

**The Influence of Different Cations on the Structure and Spectral Properties of
 Ln^{3+} Tetrakis-Complexes with CAPH-type Ligand Dimethyl-N-
trichloroacetylaminodiphosphate**

Mariia B. Struhatska,^a Nataliia S. Kariaka,^{a*} Viktoriya V. Dyakonenko,^b Svitlana V. Shishkina,^b Sergii S. Smola,^c Nataliia V. Rusakova,^c Paula Gawryszewska,^d Oscar L. Malta,^e Albano N. Carneiro Neto,^f Viktor O. Trush,^a Volodymyr M. Amirkhanov ^{a,*}

^a Inorganic Chemistry Department, Taras Shevchenko National University of Kyiv, 12, Lva Tolstogo str., Kyiv 01601, Ukraine

^b SSI “Institute for Single Crystals”, National Academy of Sciences of Ukraine Nauky ave. 60, 61001 Kharkiv, Ukraine

^c A.V. Bogatsky Physicochemical Institute, NAS of Ukraine, 86, Lustdorfska doroga str., Odessa 65080, Ukraine

^d Faculty of Chemistry, University of Wroclaw, 14 F. Joliot-Curie Str., 50-383, Wroclaw, Poland

^e Departamento de Química Fundamental, Universidade Federal de Pernambuco, 50740-560, Recife, Brazil

^f Physics Department and CICECO – Aveiro Institute of Materials, University of Aveiro, 3810-193, Aveiro, Portugal

Contents

| | |
|--|----|
| 1. Theoretical Judd-Ofelt intensity parameters | 3 |
| 2. Tables | 4 |
| Table S1 | 4 |
| Table S2 | 4 |
| Table S4 | 6 |
| Table S5 | 6 |
| Table S6 | 6 |
| Table S7 | 8 |
| Table S8 | 9 |
| Table S9 | 10 |
| Table S10 | 11 |
| Table S11 | 12 |

| | |
|-----------------|----|
| Table S12 | 13 |
| Table S13 | 14 |
| Table S14 | 16 |
| Table S15 | 18 |
| Table S16 | 20 |
| Table S17 | 22 |
| Table S18 | 24 |
| 3. Figures..... | 26 |
| Figure S1..... | 26 |
| Figure S2..... | 27 |
| Figure S3..... | 28 |
| Figure S4..... | 29 |
| Figure S5..... | 30 |
| Figure S6..... | 31 |
| Figure S7..... | 32 |
| Figure S8..... | 33 |
| Figure S9..... | 34 |
| References..... | 35 |

1. Theoretical Judd-Ofelt intensity parameters

From the theoretical point of view, the intensity parameters are mainly formed by the forced electric dipole (FED) and dynamic coupling (DC) mechanisms for the $4f$ - $4f$ intensities when the lanthanide does not occupy a centrosymmetric site [1–4]. The expressions used here for the calculations of the intensity parameters (Ω_{λ}^{theo} , $\lambda = 2, 4, 6$) have been described in several references [5–7]. For this reason, a short explanation is given here:

$$\Omega_{\lambda}^{theo} = (2\lambda + 1) \sum_{t,p} \frac{|B_{\lambda tp}|^2}{2t + 1} , \quad B_{\lambda tp} = B_{\lambda tp}^{FED} + B_{\lambda tp}^{DC} \quad S1)$$

where,

$$B_{\lambda tp}^{FED} = \frac{2}{\Delta E} \langle r^{t+1} \rangle \Theta(t, \lambda) \left(\frac{4\pi}{2t + 1} \right)^{\frac{1}{2}} \sum_j \frac{e^2 \rho_j g_j (2\beta_j)^{t+1}}{R_j^{t+1}} (Y_p^{t*})_j \quad S2)$$

$$B_{\lambda tp}^{DC} = - \left[\frac{(\lambda + 1)(2\lambda + 3)}{(2\lambda + 1)} \right]^{\frac{1}{2}} \langle r^{\lambda} \rangle \langle f \| C^{(\lambda)} \| f \rangle \times \left(\frac{4\pi}{2t + 1} \right)^{\frac{1}{2}} \sum_j \frac{[(2\beta_j)^{t+1} \alpha_{OP,j} + \alpha'_j]}{R_j^{t+1}} (Y_p^{t*})_j \delta_{t,\lambda} \quad S3)$$

with t and p being the ranks and components of the spherical harmonics (Y_p^{t*}), $\langle f \| C^{(2)} \| f \rangle = -1.366$, $\langle f \| C^{(4)} \| f \rangle = 1.128$, $\langle f \| C^{(6)} \| f \rangle = -1.27$, ρ is the overlap integral between the valence subshells of the ligating atom and the $4f$ subshell of the lanthanide ion, $\beta = 1/(1 \pm \rho)$ is a parameter that defines the centroid of the electronic density of the chemical bond Ln–X (X= ligating atom), α' is the effective polarizability from each ligand around the Ln^{3+} and g is the charge factor. Both α' and g were estimated from fitting procedures in the JOYSpectra program [8]. Eq. S2 stands for the Simple Overlap Model (SOM) [6] for the odd component of the ligand field while Eq. S3 is the Bond Overlap Model (BOM) for the polarizability-dependent term (Dynamic Coupling mechanism) of $4f$ - $4f$ transitions [7]. α_{OP} are quantities related to the covalent fraction of a chemical bond [7,9–11]. See refs. [7,12,13] for more details on these expressions.

Table S5 summarizes the theoretical intensity parameters and the contribution of the FED mechanism while the values of α' and g obtained from the fitting procedure in the JOYSpectra [8] are shown in Table S7.

2. Tables

Table S1. Crystallographic data and experimental parameters for the NMe₄[EuL₄], NEt₄[EuL₄], PPh₄[GdL₄] structures.

| Compound | NMe ₄ [EuL ₄] | NEt ₄ [EuL ₄] | PPh ₄ [GdL ₄] |
|--|--|--|--|
| Formula | C ₂₀ H ₃₆ Cl ₁₂ EuN ₅ O ₁₆ P ₄ | C ₂₄ H ₄₄ Cl ₁₂ EuN ₅ O ₁₆ P ₄ | C ₄₀ H ₄₄ Cl ₁₂ GdN ₄ O ₁₆ P ₅ |
| D _{calc} / g cm ⁻³ | 1.675 | 1.684 | 1.697 |
| m/mm ⁻¹ | 2.015 | 1.947 | 1.789 |
| Formula Weight | 1303.78 | 1359.88 | 1574.29 |
| T/K | 294 | 294 | 173.15 |
| Crystal System | | monoclinic | |
| Space Group | P2/n | | P2 ₁ /c |
| a/E | 12.0428(8) | 20.4825(6) | 19.8828(8) |
| b/E | 10.2128(6) | 12.2546(3) | 19.1092(8) |
| c/E | 21.0833(11) | 21.3808(6) | 17.3678(6) |
| a° | 90 | 90 | 90 |
| b° | 94.501(5) | 92.286(2) | 110.925(3) |
| g° | 90 | 90 | 90 |
| V/E ³ | 2585.1(3) | 5362.4(2) | 6163.6(4) |
| Z | 2 | 4 | 4 |
| Measured Refl's. | 5084 | 38874 | 97953 |
| Indep't Refl's | 5084 | 10526 | 10860 |
| Refl's I≥2 s(I) | 4166 | 7499 | 8571 |
| R _{int} | . | 0.1013 | 0.1215 |
| Parameters | 297 | 624 | 711 |
| GooF | 1.071 | 1.053 | 1.102 |
| wR ₂ (all data) | 0.1861 | 0.2276 | 0.1438 |
| wR ₂ | 0.1747 | 0.2035 | 0.1261 |
| R ₁ (all data) | 0.0878 | 0.1061 | 0.1101 |
| R ₁ | 0.0725 | 0.0785 | 0.0612 |
| CCDC | 2290967 | 2290968 | 2290969 |

Table S2. Selected bond lengths (Å) in [EuL₄]⁻ and [GdL₄]⁻ anions.

| | | NMe ₄ [EuL ₄] | NEt ₄ [EuL ₄] | PPh ₄ [GdL ₄] |
|-----|----|--------------------------------------|--------------------------------------|--------------------------------------|
| Ln1 | O2 | 2.343(5) | 2.343(5) | 2.322(5) |
| Ln1 | O3 | 2.452(5) | 2.492(7) | 2.454(5) |
| Ln1 | O4 | 2.322(5) | 2.333(5) | 2.337(5) |
| Ln1 | O5 | 2.500(5) | 2.459(5) | 2.424(5) |
| Ln1 | O6 | 2.321(5) | 2.351(6) | 2.362(5) |
| Ln1 | O7 | 2.500(5) | 2.482(6) | 2.415(5) |
| Ln1 | O8 | 2.343(5) | 2.338(5) | 2.338(5) |
| Ln1 | O9 | 2.453(5) | 2.433(6) | 2.474(5) |

The root mean square deviation (RMSD) from the best point group symmetry for the coordination polyhedron of these complexes using the equation:

$$RMSD = \sqrt{\frac{1}{N} \sum_i^N [(x_i - x_i^s)^2 + (y_i - y_i^s)^2 + (z_i - z_i^s)^2]} \quad (S4)$$

where N is the total number of atoms in the coordination polyhedron (8 for all cases), while (x_i, y_i, z_i) and (x_i^s, y_i^s, z_i^s) are the Cartesian coordinates of the actual position of atom i and its ideal position (exact position within a point group symmetry), respectively.

Table S3 illustrates the deviation to the closest group symmetry for all compounds, as well as the comparison of the coordination polyhedron and the $[EuL_4]^-$ unit with each other.

These RMSD values indicate the degree of deviation of the actual coordination polyhedron structures from their idealized symmetries (D_{2d} , D_2 , and S_4), reflecting how closely the compounds are to their respective point group symmetries. Additionally, these point groups share the C_2 axis symmetry operation. The RMSD for a perfect C_2 operation along the z -axis (Figure S8) shows that larger cations result in higher distortion, which is consistent with the observed hypersensitivity ratios.

Table S3. The closest point group symmetry of the coordination polyhedron associated with the number of emission peaks and its deviation (RMSD in Å) from a pure point group symmetry. The RMSD values between structures of the coordination polyhedron and entire $[EuL_4]^-$ unit (in parentheses) are also presented.

| Compound | Closest point group symmetry | RMSD (Å) |
|--------------------------------------|--------------------------------------|-------------------|
| NMe ₄ [EuL ₄] | D_{2d} | 0.05530 |
| NEt ₄ [EuL ₄] | D_2 | 0.05607 |
| PPh ₄ [EuL ₄] | S_4 | 0.06189 |
| Compound 1 | Compound 2 | RMSD (Å) |
| NMe ₄ [EuL ₄] | NEt ₄ [EuL ₄] | 0.05075 (0.75405) |
| NMe ₄ [EuL ₄] | PPh ₄ [EuL ₄] | 0.10009 (2.08243) |
| NEt ₄ [EuL ₄] | PPh ₄ [EuL ₄] | 0.11276 (2.07116) |

Table S4. Emission decay times (in ms) of Cat[LnL₄] (Ln = Eu, Tb) measured at

different excitation wavelengths and the deviation of the monoexponential fitting function.

| Temperature | 298 K | | | 77 K | | |
|--------------------------------------|-----------|-----------|-----------|-----------|-----------|-----------|
| Excitation wavelength (nm) | 277 nm | 300 nm | 394 nm | 277 nm | 300 nm | 394 nm |
| NMe ₄ [EuL ₄] | | 2.62±0.01 | 2.65±0.01 | - | 2.72±0.03 | 2.67±0.04 |
| NEt ₄ [EuL ₄] | - | - | 2.78±0.01 | - | - | 2.76±0.01 |
| PPh ₄ [EuL ₄] | 1.45±0.01 | - | 1.39±0.01 | 1.43±0.01 | - | 1.41±0.01 |
| Excitation wavelength (nm) | 277 nm | 300 nm | 368 nm | 277 nm | 300 nm | 368 nm |
| NMe ₄ [TbL ₄] | - | 2.34±0.01 | 2.44±0.01 | - | 2.26±0.02 | 2.28±0.03 |
| NEt ₄ [TbL ₄] | - | - | 2.90±0.01 | - | | 2.66±0.03 |
| PPh ₄ [TbL ₄] | - | - | 1.78±0.03 | 1.58±0.02 | - | 1.42±0.01 |

Table S5. Theoretical Ω_λ and the contribution of the FED mechanism (both in units of 10^{-20} cm^2) for Q[LnL₄] (Q = [NMe₄]⁺, [NEt₄]⁺, and [PPh₄]⁺; Ln = Eu³⁺ and Tb³⁺).

| | Q[EuL ₄] | | | Q[TbL ₄] | | |
|---------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|
| [Q] ⁺ | [NMe ₄] ⁺ | [NEt ₄] ⁺ | [PPh ₄] ⁺ | [NMe ₄] ⁺ | [NEt ₄] ⁺ | [PPh ₄] ⁺ |
| Ω_2 (FED) | 4.264 (0.036) | 4.556 (0.010) | 12.858 (0.013) | 3.557 (0.023) | 3.716 (0.022) | 10.578 (0.008) |
| Ω_4 (FED) | 6.886 (0.312) | 6.064 (0.241) | 5.784 (0.162) | 5.036 (0.165) | 6.768 (0.190) | 4.315 (0.085) |
| Ω_6 (FED) | 1.912 (0.600) | 1.758 (0.463) | 1.797 (0.326) | 1.111 (0.301) | 1.400 (0.371) | 1.086 (0.163) |

Table S6. Values of effective polarizability (α' in \AA^3) and charge factors g (dimensionless) obtained for different coordinated oxygen, O=C (1) and O=P (2), as illustrated in the structure fragment below.



| | $\alpha'(1)$ | $\alpha'(2)$ | $g(1)$ | $g(2)$ |
|--------------------------------------|--------------|--------------|--------|--------|
| NMe ₄ [EuL ₄] | 0.566 | 0.732 | 0.881 | 0.938 |
| NEt ₄ [EuL ₄] | 0.354 | 0.744 | 0.869 | 0.774 |
| PPh ₄ [EuL ₄] | 0.241 | 0.899 | 0.705 | 0.639 |

Tables S7–S18 present the energy transfer rates calculated using the JOYSpectra web platform [8] (<http://www.joyspectra.website>). In these tables, Δ represents the donor–acceptor energy difference between donor and acceptor transitions. W_{d-d} , W_{d-m} , and W_{ex} denote the energy transfer by the dipole–dipole, dipole–multipole, and exchange mechanisms, respectively. W is the sum of all mechanisms for a given pathway (p). The forward (ligand-to-Ln) rates perspective, W^S represents the sum over W involving the S₁ as a donor, while W^T is the sum over W involving the T₁ as a donor state. From the backward (Ln-to-ligand) rates, W_b^S is the sum over W_b involving the S₁ as an acceptor, while W_b^T is the sum over W_b involving the T₁ as the acceptor state.

Table S7. Forward (ligand-to-Eu) IET rates for **NMe₄[EuL₄]**.

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm⁻¹) | W (s⁻¹) | W_{d-d} (s⁻¹) | W_{d-m} (s⁻¹) | W_{ex} (s⁻¹) |
|-----------|--------------------------------|---|-----------------------|--|--|--|--|---|
| 1 | S ₁ →S ₀ | 7F ₀ → ⁵ D ₀ | 0.0 | 20707 | 2.6E-01 | 1.6E-05 | 2.6E-01 | 0.0E+00 |
| 2 | S ₁ →S ₀ | 7F ₀ → ⁵ D ₁ | 0.2 | 18973 | 1.2E+03 | 0.0E+00 | 0.0E+00 | 1.2E+03 |
| 3 | S ₁ →S ₀ | 7F ₀ → ⁵ D ₂ | 0.0 | 16517 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 4 | S ₁ →S ₀ | 7F ₀ → ⁵ L ₆ | 1.0 | 12675 | 4.7E+03 | 4.4E+03 | 3.0E+02 | 0.0E+00 |
| 5 | S ₁ →S ₀ | 7F ₀ → ⁵ G ₆ | 1.1 | 11248 | 5.0E+03 | 4.6E+03 | 3.2E+02 | 0.0E+00 |
| 6 | S ₁ →S ₀ | 7F ₀ → ⁵ D ₄ | 3.2 | 10414 | 1.5E+04 | 1.6E+03 | 1.3E+04 | 0.0E+00 |
| 7 | S ₁ →S ₀ | 7F ₁ → ⁵ D ₀ | 0.0 | 21079 | 8.5E+00 | 0.0E+00 | 0.0E+00 | 8.5E+00 |
| 8 | S ₁ →S ₀ | 7F ₁ → ⁵ D ₁ | 0.0 | 19345 | 4.6E+00 | 2.8E-04 | 4.6E+00 | 4.2E-02 |
| 9 | S ₁ →S ₀ | 7F ₁ → ⁵ D ₂ | 0.1 | 16889 | 3.3E+02 | 0.0E+00 | 0.0E+00 | 3.3E+02 |
| 10 | S ₁ →S ₀ | 7F ₁ → ⁵ D ₃ | 0.4 | 14017 | 1.6E+03 | 2.6E+00 | 1.6E+03 | 0.0E+00 |
| 11 | S ₁ →S ₀ | 7F ₁ → ⁵ L ₆ | 0.0 | 13047 | 1.2E+02 | 1.1E+02 | 7.9E+00 | 0.0E+00 |
| 12 | S ₁ →S ₀ | 7F ₁ → ⁵ L ₇ | 0.2 | 12015 | 7.4E+02 | 7.0E+02 | 4.8E+01 | 0.0E+00 |
| 13 | S ₁ →S ₀ | 7F ₁ → ⁵ G ₂ | 91.3 | 11980 | 4.2E+05 | 0.0E+00 | 0.0E+00 | 4.2E+05 |
| 14 | S ₁ →S ₀ | 7F ₁ → ⁵ G ₃ | 2.3 | 11750 | 1.0E+04 | 3.2E+01 | 1.0E+04 | 0.0E+00 |
| 15 | S ₁ →S ₀ | 7F ₁ → ⁵ G ₆ | 0.1 | 11620 | 3.0E+02 | 2.8E+02 | 1.9E+01 | 0.0E+00 |
| 16 | S ₁ →S ₀ | 7F ₁ → ⁵ G ₅ | 0.2 | 11609 | 7.2E+02 | 5.8E+02 | 1.4E+02 | 0.0E+00 |
| | | | | <i>W^S</i> | 4.6×10 ⁵ | | | |
| 17 | T ₁ →S ₀ | 7F ₀ → ⁵ D ₀ | 0.0 | 5296 | 3.6E+02 | 2.2E-02 | 3.6E+02 | 0.0E+00 |
| 18 | T ₁ →S ₀ | 7F ₀ → ⁵ D ₁ | 84.6 | 3562 | 1.2E+09 | 0.0E+00 | 0.0E+00 | 1.2E+09 |
| 19 | T ₁ →S ₀ | 7F ₀ → ⁵ D ₂ | 0.0 | 1106 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 20 | T ₁ →S ₀ | 7F ₀ → ⁵ L ₆ | 0.0 | -2736 | 1.9E-04 | 1.8E-04 | 1.2E-05 | 0.0E+00 |
| 21 | T ₁ →S ₀ | 7F ₀ → ⁵ G ₆ | 0.0 | -4163 | 3.6E-08 | 3.4E-08 | 2.3E-09 | 0.0E+00 |
| 22 | T ₁ →S ₀ | 7F ₀ → ⁵ D ₄ | 0.0 | -4997 | 7.2E-10 | 7.6E-11 | 6.4E-10 | 0.0E+00 |
| 23 | T ₁ →S ₀ | 7F ₁ → ⁵ D ₀ | 14.1 | 5668 | 2.1E+08 | 0.0E+00 | 0.0E+00 | 2.1E+08 |
| 24 | T ₁ →S ₀ | 7F ₁ → ⁵ D ₁ | 0.0 | 3934 | 7.9E+04 | 5.2E-02 | 8.5E+02 | 7.8E+04 |
| 25 | T ₁ →S ₀ | 7F ₁ → ⁵ D ₂ | 1.3 | 1478 | 1.8E+07 | 0.0E+00 | 0.0E+00 | 1.8E+07 |
| 26 | T ₁ →S ₀ | 7F ₁ → ⁵ D ₃ | 0.0 | -1394 | 2.4E-01 | 3.9E-04 | 2.4E-01 | 0.0E+00 |
| 27 | T ₁ →S ₀ | 7F ₁ → ⁵ L ₆ | 0.0 | -2364 | 4.8E-05 | 4.5E-05 | 3.0E-06 | 0.0E+00 |
| 28 | T ₁ →S ₀ | 7F ₁ → ⁵ L ₇ | 0.0 | -3396 | 5.6E-07 | 5.3E-07 | 3.5E-08 | 0.0E+00 |
| 29 | T ₁ →S ₀ | 7F ₁ → ⁵ G ₂ | 0.0 | -3431 | 2.6E+00 | 0.0E+00 | 0.0E+00 | 2.6E+00 |
| 30 | T ₁ →S ₀ | 7F ₁ → ⁵ G ₃ | 0.0 | -3661 | 1.6E-06 | 4.9E-09 | 1.6E-06 | 0.0E+00 |
| 31 | T ₁ →S ₀ | 7F ₁ → ⁵ G ₆ | 0.0 | -3791 | 2.1E-08 | 2.0E-08 | 1.3E-09 | 0.0E+00 |
| 32 | T ₁ →S ₀ | 7F ₁ → ⁵ G ₅ | 0.0 | -3802 | 4.7E-08 | 3.7E-08 | 9.1E-09 | 0.0E+00 |
| | | | | <i>W^T</i> | 1.5×10 ⁹ | | | |

Table S8. Backward (Eu-to-ligand) IET rates for **NMe₄[EuL₄]**.

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm ⁻¹) | W_b (s ⁻¹) | W_{d-d} (s ⁻¹) | W_{d-m} (s ⁻¹) | W_{ex} (s ⁻¹) |
|-----------|---|--------------------------------|-----------------------|------------------------------|--------------------------|------------------------------|------------------------------|-----------------------------|
| 1 | ⁵ D ₀ → ⁷ F ₀ | S ₀ →S ₁ | 0.0 | -20707 | 1.3E-44 | 7.6E-49 | 1.3E-44 | 0.0E+00 |
| 2 | ⁵ D ₁ → ⁷ F ₀ | S ₀ →S ₁ | 0.0 | -18973 | 8.0E-38 | 0.0E+00 | 0.0E+00 | 8.0E-38 |
| 3 | ⁵ D ₂ → ⁷ F ₀ | S ₀ →S ₁ | 0.0 | -16517 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 4 | ⁵ L ₆ → ⁷ F ₀ | S ₀ →S ₁ | 0.0 | -12675 | 1.2E-24 | 1.1E-24 | 7.6E-26 | 0.0E+00 |
| 5 | ⁵ G ₆ → ⁷ F ₀ | S ₀ →S ₁ | 0.3 | -11248 | 1.2E-21 | 1.1E-21 | 7.9E-23 | 0.0E+00 |
| 6 | ⁵ D ₄ → ⁷ F ₀ | S ₀ →S ₁ | 70.0 | -10414 | 3.0E-19 | 3.1E-20 | 2.7E-19 | 0.0E+00 |
| 7 | ⁵ D ₀ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -21079 | 1.0E-42 | 0.0E+00 | 0.0E+00 | 1.0E-42 |
| 8 | ⁵ D ₁ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -19345 | 8.0E-40 | 4.8E-44 | 7.9E-40 | 7.3E-42 |
| 9 | ⁵ D ₂ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -16889 | 4.8E-33 | 0.0E+00 | 0.0E+00 | 4.8E-33 |
| 10 | ⁵ D ₃ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -14017 | 1.8E-26 | 2.8E-29 | 1.8E-26 | 0.0E+00 |
| 11 | ⁵ L ₆ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -13047 | 7.7E-26 | 7.2E-26 | 5.0E-27 | 0.0E+00 |
| 12 | ⁵ L ₇ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -12015 | 5.9E-23 | 5.5E-23 | 3.8E-24 | 0.0E+00 |
| 13 | ⁵ G ₂ → ⁷ F ₁ | S ₀ →S ₁ | 28.0 | -11980 | 1.2E-19 | 0.0E+00 | 0.0E+00 | 1.2E-19 |
| 14 | ⁵ G ₃ → ⁷ F ₁ | S ₀ →S ₁ | 1.5 | -11750 | 6.4E-21 | 2.0E-23 | 6.4E-21 | 0.0E+00 |
| 15 | ⁵ G ₆ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -11620 | 1.9E-22 | 1.7E-22 | 1.2E-23 | 0.0E+00 |
| 16 | ⁵ G ₅ → ⁷ F ₁ | S ₀ →S ₁ | 0.1 | -11609 | 5.5E-22 | 4.4E-22 | 1.1E-22 | 0.0E+00 |
| | | | | W_b^S | 4×10^{-19} | | | |
| | | | | | | | | |
| 17 | ⁵ D ₀ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | -5296 | 3.5E-09 | 2.1E-13 | 3.5E-09 | 0.0E+00 |
| 18 | ⁵ D ₁ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | -3562 | 1.7E+01 | 0.0E+00 | 0.0E+00 | 1.7E+01 |
| 19 | ⁵ D ₂ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | -1106 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 20 | ⁵ L ₆ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | 2736 | 9.6E+00 | 9.0E+00 | 6.1E-01 | 0.0E+00 |
| 21 | ⁵ G ₆ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | 4163 | 1.8E+00 | 1.7E+00 | 1.1E-01 | 0.0E+00 |
| 22 | ⁵ D ₄ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | 4997 | 2.8E+00 | 3.0E-01 | 2.5E+00 | 0.0E+00 |
| 23 | ⁵ D ₀ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | -5668 | 4.9E-03 | 0.0E+00 | 0.0E+00 | 4.9E-03 |
| 24 | ⁵ D ₁ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | -3934 | 2.7E-03 | 1.8E-09 | 2.9E-05 | 2.7E-03 |
| 25 | ⁵ D ₂ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | -1478 | 5.3E+04 | 0.0E+00 | 0.0E+00 | 5.3E+04 |
| 26 | ⁵ D ₃ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 1394 | 5.2E+02 | 8.3E-01 | 5.2E+02 | 0.0E+00 |
| 27 | ⁵ L ₆ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 2364 | 6.0E+00 | 5.7E+00 | 3.8E-01 | 0.0E+00 |
| 28 | ⁵ L ₇ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 3396 | 8.8E+00 | 8.3E+00 | 5.6E-01 | 0.0E+00 |
| 29 | ⁵ G ₂ → ⁷ F ₁ | S ₀ →T ₁ | 100.0 | 3431 | 1.4E+08 | 0.0E+00 | 0.0E+00 | 1.4E+08 |
| 30 | ⁵ G ₃ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 3661 | 1.9E+02 | 5.9E-01 | 1.9E+02 | 0.0E+00 |
| 31 | ⁵ G ₆ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 3791 | 2.6E+00 | 2.4E+00 | 1.6E-01 | 0.0E+00 |
| 32 | ⁵ G ₅ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 3802 | 7.1E+00 | 5.7E+00 | 1.4E+00 | 0.0E+00 |
| | | | | W_b^T | 1.4×10^8 | | | |

Table S9. Forward (ligand-to-Eu) IET rates for **NEt₄[EuL₄]**.

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm⁻¹) | W (s⁻¹) | W_{d-d} (s⁻¹) | W_{d-m} (s⁻¹) | W_{ex} (s⁻¹) |
|-----------|--------------------------------|---|-----------------------|--|--|--|--|---|
| 1 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₀ | 0.0 | 20707 | 6.6E-02 | 5.2E-06 | 6.6E-02 | 0.0E+00 |
| 2 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₁ | 0.2 | 18973 | 1.8E+02 | 0.0E+00 | 0.0E+00 | 1.8E+02 |
| 3 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₂ | 0.0 | 16517 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 4 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ L ₆ | 2.5 | 12675 | 1.9E+03 | 1.9E+03 | 2.0E+01 | 0.0E+00 |
| 5 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ G ₆ | 2.7 | 11248 | 2.1E+03 | 2.0E+03 | 2.1E+01 | 0.0E+00 |
| 6 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₄ | 3.2 | 10414 | 2.4E+03 | 6.5E+02 | 1.8E+03 | 0.0E+00 |
| 7 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₀ | 0.0 | 21079 | 1.3E+00 | 0.0E+00 | 0.0E+00 | 1.3E+00 |
| 8 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₁ | 0.0 | 19345 | 1.2E+00 | 9.2E-05 | 1.2E+00 | 6.6E-03 |
| 9 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₂ | 0.1 | 16889 | 5.1E+01 | 0.0E+00 | 0.0E+00 | 5.1E+01 |
| 10 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₃ | 0.5 | 14017 | 4.2E+02 | 1.1E+00 | 4.1E+02 | 0.0E+00 |
| 11 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ L ₆ | 0.1 | 13047 | 5.1E+01 | 5.0E+01 | 5.3E-01 | 0.0E+00 |
| 12 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ L ₇ | 0.4 | 12015 | 3.1E+02 | 3.1E+02 | 3.2E+00 | 0.0E+00 |
| 13 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₂ | 86.3 | 11980 | 6.6E+04 | 0.0E+00 | 0.0E+00 | 6.6E+04 |
| 14 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₃ | 3.4 | 11750 | 2.6E+03 | 1.3E+01 | 2.6E+03 | 0.0E+00 |
| 15 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₆ | 0.2 | 11620 | 1.3E+02 | 1.2E+02 | 1.3E+00 | 0.0E+00 |
| 16 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₅ | 0.4 | 11609 | 2.7E+02 | 2.5E+02 | 1.6E+01 | 0.0E+00 |
| | | | | <i>W^S</i> | 7.6×10 ⁴ | | | |
| 17 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₀ | 0.0 | 4918 | 9.4E+01 | 7.6E-03 | 9.4E+01 | 0.0E+00 |
| 18 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₁ | 84.9 | 3184 | 1.9E+08 | 0.0E+00 | 0.0E+00 | 1.9E+08 |
| 19 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₂ | 0.0 | 728 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 20 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ L ₆ | 0.0 | -3114 | 1.2E-05 | 1.2E-05 | 1.1E-07 | 0.0E+00 |
| 21 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ G ₆ | 0.0 | -4541 | 2.1E-09 | 2.1E-09 | 2.0E-11 | 0.0E+00 |
| 22 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₄ | 0.0 | -5375 | 1.5E-11 | 4.2E-12 | 1.1E-11 | 0.0E+00 |
| 23 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₀ | 13.8 | 5290 | 3.2E+07 | 0.0E+00 | 0.0E+00 | 3.2E+07 |
| 24 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₁ | 0.0 | 3556 | 1.2E+04 | 1.8E-02 | 2.2E+02 | 1.2E+04 |
| 25 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₂ | 1.2 | 1100 | 2.9E+06 | 0.0E+00 | 0.0E+00 | 2.9E+06 |
| 26 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₃ | 0.0 | -1772 | 9.4E-03 | 2.5E-05 | 9.3E-03 | 0.0E+00 |
| 27 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ L ₆ | 0.0 | -2742 | 3.0E-06 | 3.0E-06 | 2.8E-08 | 0.0E+00 |
| 28 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ L ₇ | 0.0 | -3774 | 3.4E-08 | 3.3E-08 | 3.1E-10 | 0.0E+00 |
| 29 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₂ | 0.0 | -3809 | 5.5E-02 | 0.0E+00 | 0.0E+00 | 5.5E-02 |
| 30 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₃ | 0.0 | -4039 | 5.6E-08 | 2.9E-10 | 5.5E-08 | 0.0E+00 |
| 31 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₆ | 0.0 | -4169 | 1.2E-09 | 1.2E-09 | 1.1E-11 | 0.0E+00 |
| 32 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₅ | 0.0 | -4180 | 2.5E-09 | 2.3E-09 | 1.4E-10 | 0.0E+00 |
| | | | | <i>W^T</i> | 2.3×10 ⁸ | | | |

Table S10. Backward (Eu-to-ligand) IET rates for $\text{NEt}_4[\text{EuL}_4]$.

| <i>p</i> | donor | acceptor | contr. (%) | $\Delta (\text{cm}^{-1})$ | $W_b (\text{s}^{-1})$ | $W_{d-d} (\text{s}^{-1})$ | $W_{d-m} (\text{s}^{-1})$ | $W_{ex} (\text{s}^{-1})$ |
|-----------|---|-------------------------------------|-----------------------|---------------------------|-----------------------|---------------------------|---------------------------|--------------------------|
| 1 | $^5\text{D}_0 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -20707 | 3.2E-45 | 2.5E-49 | 3.2E-45 | 0.0E+00 |
| 2 | $^5\text{D}_1 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -18973 | 1.2E-38 | 0.0E+00 | 0.0E+00 | 1.2E-38 |
| 3 | $^5\text{D}_2 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -16517 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 4 | $^5\text{L}_6 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -12675 | 4.9E-25 | 4.9E-25 | 5.1E-27 | 0.0E+00 |
| 5 | $^5\text{G}_6 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.7 | -11248 | 5.1E-22 | 5.1E-22 | 5.3E-24 | 0.0E+00 |
| 6 | $^5\text{D}_4 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{S}_1$ | 69.6 | -10414 | 4.8E-20 | 1.3E-20 | 3.5E-20 | 0.0E+00 |
| 7 | $^5\text{D}_0 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -21079 | 1.6E-43 | 0.0E+00 | 0.0E+00 | 1.6E-43 |
| 8 | $^5\text{D}_1 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -19345 | 2.0E-40 | 1.6E-44 | 2.0E-40 | 1.1E-42 |
| 9 | $^5\text{D}_2 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -16889 | 7.4E-34 | 0.0E+00 | 0.0E+00 | 7.4E-34 |
| 10 | $^5\text{D}_3 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -14017 | 4.5E-27 | 1.2E-29 | 4.5E-27 | 0.0E+00 |
| 11 | $^5\text{L}_6 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -13047 | 3.2E-26 | 3.2E-26 | 3.3E-28 | 0.0E+00 |
| 12 | $^5\text{L}_7 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -12015 | 2.5E-23 | 2.4E-23 | 2.6E-25 | 0.0E+00 |
| 13 | $^5\text{G}_2 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 26.9 | -11980 | 1.9E-20 | 0.0E+00 | 0.0E+00 | 1.9E-20 |
| 14 | $^5\text{G}_3 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 2.3 | -11750 | 1.6E-21 | 8.1E-24 | 1.6E-21 | 0.0E+00 |
| 15 | $^5\text{G}_6 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.1 | -11620 | 7.8E-23 | 7.7E-23 | 8.1E-25 | 0.0E+00 |
| 16 | $^5\text{G}_5 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.3 | -11609 | 2.1E-22 | 2.0E-22 | 1.3E-23 | 0.0E+00 |
| | | | | W_b^S | 7×10^{-20} | | | |
| 17 | $^5\text{D}_0 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | -4918 | 5.5E-09 | 4.5E-13 | 5.5E-09 | 0.0E+00 |
| 18 | $^5\text{D}_1 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | -3184 | 1.6E+01 | 0.0E+00 | 0.0E+00 | 1.6E+01 |
| 19 | $^5\text{D}_2 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | -728 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 20 | $^5\text{L}_6 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | 3114 | 3.7E+00 | 3.7E+00 | 3.4E-02 | 0.0E+00 |
| 21 | $^5\text{G}_6 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | 4541 | 6.4E-01 | 6.3E-01 | 5.9E-03 | 0.0E+00 |
| 22 | $^5\text{D}_4 \rightarrow ^7\text{F}_0$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | 5375 | 3.6E-01 | 1.0E-01 | 2.6E-01 | 0.0E+00 |
| 23 | $^5\text{D}_0 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | -5290 | 4.7E-03 | 0.0E+00 | 0.0E+00 | 4.7E-03 |
| 24 | $^5\text{D}_1 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | -3556 | 2.6E-03 | 3.8E-09 | 4.7E-05 | 2.6E-03 |
| 25 | $^5\text{D}_2 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.3 | -1100 | 5.1E+04 | 0.0E+00 | 0.0E+00 | 5.1E+04 |
| 26 | $^5\text{D}_3 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | 1772 | 1.2E+02 | 3.3E-01 | 1.2E+02 | 0.0E+00 |
| 27 | $^5\text{L}_6 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | 2742 | 2.4E+00 | 2.3E+00 | 2.2E-02 | 0.0E+00 |
| 28 | $^5\text{L}_7 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | 3774 | 3.3E+00 | 3.3E+00 | 3.1E-02 | 0.0E+00 |
| 29 | $^5\text{G}_2 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 99.7 | 3809 | 1.9E+07 | 0.0E+00 | 0.0E+00 | 1.9E+07 |
| 30 | $^5\text{G}_3 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | 4039 | 4.2E+01 | 2.1E-01 | 4.2E+01 | 0.0E+00 |
| 31 | $^5\text{G}_6 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | 4169 | 9.3E-01 | 9.2E-01 | 8.7E-03 | 0.0E+00 |
| 32 | $^5\text{G}_5 \rightarrow ^7\text{F}_1$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | 4180 | 2.3E+00 | 2.2E+00 | 1.3E-01 | 0.0E+00 |
| | | | | W_b^T | 1.9×10^7 | | | |

Table S11. Forward (ligand-to-Eu) IET rates for **PPh₄[EuL₄]**.

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm⁻¹) | W (s⁻¹) | W_{d-d} (s⁻¹) | W_{d-m} (s⁻¹) | W_{ex} (s⁻¹) |
|-----------|--------------------------------|---|-----------------------|--|--|--|--|---|
| 1 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₀ | 0.0 | 17207 | 6.4E-01 | 4.5E-05 | 6.4E-01 | 0.0E+00 |
| 2 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₁ | 1.5 | 15473 | 2.7E+02 | 0.0E+00 | 0.0E+00 | 2.7E+02 |
| 3 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₂ | 0.0 | 13017 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 4 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ L ₆ | 9.3 | 9175 | 1.7E+03 | 1.7E+03 | 5.2E-01 | 0.0E+00 |
| 5 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ G ₆ | 6.4 | 7748 | 1.2E+03 | 1.2E+03 | 3.5E-01 | 0.0E+00 |
| 6 | S ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₄ | 2.3 | 6914 | 4.3E+02 | 3.0E+02 | 1.3E+02 | 0.0E+00 |
| 7 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₀ | 0.0 | 17579 | 3.8E+00 | 0.0E+00 | 0.0E+00 | 3.8E+00 |
| 8 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₁ | 0.0 | 15845 | 7.4E+00 | 5.2E-04 | 7.4E+00 | 1.1E-02 |
| 9 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₂ | 0.2 | 13389 | 4.1E+01 | 0.0E+00 | 0.0E+00 | 4.1E+01 |
| 10 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₃ | 2.8 | 10517 | 5.2E+02 | 1.4E+00 | 5.2E+02 | 0.0E+00 |
| 11 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ L ₆ | 0.3 | 9547 | 5.0E+01 | 5.0E+01 | 1.5E-02 | 0.0E+00 |
| 12 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ L ₇ | 1.2 | 8515 | 2.2E+02 | 2.2E+02 | 6.7E-02 | 0.0E+00 |
| 13 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₂ | 65.5 | 8480 | 1.2E+04 | 0.0E+00 | 0.0E+00 | 1.2E+04 |
| 14 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₃ | 9.0 | 8250 | 1.7E+03 | 9.0E+00 | 1.7E+03 | 0.0E+00 |
| 15 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₆ | 0.4 | 8120 | 8.0E+01 | 8.0E+01 | 2.4E-02 | 0.0E+00 |
| 16 | S ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₅ | 0.9 | 8109 | 1.7E+02 | 1.6E+02 | 1.5E+00 | 0.0E+00 |
| | | | | <i>W^S</i> | 1.8×10 ⁴ | | | |
| | | | | <i>W^T</i> | 1.8×10 ⁶ | | | |
| 17 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₀ | 0.0 | 5497 | 2.6E+00 | 1.9E-04 | 2.6E+00 | 0.0E+00 |
| 18 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₁ | 84.9 | 3763 | 1.5E+06 | 0.0E+00 | 0.0E+00 | 1.5E+06 |
| 19 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₂ | 0.0 | 1307 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 20 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ L ₆ | 0.0 | -2535 | 7.0E-06 | 7.0E-06 | 2.0E-09 | 0.0E+00 |
| 21 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ G ₆ | 0.0 | -3962 | 1.3E-09 | 1.3E-09 | 3.8E-13 | 0.0E+00 |
| 22 | T ₁ →S ₀ | ⁷ F ₀ → ⁵ D ₄ | 0.0 | -4796 | 4.1E-12 | 2.9E-12 | 1.2E-12 | 0.0E+00 |
| 23 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₀ | 13.8 | 5869 | 2.4E+05 | 0.0E+00 | 0.0E+00 | 2.4E+05 |
| 24 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₁ | 0.0 | 4135 | 1.0E+02 | 4.5E-04 | 6.3E+00 | 9.4E+01 |
| 25 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₂ | 1.3 | 1679 | 2.3E+04 | 0.0E+00 | 0.0E+00 | 2.3E+04 |
| 26 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ D ₃ | 0.0 | -1193 | 4.9E-03 | 1.4E-05 | 4.9E-03 | 0.0E+00 |
| 27 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ L ₆ | 0.0 | -2163 | 1.7E-06 | 1.7E-06 | 5.0E-10 | 0.0E+00 |
| 28 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ L ₇ | 0.0 | -3195 | 2.0E-08 | 2.0E-08 | 5.9E-12 | 0.0E+00 |
| 29 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₂ | 0.0 | -3230 | 8.8E-03 | 0.0E+00 | 0.0E+00 | 8.8E-03 |
| 30 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₃ | 0.0 | -3460 | 3.3E-08 | 1.8E-10 | 3.3E-08 | 0.0E+00 |
| 31 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₆ | 0.0 | -3590 | 7.6E-10 | 7.6E-10 | 2.2E-13 | 0.0E+00 |
| 32 | T ₁ →S ₀ | ⁷ F ₁ → ⁵ G ₅ | 0.0 | -3601 | 1.5E-09 | 1.5E-09 | 1.3E-11 | 0.0E+00 |

Table S12. Backward (Eu-to-ligand) IET rates for **PPh₄[EuL₄]**.

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm ⁻¹) | W_b (s ⁻¹) | W_{d-d} (s ⁻¹) | W_{d-m} (s ⁻¹) | W_{ex} (s ⁻¹) |
|-----------|---|--------------------------------|-----------------------|------------------------------|--------------------------|------------------------------|------------------------------|-----------------------------|
| 1 | ⁵ D ₀ → ⁷ F ₀ | S ₀ →S ₁ | 0.0 | -17207 | 6.6E-37 | 4.7E-41 | 6.6E-37 | 0.0E+00 |
| 2 | ⁵ D ₁ → ⁷ F ₀ | S ₀ →S ₁ | 0.0 | -15473 | 4.1E-31 | 0.0E+00 | 0.0E+00 | 4.1E-31 |
| 3 | ⁵ D ₂ → ⁷ F ₀ | S ₀ →S ₁ | 0.0 | -13017 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 4 | ⁵ L ₆ → ⁷ F ₀ | S ₀ →S ₁ | 0.0 | -9175 | 9.4E-18 | 9.4E-18 | 2.8E-21 | 0.0E+00 |
| 5 | ⁵ G ₆ → ⁷ F ₀ | S ₀ →S ₁ | 2.2 | -7748 | 6.3E-15 | 6.3E-15 | 1.9E-18 | 0.0E+00 |
| 6 | ⁵ D ₄ → ⁷ F ₀ | S ₀ →S ₁ | 63.3 | -6914 | 1.8E-13 | 1.3E-13 | 5.6E-14 | 0.0E+00 |
| 7 | ⁵ D ₀ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -17579 | 9.9E-36 | 0.0E+00 | 0.0E+00 | 9.9E-36 |
| 8 | ⁵ D ₁ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -15845 | 2.8E-32 | 2.0E-36 | 2.8E-32 | 4.2E-35 |
| 9 | ⁵ D ₂ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -13389 | 1.3E-26 | 0.0E+00 | 0.0E+00 | 1.3E-26 |
| 10 | ⁵ D ₃ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -10517 | 1.2E-19 | 3.4E-22 | 1.2E-19 | 0.0E+00 |
| 11 | ⁵ L ₆ → ⁷ F ₁ | S ₀ →S ₁ | 0.0 | -9547 | 6.8E-19 | 6.8E-19 | 2.1E-22 | 0.0E+00 |
| 12 | ⁵ L ₇ → ⁷ F ₁ | S ₀ →S ₁ | 0.1 | -8515 | 3.8E-16 | 3.8E-16 | 1.2E-19 | 0.0E+00 |
| 13 | ⁵ G ₂ → ⁷ F ₁ | S ₀ →S ₁ | 25.4 | -8480 | 7.4E-14 | 0.0E+00 | 0.0E+00 | 7.4E-14 |
| 14 | ⁵ G ₃ → ⁷ F ₁ | S ₀ →S ₁ | 7.6 | -8250 | 2.2E-14 | 1.2E-16 | 2.2E-14 | 0.0E+00 |
| 15 | ⁵ G ₆ → ⁷ F ₁ | S ₀ →S ₁ | 0.4 | -8120 | 1.1E-15 | 1.1E-15 | 3.2E-19 | 0.0E+00 |
| 16 | ⁵ G ₅ → ⁷ F ₁ | S ₀ →S ₁ | 0.9 | -8109 | 2.7E-15 | 2.7E-15 | 2.5E-17 | 0.0E+00 |
| | | | | W_b^S | 3×10^{-13} | | | |
| 17 | ⁵ D ₀ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | -5497 | 9.6E-12 | 6.8E-16 | 9.6E-12 | 0.0E+00 |
| 18 | ⁵ D ₁ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | -3763 | 7.8E-03 | 0.0E+00 | 0.0E+00 | 7.8E-03 |
| 19 | ⁵ D ₂ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | -1307 | 0.0E+00 | 0.0E+00 | 0.0E+00 | 0.0E+00 |
| 20 | ⁵ L ₆ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | 2535 | 1.3E-01 | 1.3E-01 | 3.8E-05 | 0.0E+00 |
| 21 | ⁵ G ₆ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | 3962 | 2.5E-02 | 2.5E-02 | 7.1E-06 | 0.0E+00 |
| 22 | ⁵ D ₄ → ⁷ F ₀ | S ₀ →T ₁ | 0.0 | 4796 | 6.1E-03 | 4.3E-03 | 1.8E-03 | 0.0E+00 |
| 23 | ⁵ D ₀ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | -5869 | 2.2E-06 | 0.0E+00 | 0.0E+00 | 2.2E-06 |
| 24 | ⁵ D ₁ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | -4135 | 1.3E-06 | 5.8E-12 | 8.2E-08 | 1.2E-06 |
| 25 | ⁵ D ₂ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | -1679 | 2.5E+01 | 0.0E+00 | 0.0E+00 | 2.5E+01 |
| 26 | ⁵ D ₃ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 1193 | 4.0E+00 | 1.1E-02 | 4.0E+00 | 0.0E+00 |
| 27 | ⁵ L ₆ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 2163 | 8.2E-02 | 8.2E-02 | 2.4E-05 | 0.0E+00 |
| 28 | ⁵ L ₇ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 3195 | 1.2E-01 | 1.2E-01 | 3.5E-05 | 0.0E+00 |
| 29 | ⁵ G ₂ → ⁷ F ₁ | S ₀ →T ₁ | 100.0 | 3230 | 1.9E+05 | 0.0E+00 | 0.0E+00 | 1.9E+05 |
| 30 | ⁵ G ₃ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 3460 | 1.5E+00 | 8.3E-03 | 1.5E+00 | 0.0E+00 |
| 31 | ⁵ G ₆ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 3590 | 3.5E-02 | 3.5E-02 | 1.0E-05 | 0.0E+00 |
| 32 | ⁵ G ₅ → ⁷ F ₁ | S ₀ →T ₁ | 0.0 | 3601 | 8.5E-02 | 8.4E-02 | 7.4E-04 | 0.0E+00 |
| | | | | W_b^T | 1.7×10^5 | | | |

Table S13. Forward (ligand-to-Tb) IET rates for **NMe₄[TbL₄]**.

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm ⁻¹) | W (s ⁻¹) | W_{d-d} (s ⁻¹) | W_{d-m} (s ⁻¹) | W_{ex} (s ⁻¹) |
|-----------|--------------------------------|--|---------------|------------------------------|------------------------|------------------------------|------------------------------|-----------------------------|
| 1 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₄ | 0.0 | 17556 | 3.9E+01 | 4.7E-02 | 3.9E+01 | 0.0E+00 |
| 2 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₃ | 0.0 | 11764 | 1.1E+02 | 6.2E+01 | 4.5E+01 | 0.0E+00 |
| 3 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₆ | 0.2 | 11577 | 4.5E+07 | 5.9E+03 | 1.3E+05 | 4.5E+07 |
| 4 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₁₀ | 0.0 | 11029 | 5.4E+03 | 5.0E+03 | 4.6E+02 | 0.0E+00 |
| 5 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₅ | 0.1 | 10233 | 1.1E+07 | 2.5E+03 | 3.5E+05 | 1.1E+07 |
| 6 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₄ | 0.0 | 9713 | 4.8E+04 | 2.5E+03 | 4.6E+04 | 0.0E+00 |
| 7 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₉ | 0.0 | 9592 | 1.8E+04 | 1.4E+04 | 3.8E+03 | 0.0E+00 |
| 8 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₃ | 0.0 | 9023 | 1.3E+03 | 7.3E+02 | 5.3E+02 | 0.0E+00 |
| 9 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₈ | 0.0 | 8810 | 1.4E+04 | 1.3E+04 | 1.2E+03 | 0.0E+00 |
| 10 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₇ | 0.0 | 8543 | 7.0E+05 | 8.5E+03 | 6.9E+05 | 4.4E+02 |
| 11 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₆ | 0.1 | 8330 | 1.2E+07 | 0.0E+00 | 0.0E+00 | 1.2E+07 |
| 12 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₇ | 0.2 | 6621 | 4.0E+07 | 0.0E+00 | 0.0E+00 | 4.0E+07 |
| 13 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₆ | 3.7 | 5109 | 6.9E+08 | 0.0E+00 | 0.0E+00 | 6.9E+08 |
| 14 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₅ | 0.0 | 4233 | 1.1E+01 | 0.0E+00 | 0.0E+00 | 1.1E+01 |
| 15 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ F ₅ | 15.8 | 3066 | 2.9E+09 | 0.0E+00 | 0.0E+00 | 2.9E+09 |
| 16 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₇ | 1.0 | 1411 | 1.8E+08 | 0.0E+00 | 0.0E+00 | 1.8E+08 |
| 17 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₆ | 15.1 | 402 | 2.8E+09 | 0.0E+00 | 0.0E+00 | 2.8E+09 |
| 18 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₅ | 1.3 | 14 | 2.4E+08 | 0.0E+00 | 0.0E+00 | 2.4E+08 |
| 19 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₅ | 0.0 | -3334 | 7.8E-01 | 0.0E+00 | 0.0E+00 | 7.8E-01 |
| 20 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₇ | 0.0 | -3693 | 1.5E-08 | 0.0E+00 | 0.0E+00 | 1.5E-08 |
| 21 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₄ | 0.0 | 19604 | 1.2E+02 | 4.6E-03 | 2.7E+01 | 9.5E+01 |
| 22 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₃ | 0.0 | 13812 | 4.2E+03 | 1.6E+01 | 4.2E+03 | 0.0E+00 |
| 23 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₆ | 0.0 | 13625 | 7.8E+05 | 7.0E+01 | 4.1E+04 | 7.4E+05 |
| 24 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₁₀ | 0.0 | 13077 | 1.9E+01 | 1.8E+01 | 1.2E+00 | 0.0E+00 |
| 25 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₅ | 0.1 | 12281 | 1.1E+07 | 1.9E+02 | 4.7E+03 | 1.1E+07 |
| 26 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₂ | 0.0 | 11941 | 6.3E+02 | 8.4E+01 | 5.5E+02 | 0.0E+00 |
| 27 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₄ | 0.0 | 11761 | 2.5E+06 | 1.0E+02 | 4.0E+04 | 2.4E+06 |
| 28 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₉ | 0.0 | 11640 | 1.0E+03 | 7.7E+02 | 2.4E+02 | 0.0E+00 |
| 29 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₈ | 0.0 | 10858 | 3.9E+03 | 2.6E+03 | 1.3E+03 | 0.0E+00 |
| 30 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₇ | 0.0 | 10591 | 5.1E+04 | 1.0E+03 | 5.0E+04 | 0.0E+00 |
| 31 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 0.0 | 10378 | 3.6E+05 | 0.0E+00 | 0.0E+00 | 3.6E+05 |
| 32 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₆ | 0.2 | 7157 | 3.6E+07 | 0.0E+00 | 0.0E+00 | 3.6E+07 |
| 33 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₅ | 4.0 | 6281 | 7.4E+08 | 0.0E+00 | 0.0E+00 | 7.4E+08 |
| 34 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₄ | 12.3 | 5709 | 2.3E+09 | 0.0E+00 | 0.0E+00 | 2.3E+09 |
| 35 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₅ | 9.4 | 5114 | 1.7E+09 | 0.0E+00 | 0.0E+00 | 1.7E+09 |
| 36 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₄ | 34.3 | 4674 | 6.4E+09 | 0.0E+00 | 0.0E+00 | 6.4E+09 |
| 37 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 2.1 | 2450 | 3.9E+08 | 0.0E+00 | 0.0E+00 | 3.9E+08 |
| 38 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₄ | 0.0 | 2440 | 3.9E+05 | 0.0E+00 | 0.0E+00 | 3.9E+05 |
| 39 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₅ | 0.2 | 2062 | 2.9E+07 | 0.0E+00 | 0.0E+00 | 2.9E+07 |
| 40 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ K ₅ | 0.0 | -1286 | 1.8E+04 | 0.0E+00 | 0.0E+00 | 1.8E+04 |
| | | | | W^S | 1.8×10^{10} | | | |
| 41 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₄ | 0.0 | 2145 | 5.6E+02 | 6.9E-01 | 5.6E+02 | 0.0E+00 |

| | | | | | | | | |
|-----------|-----------------------|------------------------------|-------|--------|-------------------|---------|---------|---------|
| 42 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5D_3$ | 0.0 | -3647 | 1.8E-08 | 1.0E-08 | 7.3E-09 | 0.0E+00 |
| 43 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5G_6$ | 0.0 | -3834 | 2.4E+01 | 3.2E-07 | 7.0E-06 | 2.4E+01 |
| 44 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5L_{10}$ | 0.0 | -4382 | 1.1E-08 | 9.7E-09 | 8.7E-10 | 0.0E+00 |
| 45 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5G_5$ | 0.0 | -5178 | 1.8E-03 | 4.1E-11 | 5.7E-09 | 1.8E-03 |
| 46 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5G_4$ | 0.0 | -5698 | 3.5E-11 | 1.8E-12 | 3.3E-11 | 0.0E+00 |
| 47 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5L_9$ | 0.0 | -5819 | 6.4E-12 | 5.1E-12 | 1.3E-12 | 0.0E+00 |
| 48 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5G_3$ | 0.0 | -6388 | 1.5E-14 | 8.7E-15 | 6.2E-15 | 0.0E+00 |
| 49 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5L_8$ | 0.0 | -6601 | 4.7E-14 | 4.4E-14 | 3.8E-15 | 0.0E+00 |
| 50 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5L_7$ | 0.0 | -6868 | 3.4E-12 | 5.8E-15 | 4.7E-13 | 3.0E-12 |
| 51 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5L_6$ | 0.0 | -7081 | 2.2E-08 | 0.0E+00 | 0.0E+00 | 2.2E-08 |
| 52 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5H_7$ | 0.0 | -8790 | 3.1E-12 | 0.0E+00 | 0.0E+00 | 3.1E-12 |
| 53 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5H_6$ | 0.0 | -10302 | 7.7E-15 | 0.0E+00 | 0.0E+00 | 7.7E-15 |
| 54 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5H_5$ | 0.0 | -11178 | 7.4E-25 | 0.0E+00 | 0.0E+00 | 7.4E-25 |
| 55 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5F_5$ | 0.0 | -12345 | 2.3E-19 | 0.0E+00 | 0.0E+00 | 2.3E-19 |
| 56 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5I_7$ | 0.0 | -14000 | 1.0E-24 | 0.0E+00 | 0.0E+00 | 1.0E-24 |
| 57 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5I_6$ | 0.0 | -15009 | 5.2E-26 | 0.0E+00 | 0.0E+00 | 5.2E-26 |
| 58 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5I_5$ | 0.0 | -15397 | 4.9E-28 | 0.0E+00 | 0.0E+00 | 4.9E-28 |
| 59 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5K_5$ | 0.0 | -18745 | 1.0E-37 | 0.0E+00 | 0.0E+00 | 1.0E-37 |
| 60 | $T_1 \rightarrow S_0$ | $^7F_6 \rightarrow ^5K_7$ | 0.0 | -19104 | 1.5E-45 | 0.0E+00 | 0.0E+00 | 1.5E-45 |
| 61 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5D_4$ | 100.0 | 4193 | 2.6E+08 | 1.3E+00 | 7.3E+03 | 2.6E+08 |
| 62 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5D_3$ | 0.0 | -1599 | 1.8E-01 | 6.7E-04 | 1.8E-01 | 0.0E+00 |
| 63 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5G_6$ | 0.0 | -1786 | 9.8E+04 | 9.4E-04 | 5.5E-01 | 9.8E+04 |
| 64 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5L_{10}$ | 0.0 | -2334 | 9.0E-06 | 8.5E-06 | 5.5E-07 | 0.0E+00 |
| 65 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5G_5$ | 0.0 | -3130 | 4.2E+02 | 7.1E-07 | 1.8E-05 | 4.2E+02 |
| 66 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5D_2$ | 0.0 | -3470 | 3.0E-07 | 4.1E-08 | 2.6E-07 | 0.0E+00 |
| 67 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5G_4$ | 0.0 | -3650 | 3.9E+00 | 1.7E-08 | 6.4E-06 | 3.9E+00 |
| 68 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5L_9$ | 0.0 | -3771 | 7.9E-08 | 6.0E-08 | 1.9E-08 | 0.0E+00 |
| 69 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5L_8$ | 0.0 | -4553 | 2.7E-09 | 1.8E-09 | 8.9E-10 | 0.0E+00 |
| 70 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5L_7$ | 0.0 | -4820 | 7.1E-09 | 1.4E-10 | 7.0E-09 | 0.0E+00 |
| 71 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5I_6$ | 0.0 | -5033 | 1.4E-04 | 0.0E+00 | 0.0E+00 | 1.4E-04 |
| 72 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5H_6$ | 0.0 | -8254 | 6.5E-11 | 0.0E+00 | 0.0E+00 | 6.5E-11 |
| 73 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5H_5$ | 0.0 | -9130 | 7.8E-12 | 0.0E+00 | 0.0E+00 | 7.8E-12 |
| 74 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5H_4$ | 0.0 | -9702 | 8.4E-13 | 0.0E+00 | 0.0E+00 | 8.4E-13 |
| 75 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5F_5$ | 0.0 | -10297 | 2.0E-14 | 0.0E+00 | 0.0E+00 | 2.0E-14 |
| 76 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5F_4$ | 0.0 | -10737 | 5.6E-15 | 0.0E+00 | 0.0E+00 | 5.6E-15 |
| 77 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5I_6$ | 0.0 | -12961 | 8.7E-22 | 0.0E+00 | 0.0E+00 | 8.7E-22 |
| 78 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5I_4$ | 0.0 | -12971 | 8.3E-25 | 0.0E+00 | 0.0E+00 | 8.3E-25 |
| 79 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5I_5$ | 0.0 | -13349 | 7.0E-24 | 0.0E+00 | 0.0E+00 | 7.0E-24 |
| 80 | $T_1 \rightarrow S_0$ | $^7F_5 \rightarrow ^5K_5$ | 0.0 | -16697 | 1.2E-32 | 0.0E+00 | 0.0E+00 | 1.2E-32 |
| | | | | W^T | 2.6×10^8 | | | |

Table S14. Backward (Tb-to-ligand) IET rates for **NMe₄[TbL₄]**

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm ⁻¹) | W_b (s ⁻¹) | W_{d-d} (s ⁻¹) | W_{d-m} (s ⁻¹) | W_{ex} (s ⁻¹) |
|-----------|--|--------------------------------|-----------------------|------------------------------|--------------------------|------------------------------|------------------------------|-----------------------------|
| 1 | ⁵ D ₄ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -17556 | 9.0E-36 | 1.1E-38 | 9.0E-36 | 0.0E+00 |
| 2 | ⁵ D ₃ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -11764 | 4.4E-23 | 2.6E-23 | 1.8E-23 | 0.0E+00 |
| 3 | ⁵ G ₆ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -11577 | 2.4E-17 | 3.2E-21 | 7.2E-20 | 2.4E-17 |
| 4 | ⁵ L ₁₀ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -11029 | 2.6E-20 | 2.4E-20 | 2.2E-21 | 0.0E+00 |
| 5 | ⁵ G ₅ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -10233 | 4.8E-15 | 1.1E-18 | 1.5E-16 | 4.6E-15 |
| 6 | ⁵ G ₄ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -9713 | 3.1E-16 | 1.6E-17 | 2.9E-16 | 0.0E+00 |
| 7 | ⁵ L ₉ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -9592 | 9.8E-17 | 7.7E-17 | 2.1E-17 | 0.0E+00 |
| 8 | ⁵ G ₃ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -9023 | 2.9E-16 | 1.7E-16 | 1.2E-16 | 0.0E+00 |
| 9 | ⁵ L ₈ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -8810 | 3.8E-15 | 3.4E-15 | 3.0E-16 | 0.0E+00 |
| 10 | ⁵ L ₇ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -8543 | 7.5E-13 | 9.3E-15 | 7.4E-13 | 4.8E-16 |
| 11 | ⁵ L ₆ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -8330 | 4.1E-11 | 0.0E+00 | 0.0E+00 | 4.1E-11 |
| 12 | ⁵ H ₇ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -6621 | 4.6E-07 | 0.0E+00 | 0.0E+00 | 4.6E-07 |
| 13 | ⁵ H ₆ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -5109 | 1.4E-02 | 0.0E+00 | 0.0E+00 | 1.4E-02 |
| 14 | ⁵ H ₅ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -4233 | 1.7E-08 | 0.0E+00 | 0.0E+00 | 1.7E-08 |
| 15 | ⁵ F ₅ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -3066 | 1.3E+03 | 0.0E+00 | 0.0E+00 | 1.3E+03 |
| 16 | ⁵ I ₇ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -1411 | 1.7E+05 | 0.0E+00 | 0.0E+00 | 1.7E+05 |
| 17 | ⁵ I ₆ → ⁷ F ₆ | S ₀ →S ₁ | 58.9 | -402 | 4.0E+08 | 0.0E+00 | 0.0E+00 | 4.0E+08 |
| 18 | ⁵ I ₅ → ⁷ F ₆ | S ₀ →S ₁ | 38.4 | -14 | 2.6E+08 | 0.0E+00 | 0.0E+00 | 2.6E+08 |
| 19 | ⁵ K ₅ → ⁷ F ₆ | S ₀ →S ₁ | 1.3 | 3334 | 9.0E+06 | 0.0E+00 | 0.0E+00 | 9.0E+06 |
| 20 | ⁵ K ₇ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | 3693 | 7.0E-01 | 0.0E+00 | 0.0E+00 | 7.0E-01 |
| 21 | ⁵ D ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -19604 | 1.2E-39 | 4.6E-44 | 2.7E-40 | 9.5E-40 |
| 22 | ⁵ D ₃ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -13812 | 7.5E-26 | 2.8E-28 | 7.4E-26 | 0.0E+00 |
| 23 | ⁵ G ₆ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -13625 | 1.8E-23 | 1.7E-27 | 9.7E-25 | 1.7E-23 |
| 24 | ⁵ L ₁₀ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -13077 | 3.9E-27 | 3.7E-27 | 2.4E-28 | 0.0E+00 |
| 25 | ⁵ G ₅ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -12281 | 2.0E-19 | 3.4E-24 | 8.6E-23 | 2.0E-19 |
| 26 | ⁵ D ₂ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -11941 | 1.3E-22 | 1.8E-23 | 1.1E-22 | 0.0E+00 |
| 27 | ⁵ G ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -11761 | 6.8E-19 | 2.9E-23 | 1.1E-20 | 6.7E-19 |
| 28 | ⁵ L ₉ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -11640 | 2.4E-22 | 1.8E-22 | 5.7E-23 | 0.0E+00 |
| 29 | ⁵ L ₈ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -10858 | 4.4E-20 | 3.0E-20 | 1.5E-20 | 0.0E+00 |
| 30 | ⁵ L ₇ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -10591 | 2.4E-18 | 4.8E-20 | 2.3E-18 | 0.0E+00 |
| 31 | ⁵ I ₆ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -10378 | 5.5E-17 | 0.0E+00 | 0.0E+00 | 5.5E-17 |
| 32 | ⁵ H ₆ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -7157 | 3.0E-08 | 0.0E+00 | 0.0E+00 | 3.0E-08 |
| 33 | ⁵ H ₅ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -6281 | 5.1E-05 | 0.0E+00 | 0.0E+00 | 5.1E-05 |
| 34 | ⁵ H ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -5709 | 3.0E-03 | 0.0E+00 | 0.0E+00 | 3.0E-03 |
| 35 | ⁵ F ₅ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -5114 | 3.4E-02 | 0.0E+00 | 0.0E+00 | 3.4E-02 |
| 36 | ⁵ F ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -4674 | 1.2E+00 | 0.0E+00 | 0.0E+00 | 1.2E+00 |
| 37 | ⁵ I ₆ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -2450 | 2.4E+03 | 0.0E+00 | 0.0E+00 | 2.4E+03 |
| 38 | ⁵ I ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -2440 | 3.7E+00 | 0.0E+00 | 0.0E+00 | 3.7E+00 |
| 39 | ⁵ I ₅ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -2062 | 1.4E+03 | 0.0E+00 | 0.0E+00 | 1.4E+03 |
| 40 | ⁵ K ₅ → ⁷ F ₅ | S ₀ →S ₁ | 1.3 | 1286 | 9.0E+06 | 0.0E+00 | 0.0E+00 | 9.0E+06 |
| | | | | W_b^S | 6.8×10 ⁸ | | | |
| 41 | ⁵ D ₄ → ⁷ F ₆ | S ₀ →T ₁ | 0.0 | -2145 | 2.6E-02 | 3.2E-05 | 2.6E-02 | 0.0E+00 |

| | | | | | | | | |
|-----------|------------------------------|-----------------------|------|---------|-------------------|---------|---------|---------|
| 42 | $^5D_3 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 3647 | 1.4E+00 | 8.4E-01 | 6.0E-01 | 0.0E+00 |
| 43 | $^5G_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 45.6 | 3834 | 2.6E+09 | 3.4E+01 | 7.6E+02 | 2.6E+09 |
| 44 | $^5L_{10} \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 4382 | 1.0E+01 | 9.2E+00 | 8.3E-01 | 0.0E+00 |
| 45 | $^5G_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 2.7 | 5178 | 1.5E+08 | 3.5E+00 | 4.8E+02 | 1.5E+08 |
| 46 | $^5G_4 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 5698 | 4.4E+01 | 2.3E+00 | 4.2E+01 | 0.0E+00 |
| 47 | $^5L_9 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 5819 | 6.9E+00 | 5.4E+00 | 1.4E+00 | 0.0E+00 |
| 48 | $^5G_3 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6388 | 6.7E-01 | 3.9E-01 | 2.8E-01 | 0.0E+00 |
| 49 | $^5L_8 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6601 | 2.5E+00 | 2.3E+00 | 2.0E-01 | 0.0E+00 |
| 50 | $^5L_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6868 | 7.4E+02 | 1.2E+00 | 1.0E+02 | 6.4E+02 |
| 51 | $^5L_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.3 | 7081 | 1.6E+07 | 0.0E+00 | 0.0E+00 | 1.6E+07 |
| 52 | $^5H_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.1 | 8790 | 7.1E+06 | 0.0E+00 | 0.0E+00 | 7.1E+06 |
| 53 | $^5H_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.5 | 10302 | 3.0E+07 | 0.0E+00 | 0.0E+00 | 3.0E+07 |
| 54 | $^5H_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 11178 | 2.3E-01 | 0.0E+00 | 0.0E+00 | 2.3E-01 |
| 55 | $^5F_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.4 | 12345 | 2.0E+07 | 0.0E+00 | 0.0E+00 | 2.0E+07 |
| 56 | $^5I_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 14000 | 2.0E+05 | 0.0E+00 | 0.0E+00 | 2.0E+05 |
| 57 | $^5I_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 15009 | 1.5E+06 | 0.0E+00 | 0.0E+00 | 1.5E+06 |
| 58 | $^5I_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 15397 | 1.1E+05 | 0.0E+00 | 0.0E+00 | 1.1E+05 |
| 59 | $^5K_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 18745 | 2.4E+02 | 0.0E+00 | 0.0E+00 | 2.4E+02 |
| 60 | $^5K_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 19104 | 1.4E-05 | 0.0E+00 | 0.0E+00 | 1.4E-05 |
| 61 | $^5D_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | -4193 | 5.1E-01 | 2.5E-09 | 1.4E-05 | 5.1E-01 |
| 62 | $^5D_3 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 1599 | 6.2E+02 | 2.4E+00 | 6.2E+02 | 0.0E+00 |
| 63 | $^5G_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 8.2 | 1786 | 4.6E+08 | 4.4E+00 | 2.6E+03 | 4.6E+08 |
| 64 | $^5L_{10} \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 2334 | 3.7E-01 | 3.5E-01 | 2.2E-02 | 0.0E+00 |
| 65 | $^5G_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 27.0 | 3130 | 1.5E+09 | 2.6E+00 | 6.4E+01 | 1.5E+09 |
| 66 | $^5D_2 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 3470 | 1.2E+01 | 1.7E+00 | 1.1E+01 | 0.0E+00 |
| 67 | $^5G_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 3.8 | 3650 | 2.1E+08 | 9.3E-01 | 3.5E+02 | 2.1E+08 |
| 68 | $^5L_9 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 3771 | 3.7E+00 | 2.8E+00 | 8.6E-01 | 0.0E+00 |
| 69 | $^5L_8 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 4553 | 6.1E+00 | 4.1E+00 | 2.0E+00 | 0.0E+00 |
| 70 | $^5L_7 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 4820 | 6.6E+01 | 1.3E+00 | 6.5E+01 | 0.0E+00 |
| 71 | $^5L_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.1 | 5033 | 4.2E+06 | 0.0E+00 | 0.0E+00 | 4.2E+06 |
| 72 | $^5H_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.2 | 8254 | 1.1E+07 | 0.0E+00 | 0.0E+00 | 1.1E+07 |
| 73 | $^5H_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 1.9 | 9130 | 1.1E+08 | 0.0E+00 | 0.0E+00 | 1.1E+08 |
| 74 | $^5H_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 4.0 | 9702 | 2.2E+08 | 0.0E+00 | 0.0E+00 | 2.2E+08 |
| 75 | $^5F_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 1.4 | 10297 | 7.6E+07 | 0.0E+00 | 0.0E+00 | 7.6E+07 |
| 76 | $^5F_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 3.9 | 10737 | 2.2E+08 | 0.0E+00 | 0.0E+00 | 2.2E+08 |
| 77 | $^5I_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 12961 | 1.1E+06 | 0.0E+00 | 0.0E+00 | 1.1E+06 |
| 78 | $^5I_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 12971 | 1.6E+03 | 0.0E+00 | 0.0E+00 | 1.6E+03 |
| 79 | $^5I_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 13349 | 6.6E+04 | 0.0E+00 | 0.0E+00 | 6.6E+04 |
| 80 | $^5K_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 16697 | 1.2E+03 | 0.0E+00 | 0.0E+00 | 1.2E+03 |
| | | | | W_b^T | 5.6×10^9 | | | |

Table S15. Forward (ligand-to-Tb) IET rates for **NEt₄[TbL₄]**.

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm ⁻¹) | W (s ⁻¹) | W_{d-d} (s ⁻¹) | W_{d-m} (s ⁻¹) | W_{ex} (s ⁻¹) |
|-----------|--------------------------------|--|---------------|------------------------------|------------------------|------------------------------|------------------------------|-----------------------------|
| 1 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₄ | 0.0 | 17556 | 9.8E+00 | 2.0E-02 | 9.8E+00 | 0.0E+00 |
| 2 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₃ | 0.0 | 11764 | 3.3E+01 | 2.7E+01 | 5.7E+00 | 0.0E+00 |
| 3 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₆ | 0.2 | 11577 | 7.0E+06 | 2.6E+03 | 3.3E+04 | 7.0E+06 |
| 4 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₁₀ | 0.0 | 11029 | 2.2E+03 | 2.2E+03 | 3.9E+01 | 0.0E+00 |
| 5 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₅ | 0.1 | 10233 | 1.8E+06 | 1.1E+03 | 8.8E+04 | 1.7E+06 |
| 6 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₄ | 0.0 | 9713 | 1.3E+04 | 1.1E+03 | 1.2E+04 | 0.0E+00 |
| 7 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₉ | 0.0 | 9592 | 6.7E+03 | 6.3E+03 | 4.5E+02 | 0.0E+00 |
| 8 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₃ | 0.0 | 9023 | 3.9E+02 | 3.2E+02 | 6.7E+01 | 0.0E+00 |
| 9 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₈ | 0.0 | 8810 | 5.8E+03 | 5.8E+03 | 9.6E+01 | 0.0E+00 |
| 10 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₇ | 0.0 | 8543 | 1.8E+05 | 3.7E+03 | 1.7E+05 | 6.9E+01 |
| 11 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₆ | 0.1 | 8330 | 1.8E+06 | 0.0E+00 | 0.0E+00 | 1.8E+06 |
| 12 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₇ | 0.2 | 6621 | 6.2E+06 | 0.0E+00 | 0.0E+00 | 6.2E+06 |
| 13 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₆ | 3.7 | 5109 | 1.1E+08 | 0.0E+00 | 0.0E+00 | 1.1E+08 |
| 14 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₅ | 0.0 | 4233 | 1.7E+00 | 0.0E+00 | 0.0E+00 | 1.7E+00 |
| 15 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ F ₅ | 15.8 | 3066 | 4.6E+08 | 0.0E+00 | 0.0E+00 | 4.6E+08 |
| 16 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₇ | 1.0 | 1411 | 2.8E+07 | 0.0E+00 | 0.0E+00 | 2.8E+07 |
| 17 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₆ | 15.1 | 402 | 4.4E+08 | 0.0E+00 | 0.0E+00 | 4.4E+08 |
| 18 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₅ | 1.3 | 14 | 3.7E+07 | 0.0E+00 | 0.0E+00 | 3.7E+07 |
| 19 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₅ | 0.0 | -3334 | 1.2E-01 | 0.0E+00 | 0.0E+00 | 1.2E-01 |
| 20 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₇ | 0.0 | -3693 | 2.3E-09 | 0.0E+00 | 0.0E+00 | 2.3E-09 |
| 21 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₄ | 0.0 | 19604 | 2.2E+01 | 1.9E-03 | 6.8E+00 | 1.5E+01 |
| 22 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₃ | 0.0 | 13812 | 1.1E+03 | 6.8E+00 | 1.1E+03 | 0.0E+00 |
| 23 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₆ | 0.0 | 13625 | 1.3E+05 | 3.0E+01 | 1.0E+04 | 1.2E+05 |
| 24 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₁₀ | 0.0 | 13077 | 7.9E+00 | 7.8E+00 | 7.9E-02 | 0.0E+00 |
| 25 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₅ | 0.1 | 12281 | 1.7E+06 | 8.2E+01 | 1.2E+03 | 1.7E+06 |
| 26 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₂ | 0.0 | 11941 | 1.1E+02 | 3.5E+01 | 7.2E+01 | 0.0E+00 |
| 27 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₄ | 0.0 | 11761 | 3.9E+05 | 4.6E+01 | 1.0E+04 | 3.8E+05 |
| 28 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₉ | 0.0 | 11640 | 3.7E+02 | 3.4E+02 | 2.9E+01 | 0.0E+00 |
| 29 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₈ | 0.0 | 10858 | 1.3E+03 | 1.1E+03 | 1.6E+02 | 0.0E+00 |
| 30 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₇ | 0.0 | 10591 | 1.3E+04 | 4.5E+02 | 1.3E+04 | 0.0E+00 |
| 31 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 0.0 | 10378 | 5.7E+04 | 0.0E+00 | 0.0E+00 | 5.7E+04 |
| 32 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₆ | 0.2 | 7157 | 5.6E+06 | 0.0E+00 | 0.0E+00 | 5.6E+06 |
| 33 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₅ | 4.0 | 6281 | 1.2E+08 | 0.0E+00 | 0.0E+00 | 1.2E+08 |
| 34 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₄ | 12.3 | 5709 | 3.6E+08 | 0.0E+00 | 0.0E+00 | 3.6E+08 |
| 35 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₅ | 9.4 | 5114 | 2.7E+08 | 0.0E+00 | 0.0E+00 | 2.7E+08 |
| 36 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₄ | 34.3 | 4674 | 9.9E+08 | 0.0E+00 | 0.0E+00 | 9.9E+08 |
| 37 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 2.1 | 2450 | 6.0E+07 | 0.0E+00 | 0.0E+00 | 6.0E+07 |
| 38 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₄ | 0.0 | 2440 | 6.1E+04 | 0.0E+00 | 0.0E+00 | 6.1E+04 |
| 39 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₅ | 0.2 | 2062 | 4.5E+06 | 0.0E+00 | 0.0E+00 | 4.5E+06 |
| 40 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ K ₅ | 0.0 | -1286 | 2.8E+03 | 0.0E+00 | 0.0E+00 | 2.8E+03 |
| | | | | W^S | 2.9×10^9 | | | |
| 41 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₄ | 0.0 | 1767 | 1.5E+02 | 3.1E-01 | 1.4E+02 | 0.0E+00 |

| | | | | | | | | |
|-----------|--------------------------------|--|-------|--------|---------|---------|---------|---------|
| 42 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₃ | 0.0 | -4025 | 7.6E-10 | 6.4E-10 | 1.2E-10 | 0.0E+00 |
| 43 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₆ | 0.0 | -4212 | 4.9E-01 | 1.9E-08 | 2.4E-07 | 4.9E-01 |
| 44 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₁₀ | 0.0 | -4760 | 5.9E-10 | 5.8E-10 | 9.5E-12 | 0.0E+00 |
| 45 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₅ | 0.0 | -5556 | 3.4E-05 | 2.3E-12 | 1.8E-10 | 3.4E-05 |
| 46 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₄ | 0.0 | -6076 | 1.1E-12 | 9.9E-14 | 1.0E-12 | 0.0E+00 |
| 47 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₉ | 0.0 | -6197 | 3.0E-13 | 2.8E-13 | 1.8E-14 | 0.0E+00 |
| 48 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₃ | 0.0 | -6766 | 5.5E-16 | 4.6E-16 | 8.9E-17 | 0.0E+00 |
| 49 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₈ | 0.0 | -6979 | 2.3E-15 | 2.3E-15 | 3.5E-17 | 0.0E+00 |
| 50 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₇ | 0.0 | -7246 | 6.5E-14 | 3.0E-16 | 1.3E-14 | 5.2E-14 |
| 51 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₆ | 0.0 | -7459 | 3.8E-10 | 0.0E+00 | 0.0E+00 | 3.8E-10 |
| 52 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₇ | 0.0 | -9168 | 4.6E-14 | 0.0E+00 | 0.0E+00 | 4.6E-14 |
| 53 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₆ | 0.0 | -10680 | 9.9E-17 | 0.0E+00 | 0.0E+00 | 9.9E-17 |
| 54 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₅ | 0.0 | -11556 | 8.7E-27 | 0.0E+00 | 0.0E+00 | 8.7E-27 |
| 55 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ F ₅ | 0.0 | -12723 | 2.4E-21 | 0.0E+00 | 0.0E+00 | 2.4E-21 |
| 56 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₇ | 0.0 | -14378 | 8.9E-27 | 0.0E+00 | 0.0E+00 | 8.9E-27 |
| 57 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₆ | 0.0 | -15387 | 3.9E-28 | 0.0E+00 | 0.0E+00 | 3.9E-28 |
| 58 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₅ | 0.0 | -15775 | 3.4E-30 | 0.0E+00 | 0.0E+00 | 3.4E-30 |
| 59 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₅ | 0.0 | -19123 | 4.5E-40 | 0.0E+00 | 0.0E+00 | 4.5E-40 |
| 60 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₇ | 0.0 | -19482 | 6.1E-48 | 0.0E+00 | 0.0E+00 | 6.1E-48 |
| 61 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₄ | 100.0 | 3815 | 4.0E+07 | 5.4E-01 | 1.9E+03 | 4.0E+07 |
| 62 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₃ | 0.0 | -1977 | 6.8E-03 | 4.4E-05 | 6.7E-03 | 0.0E+00 |
| 63 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₆ | 0.0 | -2164 | 2.3E+03 | 6.3E-05 | 2.1E-02 | 2.3E+03 |
| 64 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₁₀ | 0.0 | -2712 | 5.7E-07 | 5.6E-07 | 5.1E-09 | 0.0E+00 |
| 65 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₅ | 0.0 | -3508 | 9.1E+00 | 4.5E-08 | 6.4E-07 | 9.1E+00 |
| 66 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₂ | 0.0 | -3848 | 7.1E-09 | 2.4E-09 | 4.7E-09 | 0.0E+00 |
| 67 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₄ | 0.0 | -4028 | 8.3E-02 | 1.1E-09 | 2.3E-07 | 8.3E-02 |
| 68 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₉ | 0.0 | -4149 | 4.0E-09 | 3.7E-09 | 3.0E-10 | 0.0E+00 |
| 69 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₈ | 0.0 | -4931 | 1.2E-10 | 1.1E-10 | 1.4E-11 | 0.0E+00 |
| 70 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₇ | 0.0 | -5198 | 2.4E-10 | 8.5E-12 | 2.3E-10 | 0.0E+00 |
| 71 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 0.0 | -5411 | 2.8E-06 | 0.0E+00 | 0.0E+00 | 2.8E-06 |
| 72 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₆ | 0.0 | -8632 | 1.0E-12 | 0.0E+00 | 0.0E+00 | 1.0E-12 |
| 73 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₅ | 0.0 | -9508 | 1.1E-13 | 0.0E+00 | 0.0E+00 | 1.1E-13 |
| 74 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₄ | 0.0 | -10080 | 1.2E-14 | 0.0E+00 | 0.0E+00 | 1.2E-14 |
| 75 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₅ | 0.0 | -10675 | 2.6E-16 | 0.0E+00 | 0.0E+00 | 2.6E-16 |
| 76 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₄ | 0.0 | -11115 | 6.9E-17 | 0.0E+00 | 0.0E+00 | 6.9E-17 |
| 77 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 0.0 | -13339 | 8.4E-24 | 0.0E+00 | 0.0E+00 | 8.4E-24 |
| 78 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₄ | 0.0 | -13349 | 8.0E-27 | 0.0E+00 | 0.0E+00 | 8.0E-27 |
| 79 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₅ | 0.0 | -13727 | 6.4E-26 | 0.0E+00 | 0.0E+00 | 6.4E-26 |
| 80 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ K ₅ | 0.0 | -17075 | 6.9E-35 | 0.0E+00 | 0.0E+00 | 6.9E-35 |

$$W^T \quad 4.0 \times 10^7$$

Table S16. Backward (Tb-to-ligand) IET rates for $\text{NEt}_4[\text{TbL}_4]$.

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm $^{-1}$) | W_b (s $^{-1}$) | W_{d-d} (s $^{-1}$) | W_{d-m} (s $^{-1}$) | W_{ex} (s $^{-1}$) |
|-----------|--|-------------------------------------|-----------------------|------------------------|--------------------|------------------------|------------------------|-----------------------|
| 1 | $^5\text{D}_4 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -17556 | 2.3E-36 | 4.7E-39 | 2.3E-36 | 0.0E+00 |
| 2 | $^5\text{D}_3 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -11764 | 1.4E-23 | 1.1E-23 | 2.3E-24 | 0.0E+00 |
| 3 | $^5\text{G}_6 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -11577 | 3.8E-18 | 1.4E-21 | 1.8E-20 | 3.8E-18 |
| 4 | $^5\text{L}_{10} \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -11029 | 1.1E-20 | 1.0E-20 | 1.8E-22 | 0.0E+00 |
| 5 | $^5\text{G}_5 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -10233 | 7.6E-16 | 4.6E-19 | 3.7E-17 | 7.2E-16 |
| 6 | $^5\text{G}_4 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -9713 | 8.0E-17 | 6.9E-18 | 7.4E-17 | 0.0E+00 |
| 7 | $^5\text{L}_9 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -9592 | 3.6E-17 | 3.4E-17 | 2.4E-18 | 0.0E+00 |
| 8 | $^5\text{G}_3 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -9023 | 8.9E-17 | 7.3E-17 | 1.5E-17 | 0.0E+00 |
| 9 | $^5\text{L}_8 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -8810 | 1.5E-15 | 1.5E-15 | 2.5E-17 | 0.0E+00 |
| 10 | $^5\text{L}_7 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -8543 | 1.9E-13 | 4.1E-15 | 1.9E-13 | 7.4E-17 |
| 11 | $^5\text{L}_6 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -8330 | 6.4E-12 | 0.0E+00 | 0.0E+00 | 6.4E-12 |
| 12 | $^5\text{H}_7 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -6621 | 7.2E-08 | 0.0E+00 | 0.0E+00 | 7.2E-08 |
| 13 | $^5\text{H}_6 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -5109 | 2.1E-03 | 0.0E+00 | 0.0E+00 | 2.1E-03 |
| 14 | $^5\text{H}_5 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -4233 | 2.7E-09 | 0.0E+00 | 0.0E+00 | 2.7E-09 |
| 15 | $^5\text{F}_5 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -3066 | 2.0E+02 | 0.0E+00 | 0.0E+00 | 2.0E+02 |
| 16 | $^5\text{I}_7 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -1411 | 2.7E+04 | 0.0E+00 | 0.0E+00 | 2.7E+04 |
| 17 | $^5\text{I}_6 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 58.9 | -402 | 6.3E+07 | 0.0E+00 | 0.0E+00 | 6.3E+07 |
| 18 | $^5\text{I}_5 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 38.4 | -14 | 4.1E+07 | 0.0E+00 | 0.0E+00 | 4.1E+07 |
| 19 | $^5\text{K}_5 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 1.3 | 3334 | 1.4E+06 | 0.0E+00 | 0.0E+00 | 1.4E+06 |
| 20 | $^5\text{K}_7 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | 3693 | 1.1E-01 | 0.0E+00 | 0.0E+00 | 1.1E-01 |
| 21 | $^5\text{D}_4 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -19604 | 2.2E-40 | 1.9E-44 | 6.8E-41 | 1.5E-40 |
| 22 | $^5\text{D}_3 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -13812 | 1.9E-26 | 1.2E-28 | 1.9E-26 | 0.0E+00 |
| 23 | $^5\text{G}_6 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -13625 | 3.0E-24 | 7.2E-28 | 2.5E-25 | 2.7E-24 |
| 24 | $^5\text{L}_{10} \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -13077 | 1.6E-27 | 1.6E-27 | 1.6E-29 | 0.0E+00 |
| 25 | $^5\text{G}_5 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -12281 | 3.2E-20 | 1.5E-24 | 2.2E-23 | 3.2E-20 |
| 26 | $^5\text{D}_2 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -11941 | 2.2E-23 | 7.3E-24 | 1.5E-23 | 0.0E+00 |
| 27 | $^5\text{G}_4 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -11761 | 1.1E-19 | 1.3E-23 | 2.8E-21 | 1.0E-19 |
| 28 | $^5\text{L}_9 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -11640 | 8.6E-23 | 7.9E-23 | 6.7E-24 | 0.0E+00 |
| 29 | $^5\text{L}_8 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -10858 | 1.5E-20 | 1.3E-20 | 1.8E-21 | 0.0E+00 |
| 30 | $^5\text{L}_7 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -10591 | 6.1E-19 | 2.1E-20 | 5.9E-19 | 0.0E+00 |
| 31 | $^5\text{I}_6 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -10378 | 8.5E-18 | 0.0E+00 | 0.0E+00 | 8.5E-18 |
| 32 | $^5\text{H}_6 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -7157 | 4.7E-09 | 0.0E+00 | 0.0E+00 | 4.7E-09 |
| 33 | $^5\text{H}_5 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -6281 | 8.0E-06 | 0.0E+00 | 0.0E+00 | 8.0E-06 |
| 34 | $^5\text{H}_4 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -5709 | 4.7E-04 | 0.0E+00 | 0.0E+00 | 4.7E-04 |
| 35 | $^5\text{F}_5 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -5114 | 5.2E-03 | 0.0E+00 | 0.0E+00 | 5.2E-03 |
| 36 | $^5\text{F}_4 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -4674 | 1.9E-01 | 0.0E+00 | 0.0E+00 | 1.9E-01 |
| 37 | $^5\text{I}_6 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -2450 | 3.7E+02 | 0.0E+00 | 0.0E+00 | 3.7E+02 |
| 38 | $^5\text{I}_4 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -2440 | 5.7E-01 | 0.0E+00 | 0.0E+00 | 5.7E-01 |
| 39 | $^5\text{I}_5 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 0.0 | -2062 | 2.1E+02 | 0.0E+00 | 0.0E+00 | 2.1E+02 |
| 40 | $^5\text{K}_5 \rightarrow ^7\text{F}_5$ | $\text{S}_0 \rightarrow \text{S}_1$ | 1.3 | 1286 | 1.4E+06 | 0.0E+00 | 0.0E+00 | 1.4E+06 |
| | | | | W_b^S | 1.1×10^8 | | | |
| 41 | $^5\text{D}_4 \rightarrow ^7\text{F}_6$ | $\text{S}_0 \rightarrow \text{T}_1$ | 0.0 | -1767 | 4.1E-02 | 8.8E-05 | 4.1E-02 | 0.0E+00 |

| | | | | | | | | |
|-----------|------------------------------|-----------------------|------|---------|-------------------|---------|---------|---------|
| 42 | $^5D_3 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 4025 | 3.9E-01 | 3.2E-01 | 6.3E-02 | 0.0E+00 |
| 43 | $^5G_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 47.1 | 4212 | 3.3E+08 | 1.3E+01 | 1.6E+02 | 3.3E+08 |
| 44 | $^5L_{10} \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 4760 | 3.5E+00 | 3.4E+00 | 5.5E-02 | 0.0E+00 |
| 45 | $^5G_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 2.5 | 5556 | 1.8E+07 | 1.2E+00 | 9.6E+01 | 1.8E+07 |
| 46 | $^5G_4 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6076 | 8.9E+00 | 7.8E-01 | 8.1E+00 | 0.0E+00 |
| 47 | $^5L_9 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6197 | 2.0E+00 | 1.8E+00 | 1.2E-01 | 0.0E+00 |
| 48 | $^5G_3 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6766 | 1.5E-01 | 1.3E-01 | 2.5E-02 | 0.0E+00 |
| 49 | $^5L_8 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6979 | 7.5E-01 | 7.3E-01 | 1.1E-02 | 0.0E+00 |
| 50 | $^5L_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 7246 | 8.7E+01 | 3.9E-01 | 1.8E+01 | 6.8E+01 |
| 51 | $^5L_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.2 | 7459 | 1.6E+06 | 0.0E+00 | 0.0E+00 | 1.6E+06 |
| 52 | $^5H_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.1 | 9168 | 6.5E+05 | 0.0E+00 | 0.0E+00 | 6.5E+05 |
| 53 | $^5H_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.3 | 10680 | 2.4E+06 | 0.0E+00 | 0.0E+00 | 2.4E+06 |
| 54 | $^5H_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 11556 | 1.7E-02 | 0.0E+00 | 0.0E+00 | 1.7E-02 |
| 55 | $^5F_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.2 | 12723 | 1.3E+06 | 0.0E+00 | 0.0E+00 | 1.3E+06 |
| 56 | $^5I_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 14378 | 1.0E+04 | 0.0E+00 | 0.0E+00 | 1.0E+04 |
| 57 | $^5I_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 15387 | 6.8E+04 | 0.0E+00 | 0.0E+00 | 6.8E+04 |
| 58 | $^5I_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 15775 | 4.7E+03 | 0.0E+00 | 0.0E+00 | 4.7E+03 |
| 59 | $^5K_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 19123 | 6.3E+00 | 0.0E+00 | 0.0E+00 | 6.3E+00 |
| 60 | $^5K_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 19482 | 3.5E-07 | 0.0E+00 | 0.0E+00 | 3.5E-07 |
| 61 | $^5D_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | -3815 | 4.9E-01 | 6.6E-09 | 2.3E-05 | 4.9E-01 |
| 62 | $^5D_3 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 1977 | 1.5E+02 | 9.7E-01 | 1.5E+02 | 0.0E+00 |
| 63 | $^5G_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 9.3 | 2164 | 6.6E+07 | 1.8E+00 | 6.1E+02 | 6.6E+07 |
| 64 | $^5L_{10} \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 2712 | 1.4E-01 | 1.4E-01 | 1.3E-03 | 0.0E+00 |
| 65 | $^5G_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 28.9 | 3508 | 2.0E+08 | 1.0E+00 | 1.4E+01 | 2.0E+08 |
| 66 | $^5D_2 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 3848 | 1.8E+00 | 6.2E-01 | 1.2E+00 | 0.0E+00 |
| 67 | $^5G_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 4.0 | 4028 | 2.8E+07 | 3.6E-01 | 7.7E+01 | 2.8E+07 |
| 68 | $^5L_9 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 4149 | 1.2E+00 | 1.1E+00 | 8.5E-02 | 0.0E+00 |
| 69 | $^5L_8 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 4931 | 1.7E+00 | 1.5E+00 | 2.0E-01 | 0.0E+00 |
| 70 | $^5L_7 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 5198 | 1.4E+01 | 4.8E-01 | 1.3E+01 | 0.0E+00 |
| 71 | $^5L_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.1 | 5411 | 5.1E+05 | 0.0E+00 | 0.0E+00 | 5.1E+05 |
| 72 | $^5H_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.2 | 8632 | 1.1E+06 | 0.0E+00 | 0.0E+00 | 1.1E+06 |
| 73 | $^5H_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 1.4 | 9508 | 9.5E+06 | 0.0E+00 | 0.0E+00 | 9.5E+06 |
| 74 | $^5H_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 2.7 | 10080 | 1.9E+07 | 0.0E+00 | 0.0E+00 | 1.9E+07 |
| 75 | $^5F_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.9 | 10675 | 6.1E+06 | 0.0E+00 | 0.0E+00 | 6.1E+06 |
| 76 | $^5F_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 2.3 | 11115 | 1.7E+07 | 0.0E+00 | 0.0E+00 | 1.7E+07 |
| 77 | $^5I_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 13339 | 6.4E+04 | 0.0E+00 | 0.0E+00 | 6.4E+04 |
| 78 | $^5I_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 13349 | 9.3E+01 | 0.0E+00 | 0.0E+00 | 9.3E+01 |
| 79 | $^5I_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 13727 | 3.8E+03 | 0.0E+00 | 0.0E+00 | 3.8E+03 |
| 80 | $^5K_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 17075 | 4.2E+01 | 0.0E+00 | 0.0E+00 | 4.2E+01 |
| | | | | W_b^T | 7.1×10^8 | | | |

Table S17. Forward (ligand-to-Tb) IET rates for **PPh₄[TbL₄]**.

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm ⁻¹) | W (s ⁻¹) | W_{d-d} (s ⁻¹) | W_{d-m} (s ⁻¹) | W_{ex} (s ⁻¹) |
|-----------|--------------------------------|--|---------------|------------------------------|------------------------|------------------------------|------------------------------|-----------------------------|
| 1 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₄ | 0.0 | 14056 | 3.6E+01 | 8.0E-02 | 3.6E+01 | 0.0E+00 |
| 2 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₃ | 0.0 | 8264 | 1.9E+01 | 1.8E+01 | 6.0E-01 | 0.0E+00 |
| 3 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₆ | 2.5 | 8077 | 1.1E+06 | 1.7E+03 | 2.0E+04 | 1.1E+06 |
| 4 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₁₀ | 0.0 | 7529 | 1.2E+03 | 1.2E+03 | 1.8E+00 | 0.0E+00 |
| 5 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₅ | 0.5 | 6733 | 2.2E+05 | 4.7E+02 | 3.6E+04 | 1.8E+05 |
| 6 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₄ | 0.0 | 6213 | 4.4E+03 | 3.9E+02 | 4.0E+03 | 0.0E+00 |
| 7 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₉ | 0.0 | 6092 | 2.2E+03 | 2.2E+03 | 2.3E+01 | 0.0E+00 |
| 8 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₃ | 0.0 | 5523 | 9.8E+01 | 9.5E+01 | 3.1E+00 | 0.0E+00 |
| 9 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₈ | 0.0 | 5310 | 1.6E+03 | 1.6E+03 | 2.2E+00 | 0.0E+00 |
| 10 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₇ | 0.1 | 5043 | 4.3E+04 | 9.5E+02 | 4.2E+04 | 4.4E+00 |
| 11 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₆ | 0.2 | 4830 | 1.1E+05 | 0.0E+00 | 0.0E+00 | 1.1E+05 |
| 12 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₇ | 0.5 | 3121 | 2.2E+05 | 0.0E+00 | 0.0E+00 | 2.2E+05 |
| 13 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₆ | 5.5 | 1609 | 2.5E+06 | 0.0E+00 | 0.0E+00 | 2.5E+06 |
| 14 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₅ | 0.0 | 733 | 3.0E-02 | 0.0E+00 | 0.0E+00 | 3.0E-02 |
| 15 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ F ₅ | 1.5 | -434 | 6.9E+05 | 0.0E+00 | 0.0E+00 | 6.9E+05 |
| 16 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₇ | 0.0 | -2089 | 8.7E+00 | 0.0E+00 | 0.0E+00 | 8.7E+00 |
| 17 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₆ | 0.0 | -3098 | 7.7E-01 | 0.0E+00 | 0.0E+00 | 7.7E-01 |
| 18 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₅ | 0.0 | -3486 | 8.9E-03 | 0.0E+00 | 0.0E+00 | 8.9E-03 |
| 19 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₅ | 0.0 | -6834 | 9.9E-12 | 0.0E+00 | 0.0E+00 | 9.9E-12 |
| 20 | S ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₇ | 0.0 | -7193 | 1.7E-19 | 0.0E+00 | 0.0E+00 | 1.7E-19 |
| 21 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₄ | 0.0 | 16104 | 7.4E+01 | 1.3E-02 | 4.7E+01 | 2.7E+01 |
| 22 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₃ | 0.0 | 10312 | 1.3E+03 | 8.6E+00 | 1.2E+03 | 0.0E+00 |
| 23 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₆ | 0.1 | 10125 | 4.7E+04 | 3.6E+01 | 1.2E+04 | 3.5E+04 |
| 24 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₁₀ | 0.0 | 9577 | 7.9E+00 | 7.9E+00 | 2.3E-03 | 0.0E+00 |
| 25 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₅ | 0.8 | 8781 | 3.5E+05 | 6.5E+01 | 8.8E+02 | 3.5E+05 |
| 26 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₂ | 0.0 | 8441 | 3.4E+01 | 2.5E+01 | 8.4E+00 | 0.0E+00 |
| 27 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₄ | 0.2 | 8261 | 7.1E+04 | 3.1E+01 | 6.5E+03 | 6.5E+04 |
| 28 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₉ | 0.0 | 8140 | 2.2E+02 | 2.2E+02 | 2.8E+00 | 0.0E+00 |
| 29 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₈ | 0.0 | 7358 | 6.0E+02 | 5.9E+02 | 1.3E+01 | 0.0E+00 |
| 30 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₇ | 0.0 | 7091 | 5.9E+03 | 2.1E+02 | 5.6E+03 | 0.0E+00 |
| 31 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 0.0 | 6878 | 6.4E+03 | 0.0E+00 | 0.0E+00 | 6.4E+03 |
| 32 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₆ | 0.5 | 3657 | 2.4E+05 | 0.0E+00 | 0.0E+00 | 2.4E+05 |
| 33 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₅ | 8.3 | 2781 | 3.8E+06 | 0.0E+00 | 0.0E+00 | 3.8E+06 |
| 34 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₄ | 21.5 | 2209 | 9.7E+06 | 0.0E+00 | 0.0E+00 | 9.7E+06 |
| 35 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₅ | 13.8 | 1614 | 6.2E+06 | 0.0E+00 | 0.0E+00 | 6.2E+06 |
| 36 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₄ | 43.9 | 1174 | 2.0E+07 | 0.0E+00 | 0.0E+00 | 2.0E+07 |
| 37 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 0.0 | -1050 | 3.9E+03 | 0.0E+00 | 0.0E+00 | 3.9E+03 |
| 38 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₄ | 0.0 | -1060 | 3.7E+00 | 0.0E+00 | 0.0E+00 | 3.7E+00 |
| 39 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₅ | 0.0 | -1438 | 3.9E+01 | 0.0E+00 | 0.0E+00 | 3.9E+01 |
| 40 | S ₁ →S ₀ | ⁷ F ₅ → ⁵ K ₅ | 0.0 | -4786 | 4.3E-07 | 0.0E+00 | 0.0E+00 | 4.3E-07 |
| | | | | W^S | 4.5×10^7 | | | |
| 41 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₄ | 0.0 | 2346 | 4.2E+00 | 9.3E-03 | 4.2E+00 | 0.0E+00 |

| | | | | | | | | |
|-----------|--------------------------------|--|------|--------|---------|---------|---------|---------|
| 42 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ D ₃ | 0.0 | -3446 | 4.1E-10 | 4.0E-10 | 1.3E-11 | 0.0E+00 |
| 43 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₆ | 0.0 | -3633 | 8.1E-02 | 1.2E-08 | 1.5E-07 | 8.1E-02 |
| 44 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₁₀ | 0.0 | -4181 | 3.8E-10 | 3.8E-10 | 5.7E-13 | 0.0E+00 |
| 45 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₅ | 0.0 | -4977 | 6.2E-06 | 1.6E-12 | 1.2E-10 | 6.2E-06 |
| 46 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₄ | 0.0 | -5497 | 7.8E-13 | 7.1E-14 | 7.1E-13 | 0.0E+00 |
| 47 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₉ | 0.0 | -5618 | 2.0E-13 | 2.0E-13 | 2.0E-15 | 0.0E+00 |
| 48 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ G ₃ | 0.0 | -6187 | 3.6E-16 | 3.4E-16 | 1.1E-17 | 0.0E+00 |
| 49 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₈ | 0.0 | -6400 | 1.7E-15 | 1.7E-15 | 2.3E-18 | 0.0E+00 |
| 50 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₇ | 0.0 | -6667 | 2.1E-14 | 2.3E-16 | 1.0E-14 | 1.1E-14 |
| 51 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ L ₆ | 0.0 | -6880 | 8.0E-11 | 0.0E+00 | 0.0E+00 | 8.0E-11 |
| 52 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₇ | 0.0 | -8589 | 1.1E-14 | 0.0E+00 | 0.0E+00 | 1.1E-14 |
| 53 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₆ | 0.0 | -10101 | 2.8E-17 | 0.0E+00 | 0.0E+00 | 2.8E-17 |
| 54 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ H ₅ | 0.0 | -10977 | 2.7E-27 | 0.0E+00 | 0.0E+00 | 2.7E-27 |
| 55 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ F ₅ | 0.0 | -12144 | 8.6E-22 | 0.0E+00 | 0.0E+00 | 8.6E-22 |
| 56 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₇ | 0.0 | -13799 | 3.9E-27 | 0.0E+00 | 0.0E+00 | 3.9E-27 |
| 57 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₆ | 0.0 | -14808 | 2.0E-28 | 0.0E+00 | 0.0E+00 | 2.0E-28 |
| 58 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ I ₅ | 0.0 | -15196 | 1.8E-30 | 0.0E+00 | 0.0E+00 | 1.8E-30 |
| 59 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₅ | 0.0 | -18544 | 4.0E-40 | 0.0E+00 | 0.0E+00 | 4.0E-40 |
| 60 | T ₁ →S ₀ | ⁷ F ₆ → ⁵ K ₇ | 0.0 | -18903 | 5.8E-48 | 0.0E+00 | 0.0E+00 | 5.8E-48 |
| 61 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₄ | 99.9 | 4394 | 3.1E+05 | 1.5E-02 | 5.3E+01 | 3.1E+05 |
| 62 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₃ | 0.0 | -1398 | 3.6E-03 | 2.5E-05 | 3.6E-03 | 0.0E+00 |
| 63 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₆ | 0.1 | -1585 | 3.3E+02 | 3.5E-05 | 1.1E-02 | 3.3E+02 |
| 64 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₁₀ | 0.0 | -2133 | 3.2E-07 | 3.2E-07 | 9.0E-11 | 0.0E+00 |
| 65 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₅ | 0.0 | -2929 | 1.4E+00 | 2.7E-08 | 3.7E-07 | 1.4E+00 |
| 66 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ D ₂ | 0.0 | -3269 | 2.0E-09 | 1.5E-09 | 4.9E-10 | 0.0E+00 |
| 67 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ G ₄ | 0.0 | -3449 | 1.3E-02 | 6.5E-10 | 1.4E-07 | 1.3E-02 |
| 68 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₉ | 0.0 | -3570 | 2.4E-09 | 2.3E-09 | 2.9E-11 | 0.0E+00 |
| 69 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₈ | 0.0 | -4352 | 7.3E-11 | 7.1E-11 | 1.5E-12 | 0.0E+00 |
| 70 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ L ₇ | 0.0 | -4619 | 1.5E-10 | 5.7E-12 | 1.5E-10 | 0.0E+00 |
| 71 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 0.0 | -4832 | 4.9E-07 | 0.0E+00 | 0.0E+00 | 4.9E-07 |
| 72 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₆ | 0.0 | -8053 | 2.4E-13 | 0.0E+00 | 0.0E+00 | 2.4E-13 |
| 73 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₅ | 0.0 | -8929 | 2.8E-14 | 0.0E+00 | 0.0E+00 | 2.8E-14 |
| 74 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ H ₄ | 0.0 | -9501 | 3.1E-15 | 0.0E+00 | 0.0E+00 | 3.1E-15 |
| 75 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₅ | 0.0 | -10096 | 7.3E-17 | 0.0E+00 | 0.0E+00 | 7.3E-17 |
| 76 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ F ₄ | 0.0 | -10536 | 2.1E-17 | 0.0E+00 | 0.0E+00 | 2.1E-17 |
| 77 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₆ | 0.0 | -12760 | 3.3E-24 | 0.0E+00 | 0.0E+00 | 3.3E-24 |
| 78 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₄ | 0.0 | -12770 | 3.1E-27 | 0.0E+00 | 0.0E+00 | 3.1E-27 |
| 79 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ I ₅ | 0.0 | -13148 | 2.6E-26 | 0.0E+00 | 0.0E+00 | 2.6E-26 |
| 80 | T ₁ →S ₀ | ⁷ F ₅ → ⁵ K ₅ | 0.0 | -16496 | 4.5E-35 | 0.0E+00 | 0.0E+00 | 4.5E-35 |

$$W^T \quad 3.1 \times 10^5$$

Table S18. Backward (Tb-to-ligand) IET rates for **PPh₄[TbL₄]**

| <i>p</i> | donor | acceptor | contr. (%) | Δ (cm ⁻¹) | W_b (s ⁻¹) | W_{d-d} (s ⁻¹) | W_{d-m} (s ⁻¹) | W_{ex} (s ⁻¹) |
|-----------|--|--------------------------------|-----------------------|------------------------------|--------------------------|------------------------------|------------------------------|-----------------------------|
| 1 | ⁵ D ₄ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -14056 | 1.8E-28 | 4.0E-31 | 1.8E-28 | 0.0E+00 |
| 2 | ⁵ D ₃ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -8264 | 1.7E-16 | 1.6E-16 | 5.4E-18 | 0.0E+00 |
| 3 | ⁵ G ₆ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -8077 | 1.4E-11 | 2.0E-14 | 2.4E-13 | 1.3E-11 |
| 4 | ⁵ L ₁₀ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -7529 | 1.2E-13 | 1.2E-13 | 1.9E-16 | 0.0E+00 |
| 5 | ⁵ G ₅ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -6733 | 2.0E-09 | 4.3E-12 | 3.3E-10 | 1.7E-09 |
| 6 | ⁵ G ₄ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -6213 | 6.0E-10 | 5.4E-11 | 5.5E-10 | 0.0E+00 |
| 7 | ⁵ L ₉ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -6092 | 2.6E-10 | 2.6E-10 | 2.6E-12 | 0.0E+00 |
| 8 | ⁵ G ₃ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -5523 | 4.8E-10 | 4.7E-10 | 1.5E-11 | 0.0E+00 |
| 9 | ⁵ L ₈ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -5310 | 9.1E-09 | 9.0E-09 | 1.2E-11 | 0.0E+00 |
| 10 | ⁵ L ₇ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -5043 | 1.0E-06 | 2.2E-08 | 9.8E-07 | 1.0E-10 |
| 11 | ⁵ L ₆ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -4830 | 8.4E-06 | 0.0E+00 | 0.0E+00 | 8.4E-06 |
| 12 | ⁵ H ₇ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -3121 | 5.6E-02 | 0.0E+00 | 0.0E+00 | 5.6E-02 |
| 13 | ⁵ H ₆ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -1609 | 1.0E+03 | 0.0E+00 | 0.0E+00 | 1.0E+03 |
| 14 | ⁵ H ₅ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | -733 | 1.0E-03 | 0.0E+00 | 0.0E+00 | 1.0E-03 |
| 15 | ⁵ F ₅ → ⁷ F ₆ | S ₀ →S ₁ | 65.8 | 434 | 6.6E+06 | 0.0E+00 | 0.0E+00 | 6.6E+06 |
| 16 | ⁵ I ₇ → ⁷ F ₆ | S ₀ →S ₁ | 1.8 | 2089 | 1.8E+05 | 0.0E+00 | 0.0E+00 | 1.8E+05 |
| 17 | ⁵ I ₆ → ⁷ F ₆ | S ₀ →S ₁ | 23.8 | 3098 | 2.4E+06 | 0.0E+00 | 0.0E+00 | 2.4E+06 |
| 18 | ⁵ I ₅ → ⁷ F ₆ | S ₀ →S ₁ | 2.1 | 3486 | 2.1E+05 | 0.0E+00 | 0.0E+00 | 2.1E+05 |
| 19 | ⁵ K ₅ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | 6834 | 2.5E+03 | 0.0E+00 | 0.0E+00 | 2.5E+03 |
| 20 | ⁵ K ₇ → ⁷ F ₆ | S ₀ →S ₁ | 0.0 | 7193 | 1.7E-04 | 0.0E+00 | 0.0E+00 | 1.7E-04 |
| 21 | ⁵ D ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -16104 | 1.6E-32 | 2.9E-36 | 1.0E-32 | 5.9E-33 |
| 22 | ⁵ D ₃ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -10312 | 4.8E-19 | 3.3E-21 | 4.8E-19 | 0.0E+00 |
| 23 | ⁵ G ₆ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -10125 | 2.4E-17 | 1.8E-20 | 6.0E-18 | 1.8E-17 |
| 24 | ⁵ L ₁₀ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -9577 | 3.5E-20 | 3.5E-20 | 1.0E-23 | 0.0E+00 |
| 25 | ⁵ G ₅ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -8781 | 1.4E-13 | 2.6E-17 | 3.5E-16 | 1.4E-13 |
| 26 | ⁵ D ₂ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -8441 | 1.5E-16 | 1.1E-16 | 3.8E-17 | 0.0E+00 |
| 27 | ⁵ G ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -8261 | 4.2E-13 | 1.8E-16 | 3.9E-14 | 3.9E-13 |
| 28 | ⁵ L ₉ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -8140 | 1.1E-15 | 1.1E-15 | 1.4E-17 | 0.0E+00 |
| 29 | ⁵ L ₈ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -7358 | 1.5E-13 | 1.4E-13 | 3.1E-15 | 0.0E+00 |
| 30 | ⁵ L ₇ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -7091 | 5.9E-12 | 2.2E-13 | 5.7E-12 | 0.0E+00 |
| 31 | ⁵ I ₆ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -6878 | 2.1E-11 | 0.0E+00 | 0.0E+00 | 2.1E-11 |
| 32 | ⁵ H ₆ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -3657 | 4.3E-03 | 0.0E+00 | 0.0E+00 | 4.3E-03 |
| 33 | ⁵ H ₅ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -2781 | 5.6E+00 | 0.0E+00 | 0.0E+00 | 5.6E+00 |
| 34 | ⁵ H ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -2209 | 2.8E+02 | 0.0E+00 | 0.0E+00 | 2.8E+02 |
| 35 | ⁵ F ₅ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | -1614 | 2.6E+03 | 0.0E+00 | 0.0E+00 | 2.6E+03 |
| 36 | ⁵ F ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.8 | -1174 | 8.4E+04 | 0.0E+00 | 0.0E+00 | 8.4E+04 |
| 37 | ⁵ I ₆ → ⁷ F ₅ | S ₀ →S ₁ | 5.2 | 1050 | 5.2E+05 | 0.0E+00 | 0.0E+00 | 5.2E+05 |
| 38 | ⁵ I ₄ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | 1060 | 7.5E+02 | 0.0E+00 | 0.0E+00 | 7.5E+02 |
| 39 | ⁵ I ₅ → ⁷ F ₅ | S ₀ →S ₁ | 0.4 | 1438 | 4.0E+04 | 0.0E+00 | 0.0E+00 | 4.0E+04 |
| 40 | ⁵ K ₅ → ⁷ F ₅ | S ₀ →S ₁ | 0.0 | 4786 | 4.6E+03 | 0.0E+00 | 0.0E+00 | 4.6E+03 |
| | | | | W_b^S | 1.0×10 ⁷ | | | |
| 41 | ⁵ D ₄ → ⁷ F ₆ | S ₀ →T ₁ | 0.0 | -2346 | 7.4E-05 | 1.6E-07 | 7.3E-05 | 0.0E+00 |

| | | | | | | | | |
|-----------|------------------------------|-----------------------|------|-------|---------|---------|---------|---------|
| 42 | $^5D_3 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 3446 | 1.3E-02 | 1.2E-02 | 3.9E-04 | 0.0E+00 |
| 43 | $^5G_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 45.4 | 3633 | 3.3E+06 | 5.0E-01 | 6.0E+00 | 3.3E+06 |
| 44 | $^5L_{10} \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 4181 | 1.4E-01 | 1.4E-01 | 2.0E-04 | 0.0E+00 |
| 45 | $^5G_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 2.7 | 4977 | 2.0E+05 | 5.1E-02 | 3.9E+00 | 2.0E+05 |
| 46 | $^5G_4 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 5497 | 3.7E-01 | 3.4E-02 | 3.4E-01 | 0.0E+00 |
| 47 | $^5L_9 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 5618 | 8.2E-02 | 8.1E-02 | 8.1E-04 | 0.0E+00 |
| 48 | $^5G_3 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6187 | 6.1E-03 | 5.9E-03 | 1.9E-04 | 0.0E+00 |
| 49 | $^5L_8 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6400 | 3.4E-02 | 3.4E-02 | 4.5E-05 | 0.0E+00 |
| 50 | $^5L_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 6667 | 1.7E+00 | 1.9E-02 | 8.2E-01 | 8.6E-01 |
| 51 | $^5L_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.3 | 6880 | 2.1E+04 | 0.0E+00 | 0.0E+00 | 2.1E+04 |
| 52 | $^5H_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.1 | 8589 | 9.7E+03 | 0.0E+00 | 0.0E+00 | 9.7E+03 |
| 53 | $^5H_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.6 | 10101 | 4.1E+04 | 0.0E+00 | 0.0E+00 | 4.1E+04 |
| 54 | $^5H_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 10977 | 3.2E-04 | 0.0E+00 | 0.0E+00 | 3.2E-04 |
| 55 | $^5F_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.4 | 12144 | 2.9E+04 | 0.0E+00 | 0.0E+00 | 2.9E+04 |
| 56 | $^5I_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 13799 | 2.8E+02 | 0.0E+00 | 0.0E+00 | 2.8E+02 |
| 57 | $^5I_6 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 14808 | 2.1E+03 | 0.0E+00 | 0.0E+00 | 2.1E+03 |
| 58 | $^5I_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 15196 | 1.5E+02 | 0.0E+00 | 0.0E+00 | 1.5E+02 |
| 59 | $^5K_5 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 18544 | 3.5E-01 | 0.0E+00 | 0.0E+00 | 3.5E-01 |
| 60 | $^5K_7 \rightarrow ^7F_6$ | $S_0 \rightarrow T_1$ | 0.0 | 18903 | 2.1E-08 | 0.0E+00 | 0.0E+00 | 2.1E-08 |
| 61 | $^5D_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | -4394 | 2.3E-04 | 1.2E-11 | 4.0E-08 | 2.3E-04 |
| 62 | $^5D_3 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 1398 | 4.8E+00 | 3.3E-02 | 4.8E+00 | 0.0E+00 |
| 63 | $^5G_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 8.0 | 1585 | 5.9E+05 | 6.3E-02 | 2.0E+01 | 5.9E+05 |
| 64 | $^5L_{10} \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 2133 | 5.0E-03 | 5.0E-03 | 1.4E-06 | 0.0E+00 |
| 65 | $^5G_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 26.7 | 2929 | 2.0E+06 | 3.8E-02 | 5.1E-01 | 2.0E+06 |
| 66 | $^5D_2 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 3269 | 3.1E-02 | 2.4E-02 | 7.6E-03 | 0.0E+00 |
| 67 | $^5G_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 3.8 | 3449 | 2.8E+05 | 1.4E-02 | 2.8E+00 | 2.8E+05 |
| 68 | $^5L_9 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 3570 | 4.2E-02 | 4.1E-02 | 5.0E-04 | 0.0E+00 |
| 69 | $^5L_8 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 4352 | 6.2E-02 | 6.1E-02 | 1.3E-03 | 0.0E+00 |
| 70 | $^5L_7 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 4619 | 5.4E-01 | 2.0E-02 | 5.2E-01 | 0.0E+00 |
| 71 | $^5L_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.1 | 4832 | 5.6E+03 | 0.0E+00 | 0.0E+00 | 5.6E+03 |
| 72 | $^5H_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.2 | 8053 | 1.5E+04 | 0.0E+00 | 0.0E+00 | 1.5E+04 |
| 73 | $^5H_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 2.0 | 8929 | 1.5E+05 | 0.0E+00 | 0.0E+00 | 1.5E+05 |
| 74 | $^5H_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 4.2 | 9501 | 3.1E+05 | 0.0E+00 | 0.0E+00 | 3.1E+05 |
| 75 | $^5F_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 1.4 | 10096 | 1.1E+05 | 0.0E+00 | 0.0E+00 | 1.1E+05 |
| 76 | $^5F_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 4.1 | 10536 | 3.0E+05 | 0.0E+00 | 0.0E+00 | 3.0E+05 |
| 77 | $^5I_6 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 12760 | 1.5E+03 | 0.0E+00 | 0.0E+00 | 1.5E+03 |
| 78 | $^5I_4 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 12770 | 2.2E+00 | 0.0E+00 | 0.0E+00 | 2.2E+00 |
| 79 | $^5I_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 13148 | 9.3E+01 | 0.0E+00 | 0.0E+00 | 9.3E+01 |
| 80 | $^5K_5 \rightarrow ^7F_5$ | $S_0 \rightarrow T_1$ | 0.0 | 16496 | 1.7E+00 | 0.0E+00 | 0.0E+00 | 1.7E+00 |

$$W_b^T \quad 7.4 \times 10^6$$

3. Figures

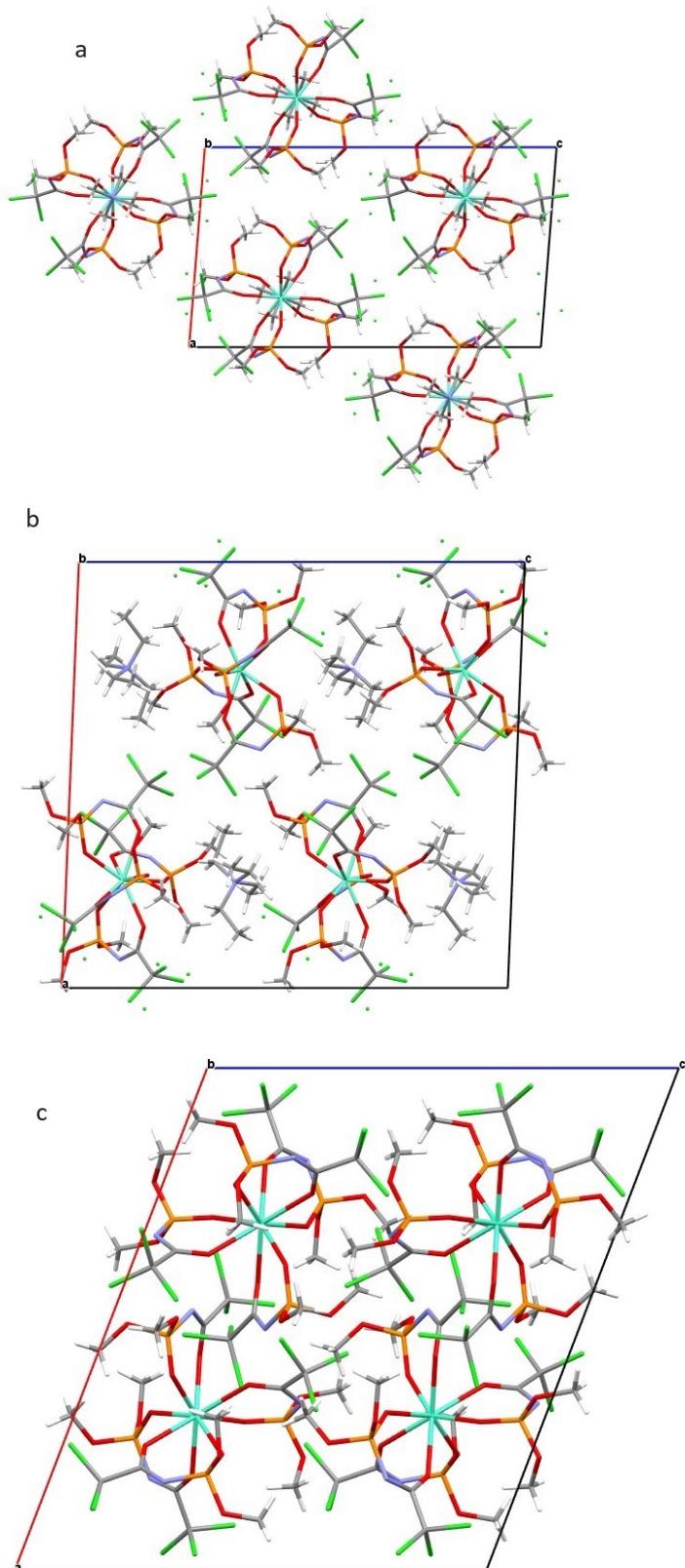


Figure S1. The crystal packing of $\text{NMe}_4[\text{EuL}_4]$ (a), $\text{NEt}_4[\text{EuL}_4]$ (b), $\text{PPh}_4[\text{GdL}_4]$ (the cations are omitted) (c) viewed along the b -axis direction.

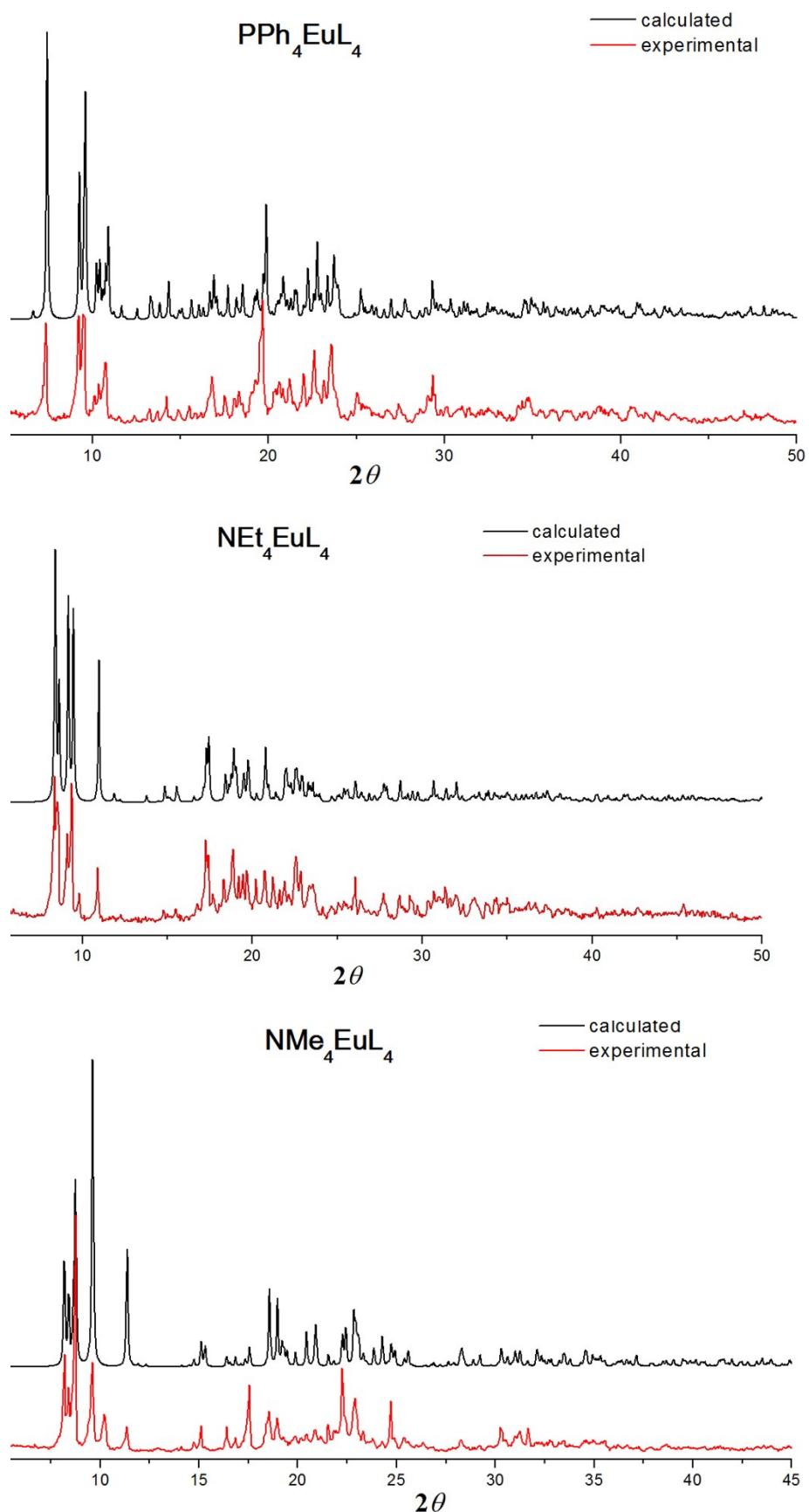


Figure S2. Calculated and experimental XRD patterns for the obtained europium complexes.

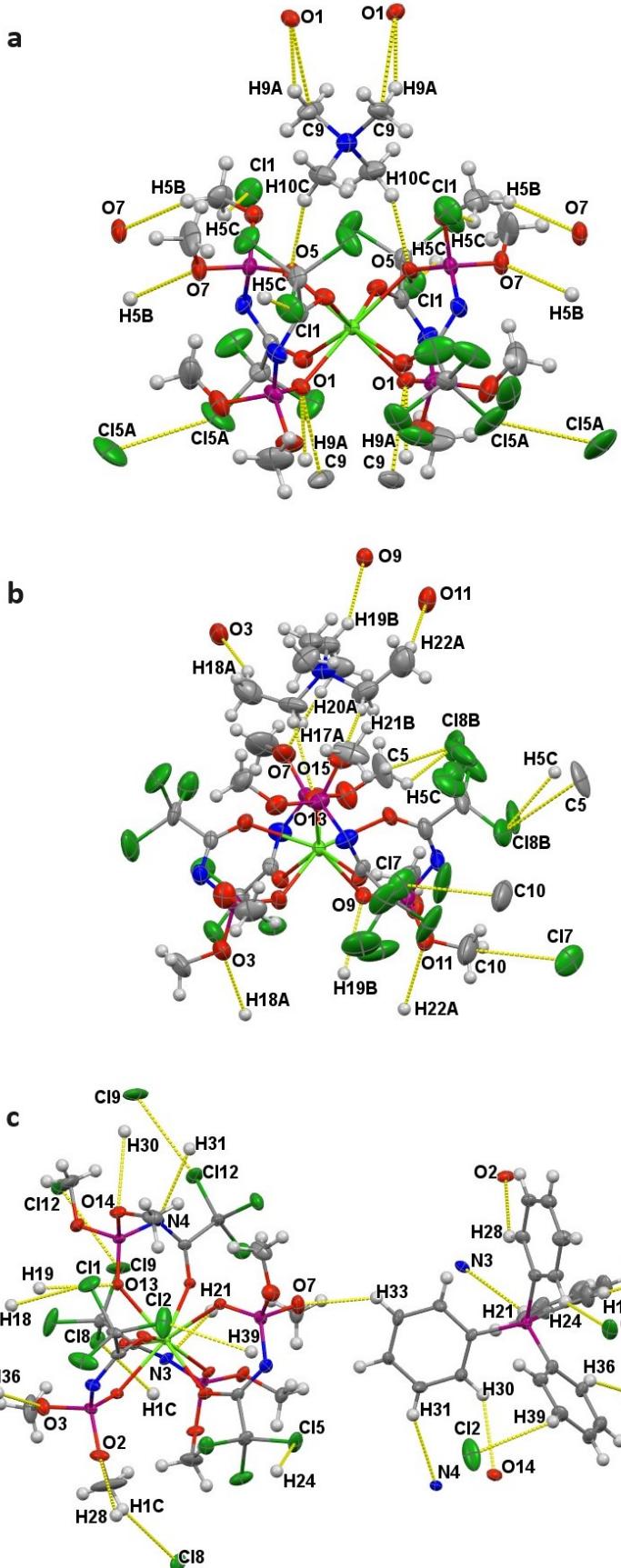


Figure S3. The inter- and intramolecular interactions in $\text{NMe}_4[\text{EuL}_4]$ (a), $\text{NEt}_4[\text{EuL}_4]$ (b), $\text{PPh}_4[\text{GdL}_4]$ (c).

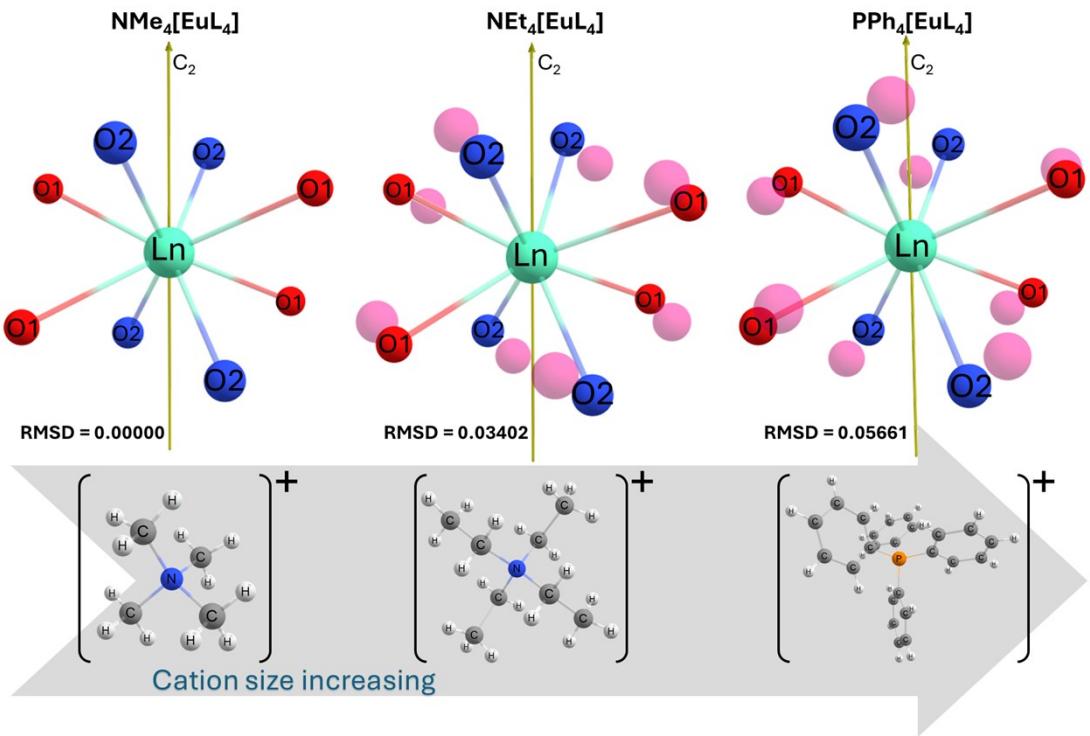


Figure S4. The effect of increasing cation size on the distortion of the coordination polyhedron of the studied compounds. The $\text{NM}_4[\text{EuL}_4]$ has an exact C_2 axis ($\text{RMSD} = 0.00000$), while the others deviate from the exact C_2 positions, represented by pink spheres. When the cation is changed to a larger one, the coordination polyhedron starts to distort, increasing the RMSD values, as illustrated. O1 stands for the oxygen atoms of the $\text{C}=\text{O}$ groups, while O2 stands for the oxygen atoms of the $\text{P}=\text{O}$ groups.

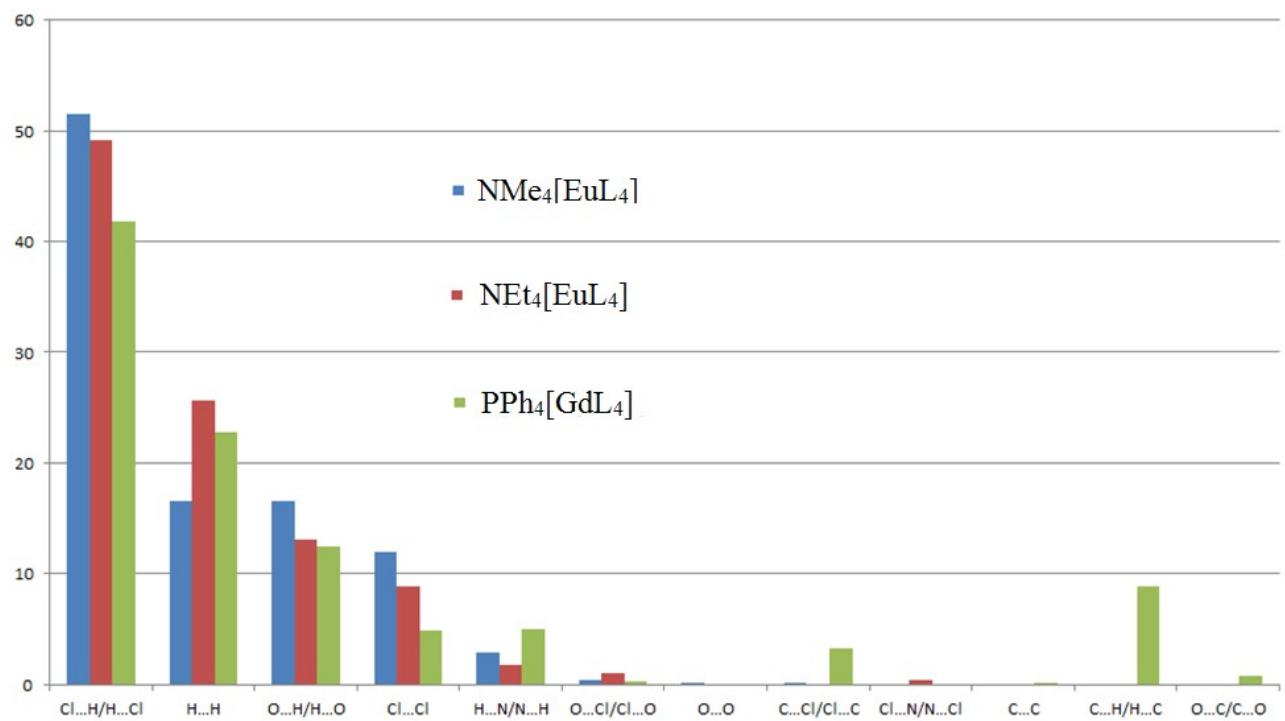


Figure S5. The relative contributions of various interactions into the total Hirshfeld surfaces for the obtained complexes (in %).

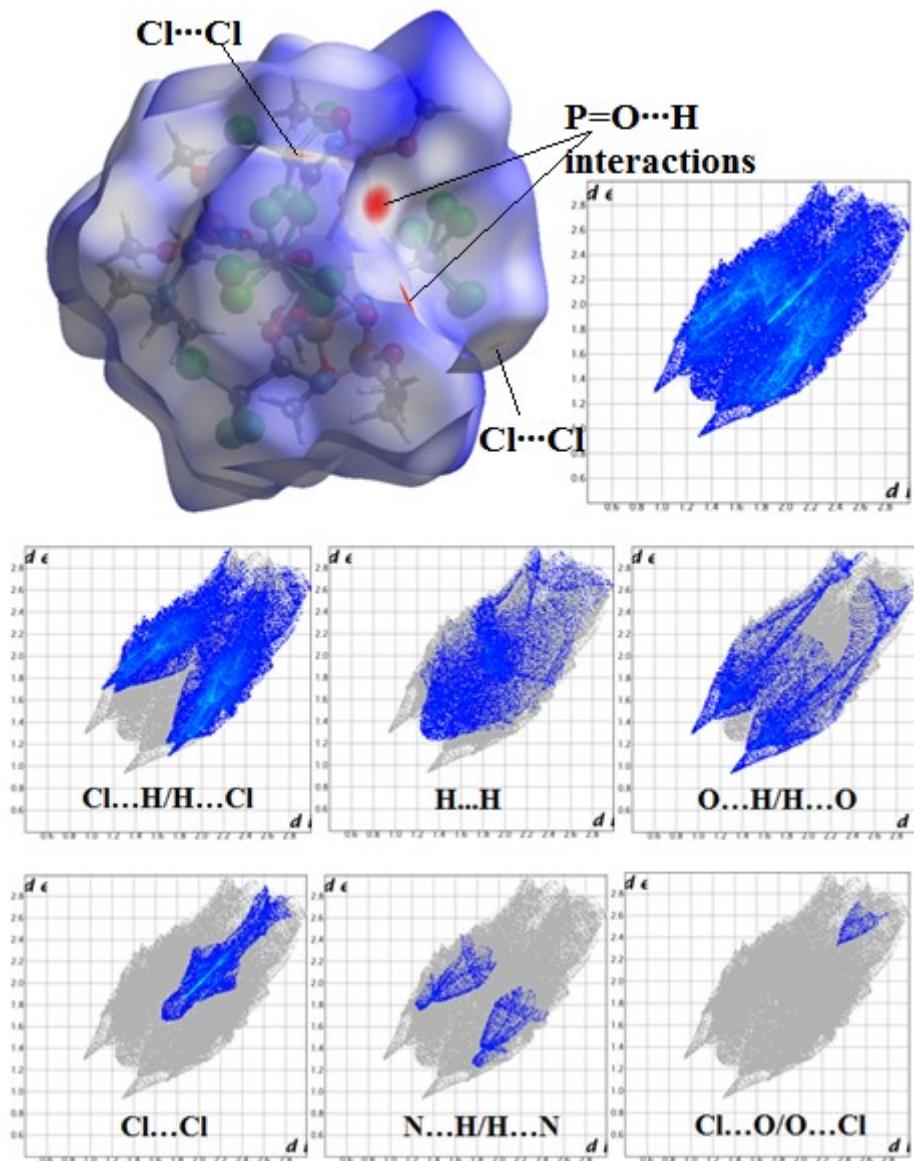


Figure S6. The Hirshfeld surface mapped over d_{norm} and two-dimensional fingerprint plots for the interactions with major contribution of $\text{Cl}\cdots\text{H}/\text{H}\cdots\text{Cl}$ (51.5%), $\text{H}\cdots\text{H}$ (16.5%), $\text{O}\cdots\text{H}/\text{H}\cdots\text{O}$ (16.5%), $\text{Cl}\cdots\text{Cl}$ (12.0%), $\text{H}\cdots\text{N}/\text{N}\cdots\text{H}$ (2.9%), and $\text{Cl}\cdots\text{O}/\text{O}\cdots\text{Cl}$ (0.4%) in $\text{NMe}_4[\text{EuL}_4]$.

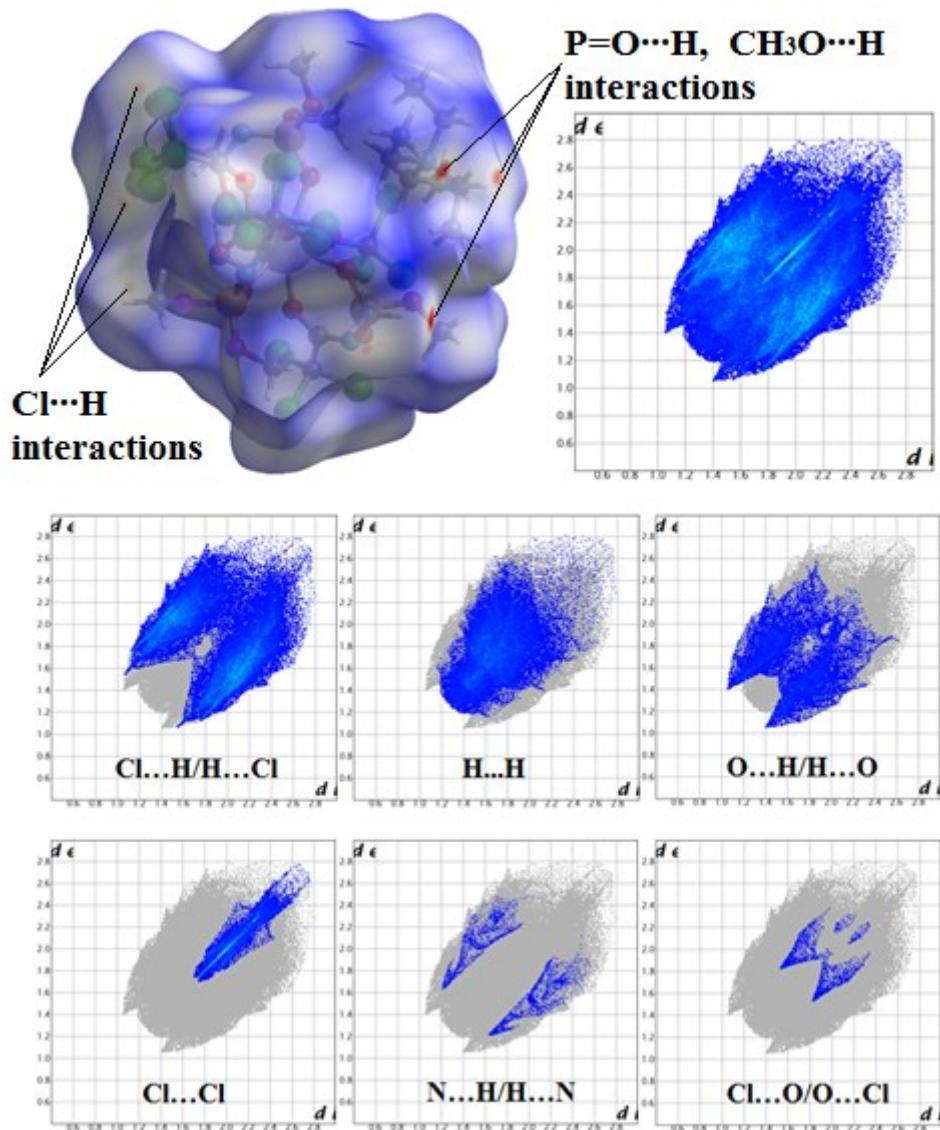


Figure S7. The Hirshfeld surface mapped over d_{norm} and two-dimensional fingerprint plots for the interactions with major contribution of Cl···H/H···Cl (49.1%), H···H (25.7%), O···H/H···O (13.1%), Cl···Cl (8.8%), H···N/N···H (1.7%), and Cl···O/O···Cl (1.0%) in NEt₄[EuL₄].

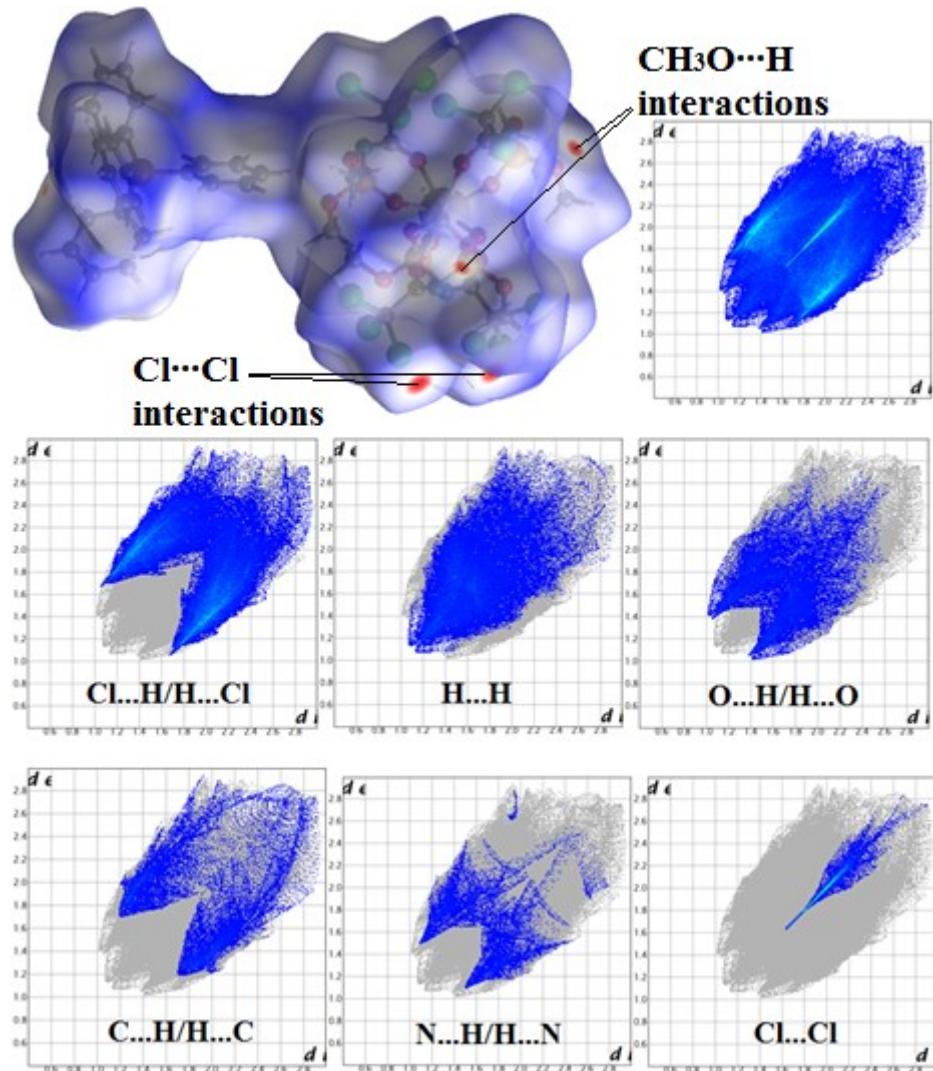


Figure S8. The Hirshfeld surface mapped over d_{norm} and two-dimensional fingerprint plots for the interactions with major contribution of Cl···H/H···Cl (41.8%), H···H (22.8%), O···H/H···O (12.5%), C···H/H···C (8.8%), H···N/N···H (5.0%), and Cl···Cl (4.9%) in PPh₄[GdL₄].

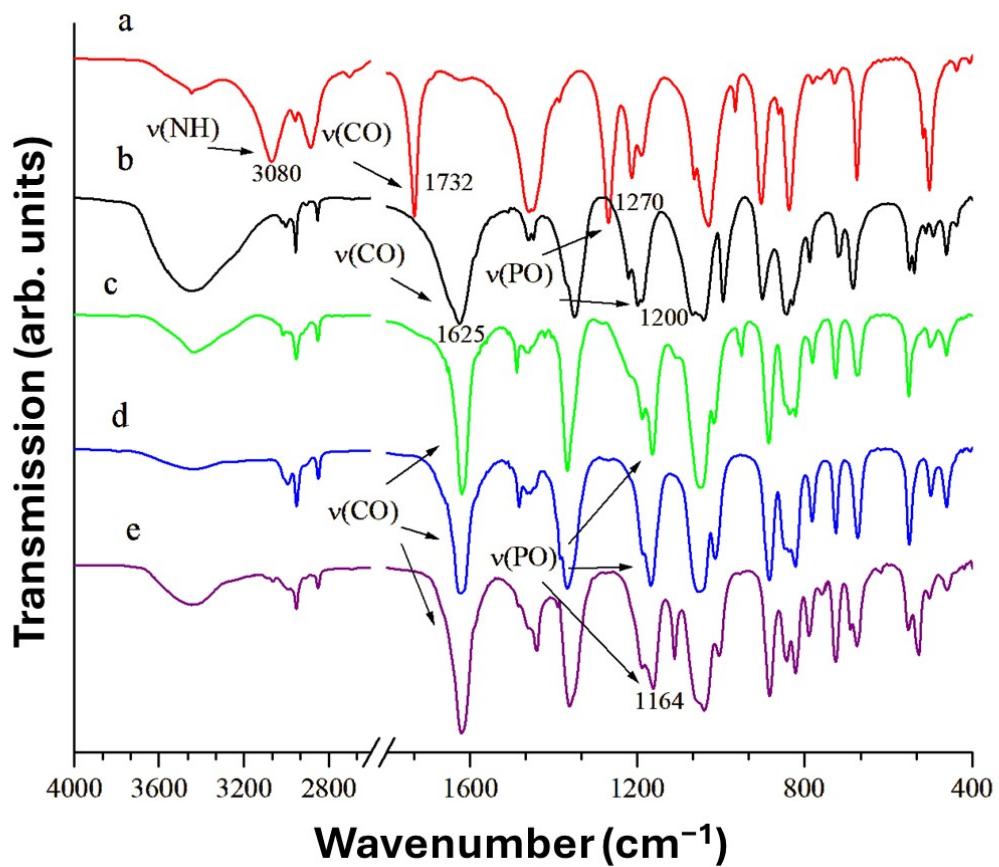


Figure S9. IR spectra for a) HL, b) NaL, c) NMe₄[GdL₄], d) NEt₄[GdL₄], and e) PPh₄[GdL₄].

References

- [1] B.R. Judd, Optical absorption intensities of rare-earth ions, *Phys. Rev.* 127 (1962) 750–761. <https://doi.org/10.1103/PhysRev.127.750>.
- [2] C.K. Jørgensen, B.R. Judd, Hypersensitive pseudoquadrupole transitions in lanthanides, *Mol. Phys.* 8 (1964) 281–290. <https://doi.org/10.1080/00268976400100321>.
- [3] G.S. Ofelt, Intensities of Crystal Spectra of Rare-Earth Ions, *J. Chem. Phys.* 37 (1962) 511–520. <https://doi.org/10.1063/1.1701366>.
- [4] S.F. Mason, R.D. Peacock, B. Stewart, Ligand-polarization contributions to the intensity of hypersensitive trivalent lanthanide transitions, *Mol. Phys.* 30 (1975) 1829–1841. <https://doi.org/10.1080/00268977500103321>.
- [5] B.G. Wybourne, *Spectroscopic Properties of Rare Earths*, John Wiley & Sons, New York, 1965.
- [6] G.F. de Sá, O.L. Malta, C. de Mello Donegá, A.M. Simas, R.L. Longo, P.A. Santa-Cruz, E.F. da Silva, Spectroscopic properties and design of highly luminescent lanthanide coordination complexes, *Coord. Chem. Rev.* 196 (2000) 165–195. [https://doi.org/10.1016/S0010-8545\(99\)00054-5](https://doi.org/10.1016/S0010-8545(99)00054-5).
- [7] R.T. Moura Jr., A.N. Carneiro Neto, R.L. Longo, O.L. Malta, On the calculation and interpretation of covalency in the intensity parameters of 4f-4f transitions in Eu³⁺ complexes based on the chemical bond overlap polarizability, *J. Lumin.* 170 (2016) 420–430. <https://doi.org/10.1016/j.jlumin.2015.08.016>.
- [8] R.T. Moura Jr., A.N. Carneiro Neto, E.C. Aguiar, C. V. Santos-Jr., E.M. de Lima, W.M. Faustino, E.E.S. Teotonio, H.F. Brito, M.C.F.C. Felinto, R.A.S. Ferreira, L.D. Carlos, R.L. Longo, O.L. Malta, (INVITED) JOYSpectra: A web platform for luminescence of lanthanides, *Opt. Mater. X* 11 (2021) 100080. <https://doi.org/10.1016/j.omx.2021.100080>.
- [9] O.L. Malta, H.J. Batista, L.D. Carlos, Overlap polarizability of a chemical bond: a scale of covalency and application to lanthanide compounds, *Chem. Phys.* 282 (2002) 21–30. [https://doi.org/10.1016/S0301-0104\(02\)00631-6](https://doi.org/10.1016/S0301-0104(02)00631-6).
- [10] R.T. Moura, O.L. Malta, R.L. Longo, The chemical bond overlap plasmon as a tool for quantifying covalency in solid state materials and its applications to spectroscopy, *Int. J. Quantum Chem.* 111 (2011) 1626–1638. <https://doi.org/10.1002/qua.22782>.
- [11] R.T. Moura Jr., G.C.S. Duarte, T.E. da Silva, O.L. Malta, R.L. Longo, Features of chemical bonds based on the overlap polarizabilities: diatomic and solid-state systems with the frozen-density embedding approach, *Phys. Chem. Chem. Phys.* 17 (2015) 7731–7742. <https://doi.org/10.1039/C4CP05283H>.
- [12] I.F. Costa, L. Blois, A.N. Carneiro Neto, E.E.S. Teotonio, H.F. Brito, L.D. Carlos, M.C.F.C. Felinto, R.T. Moura Jr., R.L. Longo, W.M. Faustino, O.L. Malta, Chapter 2 Reinterpreting the Judd–Ofelt parameters based on recent theoretical advances, in: M.G. Brik, A.M. Srivastava (Eds.), *Lumin. Mater.*, 1st ed., De Gruyter, 2023: pp. 19–62. <https://doi.org/10.1515/9783110607871-002>.

- [13] A.N. Carneiro Neto, R.T. Moura Jr., Overlap integrals and excitation energies calculations in trivalent lanthanides 4f orbitals in pairs Ln-L (L = Ln, N, O, F, P, S, Cl, Se, Br, and I), *Chem. Phys. Lett.* 757 (2020) 137884. <https://doi.org/10.1016/j.cplett.2020.137884>.