## Supporting Information for

# Effect of coordinated anions on ferromagnetically coupled Dy zero-field single-molecule magnets 

Cai-Ming Liu, ${ }^{* a}$ Xiang Hao, ${ }^{\text {a }}$ Dong-Mei Zhu ${ }^{* b}$ and Yi-Quan Zhang ${ }^{\text {b }}$<br>${ }^{a}$ Beijing National Laboratory for Molecular Sciences, CAS Key Laboratory for Organic Solids, Institute of Chemistry, Chinese Academy of Sciences, Beijing 100190, China. E-mail: cmliu@iccas.ac.cn<br>${ }^{b}$ Jiangsu Key Laboratory for NSLSCS, School of Physical Science and Technology, Nanjing Normal University, Nanjing 210023, China. E-mail: 221001007@njnu.edu.cn

1. Fig. S1 and S2.The simulative and experimental powder X-ray diffraction patterns for $\mathbf{1}$ and 2.
2. Table S1. Dy (III) ion geometry analysis by SHAPE 2.1 software for $\mathbf{1}$ and $\mathbf{2}$.
3. Fig. S3 and S4. $M$ versus $H$ plots at $2-6 \mathrm{~K}$ of $\mathbf{1}$ and $\mathbf{2}$.
4. Fig. S5. Hysteresis loop for $\mathbf{1}$ at 1.9 K .
5. Fig. S6. Plots of $\chi^{\prime \prime}$ versus $T$ for $\mathbf{1}\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$.
6. Fig. S7. Plots of $\chi^{\prime \prime}$ versus $v$ for $\mathbf{1}\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$.
7. Fig. S8. Plot of $\ln (\tau)$ versus $1 / T$ for $\mathbf{1}\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$
8. Fig. S9. Hysteresis loop for $\mathbf{2}$ at 1.9 K
9. Fig. S10. Plots of $\chi^{\prime \prime}$ versus $T$ for $2\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$.
10. Fig. S11. Plots of $\chi^{\prime \prime}$ versus $v$ for $2\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$.
11. Fig. S12. Plot of $\ln (\tau)$ versus $1 / T$ for $2\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$.
12. Fig. S13. Calculated individual Dy ${ }^{\text {III }}$ fragments of $\mathbf{1}$ and $\mathbf{2}$.
13. Table S2. Calculated energy levels $\left(\mathrm{cm}^{-1}\right), \boldsymbol{g}\left(g_{x}, g_{y}, g_{z}\right)$ tensors and predominant $m_{J}$ values of the lowest eight Kramers doublets (KDs) of individual Dy ${ }^{\text {III }}$ fragments for $\mathbf{1}$ and $\mathbf{2}$.
14. Table S3. Wave functions with definite projection of the total moment $\mid \mathrm{mJ}>$ for the lowest eight KDs of individual $\mathrm{Dy}^{\text {III }}$ fragments for $\mathbf{1}$ and $\mathbf{2}$.
15. Fig. S14. Magnetization blocking barriers of individual Dy ${ }^{\text {III }}$ fragments for $\mathbf{1}$ and $\mathbf{2}$.
16. Table S 4 . Exchange energies $E\left(\mathrm{~cm}^{-1}\right)$, the energy difference between each exchange doublets $\Delta_{t}\left(\mathrm{~cm}^{-1}\right)$ and the main values of the $g_{z}$ for the lowest two exchange doublets of $\mathbf{1}$ and 2.


Fig. S1. The simulative and experimental powder X-ray diffraction patterns for $\mathbf{1}$.


Fig. S2. The simulative and experimental powder X-ray diffraction patterns for $\mathbf{2}$.

Table S1. Dy (III) ion geometry analysis by SHAPE 2.1 software for $\mathbf{1}$ and $\mathbf{2}$.

| Complex | $\mathbf{1}$ |  |
| :--- | :--- | :--- |
| Configuration | ABOXIY <br> Dy1 | ABOXIY <br> Dy1 |
| Octagon $\left(D_{8 \mathrm{~h}}\right)$ | 31.479 | 31.324 |
| Heptagonal pyramid $\left(C_{7 \mathrm{v}}\right)$ | 21.065 | 21.438 |
| Cube $\left(\mathrm{O}_{\mathrm{h}}\right)$ | 15.285 | 15.371 |
| Hexagonal bipyramid $\left(D_{6 \mathrm{~h}}\right)$ | 13.237 | 13.991 |
| Square antiprism $\left(D_{4 \mathrm{~d}}\right)$ | 5.901 | 5.942 |
| Triangular dodecahedron $\left(D_{2 \mathrm{~d}}\right)$ | $\mathbf{3 . 4 9 5}$ | 3.917 |
| Johnson gyrobifastigium J26 $\left(D_{2 \mathrm{~d}}\right)$ | 11.369 | 11.438 |
| Johnson elongated triangular bipyramid J14 <br> $\left(D_{3 \mathrm{~h}}\right)$ | 23.067 | 22.734 |
| Biaugmented trigonal prism J50 $\left(C_{2 \mathrm{v}}\right)$ | 3.663 | 3.496 |
| Biaugmented trigonal prism $\left(C_{2 \mathrm{v}}\right)$ | 3.631 | $\mathbf{3 . 3 2 5}$ |
| Snub diphenoid J84 $\left(D_{2 \mathrm{~d}}\right)$ | 4.267 | 4.807 |
| Triakis tetrahedron $\left(T_{\mathrm{d}}\right)$ | 13.924 | 14.620 |
| Elongated trigonal bipyramid $\left(D_{3 \mathrm{~h}}\right)$ | 21.413 | 20.796 |



Fig. S3. $M$ versus $H$ plots at $2-6 \mathrm{~K}$ of $\mathbf{1}$.


Fig. S4. $M$ versus $H$ plots at $2-6 \mathrm{~K}$ of $\mathbf{2}$.


Fig. S5. Hysteresis loop for $\mathbf{1}$ at 1.9 K with the normal sweep rate ( $100-300 \mathrm{Oe} \mathrm{min}^{-1}$ ).


Fig. S6. Plots of $\chi^{\prime \prime}$ versus $T$ for $\mathbf{1}\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$.


Fig. S7. Plots of $\chi^{\prime \prime}$ versus $v$ for $\mathbf{1}\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$.


Fig. S8. Plot of $\ln (\tau)$ versus $1 / T$ for $\mathbf{1}\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$; the solid line represents the best fitting with Orbach plus Raman.


Fig. S9. Hysteresis loop for 2 at 1.9 K with the normal sweep rate ( $100-300 \mathrm{Oe} \mathrm{min}^{-1}$ ).


Fig. S10. Plots of $\chi^{\prime \prime}$ versus $T$ for $2\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$.


Fig. S11. Plots of $\chi^{\prime \prime}$ versus $v$ for $2\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$.


Fig. S12. Plot of $\ln (\tau)$ versus $1 / T$ for $2\left(H_{\mathrm{dc}}=1500 \mathrm{Oe}\right)$; the solid line represents the best fitting with Orbach plus Raman.

## Computational details

For each of binuclear complexes $\mathbf{1}$ and $\mathbf{2}$, we only need to calculate one individual Dy ${ }^{\text {III }}$ fragment (1_Dy1 and 2_Dy1, respectively) due to their centrosymmetric structures. Complete-active-space self-consistent field (CASSCF) calculations on individual Dy ${ }^{\text {III }}$ fragments for $\mathbf{1}$ and 2 (see Fig. S1 for the calculated complete structures of $\mathbf{1}$ and $\mathbf{2}$ ) on the basis of singlecrystal X-ray determined geometries have been carried out with the OpenMolcas ${ }^{\text {S1 }}$ program package. Each individual $\mathrm{Dy}^{\mathrm{III}}$ fragment in $\mathbf{1}$ and $\mathbf{2}$ was calculated keeping the experimentally determined structure of the corresponding compound while replacing the neighboring Dy ${ }^{\text {III }}$ ion by diamagnetic $\mathrm{Lu}^{\text {III }}$.

The basis sets for all atoms are atomic natural orbitals from the OpenMolcas ${ }^{\text {S1 }}$ ANO-RCC library: ANO-RCC-VTZP for Dy ${ }^{\text {III }}$; VTZ for close N and O; VDZ for distant atoms. The calculations employed the second order Douglas-Kroll-Hess Hamiltonian, where scalar relativistic contractions were taken into account in the basis set and the spin-orbit couplings were handled separately in the restricted active space state interaction (RASSI-SO) procedure. ${ }^{52-S 3}$ Active electrons in 7 active orbitals include all $f$ electrons (CAS ( 9 in 7 ) in the CASSCF calculation. To exclude all the doubts, we calculated all the roots in the active space. We have mixed the maximum number of spin-free state which was possible with our hardware (all from 21 sextets, 128 from 224 quadruplets, 130 from 490 doublets for Dy ${ }^{\text {III }}$. SINGLE_ANISO ${ }^{\text {S2 }}$ program was used to obtain the energy levels, $\boldsymbol{g}$ tensors, magnetic axes, et al. based on the above CASSCF/RASSI-SO calculations.

1_Dy1

2_Dy1

Fig. S13. Calculated individual Dy ${ }^{\text {III }}$ fragments of $\mathbf{1}$ and 2; H atoms are omitted for clarify.

Table S2. Calculated energy levels $\left(\mathrm{cm}^{-1}\right), \boldsymbol{g}\left(g_{x}, g_{y}, g_{z}\right)$ tensors and predominant $m_{J}$ values of the lowest eight Kramers doublets (KDs) of individual Dy ${ }^{\text {III }}$ fragments for $\mathbf{1}$ and 2 using CASSCF/RASSI-SO with the OpenMolcas.

| KDs | 1_Dy1 |  |  | 2_Dy1 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | E | $g$ | $m_{J}$ | E | $g$ | $m_{J}$ |
| 0 | 0.0 | $\begin{array}{r} 0.007 \\ 0.012 \\ 19.637 \end{array}$ | $\pm 15 / 2$ | 0.0 | $\begin{gathered} 0.011 \\ 0.022 \\ 19.571 \end{gathered}$ | $\pm 15 / 2$ |
| 1 | 211.2 | $\begin{array}{r} 0.133 \\ 0.165 \\ 16.999 \end{array}$ | $\pm 13 / 2$ | 170.9 | $\begin{gathered} 0.194 \\ 0.381 \\ 16.983 \end{gathered}$ | $\pm 13 / 2$ |
| 2 | 385.8 | $\begin{array}{r} 3.195 \\ 6.061 \\ 10.367 \end{array}$ | - | 269.8 | $\begin{gathered} 0.443 \\ 1.244 \\ 17.030 \end{gathered}$ | - |
| 3 | 425.9 | $\begin{array}{r} 0.071 \\ 3.376 \\ 12.996 \end{array}$ | - | 328.1 | $\begin{gathered} 1.223 \\ 2.725 \\ 13.897 \end{gathered}$ | - |
| 4 | 441.8 | $\begin{array}{r} 3.634 \\ 3.833 \\ 10.432 \end{array}$ | - | 349.7 | $\begin{gathered} 1.097 \\ 2.116 \\ 10.712 \end{gathered}$ | - |
| 5 | 532.4 | $\begin{aligned} & 9.828 \\ & 6.563 \\ & 3.029 \end{aligned}$ | - | 425.0 | $\begin{gathered} 4.433 \\ 5.652 \\ 10.139 \end{gathered}$ | - |
| 6 | 563.4 | $\begin{array}{r} 1.641 \\ 3.929 \\ 14.443 \end{array}$ | - | 454.9 | $\begin{gathered} 2.184 \\ 2.848 \\ 14.239 \end{gathered}$ | - |
| 7 | 577.1 | $\begin{array}{r} 0.563 \\ 5.609 \\ 11.326 \end{array}$ | - | 538.8 | $\begin{gathered} 0.153 \\ 0.269 \\ 19.034 \end{gathered}$ | - |

Table S3. Wave functions with definite projection of the total moment $\mid m_{J}>$ for the lowest eight KDs of individual Dy ${ }^{\text {III }}$ fragments for $\mathbf{1}$ and 2 using CASSCF/RASSI-SO with the OpenMolcas.

|  | $E / \mathrm{cm}^{-1}$ | wave functions |
| :---: | :---: | :---: |
| 1_Dy1 | 0.0 | 96.0\% $\mid \pm 15 / 2>$ |
|  | 211.2 | $82.7 \%\| \pm 13 / 2>+7.9 \%\| \pm 9 / 2>$ |
|  | 385.8 | $33.0 \%\| \pm 11 / 2>+26.7 \%\| \pm 1 / 2>+20.5 \%\| \pm 3 / 2>+5.5 \%\| \pm 13 / 2>+5.4 \% \mid \pm 7 / 2>$ |
|  | 425.9 | $21.0 \%\| \pm 5 / 2>+20.6 \%\| \pm 1 / 2>+19.5 \%\| \pm 7 / 2>+15.5 \%\| \pm 11 / 2>+15.1 \% \mid \pm 3 / 2>$ |
|  | 441.8 | $22.4 \%\| \pm 1 / 2>+19.9 \%\| \pm 3 / 2>+19.2 \%\| \pm 5 / 2>+16.7 \%\| \pm 11 / 2>+12.8 \% \mid \pm 9 / 2>$ |
|  | 532.4 | $34.2 \%\| \pm 9 / 2>+20.1 \%\| \pm 11 / 2>+14.1 \%\| \pm 7 / 2>+11.9 \%\| \pm 3 / 2>+11.7 \% \mid \pm 5 / 2>$ |
|  | 563.4 | $27.6 \%\| \pm 3 / 2>+25.5 \%\| \pm 5 / 2>+20.0 \%\| \pm 7 / 2>+14.0 \%\| \pm 1 / 2>+10.0 \% \mid \pm 9 / 2>$ |
|  | 577.1 | $36.2 \%\| \pm 7 / 2>+26.9 \%\| \pm 9 / 2>+20.3 \%\| \pm 5 / 2>+9.4 \%\| \pm 1 / 2>$ |
| 2_Dy1 | 0.0 | 94.9\% $\mid \pm 15 / 2>$ |
|  | 170.9 | $71.9 \%\| \pm 13 / 2>+10.9 \%\| \pm 9 / 2>+10.7 \% \mid \pm 11 / 2>$ |
|  | 269.8 | $43.7 \%\| \pm 1 / 2>+31.2 \%\| \pm 3 / 2>+10.5 \%\| \pm 5 / 2>+4.8 \%\| \pm 7 / 2>$ |
|  | 328.1 | $27.8 \%\| \pm 5 / 2>+19.6 \%\| \pm 1 / 2>+14.4 \%\| \pm 3 / 2>+13.0 \%\| \pm 7 / 2>+10.8 \%\| \pm 9 / 2>+9.3 \%\| \pm 11 / 2>$ |
|  | 349.7 | $29.3 \%\| \pm 11 / 2>+17.5 \%\| \pm 7 / 2>+16.7 \%\| \pm 13 / 2>+13.2 \%\| \pm 3 / 2>+11.0 \%\| \pm 9 / 2>+6.9 \%\| \pm 5 / 2>$ |
|  | 425.0 | $28.7 \%\| \pm 7 / 2>+24.4 \%\| \pm 11 / 2>+20.5 \%\| \pm 5 / 2>+13.8 \%\| \pm 9 / 2>+7.1 \% \mid \pm 3 / 2>$ |
|  | 454.9 | $26.7 \%\| \pm 3 / 2>+20.8 \%\| \pm 1 / 2>+20.0 \%\| \pm 9 / 2>+19.7 \%\| \pm 5 / 2>+8.3 \% \mid \pm 11 / 2>$ |
|  | 538.8 | $31.6 \%\| \pm 9 / 2>+29.7 \%\| \pm 7 / 2>+13.6 \%\| \pm 5 / 2>+9.4 \%\| \pm 11 / 2>+6.9 \% \mid \pm 3 / 2>$ |



Fig. S14. Magnetization blocking barriers of individual $\mathrm{Dy}^{\text {III }}$ fragments for $\mathbf{1}$ and 2. The thick black lines represent the KDs as a function of their magnetic moment along the magnetic axis. The green lines correspond to diagonal quantum tunneling of magnetization (QTM); the blue line represent off-diagonal relaxation process. The path shown by the red arrows represents the most probable path for magnetic relaxation in the corresponding compounds. The numbers at each arrow stand for the mean absolute value of the corresponding matrix element of transition magnetic moment.

To fit the exchange interactions in $\mathbf{1}$ and $\mathbf{2}$, we took two steps to obtain them. Firstly, we calculated individual Dy ${ }^{\text {III }}$ fragments using CASSCF/RASSI-SO to obtain the corresponding magnetic properties. Then, the exchange interaction between the magnetic centers was considered within the Lines model, ${ }^{\mathrm{S7}}$ while the account of the dipole-dipole magnetic coupling was treated exactly. The Lines model is effective and has been successfully used widely in the research field of $d$ and $f$-elements single-molecule magnets. ${ }^{\text {s- }}$ s9

For complexes $\mathbf{1}$ and $\mathbf{2}$, there is only one type of $\tilde{J}$. The Ising exchange Hamiltonian is:

$$
\begin{equation*}
\hat{H}_{e x c h}=-\tilde{J} \hat{\tilde{S}}_{D y 1} \hat{\tilde{S}}_{D y 2} \tag{S1}
\end{equation*}
$$

$\tilde{J}=25 \cos \varphi J$, where $\varphi$ is the angle between the anisotropy axes on two Dy ${ }^{\text {III }}$ sites, and $J$ is the Lines exchange coupling parameter. $\tilde{S}_{D y}=1 / 2$ is the ground pseudospin on the Dy ${ }^{\text {III }}$ site. $\tilde{J}_{\text {total }}$ is the parameter of the total magnetic interaction $\left(\tilde{J}_{\text {toata }}=\tilde{J}_{\text {dip }}+\tilde{J}_{\text {exch }}\right)$ between magnetic center ions. The dipolar magnetic coupling can be calculated exactly, while the exchange coupling constant was fitted through comparison of the computed and measured magnetic susceptibilities using the POLY_ANISO program. ${ }^{\text {S4-S6 }}$

Table S4. Exchange energies $E\left(\mathrm{~cm}^{-1}\right)$, the energy difference between each exchange doublets $\Delta_{t}\left(\mathrm{~cm}^{-1}\right)$ and the main values of the $g_{z}$ for the lowest two exchange doublets of $\mathbf{1}$ and $\mathbf{2}$.

|  | 1 |  |  | 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | E | $\Delta_{t}$ | $g_{z}$ | E | $\Delta_{t}$ | $g_{\text {z }}$ |
| 1 | 0.000000000000 | $8.091 \times 10^{-7}$ | 39.276 | 0.000000000000 | $3.199 \times 10^{-6}$ | 39.144 |
|  | 0.000000809097 |  |  | 0.000003198535 |  |  |
| 2 | 1.636012385591 | $1.529 \times 10^{-6}$ | 0.000 | 1.217504953395 | $5.096 \times 10^{-6}$ | 0.000 |
|  | 1.636013915023 |  |  | 1.217510049869 |  |  |

## References:

S1 Galván, I. F.; Vacher, M.; Alavi, A.; Angeli, C.; Aquilante, F.; Autschbach, J.; Bao, J. J.; Bokarev, S. I.; Bogdanov, N. A.; Carlson, R. K.; Chibotaru, L. F.; Creutzberg, J.; Dattani, N.; Delcey, M. G.; Dong, S. S.; Dreuw, A.; Freitag, L.; Frutos, L. M.; Gagliardi, L.; Gendron, F.; Giussani, A.; González, L.; Grell, G.; Guo, M. Y.; Hoyer, C. E.; Johansson, M.; Keller, S.; Knecht, S.; Kovacevic, G.; Källman, E.; Manni, G. L.; Lundberg, M.; Ma, Y. J.; Mai, S.; Malhado, J. P.; Malmqvist, P. Å.; Marquetand, P.; Mewes, S. A.; Norell, J.; Olivucci, M.; Oppel, M.; Phung, Q. M.; Pierloot, K.; Plasser, F.; Reiher, M.; Sand, A. M.; Schapiro, I.; Sharma, P.; Stein, C. J.; Sørensen, L. K.; Truhlar, D. G.; Ugandi, M.; Ungur, L.; Valentini, A.; Vancoillie, S.; Veryazov, V.; Weser, O.; Wesołowski, T. A.; Widmark, Per-Olof.; Wouters, S.; Zech, A.; Zobel, J. P.; Lindh. R. J. Chem. Theory Comput. 2019, 15, 5925-5964.

S2 Malmqvist, P. Å.; Roos, B. O.; Schimmelpfennig, B. Chem. Phys. Lett., 2002, 357, 230240.

S3 Heß, B. A.; Marian, C. M.; Wahlgren, U.; Gropen, O. Chem. Phys. Lett., 1996, 251, 365371.

S4 Chibotaru, L. F.; Ungur, L.; Soncini, A. Angew. Chem., Int. Ed. 2008, 47, 4126-4129.
S5 Ungur, L.; Van den Heuvel, W.; Chibotaru, L. F. New J. Chem. 2009, 33, 1224-1230.
S6 Chibotaru, L. F.; Ungur, L.; Aronica, C.; Elmoll, H.; Pilet, G.; Luneau, D. J. Am. Chem. Soc. 2008, 130, 12445-12455.
S7 Lines, M. E. J. Chem. Phys. 1971, 55, 2977-2984.
S8 Mondal, K. C.; Sundt, A.; Lan, Y. H.; Kostakis, G. E.; Waldmann, O.; Ungur, L.; Chibotaru, L. F.; Anson, C. E.; Powell, A. K. Angew. Chem., Int. Ed. 2012, 51, 7550-7554.

S9 Langley, S. K.; Wielechowski, D. P.; Vieru, V.; Chilton, N. F.; Moubaraki, B.; Abrahams, B. F.; Chibotaru, L. F.; Murray, K. S. Angew. Chem., Int. Ed. 2013, 52, 12014-12019.

