

**Supplementary Material**  
**for**  
**Carrier Transport in Bulk and Two-Dimensional**  
**Zn<sub>2</sub>(V, Nb, Ta)N<sub>3</sub> Ternary Nitrides**

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**Table S1.** The calculated elastic constants  $C_{ij}$  for bulk  $Zn_2(V, Nb, Ta)N_3$ .

Elastic constants	bulk $Zn_2VN_3$ , GPa	bulk $Zn_2NbN_3$ , GPa	bulk $Zn_2TaN_3$ , GPa
$C_{11}$	235	217	219
$C_{22}$	239	210	210
$C_{33}$	258	221	231
$C_{12}$	105	99	96
$C_{13}$	114	112	112
$C_{23}$	103	95	95
$C_{44}$	59	52	54
$C_{55}$	55	49	51
$C_{66}$	52	52	53

**Table S2.** The Young modulus for 2D  $Zn_2(V, Nb, Ta)N_3$ .

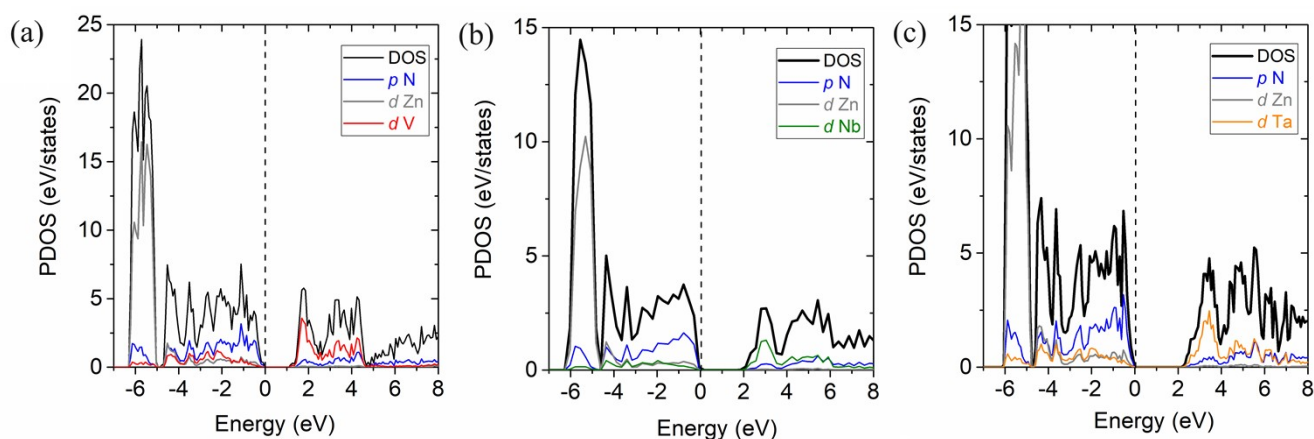
Material	$E_{xx}$ , N/m	$E_{yy}$ , N/m
bulk $Zn_2VN_3$	109	108
bulk $Zn_2NbN_3$	87	95
bulk $Zn_2TaN_3$	88	88

**Table S3.** Cohesive energy for bulk and 2D  $Zn_2(V, Nb, Ta)N_3$ .

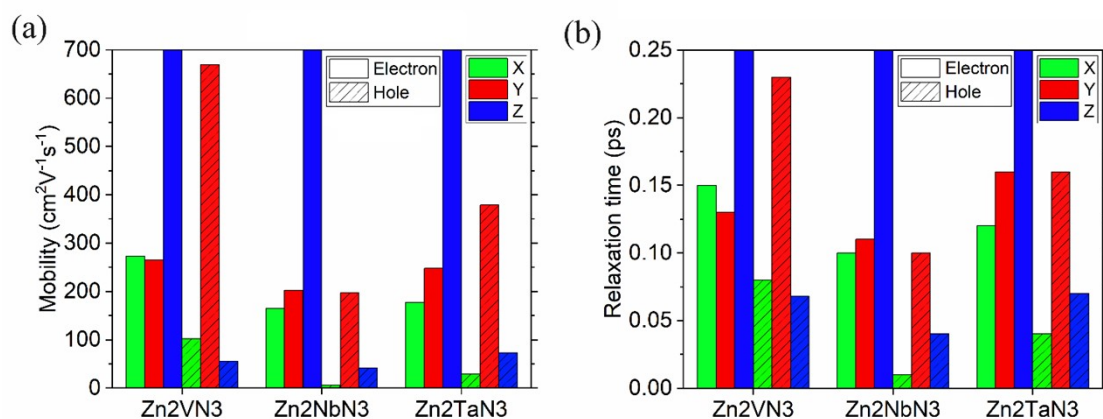
Structure	Cohesive energy, eV per atom
bulk $Zn_2VN_3$	-3.84
bulk $Zn_2NbN_3$	-4.11
bulk $Zn_2TaN_3$	-4.21
2D $Zn_2VN_3$	-3.60
2D $Zn_2NbN_3$	-3.82
2D $Zn_2TaN_3$	-3.91

**Table S4.** Calculated charge carrier effective mass ( $m_x^*$ ,  $m_y^*$  and  $m_z^*$  in units of electron mass  $m_0$ ), deformation potential ( $\delta_x$ ,  $\delta_y$ , and  $\delta_z$ , eV), mobility ( $\mu_x$ ,  $\mu_y$ , and  $\mu_z$ ,  $\text{cm}^2/\text{V}\cdot\text{s}$ ), and relaxation time ( $\tau_x$ ,  $\tau_y$  and  $\tau_z$ , ps) in bulk  $\text{Zn}_2(\text{V}, \text{Nb}, \text{Ta})\text{N}_3$  at  $T = 300$  K.

Material	Reciprocal coordinate	$m_x^*/m_0$	$m_y^*/m_0$	$m_z^*/m_0$	$\delta_x$	$\delta_y$	$\delta_z$	$\mu_x$	$\mu_y$	$\mu_z$	$\tau_x$	$\tau_y$	$\tau_z$
$\text{Zn}_2\text{VN}_3$	Electrons												
	(-0.500; 0.500; 0)	0.94	0.87	0.60	7.83	8.78	6.75	$2.73 \cdot 10^2$	$2.64 \cdot 10^2$	$1.26 \cdot 10^3$	0.15	0.13	0.43
$\text{Zn}_2\text{VN}_3$	Holes												
	(0.314; 0.314; 0)	1.38	0.59	2.15	7.93	8.99	6.49	$1.02 \cdot 10^2$	$6.69 \cdot 10^2$	$0.55 \cdot 10^2$	0.08	0.23	0.07
$\text{Zn}_2\text{NbN}_3$	Electrons												
	(-0.500; 0.500; 0)	1.03	0.94	0.40	8.62	8.59	7.81	$1.65 \cdot 10^2$	$2.02 \cdot 10^2$	$2.20 \cdot 10^3$	0.10	0.11	0.50
$\text{Zn}_2\text{NbN}_3$	Holes												
	(-0.346; 0.653; 0)	3.86	0.87	1.88	8.98	9.60	8.26	$0.06 \cdot 10^2$	$1.97 \cdot 10^2$	$0.40 \cdot 10^2$	0.01	0.10	0.04
$\text{Zn}_2\text{Ta}_3$	Electrons												
	(-0.500; 0.500; 0)	1.15	1.12	0.43	7.31	6.23	5.68	$1.77 \cdot 10^2$	$2.47 \cdot 10^2$	$3.68 \cdot 10^3$	0.12	0.16	0.89
$\text{Zn}_2\text{Ta}_3$	Holes												
	(-0.335; 0.664; 0)	2.24	0.75	1.69	7.83	8.37	7.23	$0.29 \cdot 10^2$	$3.78 \cdot 10^2$	$0.73 \cdot 10^2$	0.04	0.16	0.07



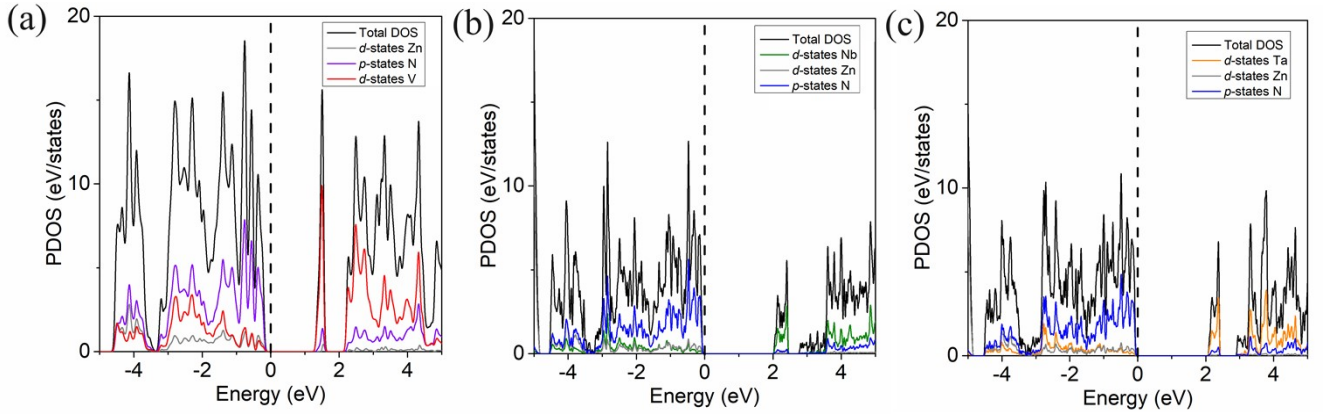
**Figure S1.** PDOS of bulk  $\text{Zn}_2\text{VN}_3$  (a),  $\text{Zn}_2\text{NbN}_3$  (b), and  $\text{Zn}_2\text{Ta}_3$  (c).



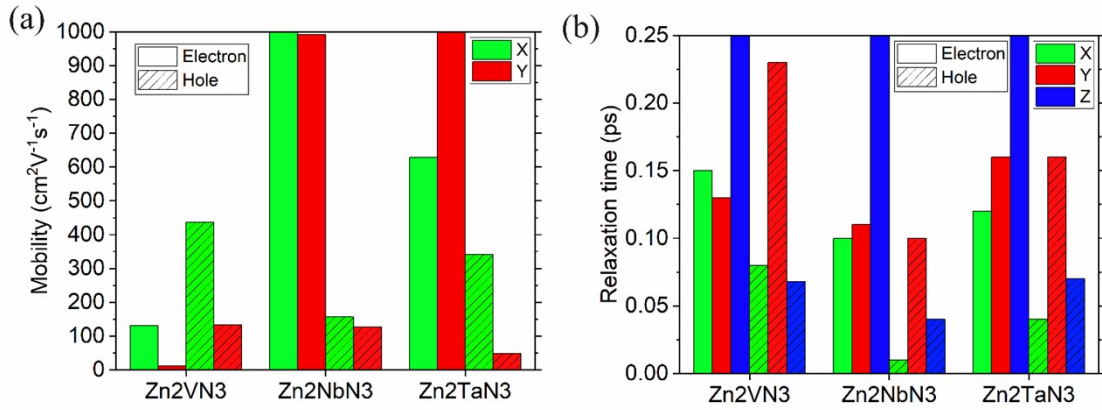
**Figure S2.** Magnified plots for charge mobility ( $\mu$ ) (a) and relaxation time ( $\tau$ ) (b) for holes and electrons in bulk  $\text{Zn}_2(\text{V}, \text{Nb}, \text{Ta})\text{N}_3$ .

**Table S5.** Calculated charge carrier effective mass ( $m_x^*$ ,  $m_y^*$  and  $m_z^*$  in units of electron mass  $m_0$ ), deformation potential ( $\delta_x$ ,  $\delta_y$ ,  $\delta_z$ , eV), mobility ( $\mu_x$ ,  $\mu_y$ , and  $\mu_z$ ,  $\text{cm}^2/\text{V}\cdot\text{s}$ ), and relaxation time ( $\tau_x$ ,  $\tau_y$  and  $\tau_z$ , ps) in 2D  $\text{Zn}_2(\text{V, Nb, Ta})\text{N}_3$  at  $T = 300$  K.

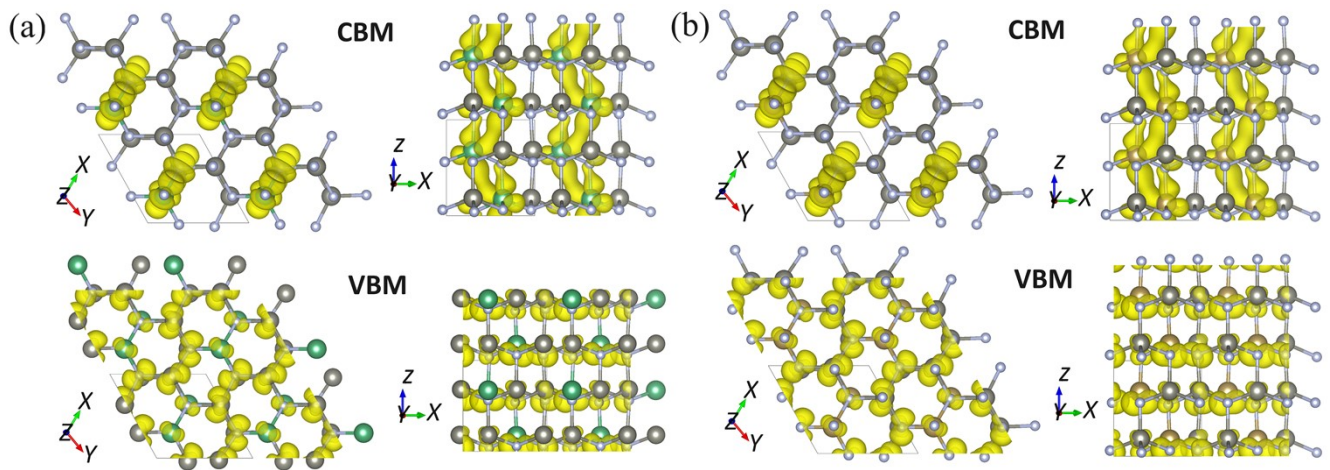
Material	Reciprocal coordinate	$m_x^*/m_0$	$m_y^*/m_0$	$\delta_x$	$\delta_y$	$\mu_x$	$\mu_y$	$\tau_x$	$\tau_y$
$\text{Zn}_2\text{VN}_3$	Electrons								
	(0; 0; 0)	2.15	4.07	1.67	4.00	$1.30 \cdot 10^2$	$0.12 \cdot 10^2$	0.16	0.03
	Holes								
	(-0.255; 0.255; 0)	2.55	2.31	-0.92	1.75	$0.44 \cdot 10^3$	$1.33 \cdot 10^2$	0.63	0.17
$\text{Zn}_2\text{NbN}_3$	Electrons								
	(-0.500; 0.500; 0)	1.01	2.15	0.27	0.80	$1.67 \cdot 10^4$	$0.99 \cdot 10^3$	9.60	1.21
	Holes								
	(-0.216; 0.216; 0)	2.06	1.63	1.78	2.31	$1.56 \cdot 10^2$	$1.27 \cdot 10^2$	0.18	0.12
$\text{Zn}_2\text{Ta}_3$	Electrons								
	(-0.500; 0.500; 0)	0.88	2.39	-1.53	0.57	$0.63 \cdot 10^3$	$1.67 \cdot 10^3$	0.31	2.27
	Holes								
	(-0.167; 0.167; 0)	2.16	2.95	1.00	2.30	$3.41 \cdot 10^2$	$0.47 \cdot 10^2$	0.42	0.08



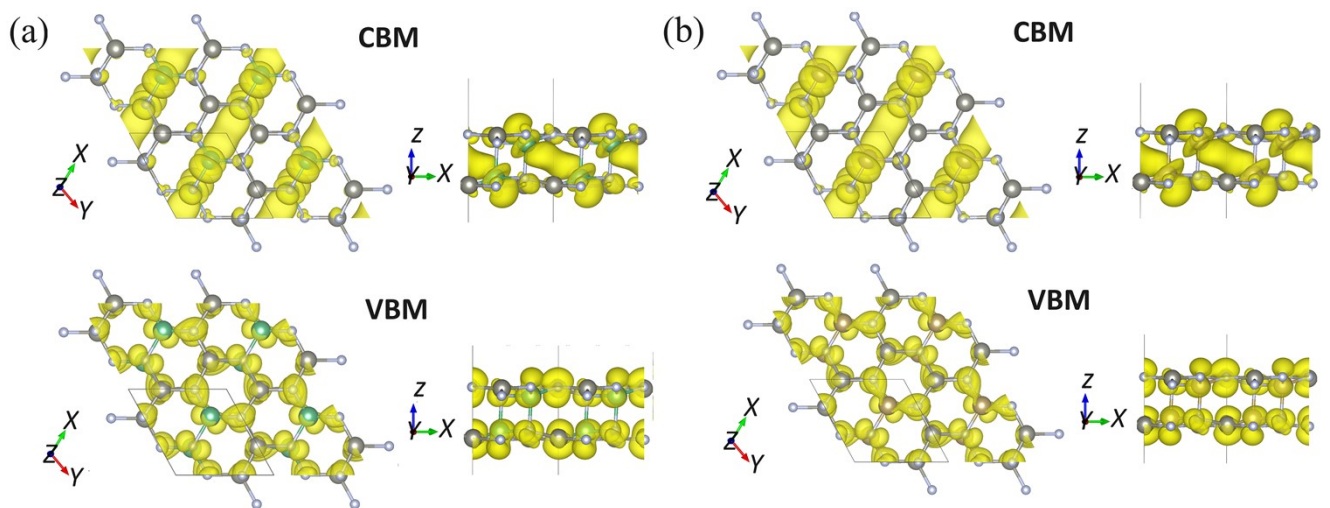
**Figure S3.** PDOS of 2D  $\text{Zn}_2\text{VN}_3$  (a), 2D  $\text{Zn}_2\text{NbN}_3$  (b), and 2D  $\text{Zn}_2\text{Ta}_3$  (c).



**Figure S4.** Magnified charge mobility ( $\mu$ ) (a) and relaxation time ( $\tau$ ) (b) for holes and electrons in 2D  $\text{Zn}_2(\text{V, Nb, Ta})\text{N}_3$ .



**Figure S5.** Top and side views of the spatial structure of wave functions in VBM and CBM for bulk  $\text{Zn}_2\text{NbN}_3$  (a) and  $\text{Zn}_2\text{TaN}_3$  (b) at the  $k$  points corresponding to VBM and CBM, respectively (Table S4). The isosurface of  $0.003 \text{ e } \text{\AA}^{-3}$  is adopted.



**Figure S6.** Top and side views of the spatial structure of wave functions in VBM and CBM for 2D  $\text{Zn}_2\text{NbN}_3$  (a) and 2D  $\text{Zn}_2\text{TaN}_3$  (b) at the  $k$  points corresponding to VBM and CBM, respectively (Table S5). The isosurface of  $0.003 \text{ e } \text{\AA}^{-3}$  is adopted.