

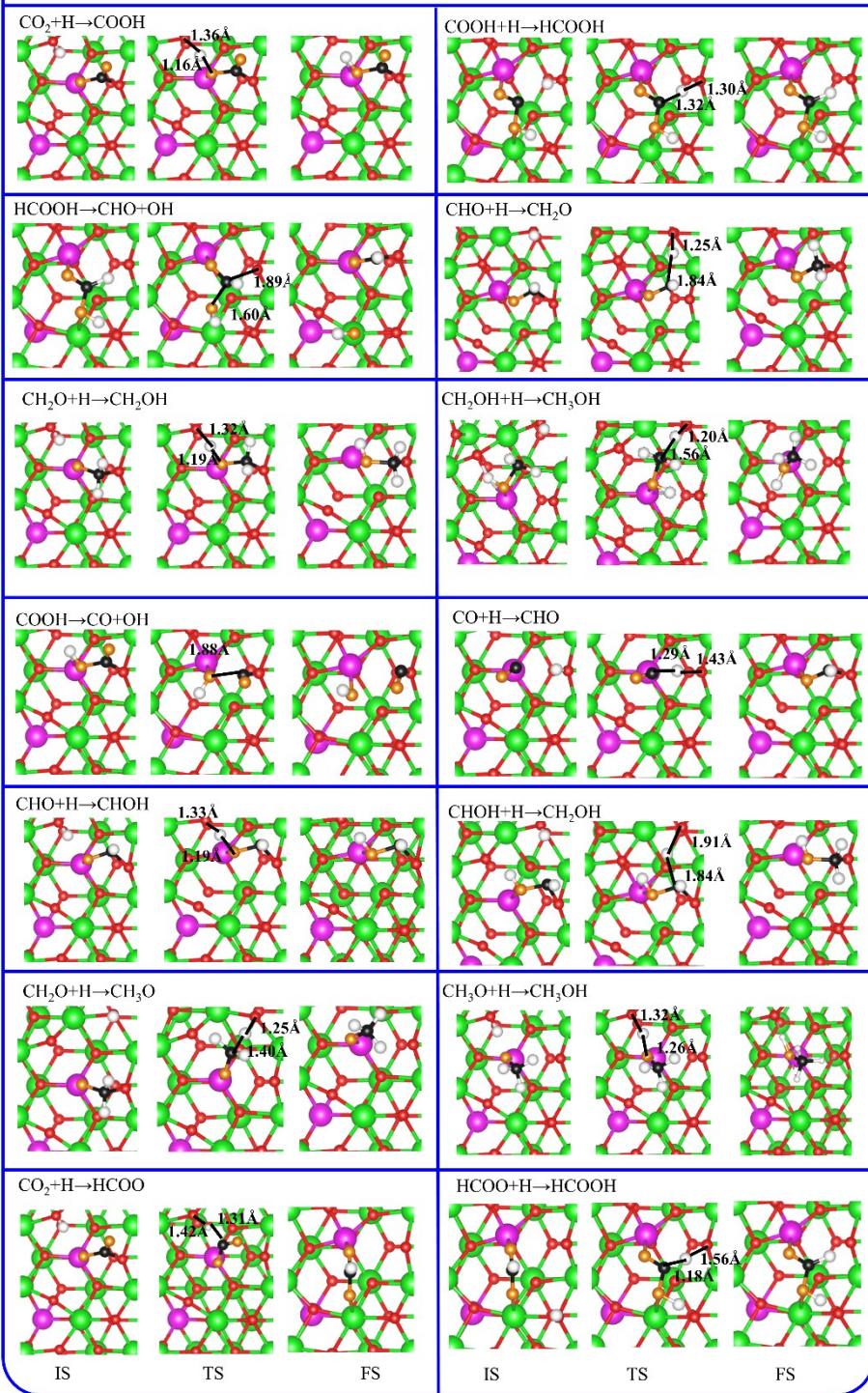
The Mechanism of CO<sub>2</sub> Hydrogenation to CH<sub>3</sub>OH on MZrO<sub>x</sub> (M = Ga,  
Cr) Solid-Solution Catalysts and Effects of Lattice Strain

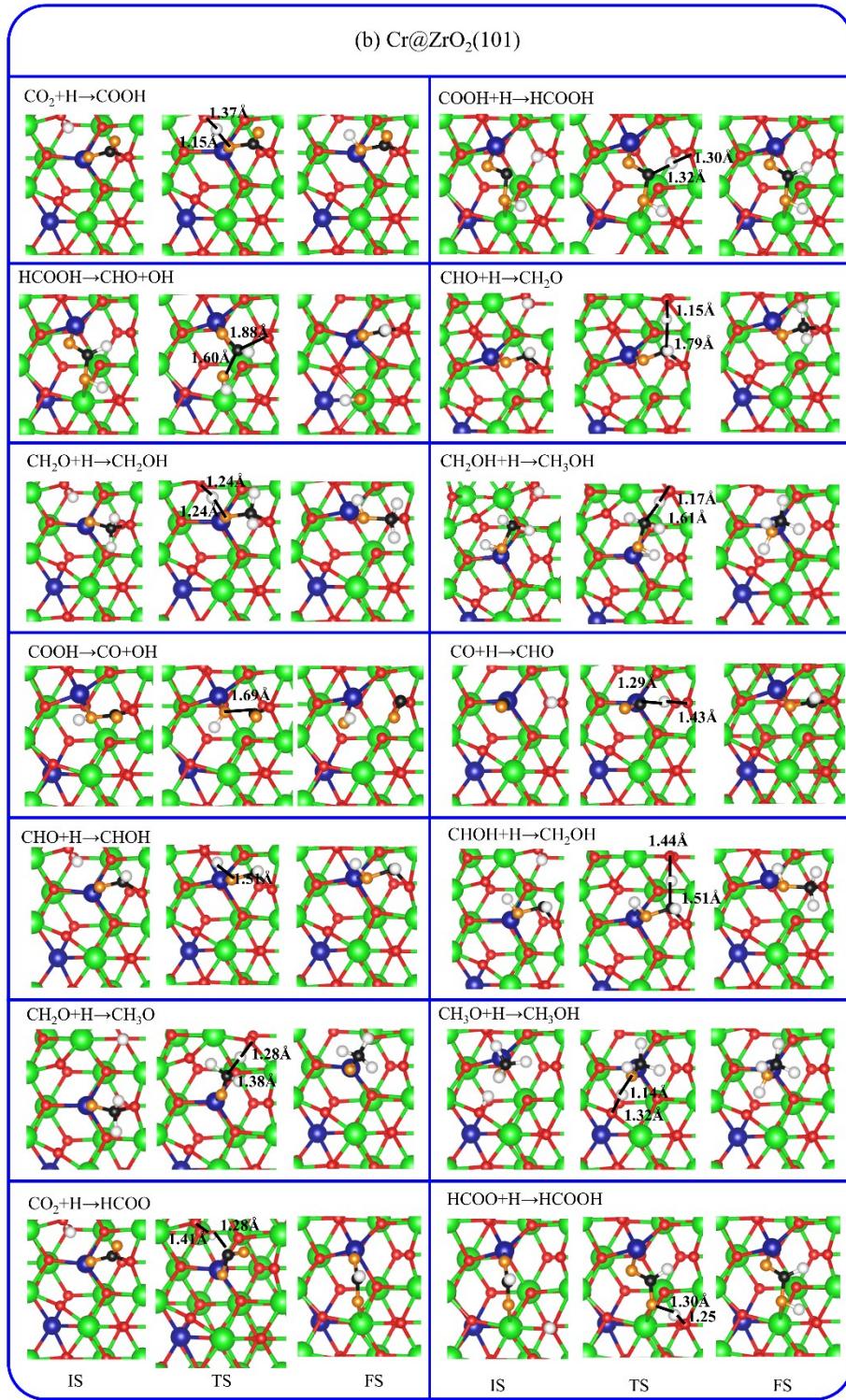
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(a) Ga@ZrO<sub>2</sub>(101)



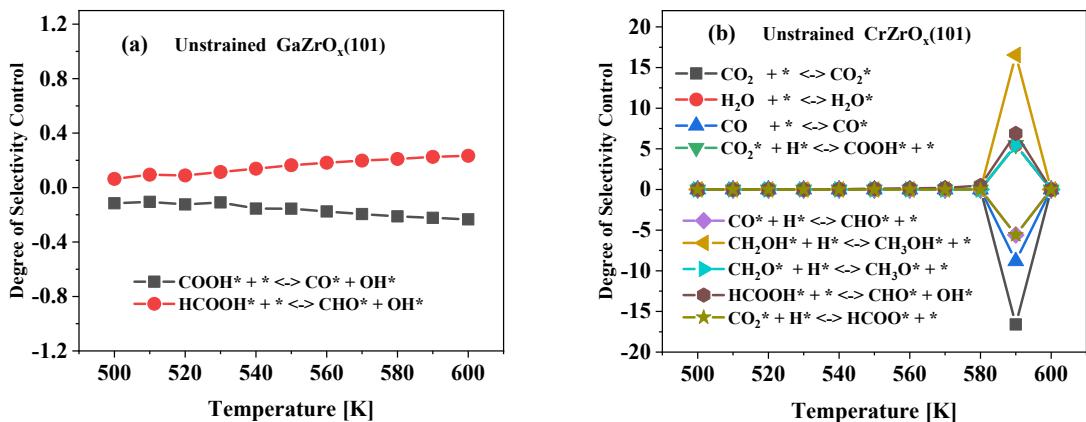


**Figure S1.** The initial state (IS), transition state (TS) and final state (FS) of elementary steps involved in  $\text{CO}_2$  hydrogenation to methanol on the GaZrO<sub>x</sub>(101) (a) and CrZrO<sub>x</sub>(101) (b) surfaces.

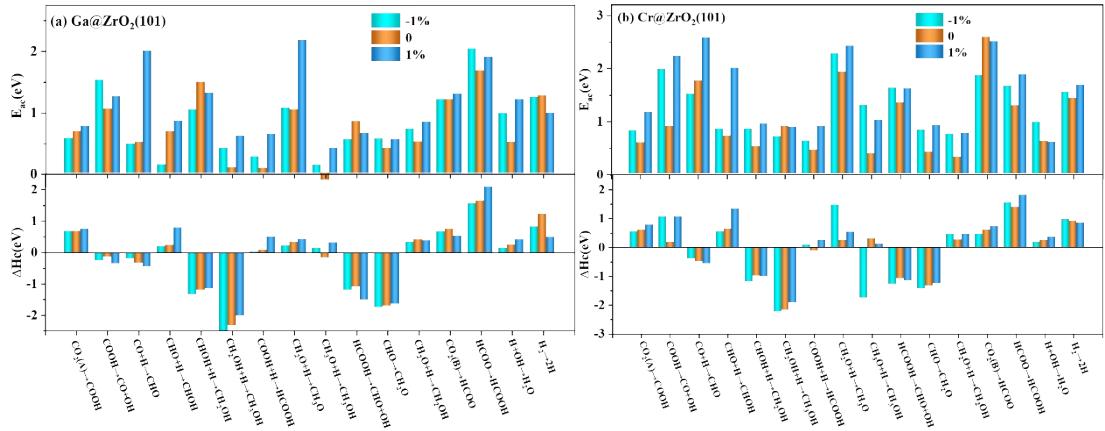
**Table S1.** The barrier ( $E_a$ ) and reaction heat ( $\Delta H$ ) without zero-point energy corrections of elementary steps involved in CO<sub>2</sub> hydrogenation to methanol on the MZrO<sub>x</sub>(101) (M = Ga, Cr) surfaces with strain from -1% to 1% <sup>a</sup>.

Elementary step	$E_a/\text{eV} (-1\%/0\%/1\%)$		$\Delta H/\text{eV} (-1\%/0\%/1\%)$	
	GaZrO <sub>x</sub> (101)	CrZrO <sub>x</sub> (101)	GaZrO <sub>x</sub> (101)	CrZrO <sub>x</sub> (101)
CO*+H*→CHO*+*	0.60/0.62/2.13	1.66/1.86/2.75	-0.25/-0.40/-0.49	-0.45/-0.54/-0.61
CHOH*+H*→CH <sub>2</sub> OH*+*	1.22/1.68/1.49	0.94/0.64/1.08	-1.38/-1.20/-1.21	-1.25/-1.02/-1.05
CH <sub>2</sub> OH*+H*→CH <sub>3</sub> OH*+*	0.52/0.22/0.75	0.78/1.04/1.01	-2.51/-2.34/-2.05	-2.29/-2.21/-1.95
COOH*+H*→HCOOH*+*	0.35/0.25/0.75	0.72/0.62/1.01	0.00/0.08/0.47	0.05/-0.15/0.22
CH <sub>2</sub> O*+H*→CH <sub>3</sub> O*+*	1.29/1.27/2.40	2.46/2.13/2.63	0.29/0.32/0.49	1.51/0.28/0.57
CHO*+H*→CH <sub>2</sub> O*+*	0.67/0.53/0.68	0.91/0.52/1.03	-1.81/-1.70/-1.70	-1.49/-1.39/-1.31
CO <sub>2</sub> *+H*→HCOO*+*	1.41/1.40/1.50	1.66/1.04/2.76	0.69/0.76/0.55	-0.26/-0.22/-0.01
CO <sub>2</sub> *+H*→COOH*+*	0.70/0.81/0.89	0.93/0.70/1.30	0.68/0.68/0.78	0.60/0.59/0.79
CHO*+H*→CHOH*+*	0.26/0.81/0.98	0.98/0.84/2.17	0.12/0.24/0.80	0.54/0.64/1.37
CH <sub>2</sub> O*+H*→CH <sub>2</sub> OH*+*	0.84/0.63/0.97	0.85/0.44/0.90	0.32/0.41/0.39	0.43/0.28/0.44
CH <sub>3</sub> O*+H*→CH <sub>3</sub> OH*+*	0.23/0.38/0.50	1.36/0.48/1.12	0.14/0.17/0.30	-1.81/0.27/0.09
H*+HCOO*→HCOOH*+*	2.19/1.85/2.05	1.79/1.43/2.03	1.58/1.65/2.11	1.58/1.42/1.84
H*+OH*→H <sub>2</sub> O*+*	1.09/0.61/1.32	1.09/0.72/0.70	0.15/0.24/0.40	0.17/0.24/0.34
HCOOH*+*→CHO*+OH*	0.54/0.75/0.69	1.66/1.38/1.60	-1.20/-1.11/-1.51	-1.25/-1.08/-1.19
COOH*+*→CO*+OH*	1.64/1.16/1.38	1.99/0.96/2.34	-0.25/-0.14/-0.28	1.11/0.24/1.15
H <sub>2</sub> *+*→2H*	1.22/1.25/0.96	1.53/1.42/1.64	0.82/1.24/0.37	0.87/0.79/0.72

a: The data of each column represents the result at -1%, 0 and 1% strain respectively.



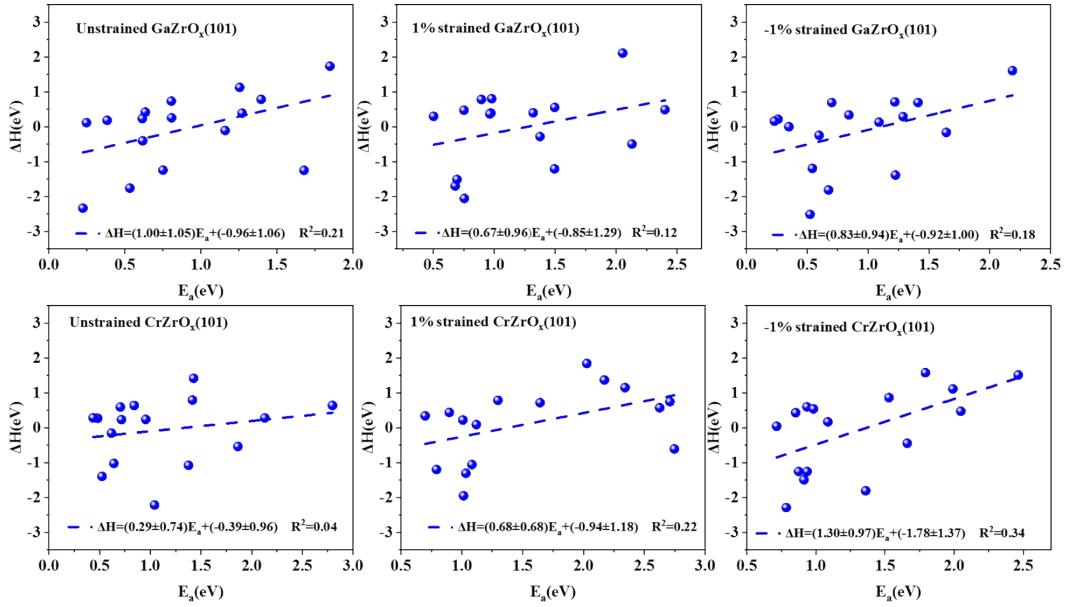
**Figure S2.** Degree of selectivity control (DSC) of methanol as a function of temperature on the GaZrO<sub>x</sub>(101) (a) and CrZrO<sub>x</sub>(101) (b) surface with strain from -1% to 1%. Simulation conditions: CO<sub>2</sub>:H<sub>2</sub> = 1:3, p = 20 bar. Only elementary steps with the DSC coefficients greater than 0.2 (absolute values) are shown.



**Figure S3.** Zero-point corrected barriers ( $E_{ac}$ ) and reaction heats ( $\Delta H_c$ ) of elementary steps involved in  $\text{CO}_2$  hydrogenation to methanol over the  $\text{GaZrO}_x(101)$  ((a), (b)) and  $\text{CrZrO}_x(101)$  ((c), (d)) surfaces with strain from -1% to 1%.

**Table S2.** The bond length ( $d, \text{\AA}$ ) of the initial and transition states of the step of  $\text{HCOOH} \rightarrow \text{CHO} + \text{OH}$  on  $\text{M}\text{ZrO}_x(101)$  ( $\text{M} = \text{Ga, Cr}$ ) surfaces. All unit are in  $\text{\AA}$ . For the atomic numbering, please see Figure 1c in the body text.

GaZrO <sub>x</sub> (101)						CrZrO <sub>x</sub> (101)							
	IS			TS				IS			TS		
M-O <sub>M</sub>	2.2859	2.0506	2.3467	1.9168	1.9832	2.0009	2.2364	2.1264	2.1333	1.9767	1.9834	2.0033	
Zr-O <sub>Z</sub>	2.5760	2.6399	2.7454	2.2908	2.3001	2.3211	2.5506	2.6146	2.5189	2.2752	2.2999	2.3229	
C-O <sub>M</sub>	1.2120	1.2578	1.2081	1.2871	1.2532	1.2549	1.2109	1.2396	1.2303	1.2439	1.2531	1.2655	
C-O <sub>Z</sub>	1.3573	1.3666	1.3539	1.5431	1.6005	1.6162	1.3598	1.3500	1.3409	1.5465	1.6004	1.6164	
C-H <sub>2</sub>	1.1015	1.1778	1.1070	1.0922	1.0983	1.0938	1.1037	1.1158	1.1008	1.0884	1.0981	1.1091	
O <sub>Z</sub> -H <sub>1</sub>	0.9798	1.0345	0.9800	0.9953	0.9881	0.9866	1.1037	1.0235	1.0698	0.9840	0.9880	0.9978	
C-O <sub>1</sub>	---	---	---	1.6528	1.8851	1.8579	---	---	---	1.9342	1.8846	1.9034	
H <sub>2</sub> -O <sub>1</sub>	3.7242	1.5652	3.7725	2.0301	2.1236	2.1236	3.6934	1.8142	2.5375	2.1174	2.1234	2.1446	
O <sub>2</sub> -H <sub>1</sub>	2.8582	1.6821	3.0432	1.8640	2.6800	2.7046	2.1602	1.7786	1.5788	2.6431	2.6796	2.7063	



**Figure S4.** BEP relationship on MZrO<sub>x</sub>(101)(M = Ga, Cr) surfaces with strain from -1% to 1%.

**Table S3.** The absolute errors (AEs, eV) between predicted barrier by BEP relationship between the oxygen hydrogenation or carbon hydrogenation elementary steps and calculated barrier by DFT on MZrO<sub>x</sub>(101) (M = Ga, Cr) with strain from -1% to 1%.

	Absolute Errors(AEs)	GaZrO <sub>x</sub> (101)			CrZrO <sub>x</sub> (101)		
		-1%	0	1%	-1%	0	1%
	CO*+H*→CHO*+*	0.78	0.41	0.51	0.40	0.28	0.87
	CHOH*+H*→CH <sub>2</sub> OH*+*	1.09	1.26	0.73	0.13	0.16	0.08
	CH <sub>2</sub> OH*+H*→CH <sub>3</sub> OH*+*	1.40	1.21	1.00	0.93	1.33	0.93
C-H bond	COOH*+H*→HCOOH*+*	1.31	1.22	1.53	1.50	1.05	1.25
	CH <sub>2</sub> O*+H*→CH <sub>3</sub> O*+*	0.51	0.70	0.26	0.36	0.33	0.40
	CHO*+H*→CH <sub>2</sub> O*+*	0.88	0.87	0.59	0.33	0.12	0.29
	CO <sub>2</sub> (B)*+H*→HCOO*+*	0.77	1.00	1.03	0.06	0.18	0.51
	CO <sub>2</sub> (A)*+H*→COOH*+*	0.29	0.19	0.23	0.44	0.10	0.04
O-H bond	CHO*+H*→CHOH*+*	0.11	0.29	0.16	0.36	0.02	0.24
	CH <sub>2</sub> O*+H*→CH <sub>2</sub> OH*+*	0.16	0.06	0.24	0.31	0.10	0.09
	CH <sub>3</sub> O*+H*→CH <sub>3</sub> OH*+*	0.07	0.10	0.18	2.13	0.04	0.47
	H*+HCOO*→HCOOH*+*	0.21	0.03	0.29	1.08	0.06	0.38
	H*+OH*→H <sub>2</sub> O*+*	0.53	0.10	0.62	0.05	0.28	0.19

**Table S4.** The slope, intercept (eV), correlation ( $R^2$ ) of BEP relationship between the oxygen hydrogenation or carbon hydrogenation elementary steps on  $\text{GaZrO}_x(101)/\text{CrZrO}_x(101)$  surfaces with strain from -1% to 1%, the mean/maximum absolute error(eV) between predicted value by BEP and calculated value by DFT.

C-H bond	GaZrO <sub>x</sub> (101)			CrZrO <sub>x</sub> (101)		
	-1%	0	1%	-1%	0	1%
slope	1.17±2.28	0.78±1.64	0.78±1.24	1.49±0.99	0.76±0.73	0.74±0.79
intercept	-1.72±2.17	-1.30±1.66	-1.64±1.90	-2.52±1.48	-1.68±1.16	-1.78±1.52
$R^2$	0.17	0.15	0.24	0.65	0.47	0.41
mean absolute error	0.96	0.95	0.81	0.53	0.49	0.62
maximum absolute error	1.40	1.26	1.53	1.50	1.33	1.25
O-H bond	GaZrO <sub>x</sub> (101)			CrZrO <sub>x</sub> (101)		
	-1%	0	1%	-1%	0	1%
slope	0.67±0.42	1.11±0.33	1.09±0.68	0.40±3.14	1.19±0.40	0.99±0.51
intercept	-0.07±0.46	-0.34±0.32	-0.43±0.82	-0.21±3.81	-0.34±0.33	-0.54±0.75
$R^2$	0.72	0.92	0.72	0.02	0.90	0.79
mean absolute error	0.23	0.13	0.29	0.73	0.10	0.24
maximum absolute error	0.53	0.29	0.62	2.13	0.28	0.47

**Table S5.** The absolute errors (AEs, eV) between predicted barrier by TSS relationship between the oxygen hydrogenation or carbon hydrogenation elementary steps and calculated barrier by DFT on  $\text{M}\text{ZrO}_x(101)$  ( $\text{M} = \text{Ga}, \text{Cr}$ ) with strain from -1% to 1%.

Absolute Errors(AEs)	GaZrO <sub>x</sub> (101)			CrZrO <sub>x</sub> (101)		
	-1%	0	1%	-1%	0	1%
$\text{CO}^*+\text{H}^*\rightarrow\text{CHO}^*+*$	0.39	0.33	0.35	0.16	0.26	0.68
$\text{CHOH}^*+\text{H}^*\rightarrow\text{CH}_2\text{OH}^*+*$	0.53	0.94	0.53	0.01	0.03	0.05
$\text{CH}_2\text{OH}^*+\text{H}^*\rightarrow\text{CH}_3\text{OH}^*+*$	0.43	0.67	0.80	0.94	0.97	1.25
C-H bond	$\text{COOH}^*+\text{H}^*\rightarrow\text{HCOOH}^*+*$	0.30	0.46	0.02	0.40	0.43
	$\text{CH}_2\text{O}^*+\text{H}^*\rightarrow\text{CH}_3\text{O}^*+*$	0.27	0.32	0.62	0.97	0.59
	$\text{CHO}^*+\text{H}^*\rightarrow\text{CH}_2\text{O}^*+*$	0.06	0.23	0.32	0.38	0.70
	$\text{CO}_2^*+\text{H}^*\rightarrow\text{HCOO}^*+*$	0.37	0.43	0.351	0.57	1.27
O-H bond	$\text{CO}_2^*+\text{H}^*\rightarrow\text{COOH}^*+*$	0.18	0.17	0.12	0.03	0.21
	$\text{CHO}^*+\text{H}^*\rightarrow\text{CHOH}^*+*$	0.60	0.02	0.10	0.17	0.14

$\text{CH}_2\text{O}^* + \text{H}^* \rightarrow \text{CH}_2\text{OH}^* + *$	0.17	0.08	0.06	0.25	0.21	0.35
$\text{CH}_3\text{O}^* + \text{H}^* \rightarrow \text{CH}_3\text{OH}^* + *$	0.85	0.58	0.79	0.36	0.35	0.29
$\text{H}^* + \text{HCOO}^* \rightarrow \text{HCOOH}^* + *$	1.07	0.85	0.67	0.37	0.43	0.47
$\text{H}^* + \text{OH}^* \rightarrow \text{H}_2\text{O}^* + *$	0.03	0.34	0.03	0.28	0.22	0.79

**Table S6.** The slope, intercept (eV), correlation ( $R^2$ ) of TSS relationship between the oxygen hydrogenation or carbon hydrogenation elementary steps on  $\text{GaZrO}_x(101)/\text{CrZrO}_x(101)$  surfaces with strain from -1% to 1%, the mean/maximum absolute error(eV) between predicted value by TSS and calculated value by DFT.

C-H bond	GaZrO <sub>x</sub> (101)			CrZrO <sub>x</sub> (101)		
	-1%	0	1%	-1%	0	1%
slope	1.21±0.43	1.13±0.60	1.51±0.52	1.34±0.72	1.48±0.77	1.52±0.86
intercept	-1.64±1.66	-1.34±2.34	-3.34±2.04	-2.78±3.08	-3.46±3.43	-4.13±3.99
$R^2$	0.86	0.74	0.87	0.74	0.75	0.71
mean absolute error	0.34	0.48	0.43	0.49	0.61	0.64
maximum absolute error	0.53	0.94	0.80	0.94	1.27	1.25

O-H bond	GaZrO <sub>x</sub> (101)			CrZrO <sub>x</sub> (101)		
	-1%	0	1%	-1%	0	1%
slope	0.84±0.44	0.90±0.32	0.85±0.30	0.84±0.25	0.82±0.29	0.85±0.55
intercept	-0.06±2.37	-0.34±1.72	-0.33±1.60	-0.35±1.32	0.22±1.63	-0.50±3.24
$R^2$	0.79	0.89	0.89	0.92	0.89	0.70
mean absolute error	0.48	0.34	0.29	0.24	0.26	0.47
maximum absolute error	1.07	0.85	0.79	0.37	0.43	0.79