Mechanism-Guided Descriptor for Hydrogen Evolution Reaction in 2D Ordered Double Transition-Metal Carbide MXenes

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Table S1. The thermodynamic competitors for 19 MAX phase candidates are selected from the Materials Project database, along with their calculated formation energies. Specially, the formation energy of the experimental synthetic $Mo_2Ti_2AlC_3$ is calculated to be 16.565 eV/atom.^{1, 2} Thus, formation energies less than 20 eV/atom at 0 K is regarded stable. Notably, reference 3 reported that $W_2Hf_2AlC_3$ is unstable based on formation energy calculations.^{3, 4} In contrast, our findings suggest that $W_2Hf_2SiC_3$ may be stable compared to competitors.

MAX	Competitors	E _{formation} (eV/atom)
Cr ₂ TiAlC ₂	TiAl, CrC	-0.494
Cr ₂ VAlC ₂	AlCr ₂ , VC, C	1.283
W ₂ TiAlC ₂	AlW ₂ C, TiC,	-0.500
Mo ₂ VAlC ₂	AlC, MoC, VMo	-3.007
Mo ₂ TiAlC ₂	TiAl, MoC	-1.873
Mo ₂ ZrAlC ₂	ZrMo, MoC, AlC	-3.689
Mo ₂ HfAlC ₂	HfMo, MoC, AlC	-3.831
Mo ₂ NbAlC ₂	NbMo, MoC, AlC	-2.586
Mo ₂ TaAlC ₂	TaMo, MoC, AlC	-2.709
Nb ₂ Hf ₂ AlC ₃	HfNb, AlC ₃	-14.383
Cr ₂ Ti ₂ AlC ₃	Ti ₂ AlC, CrC	-0.436
$Cr_2V_2AlC_3$	AlV ₂ C, CrC	0.625
$Cr_2Ta_2AlC_3$	Ta ₂ AlC, CrC	-0.282
W ₂ Ti ₂ AlC ₃	TiW, AlC ₃	-14.528
Mo ₂ Ti ₂ AlC ₃	TiMo, AlC ₃	16.565
Mo ₂ Zr ₂ AlC ₃	ZrMo, AlC ₃	3.954
Mo ₂ Hf ₂ AlC ₃	MoHf, AlC ₃	5.291
Mo ₂ Nb ₂ AlC ₃	NbMo, AlC ₃	-12.493

$Mo_2Ta_2AlC_3$	TaMo, AlC ₃	-12.819
$W_2Hf_2SiC_3$	HfW ₂ , HfSi,C	-19.921

Table S2. The energies of four unique configurations of O-terminated MXenes aftergeometric optimization.

MXenes	hcp-fcc	fcc-hcp	fcc-fcc	hcp-hcp
Cr ₂ TiC ₂ O ₂	-62.29316887	-62.58999530	-62.57806371	-62.79932329
$Cr_2VC_2O_2$	-62.91888139	-62.65982005	-62.99283369	-63.03072347
W ₂ TiC ₂ O ₂	-70.42501407	-70.42506373	-69.80046285	-71.12732904
$Mo_2VC_2O_2$	-67.22922395	-66.49722447	-65.88306397	-67.22988186
Mo ₂ TiC ₂ O ₂	-66.73865261	-66.73878875	-66.15475182	-67.35062443
$Mo_2ZrC_2O_2$	-66.85718421	-66.87978266	-66.24968109	-67.40379599
$Mo_2HfC_2O_2$	-68.43626310	-68.34209335	-67.92651424	-69.0124171
$Mo_2NbC_2O_2$	-67.60385938	-67.72733877	-67.37521414	-68.06066883
$Mo_2TaC_2O_2$	-69.45909649	-69.47304364	-68.94471227	-69.72906875
$Nb_2Hf_2C_3O_2$	-90.63782585	-90.64447992	-90.94965044	-90.27246643
$Cr_2Ti_2C_3O_2$	-81.15490772	-81.15458795	-81.28082960	-81.21016333
$Cr_2V_2C_3O_2$	-79.72878967	-79.72889020	-80.48541463	-79.20834079
$Cr_2Ta_2C_3O_2$	-87.76774479	-87.76765430	-88.36857801	-87.09969920
$W_2Ti_2C_3O_2$	-89.40253520	-89.40227667	-88.79891700	-90.05977445
Mo ₂ Ti ₂ C ₃ O ₂	-85.64097750	-85.64086701	-85.10330856	-86.25980388
$Mo_2Zr_2C_3O_2$	-86.56488878	-86.56494706	-86.23249742	-86.95799804
$Mo_2Hf_2C_3O_2$	-89.75590340	-89.75797703	-89.38242849	-90.17013688
$Mo_2Nb_2C_3O_2$	-88.05220668	-88.05227979	-87.78076802	-88.49641118
Mo ₂ Ta ₂ C ₃ O ₂	-92.18208384	-92.18213071	-91.95617650	-92.62988472

Bond	BDE (eV)	Bond	BDE (eV)
Cr-O	4.45	Nb-O	7.80
Mo-O	6.32	Ti-O	6.91
W-O	6.90	V-O	5.68
Hf-O	8.30		

Table S3. The value of bond dissociation enthalpies (BDE) in M-O.⁵

 Table S4. The lattice constant of MXenes.

MXene	a	b	c	alpha	beta	gamma
Mo ₂ Zr ₂ C ₃ O ₂	6.16	6.16	24.85	90.00	90.04	120.00
$Mo_2Hf_2C_3O_2$	6.12	6.12	30.98	90.00	90.00	120.00
Mo ₂ HfC ₂ O ₂	6.00	5.99	28.20	90.00	90.00	120.00
$Mo_2Nb_2C_3O_2$	6.01	6.01	24.92	90.00	90.02	120.00
Mo ₂ NbC ₂ O ₂	5.90	5.91	27.02	90.00	90.00	120.00
Mo ₂ Ta ₂ C ₃ O ₂	5.99	5.99	29.92	90.00	90.00	120.00
Mo ₂ TaC ₂ O ₂	5.90	5.90	28.20	90.00	90.00	120.00
$Mo_2Ti_2C_3O_2$	5.90	5.90	24.92	90.00	90.02	120.00
Mo ₂ TiC ₂ O ₂	5.85	5.85	27.88	90.00	90.00	120.00
Mo ₂ VC ₂ O ₂	5.78	5.78	29.10	90.00	90.00	120.00
$Mo_2ZrC_2O_2$	6.01	6.01	27.29	90.00	90.06	120.00
$Cr_2Ta_2C_3O_2$	6.12	6.12	29.62	90.00	90.00	120.00
$Cr_2Ti_2C_3O_2$	5.96	5.96	28.45	90.00	90.00	120.00
Cr ₂ TiC ₂ O ₂	5.61	5.61	26.99	90.00	90.00	120.00
$Cr_2V_2C_3O_2$	5.94	5.94	28.45	90.00	90.00	120.00
$Cr_2VC_2O_2$	5.52	5.52	28.95	90.05	90.00	120.00
$Nb_2Hf_2C_3O_2$	6.38	6.38	30.98	90.00	90.00	120.00
W ₂ Ti ₂ C ₃ O ₂	5.91	5.91	29.92	90.00	90.00	120.00

Table S5. The calculated for slab energy of $Cr_2TiC_2O_2$, energy of adsorbed H on $Cr_2TiC_2O_2$, and the corresponding ΔG_H in Vacuum, with implicit solvent effect and explicit solvent effect.

Cr ₂ TiC ₂ O ₂	Slab Energy (eV)	Slab-H Energy (eV)	Slab-H ΔG (eV)	$\Delta G_{\mathrm{H}^{*}}$ (eV)
Vacuum	-249.51	-253.63	0.22	-0.49
Implicit	-249.51	-254.16	0.30	-0.94
Explicit	-303.41	-307.97	0.30	-0.86

Table S6. The Gibbs free energy results are calculated in vacuum and solvent environment.

MXene	$\Delta G_{\rm H}$ (eV) (vacuum)	$\Delta G_{ m H}$ (ev) (implicit solvation)
Mo ₂ TiC ₂ O ₂	0.175	-0.388
$Mo_2VC_2O_2$	-0.028	-0.592
$Mo_2NbC_2O_2$	-0.054	-0.610
$Mo_2HfC_2O_2$	0.660	-0.678
$Mo_2Ta_2C_3O_2$	0.144	-0.527
$Mo_2Zr_2C_3O_2$	0.189	-0.376
$Mo_2Ti_2C_3O_2$	0.125	-0.500
$Mo_2Nb_2C_3O_2$	-0.004	-0.117
$Mo_2Hf_2C_3O_2$	0.358	-0.155
$Ti_2MnC_2O_2$	-0.10	-0.590
$Ti_2TaC_2O_2$	-0.189	-0.492
$Ti_2Nb_2C_3O_2$	-0.079	-0.478
W ₂ TiC ₂ O ₂	0.525	-0.482
$W_2ZrC_2O_2$	0.766	0.237
$W_2Zr_2C_3O_2$	0.503	-0.070

$W_2Hf_2C_3O_2$	0.584	-0.033
$Nb_2Ta_2C_3O_2$	0.152	-0.333



Fig. S1 The convergence tests of k-point mesh and energy cutoff for the computational accuracy on single or supercell MXenes. (a) The energy convergence tests of k-point mesh from $9\times9\times1$ to $13\times13\times1$ are performed to test the calculation accuracy on single cell, take Mo₂Nb₂C₃O₂ as example. (b)-(c) Energy convergence and computational cost (CPU time) tests are systematically conducted by varying the k-point mesh from $3\times3\times1$ to $8\times8\times1$ in a $2\times2\times1$ supercell, respectively. Two representative systems are selected: Cr₂Ta₂C₃O₂ (top panel) and Mo₂ZrC₂O₂ (bottom panel), as shown in the respective panels. (d)-(e) Energy convergence and computational cost (CPU time) tests are systematically conducted by varying energy cutoff from 440 to 540 in a $2\times2\times1$ supercell, respectively. Four representative systems are selected: Cr₂TiC₂O₂ (upper-left



panel), $Mo_2TiC_2O_2$ (upper-right panel), $Ti_2Ta_2C_3O_2$ (bottom-left panel) and $W_2Ti_2C_3O_2$ (bottom- right panel) as shown in the respective panels.



 $W_2Ti_2C_3O_2$

Fig. S2 Calculated band structures of 19 transition ordered double MXenes.



Fig. S3 Relationships between $\Delta G_{\rm H}$ and descriptors of d-band center of the first-layer transition metal among different MXenes system.



Fig. S4 The projected crystal orbital Hamilton population (pCOHP) of H-O bond when H adsorption on $Mo_2Ti_2C_3O_2$ as example.



Fig. S5 The projected density of states (pDOS) and pCOHP with H adsorption on $Mo_2Ti_2C_3O_2$ as example.





Fig. S6 The diagram of pCOHP plots of H-O, $H(1s)-O(p_z)$, O(p)-M'(d) and $O(p_y)-M'(d)$ $d_{x^2-y^2}$ for MXenes, including Cr₂TiC₂O₂, W₂TiC₂O₂, Ti₂NbC₂O₂, Mo₂VC₂O₂, Nb₂Hf₂C₃O₂, and V₂Ta₂C₃O₂, respectively.



Fig. S7 Regulation between $\Delta G_{\rm H}$ and electronegativity of the inner transition metal, and $\Delta G_{\rm H}$ with the number of inner transition layers. a) The electronegativity values of elements in the third to sixth period and groups IVB-VIB, corresponding to the transition metals in M₂MC₂O₂ and M₂M₂C₃O₂, are illustrated. b-c) The overall trend of calculated $\Delta G_{\rm H}$ decreases with increasing electronegativity of the inner transition metal based on Mo-based M₂MC₂O₂ and M₂M₂C₃O₂, respectively. Only a few materials, such as Mo₂TaC₂O₂ and Mo₂Ta₂C₃O₂, deviate from this trend. Additionally, the overall trend of calculated $\Delta G_{\rm H}$ decreases with the increased number of inner transition layers, exception for Mo₂Ta₂C₃O₂.



Fig. S8 Relationships between $\Delta G_{\rm H}$ and descriptor δ of M'₂M"N₂O₂ system.



Fig. S9 The configuration of $Cr_2TiC_2O_2$ with explicit solvation by using four H₂O molecules.



Fig. S10 a-c) Phonopy spectrum of $Mo_2Hf_2C_3O_2$, $W_2Hf_2C_3O_2$ and $W_2Zr_2C_3O_2$, respectively. d-f) Ab initio molecular dynamic of $Mo_2Hf_2C_3O_2$, $W_2Hf_2C_3O_2$ and $W_2Zr_2C_3O_2$, respectively.

Equation S1. Pauli electronegativity formula as follows,^{6,7}

$$|x_A - x_B| = eV^{-1/2} \sqrt{E_d(AB) - \frac{E_d(AA) + E_d(BB)}{2}}$$

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