CF ₃	Me	Et	0.78	1.94	2.24	0.32	1.15	0.32
183	CF ₃	tBu	Et	0.97	1.83	2.10	0.51	1.15	0.43
184	CF ₃	Et	Et	0.93	1.78	2.14	0.30	1.14	0.52
185	CF ₃	iPr	Et	0.85	1.88	2.16	0.45	1.15	0.36
186	CF ₃	OMe	Et	0.94	1.86	2.18	0.47	1.19	0.48
187	CF ₃	OEt	Et	0.98	2.04	2.40	0.49	1.18	0.48
188	H	H	Pr	0.63	1.76	2.09	0.38	1.11	-0.01
189	Me	Me	Pr	0.53	1.64	2.00	0.24	1.02	0.02
190	Ph	Ph	Pr	0.57	1.68	2.03	0.33	1.04	-0.08
191	Et	Et	Pr	0.51	1.69	1.97	0.28	0.99	0.02
192	tBu	tBu	Pr	0.75	1.66	1.93	0.48	0.92	0.02
193	Pr	Pr	Pr	0.64	1.76	1.97	0.27	0.92	0.03
194	iPr	iPr	Pr	0.62	1.69	1.97	0.36	0.98	-0.01
195	OMe	OMe	Pr	0.70	1.87	2.24	0.41	1.11	0.02
196	OEt	OEt	Pr	0.75	1.97	2.23	0.43	1.09	-0.05
197	Me	H	Pr	0.54	1.72	2.06	0.24	1.10	-0.03
198	Ph	H	Pr	0.54	1.79	2.12	0.25	1.13	-0.06
199	Et	H	Pr	0.51	1.77	2.07	0.28	1.09	0.01
200	tBu	H	Pr	0.69	1.71	2.01	0.47	0.97	-0.03
201	Pr	H	Pr	0.60	1.81	2.04	0.25	1.04	0.07
202	OMe	H	Pr	0.65	1.85	2.19	0.40	1.13	-0.01
203	OEt	H	Pr	0.69	1.99	2.23	0.39	1.13	-0.09
204	Ph	Me	Pr	0.51	1.64	1.97	0.23	1.04	-0.01
205	Et	Me	Pr	0.50	1.63	2.01	0.26	1.00	0.01
206	tBu	Me	Pr	0.58	1.60	1.91	0.29	0.91	0.02
207	Pr	Me	Pr	0.53	1.74	1.99	0.25	0.91	0.01
208	iPr	Me	Pr	0.46	1.67	1.98	0.25	0.97	0.03
209	OMe	Me	Pr	0.54	1.82	2.16	0.24	1.12	0.04
210	tBu	Ph	Pr	0.62	1.64	1.94	0.39	0.95	-0.08
211	iPr	Ph	Pr	0.50	1.70	2.00	0.28	1.00	-0.17
212	Pr	Ph	Pr	0.52	1.69	1.90	0.24	0.95	-0.07
213	OMe	Ph	Pr	0.59	1.86	2.19	0.33	1.12	-0.08
214	OEt	Ph	Pr	0.64	1.96	2.21	0.35	1.09	-0.17
215	tBu	Et	Pr	0.56	1.62	1.90	0.29	0.91	0.02

216	iPr	Et	Pr	0.44	1.68	1.95	0.27	0.96	-0.04
217	Pr	Et	Pr	0.50	1.72	1.97	0.27	0.95	0.03
218	OEt	Et	Pr	0.60	1.97	2.21	0.32	1.04	-0.06
219	iPr	tBu	Pr	0.74	1.68	1.92	0.46	0.93	0.03
220	Pr	tBu	Pr	0.69	1.75	1.96	0.24	0.90	0.04
221	OMe	tBu	Pr	0.75	1.85	2.13	0.47	0.96	-0.01
222	OEt	tBu	Pr	0.77	1.96	2.15	0.49	0.96	-0.03
223	Pr	iPr	Pr	0.56	1.77	1.97	0.26	0.92	0.00
224	OMe	iPr	Pr	0.64	1.84	2.21	0.40	1.05	-0.02
225	OEt	iPr	Pr	0.75	1.97	2.22	0.37	1.05	-0.01
226	OMe	Pr	Pr	0.65	1.90	2.14	0.27	0.99	0.01
227	OEt	OMe	Pr	0.74	1.94	2.25	0.44	1.12	-0.06
228	CF₃	CF₃	Pr	0.89	1.94	2.26	0.48	1.16	0.35
229	CF₃	Me	Pr	0.78	1.95	2.30	0.32	1.15	0.20
230	CF₃	Ph	Pr	0.89	1.86	2.17	0.43	1.16	0.37
231	CF₃	tBu	Pr	0.93	1.93	2.18	0.51	1.16	0.28
232	CF₃	Et	Pr	0.89	1.87	2.22	0.32	1.13	0.43
233	CF₃	iPr	Pr	0.81	1.96	2.23	0.46	1.17	0.22
234	CF₃	Pr	Pr	0.89	1.98	2.29	0.34	1.17	0.35
235	CF₃	OMe	Pr	0.90	1.96	2.27	0.47	1.19	0.35
236	H	H	iPr	0.62	1.68	2.13	0.34	1.10	0.11
237	Me	Me	iPr	0.51	1.59	1.97	0.21	0.89	0.17
238	Ph	Ph	iPr	0.56	1.56	1.98	0.28	0.92	0.01
239	Et	Et	iPr	0.51	1.58	1.91	0.26	0.92	0.19
240	Pr	Pr	iPr	0.62	1.69	2.04	0.21	0.87	0.25
241	OMe	OMe	iPr	0.68	1.50	2.01	0.30	1.06	0.12
242	OEt	OEt	iPr	0.73	1.83	2.16	0.40	0.92	0.09
243	Me	H	iPr	0.51	1.68	2.16	0.23	1.10	0.04
244	Ph	H	iPr	0.52	1.72	2.17	0.24	1.14	-0.03
245	Et	H	iPr	0.50	1.76	2.15	0.25	1.13	0.11
246	tBu	H	iPr	0.71	1.60	2.03	0.49	0.94	0.23
247	iPr	H	iPr	0.61	1.61	2.03	0.34	1.04	0.13
248	Pr	H	iPr	0.58	1.76	2.17	0.22	1.05	0.21
249	OMe	H	iPr	0.61	1.63	2.14	0.34	1.12	0.02
250	Ph	Me	iPr	0.48	1.64	2.03	0.20	0.94	0.04
251	tBu	Me	iPr	0.59	1.53	1.85	0.31	0.81	0.29
252	Pr	Me	iPr	0.51	1.75	2.08	0.22	0.87	0.18
253	iPr	Me	iPr	0.51	1.55	1.85	0.25	0.82	0.23
254	OMe	Me	iPr	0.50	1.60	2.06	0.21	1.08	0.13
255	OEt	Me	iPr	0.53	1.87	2.20	0.25	0.93	0.08
256	Et	Ph	iPr	0.51	1.61	2.00	0.26	0.92	-0.03
257	tBu	Ph	iPr	0.65	1.50	1.87	0.44	0.86	0.15
258	Pr	Ph	iPr	0.49	1.68	2.01	0.21	0.92	0.05
259	OMe	Ph	iPr	0.56	1.56	2.06	0.23	1.10	-0.07
260	OEt	Ph	iPr	0.62	1.90	2.21	0.33	0.94	-0.11
261	tBu	Et	iPr	0.60	1.52	1.82	0.33	0.86	0.32

262	ⁱ Pr	Et	ⁱ Pr	0.51	1.52	1.78	0.26	0.86	0.18
263	Pr	Et	ⁱ Pr	0.47	1.71	2.06	0.23	0.92	0.22
264	OMe	Et	ⁱ Pr	0.50	1.59	2.04	0.22	1.09	0.09
265	OEt	Et	ⁱ Pr	0.59	1.90	2.21	0.30	0.93	0.07
266	ⁱ Pr	^t Bu	ⁱ Pr	0.77	1.40	1.68	0.47	0.79	0.36
267	OMe	^t Bu	ⁱ Pr	0.76	1.45	1.91	0.47	0.90	0.25
268	OEt	^t Bu	ⁱ Pr	0.81	1.80	2.08	0.51	0.84	0.25
269	Pr	ⁱ Pr	ⁱ Pr	0.61	1.63	1.95	0.23	0.87	0.27
270	OMe	ⁱ Pr	ⁱ Pr	0.68	1.44	1.96	0.34	0.99	0.14
271	OEt	ⁱ Pr	ⁱ Pr	0.73	1.81	2.10	0.37	0.87	0.18
272	OMe	Pr	ⁱ Pr	0.61	1.64	2.11	0.21	1.00	0.14
273	OEt	Pr	ⁱ Pr	0.65	2.01	2.27	0.24	0.94	0.12
274	CF ₃	CF ₃	ⁱ Pr	0.90	1.89	2.24	0.37	1.12	0.37
275	CF ₃	Me	ⁱ Pr	0.74	2.00	2.33	0.25	1.12	0.17
276	CF ₃	Ph	ⁱ Pr	0.90	1.91	2.28	0.32	1.13	0.32
277	CF ₃	^t Bu	ⁱ Pr	0.97	1.89	2.15	0.51	1.12	0.43
278	CF ₃	Et	ⁱ Pr	0.90	1.89	2.25	0.29	1.12	0.43
279	CF ₃	ⁱ Pr	ⁱ Pr	0.88	1.86	2.16	0.35	1.12	0.29
280	CF ₃	Pr	ⁱ Pr	0.85	2.00	2.36	0.26	1.16	0.39
281	CF ₃	OMe	ⁱ Pr	0.89	1.89	2.24	0.32	1.19	0.28
282	CF ₃	OEt	ⁱ Pr	0.91	2.02	2.38	0.42	1.13	0.32
283	H	H	^t Bu	0.64	1.86	2.21	0.43	1.16	0.01
284	Me	Me	^t Bu	0.53	1.74	2.05	0.23	1.05	-0.01
285	Ph	Ph	^t Bu	0.56	1.75	2.08	0.39	1.07	-0.04
286	Et	Et	^t Bu	0.53	1.72	2.06	0.32	1.05	0.00
287	^t Bu	^t Bu	^t Bu	0.76	1.74	1.96	0.53	0.99	0.01
288	Pr	Pr	^t Bu	0.63	1.70	2.01	0.27	0.97	0.02
289	ⁱ Pr	ⁱ Pr	^t Bu	0.63	1.78	2.05	0.42	1.04	-0.02
290	OEt	OEt	^t Bu	0.78	2.00	2.30	0.51	1.11	-0.07
291	Me	H	^t Bu	0.53	1.82	2.15	0.22	1.14	-0.02
292	Et	H	^t Bu	0.52	1.84	2.18	0.28	1.15	0.04
293	^t Bu	H	^t Bu	0.69	1.81	2.07	0.49	1.05	-0.01
294	ⁱ Pr	H	^t Bu	0.57	1.84	2.19	0.40	1.13	-0.02
295	Pr	H	^t Bu	0.60	1.77	2.11	0.25	1.09	0.10
296	OMe	H	^t Bu	0.65	1.94	2.32	0.45	1.19	0.01
297	OEt	H	^t Bu	0.72	2.04	2.33	0.45	1.16	-0.07
298	Et	Me	^t Bu	0.50	1.70	2.06	0.22	1.04	-0.03
299	^t Bu	Me	^t Bu	0.58	1.70	1.93	0.29	0.97	-0.01
300	Pr	Me	^t Bu	0.53	1.74	2.01	0.24	0.95	-0.02
301	ⁱ Pr	Me	^t Bu	0.46	1.75	2.02	0.23	1.02	0.00
302	OMe	Me	^t Bu	0.54	1.92	2.23	0.23	1.16	0.03
303	OEt	Me	^t Bu	0.58	1.91	2.22	0.25	1.09	-0.06
304	Et	Ph	^t Bu	0.51	1.72	2.04	0.33	1.05	-0.07
305	^t Bu	Ph	^t Bu	0.61	1.71	1.96	0.40	1.00	-0.04
306	ⁱ Pr	Ph	^t Bu	0.49	1.76	2.04	0.30	1.05	-0.14
307	OMe	Ph	^t Bu	0.57	1.93	2.25	0.36	1.16	-0.05

308	OEt	Ph	tBu	0.67	1.99	2.26	0.40	1.10	-0.14
309	tBu	Et	tBu	0.58	1.68	1.94	0.32	0.99	0.00
310	iPr	Et	tBu	0.46	1.73	2.03	0.29	1.03	-0.07
311	Pr	Et	tBu	0.49	1.67	2.00	0.25	0.98	0.01
312	OMe	Et	tBu	0.54	1.94	2.29	0.29	1.13	0.00
313	OEt	Et	tBu	0.64	1.97	2.28	0.37	1.08	-0.08
314	iPr	tBu	tBu	0.75	1.76	1.95	0.48	0.99	0.02
315	Pr	tBu	tBu	0.68	1.70	1.99	0.24	0.95	0.03
316	OEt	tBu	tBu	0.79	1.97	2.18	0.53	1.02	-0.05
317	Pr	iPr	tBu	0.56	1.73	2.01	0.26	0.97	-0.01
318	OMe	iPr	tBu	0.65	1.93	2.31	0.45	1.12	-0.03
319	OEt	iPr	tBu	0.78	2.00	2.30	0.42	1.08	-0.03
320	OMe	Pr	tBu	0.64	1.85	2.19	0.27	1.06	0.01
321	OEt	Pr	tBu	0.69	2.06	2.19	0.29	0.99	-0.06
322	OEt	OMe	tBu	0.76	1.99	2.32	0.50	1.16	-0.07
323	CF ₃	CF ₃	tBu	0.93	1.90	2.25	0.55	1.16	0.34
324	CF ₃	H	tBu	0.88	1.91	2.28	0.50	1.20	0.18
325	CF ₃	Ph	tBu	0.93	1.82	2.15	0.46	1.16	0.39
326	CF ₃	tBu	tBu	0.97	1.90	2.14	0.55	1.16	0.28
327	CF ₃	Et	tBu	0.93	1.81	2.21	0.37	1.14	0.41
328	CF ₃	iPr	tBu	0.85	1.94	2.22	0.49	1.17	0.21
329	CF ₃	Pr	tBu	0.89	1.93	2.27	0.34	1.16	0.35
330	CF ₃	OEt	tBu	0.97	2.05	2.45	0.55	1.19	0.33

H. DFT validation of ML predicted energies of all the descriptors.

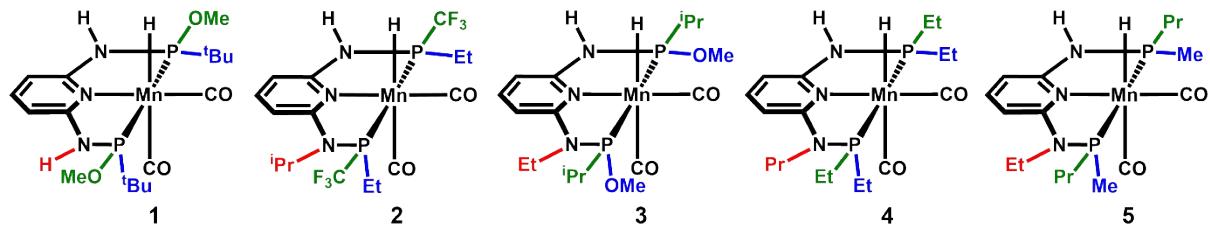


Fig. S3 Considered catalysts for the DFT validation of ML predicted energies of all the descriptors.

Table S6. Comparison of DFT calculated and ML predicted results for all the catalysts mentioned in Fig. S3. All the energies are in eV.

Catalysts	$\Delta G^{\ddagger\text{TS1}}$		$\Delta G^{\ddagger\text{TS2}}$		$\Delta G^{\ddagger\text{TS3}}$	
	DFT	ML	DFT	ML	DFT	ML
1	0.39	0.49	1.03	0.96	-0.01	0.01
2	0.44	0.29	1.13	1.12	0.38	0.43
3	0.46	0.36	0.99	1.05	-0.06	-0.02
4	0.39	0.24	1.02	1.02	-0.02	0.02
5	0.29	0.25	1.01	0.91	-0.01	0.01

I. Proposed best performing catalysts to produce HCOOH from CO₂.

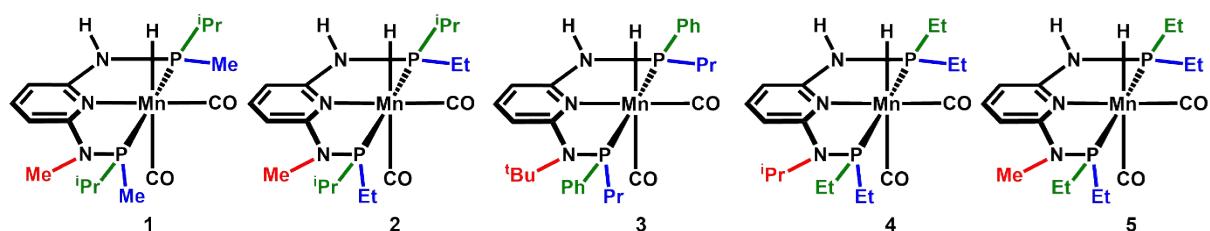


Fig. S4. DFT+ML predicted best catalysts to produce HCOOH.

J. Natural bond orbital (NBO) analysis of catalysts

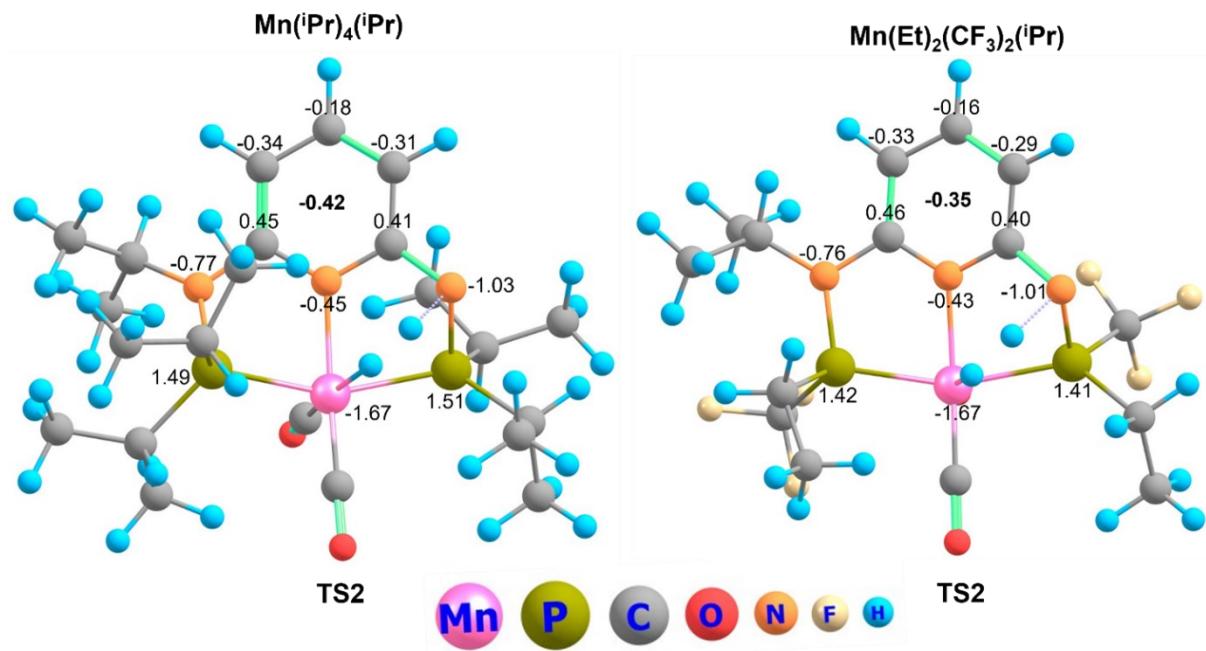


Fig. S5 NBO analysis of catalysts.