Titanium Nitride-Based Hyperbolic Metamaterial for Near-Infrared Ultrasensitive Sensing of Microbes: ESI

S1. SUGGESTED FABRICATION TECHNIQUE

It is essential to meticulously adopt the fabrication procedure to produce our proposed TiN nanowire HMM structure. We could employ electron beam lithography (EBL) and electroplating techniques to fabricate the TiN nanowire HMM structure. Yan et al. fabricated a nanowire HMM structure on the glass-metal hybrid substrate using EBL and electroplating methods [1]. Sahoo et al. reported an HMM structure comprising highly packed nanowires (high FF) using sputtering and electroplating methods [2]. Figure S1 illustrates a simplified diagram of the suggested fabrication method for building the proposed nanowire HMM structure. Initially, we could use sputtering or electroplating methods to deposit TiN on PMMA glass to support nanowires. EBL can achieve a well-structured periodic array of holes that can be removed using an etchant such as acetone. After that, we might grow TiN nanowires using the electroplating method. Then, ultraviolet (UV) light can be utilized to soften the PMMA material. Finally, we could use acetone to remove all PMMA materials.

Fig. S1. Suggested fabrication technique of our proposed TiN nanowire HMM sensor structure.

S2. MATERIAL PROPERTIES OF TITANIUM NITRIDE

We adopted the complex refractive index of titanium nitride (TiN) from experimental data of Naik et al. [3]. The complex refractive index, $\tilde{n}$, is defined by,

$$\tilde{n} = n + ik.$$  \hspace{1cm} (S1)

Here, $n$ and $k$ denote the refractive index and extinction coefficient. The $n$ controls the light’s speed through the medium, while the $k$ governs its scattering and absorption. The dielectric constants of TiN are given in Fig. S2. The magnetic permeability of the TiN was set to be 1 for our study.

S3. REFLECTANCE, TRANSMITTANCE, AND ABSORPTANCE SPECTRA

To calculate the reflectance (R), transmittance (T), and absorptance (A) of our proposed structure, we utilized two power monitors: one was set below the structure, and the other was set on the
Fig. S2. Refractive index (n) and extinction coefficient (k) spectra of TiN.

\[ R = \frac{P_r}{P_i}, \]  \hspace{1cm} \text{(S2)}

\[ T = \frac{P_t}{P_i}, \]  \hspace{1cm} \text{(S3)}

\[ A = 1 - R - T. \]  \hspace{1cm} \text{(S4)}

Here, \( P_r \), \( P_t \), and \( P_i \) represent the monitors’ reflected, transmitted, and incident power. We obtained two bulk plasmon polariton (BPP) modes at the resonance wavelengths of 1267 and 1935 nm, as shown in Fig. S3, where the water (refractive index, \( n = 1.333 \) RIU) was considered as the surrounding medium. Consequently, our proposed hyperbolic metamaterials (HMM) structure exhibited absorptance at the resonance wavelengths, as no transmission through the structure was supported because of maintaining dispersion relations. The effective permittivity, \( \varepsilon \), of the proposed HMM structure is negative; therefore, the propagation constant, \( k = \sqrt{\varepsilon \omega} \), of the electromagnetic wave is imaginary. Thus, the proposed HMM sensor structure exhibited negligible transmittance.

Fig. S3. Reflectance, transmittance, and absorptance spectra of the proposed HMM sensor structure. Here, the fill factor of TiN nanowire was set to be 70%.
S4. EFFECTS OF FILL FACTOR ON REFLECTANCE SPECTRA

We studied the impact of various fill factors, \( FF \), on the reflectance spectra. The BPP modes disappeared while we increased the \( FF \) beyond 78.54% because nanowires overlapped each other. We observed it for the \( FF \) of 78.54%, as depicted in Fig. S4. Moreover, it can be inferred from Fig. S4 that BPP modes initiated to disappear with increasing \( FF \) beyond 70%. Therefore, we considered the 70% \( FF \) for our proposed HMM sensor structure.

![Fig. S4. Reflectance spectra of the nanowire HMM sensor structure for different \( FF \).](image)

S5. MODE FREQUENCY SHIFT FOR DIFFERENT FILL FACTOR

We analyzed the mode frequency shift of the second (\( q = 2 \)) BPP mode by varying the \( FF \) of the TiN nanowire, where other structural parameters were kept the same. An improved mode frequency shift was obtained when we increased the \( FF \), as shown in Fig. S5. Meanwhile, this happened due to strong hyperbolic dispersion, which resulted in the shift of BPP mode in the longer wavelength.

![Fig. S5. The calculated mode frequency shift of \( q = 2 \) BPP mode for different \( FF \), where \( h_p \) was set to be 400 nm.](image)
S6. SENSING CAPABILITIES OF VARIOUS MICROBES

We slightly changed the surrounding medium’s RI due to injecting microbes into freshwater solutions. Here, we injected a single *Escherichia coli* (*E. coli*), 4% Dengue infected platelets, and 4% *Haemophilus influenzae* (*H. influenzae*) into freshwater. We collected the RI of single *E. coli* bacteria (difference of RI, $\Delta = 0.005$ RIU) from an experimental report of the optofluidic immersion refractometry technique [4]. The optical properties of Dengue infected platelets ($n = 1.39$) and *H. influenzae* ($n = 1.45$) were adopted from Sharma et al. [5] and Locke et al. [6], respectively. After that, we mixed 4% of Dengue-infected platelets and *H. influenzae* with freshwater and obtained the effective relative complex permittivity, $\varepsilon_{\text{eff}}$, of the mixture by solving the Maxwell Garnett equation [7],

$$
\varepsilon_{\text{eff}} = \varepsilon_w \left[ 1 + \frac{3c_m}{\varepsilon_m + 2c_m(\varepsilon_m - \varepsilon_w)} \right].
$$

(S5)

Here, $\varepsilon_m$ and $\varepsilon_w$ denote the permittivity of the microbe and freshwater. $c_m$ represents the volume fraction of the microbe in freshwater. All the structural and simulation parameters were kept constant.

The proposed HMM sensor structure redshifted the resonance dips in the reflectance, when we injected a single *E. coli*, 4% Dengue infected platelets, and 4% *H. influenzae* into freshwater, as depicted in Fig. S6. We compared the reflectance spectra of freshwater and the aqueous solution containing microbes and calculated the resonance wavelength shift. Two BPP modes were redshifted due to the addition of microbes in freshwater. We obtained the resonance wavelength shifts of 11, 5, and 8 nm for $q = 1$ BPP mode and 5.41, 3.11, and 6 nm for $q = 2$ BPP mode, respectively, as shown in Figs. S6(b) and (c), for a single *E. coli*, 4% Dengue infected platelets, and 4% *H. influenzae* into freshwater, respectively. Therefore, it can be inferred that our proposed HMM sensor structure is capable of detecting a small amount of several microbes in freshwater solution.

S7. LIMIT OF DETECTION

We studied the impact of the refractive index difference, $\Delta n$, on the resonance shift of the reflectance spectra. The limit of detection (LOD) of our proposed nanowire HMM sensor structure is 0.00008 RIU. Here, we obtained a resonance shift of 0.27 nm for both BPP modes, as shown in Fig. S7. When we reduced $\Delta n$, no resonance shifts were achieved in either BPP mode.
Resonance wavelength shift of BPP 1 and 2 modes for varying the refractive index difference, $\Delta n$. We obtained an LOD of 0.00008 RIU for our proposed HMM sensor structure.

**S8. ELECTRIC FIELD DISTRIBUTIONS AROUND NANOWIRE**

The resonance wavelength shift exhibited irregular fluctuations with varying $D/h_p$ due to the fluctuations of the electric field around the nanowire. The binding of *E. coli* bacteria with nanowires altered with varying $D/h_p$, which resulted in the electric field fluctuations for both BPP modes, as shown in Fig. S8. We achieved the highest electric field distributions around the TiN nanowire for BPP 1 mode due to the strong hyperbolic dispersion. Thus, we observed a high resonance wavelength shift for the BPP 1 mode compared to the BPP 2 mode. However, our proposed structure at the $D/h_p$ of 0.5 and 0.6 exhibited a high resonance wavelength shift for the BPP 2 mode because of high electric field distributions around TiN nanowire, as shown in Fig. S8(b).

**S9. DEPENDENCY OF A SINGLE MICROBE’S POSITION ON RESONANCE SHIFT**

We analyzed the effect of a single *E. coli*’s position on the resonance shift of the proposed nanowire HMM sensor structure. We varied the *E. coli*’s position by changing $D/h_p$ in our proposed structure. We obtained different resonance shifts for both BPP modes while we varied the $D/h_p$, as shown in Fig. S9. Meanwhile, the binding of the microbe with the HMM’s nanowire altered...
with varying D/hp. Interestingly, our proposed sensor structure exhibited resonance wavelength shift for the worst cases of D/hp.

![Fig. S9. Numerically calculated resonance shift of dips in reflectance spectra for varying a single E. coli’s D/hp.](image)

**REFERENCES**