

Breaking Scaling Relations and Boosting Ammonia Synthesis in Nitrogen Reduction with V-Containing Heteronuclear Double Metal Atoms

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Supporting Information

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Note S1 Calculations of formation energy (E_f) and the dissolution potential (U_{diss}) for V-TM@GDY.

The thermodynamic stability and electrochemical stability were evaluated by the formation energy (E_f) and the dissolution potential (U_{diss}), defined as:¹

$$E_f = E(\text{total}) - E(\text{GDY}) - E(\text{V-bulk}) - E(\text{TM-bulk})$$

$$U_{\text{diss}} = U^0 - E_f/n e$$

Where $E(\text{total})$ and $E(\text{GDY})$ are the total energies of GDY with and without the V-TM pairs, respectively, and $E(\text{V-bulk})$ and $E(\text{TM-bulk})$ are the energies of the V and TM atoms in their bulk, respectively. U^0 denotes the standard dissolution potential of bulk TM, and n is the number of electrons involved in the dissolution. The values of U^0 and n comes from the previous literature.¹

Note S2 Calculations of binding energy (E_b) between the V-TM pairs and GDY

The binding energy (E_b) was calculated to estimate the binding ability, which is defined as:

$$E_b = E(\text{total}) - E(\text{GDY}) - E(\text{V-atom}) - E(\text{TM-atom})$$

Here, $E(\text{total})$ and $E(\text{GDY})$ represent the total energies of the GDY monolayer with and without the anchored atoms, respectively. $E(\text{V-atom})$ and $E(\text{TM-atom})$ are the energies of the V and TM atoms in vacuum, respectively. The more negative E_b represents a larger binding strength.

Note S3 Calculations of the adsorption free energy for the absorbates.

The adsorption free energy, $\Delta G(X)$, was calculated using the equation:

$$\Delta G(X) = G(\text{sub}+X) - G(\text{sub}) - G(X)$$

where $G(\text{sub}+X)$ and $G(\text{sub})$ are the free energies of the systems with and without the adsorbate, respectively, and $G(X)$ is the free energy of the X molecule in vacuum.

Note S4 Calculations of theoretical Faradaic efficiency (FE)

HER is a major competing reaction to NRR. The catalytic selectivity based on theoretical FE can be estimated using the Boltzmann distribution² and is calculated using the following formula:³⁻⁴

$$FE = \frac{1}{1 + e^{-\frac{\delta G}{k_B T}}} \times 100\%$$

where δG represents the difference in Gibbs free energy change of the PDS between HER and NRR, k_B is the Boltzmann constant, and $T = 298.15$ K. This formula is based on two assumptions: (1) only HER and NRR are considered as competing side reactions, and (2) proton and electron transfer are not the rate-determining steps for either HER or NRR.

Table S1 Zero-point energy corrections (ΔE_{ZPE} , eV), and entropic contributions (at 298.15 K) to the free energies ($T\Delta S$, eV). The values for the free molecules were obtained from Ref. 5.

| Species | ΔE_{ZPE} (eV) | $T\Delta S$ (eV) |
|---------------|-----------------------|------------------|
| N_2 | 0.15 | 0.58 |
| $*N-*N$ | 0.21 | 0.09 |
| $*N-*NH$ | 0.52 | 0.09 |
| $*N-*NH_2$ | 0.86 | 0.11 |
| $*NH-*NH$ | 0.81 | 0.12 |
| $*NH-*NH_2$ | 1.15 | 0.15 |
| $*NH_2-*NH_2$ | 1.51 | 0.16 |
| $*N$ | 0.09 | 0.04 |
| $*NH$ | 0.36 | 0.07 |
| $*NH_2$ | 0.69 | 0.08 |
| $*NH_3$ | 1.03 | 0.15 |
| NH_3 | 0.89 | 0.60 |
| H_2O | 0.56 | 0.67 |
| $*H_2O$ | 0.66 | 0.14 |
| $*H$ | 0.16 | 0.02 |

Table S2 Binding energy (E_b , eV), formation energy (E_f , eV), dissolution potential (U_{diss} , V), bond length between V and the TM (d_{V-TM} , Å), number of transferred electrons to V (Q_V , e) and TM (Q_{TM} , e) for V-TM@GDY, and d band center of V ($\varepsilon_d(V)$, eV) and TM ($\varepsilon_d(TM)$, eV) atoms.

| System | E_b | E_f | U_{diss} | d_{V-TM} | Q_V | Q_{TM} | $\varepsilon_d(V)$ | $\varepsilon_d(TM)$ |
|--------|-------|-------|------------|------------|-------|----------|--------------------|---------------------|
| V-Sc | -8.98 | 1.62 | -1.95 | 2.68 | -0.89 | -1.39 | -0.01 | 0.47 |
| V-Ti | -9.11 | 2.90 | -2.13 | 2.70 | -0.90 | -1.17 | -0.01 | -0.02 |
| V-V | -7.99 | 3.78 | -2.12 | 2.64 | -0.95 | -0.95 | -0.21 | -0.22 |
| V-Cr | -6.62 | 3.68 | -1.96 | 2.57 | -0.96 | -0.83 | -0.24 | -0.20 |
| V-Mn | -6.78 | 3.14 | -1.97 | 2.59 | -0.97 | -0.68 | -0.26 | -0.86 |
| V-Fe | -8.09 | 3.22 | -1.62 | 2.35 | -0.99 | -0.45 | -0.30 | -1.42 |
| V-Co | -8.45 | 3.08 | -1.50 | 2.34 | -1.02 | -0.25 | -0.23 | -1.32 |
| V-Ni | -8.12 | 2.94 | -1.45 | 2.41 | -1.00 | -0.23 | -0.20 | -1.98 |
| V-Cu | -3.84 | 3.86 | -1.39 | 2.60 | -0.97 | -0.30 | 0.02 | -3.33 |

Table S3 N₂ adsorption free energy ($\Delta G(N_2)$, eV), N-N bond length (d_{N-N} , Å), number of transferred electrons to N₂ ($\Delta Q(N_2)$, e), N-N ICOHP for the adsorbed N₂ molecules (ICOHP(N₂)), potential-determining step (PDS), and limiting potential (U_L(NH₃), in V) for NRR on V-TM@GDY.

| System | $\Delta G(N_2)$ | d_{N-N} | $\Delta Q(N_2)$ | ICOHP(N ₂) | PDS | U _L (NH ₃) |
|-----------|-----------------|-----------|-----------------|------------------------|---------------------------------------|-----------------------------------|
| V-Sc-side | -0.88 | 1.20 | 0.77 | -9.27 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.99 |
| V-Ti-side | -1.32 | 1.21 | 0.76 | -9.01 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.87 |
| V-V-side | -1.34 | 1.23 | 0.85 | -8.46 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.74 |
| V-Cr-side | -1.00 | 1.21 | 0.74 | -9.18 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.36 |
| V-Mn-side | -0.62 | 1.18 | 0.61 | -9.81 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.41 |
| V-Fe-side | -0.69 | 1.19 | 0.59 | -9.73 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.42 |
| V-Co-side | -0.63 | 1.18 | 0.59 | -9.70 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.63 |
| V-Ni-side | -0.36 | 1.17 | 0.52 | -10.02 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.71 |
| V-Cu-side | -0.40 | 1.19 | 0.62 | -9.52 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.42 |
| V-Cr-end | -0.16 | 1.13 | 0.25 | -11.09 | / | / |
| V-Mn-end | -0.26 | 1.14 | 0.36 | -10.71 | / | / |
| V-Fe-end | -0.66 | 1.14 | 0.37 | -10.63 | $*NN + H^+ + e^- \rightarrow *NNH$ | -0.50 |
| V-Co-end | -0.67 | 1.14 | 0.35 | -10.62 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.63 |
| V-Ni-end | -0.41 | 1.15 | 0.38 | -10.35 | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.71 |
| V-Cu-end | -0.59 | 1.14 | 0.26 | -10.98 | $*NN + H^+ + e^- \rightarrow *NNH$ | -0.53 |

Table S4 Adsorption free energy of NH₂ ($\Delta G(\text{NH}_2)$, eV), NH₃ ($\Delta G(\text{NH}_3)$, eV), H ($\Delta G(\text{H})$, eV), and H₂O ($\Delta G(\text{H}_2\text{O})$, eV), desorption energy of NH₃ ($\Delta G_{\text{des}}(\text{NH}_3)$, eV), and Faradaic efficiency (FE) of NRR.

| System | $\Delta G(\text{NH}_2)$ | $\Delta G(\text{NH}_3)$ | $\Delta G_{\text{des}}(\text{NH}_3)$ | $\Delta G(\text{H})$ | FE | $\Delta G(\text{H}_2\text{O})$ |
|--------|-------------------------|-------------------------|--------------------------------------|----------------------|--------|--------------------------------|
| V-Sc | -2.51 | -1.52 | 0.79 | -0.54 | 0% | -0.48 |
| V-Ti | -2.63 | -1.76 | 1.03 | -0.61 | 0% | -0.57 |
| V-V | -2.67 | -1.93 | 1.20 | -0.19 | 0% | -0.73 |
| V-Cr | -2.25 | -1.88 | 1.15 | -0.76 | 100% | -0.59 |
| V-Mn | -2.34 | -1.93 | 1.20 | -0.68 | 100% | -0.40 |
| V-Fe | -2.24 | -1.82 | 1.08 | -0.67 | 99.99% | -0.60 |
| V-Co | -2.36 | -1.73 | 0.99 | -0.79 | 99.81% | -0.68 |
| V-Ni | -2.46 | -1.75 | 1.02 | -0.86 | 99.72% | -0.56 |
| V-Cu | -2.43 | -2.01 | 1.28 | -1.01 | 100% | -0.61 |

Table S5 Number of electrons transferred to V-Cr ($Q(V\text{-Cr})$, e), V-Fe ($Q(V\text{-Fe})$, e), N_xH_y ($Q(N_xH_y)$, e), and GDY ($Q(GDY)$, e) during the NRR processes on V-Cr@GDY and V-Fe@GDY, respectively.

| V-Cr | $Q(V\text{-Cr})$ | $Q(N_xH_y)$ | $Q(GDY)$ | V-Fe | $Q(V\text{-Fe})$ | $Q(N_xH_y)$ | $Q(GDY)$ |
|----------------------|------------------|-------------|----------|----------------------|------------------|-------------|----------|
| *+N ₂ | -1.79 | 0.00 | 1.79 | *+N ₂ | -1.46 | 0.00 | 1.46 |
| *N-*N | -2.28 | 0.74 | 1.55 | *N-*N | -1.88 | 0.58 | 1.29 |
| *N-*NH | -2.36 | 0.77 | 1.59 | *N-*NH | -2.01 | 0.70 | 1.31 |
| *NH-*NH | -2.29 | 0.70 | 1.59 | *NH-*NH | -2.05 | 0.59 | 1.46 |
| *NH-*NH ₂ | -2.20 | 0.34 | 1.86 | *NH-*NH ₂ | -1.93 | 0.28 | 1.65 |
| *NH | -2.32 | 0.78 | 1.54 | *NH | -1.92 | 0.69 | 1.23 |
| *NH ₂ | -2.17 | 0.42 | 1.76 | *NH ₂ | -1.83 | 0.39 | 1.45 |
| *NH ₃ | -1.97 | -0.15 | 2.12 | *NH ₃ | -1.62 | -0.15 | 1.77 |

Table S6 The potential-determining step (PDS) and limiting potential ($U_L(NH_3)$, in V) for V-TM@GDY in our work, compared with those for TM@GDY from reference⁶.

| System | PDS | $U_L(NH_3)$ | system | PDS | $U_L(NH_3)$ |
|--------|---------------------------------------|-------------|--------|-------------------------------------|-------------|
| V-Sc | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.99 | Sc@GDY | $*N_2 + H^+ + e^- \rightarrow *NNH$ | -1.41 |
| V-Ti | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.87 | Ti@GDY | $*N_2 + H^+ + e^- \rightarrow *NNH$ | -0.87 |
| V-V | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.74 | V@GDY | $*N_2 + H^+ + e^- \rightarrow *NNH$ | -0.67 |
| V-Cr | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.36 | Cr@GDY | --- | --- |
| V-Mn | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.41 | Mn@GDY | $*N_2 + H^+ + e^- \rightarrow *NNH$ | -1.00 |
| V-Fe | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.42 | Fe@GDY | $*N_2 + H^+ + e^- \rightarrow *NNH$ | -0.74 |
| V-Co | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.63 | Co@GDY | $*N_2 + H^+ + e^- \rightarrow *NNH$ | -0.78 |
| V-Ni | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.71 | Ni@GDY | $*N_2 + H^+ + e^- \rightarrow *NNH$ | -1.75 |
| V-Cu | $*NH_2 + H^+ + e^- \rightarrow *NH_3$ | -0.42 | Cu@GDY | $*N_2 + H^+ + e^- \rightarrow *NNH$ | -1.69 |

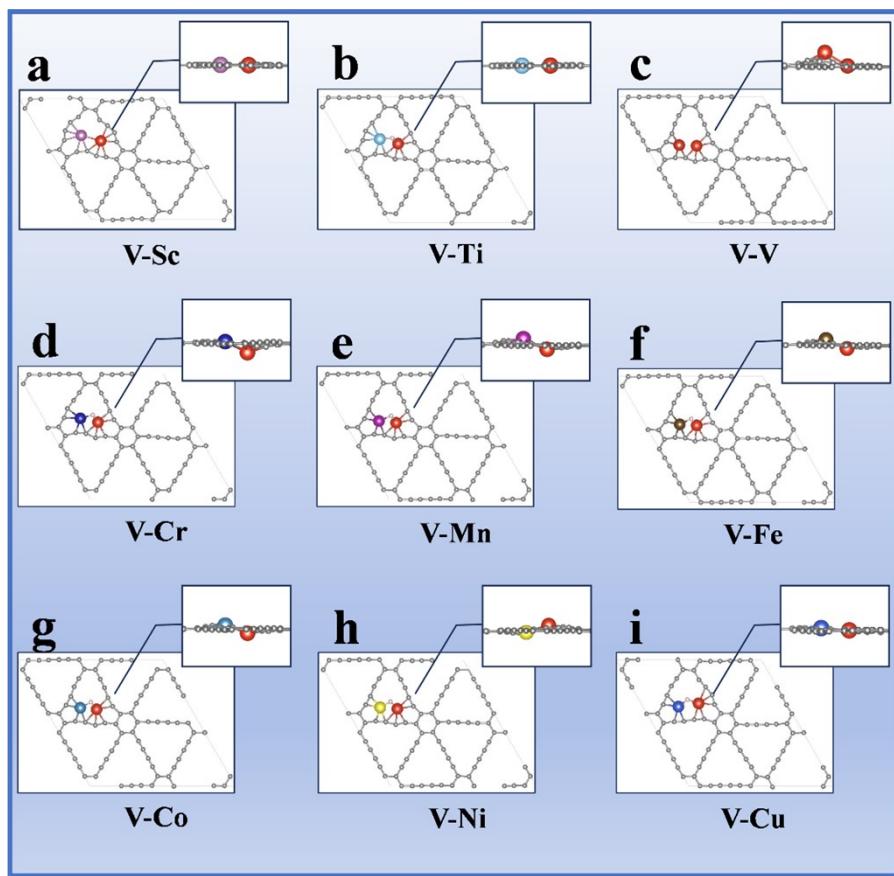
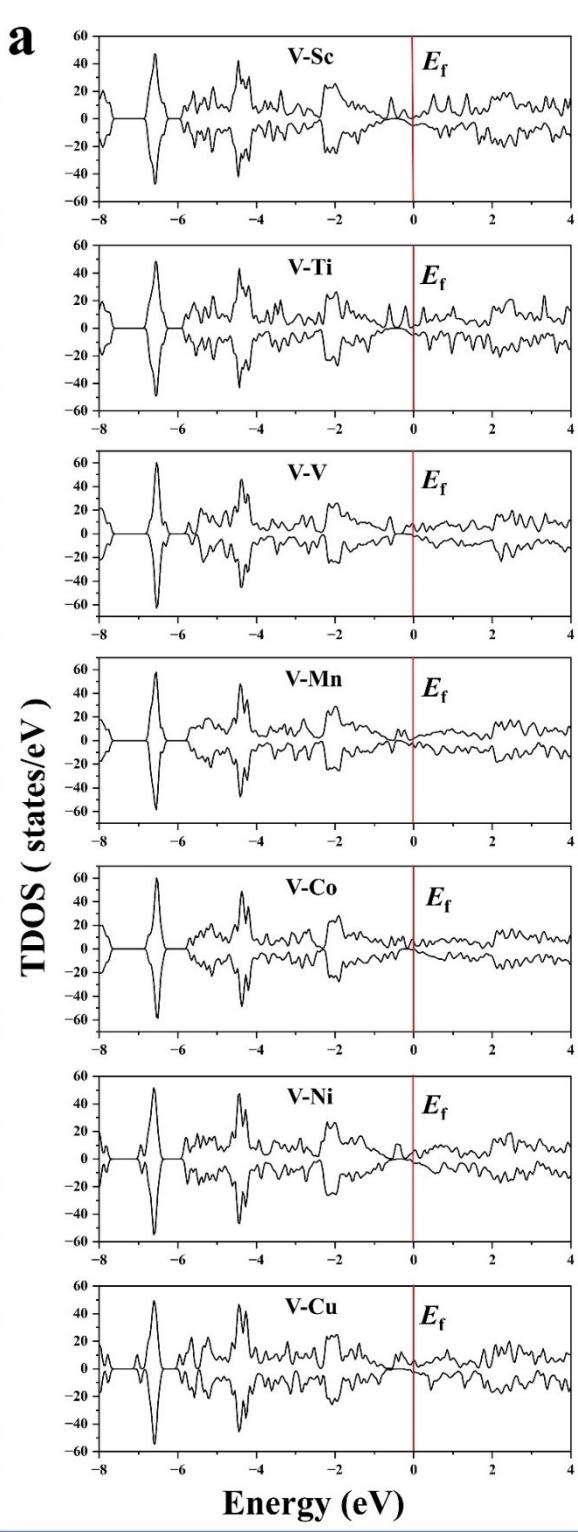


Fig. S1 Optimized structures of V-Sc@GDY (a), V-Ti@GDY (b), V-V@GDY (c), V-Cr@GDY (d), V-Mn@GDY (e), V-Fe@GDY (f), V-Co@GDY (g), V-Ni@GDY (h), and V-Cu@GDY (i).



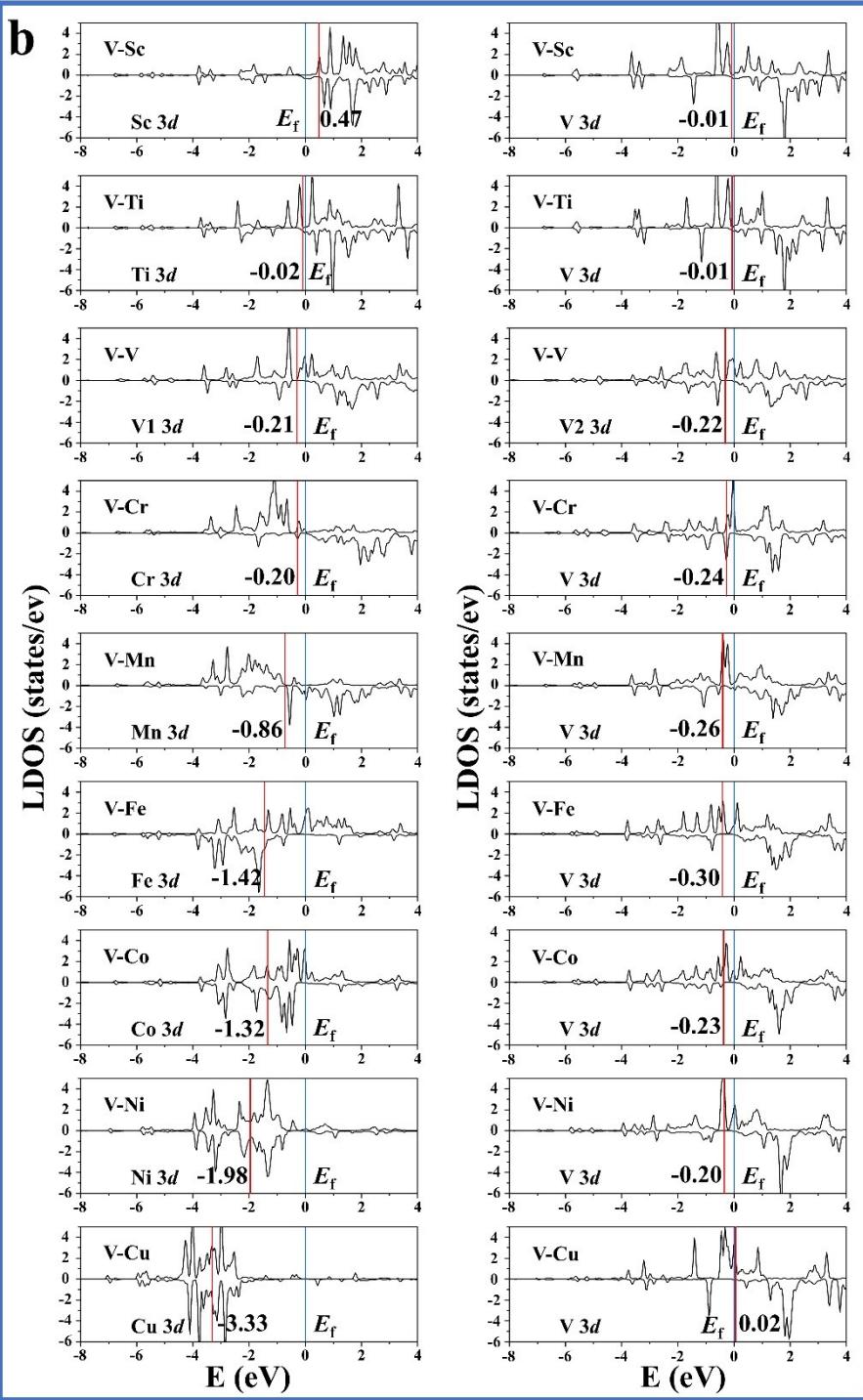


Fig. S2 The TDOS (a) and LDOS (b) for the V-TM@GDY (TM = Sc ~ Cu).

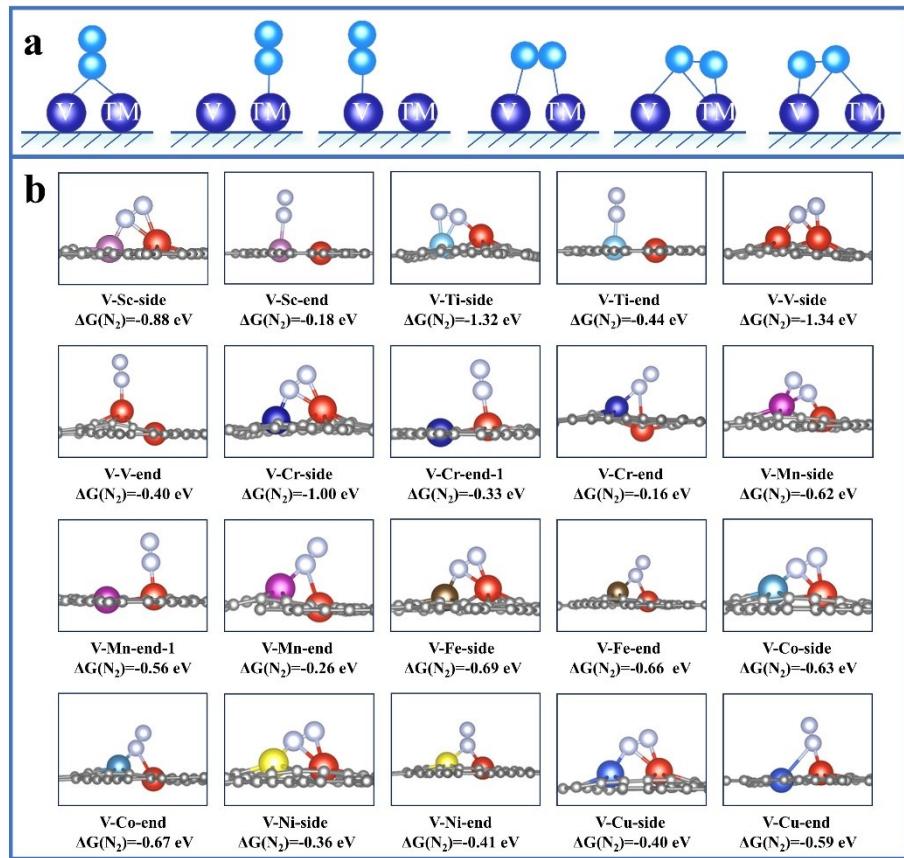


Fig. S3 The considered N₂ adsorption configuration (a), and most stable N₂ side-on and end-on configurations on V-TM@GDY (Sc = Sc to V).

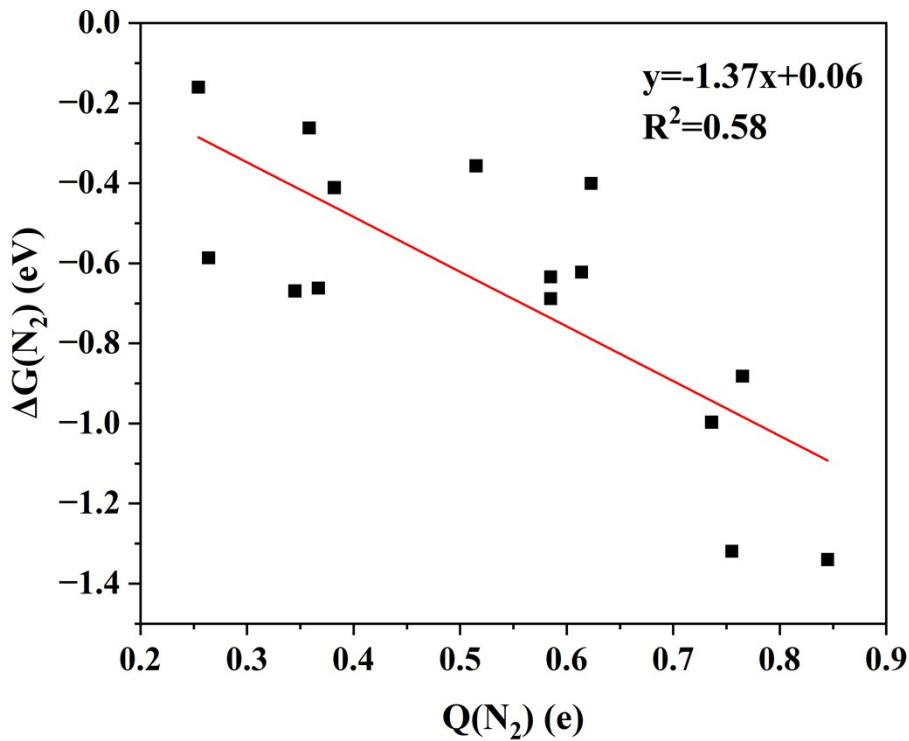


Fig. S4 The N_2 adsorption free energy ($\Delta G(N_2)$) versus the corresponding number of transferred electrons on N_2 ($Q(N_2)$). A positive $Q(N_2)$ value indicates that the N_2 molecules have gained electrons.

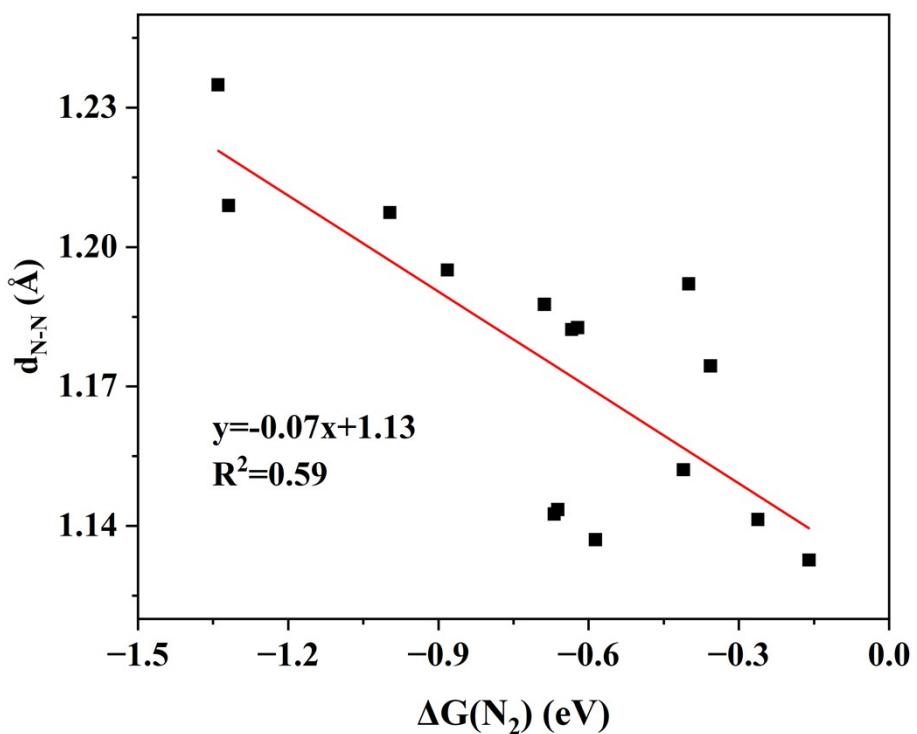


Fig. S5 The N-N bond length (d_{N-N}) versus the corresponding N_2 adsorption free energy ($\Delta G(N_2)$).

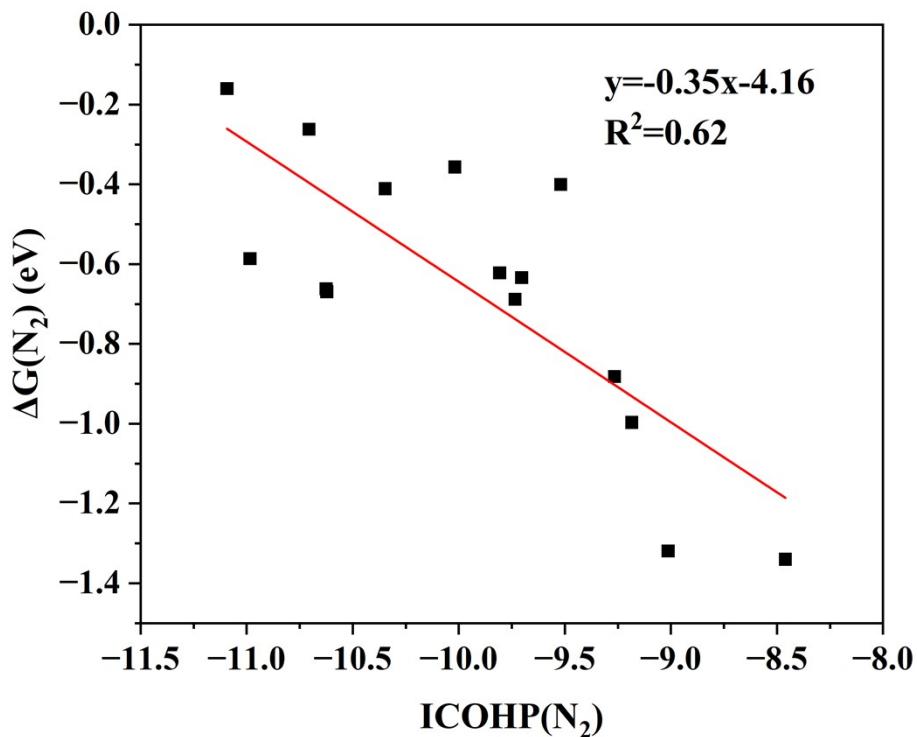


Fig. S6 The N₂ adsorption free energy ($\Delta G(N_2)$) versus the ICOHP of N-N bond (ICOHP(N₂)).

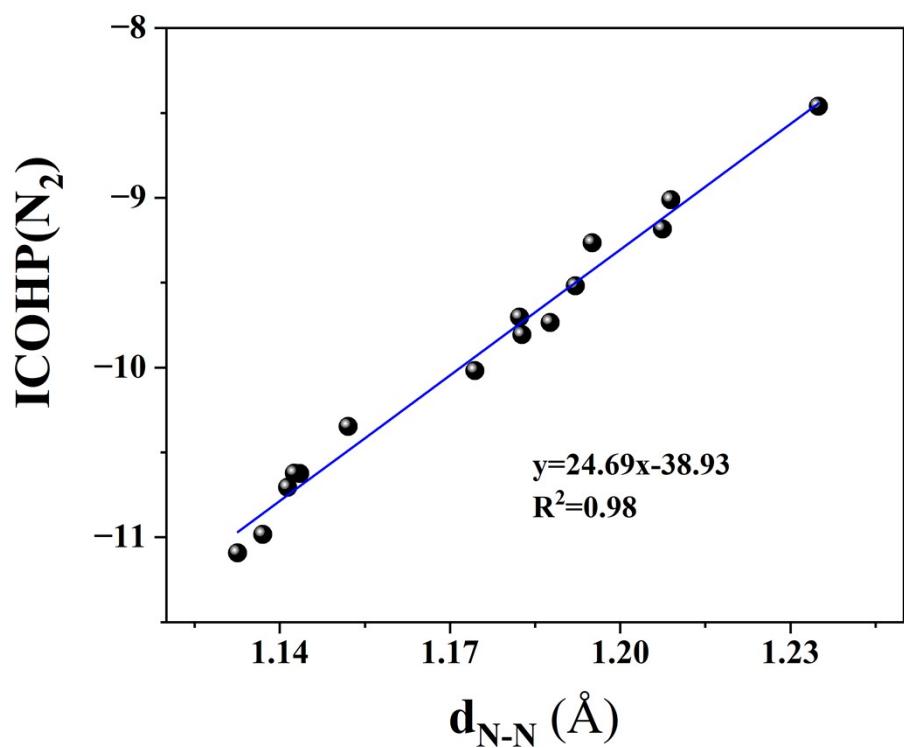


Fig. S7 The ICOHP of N-N bond ($\text{ICOHP}(\text{N}_2)$) versus the N-N bond length ($d_{\text{N-N}}$).

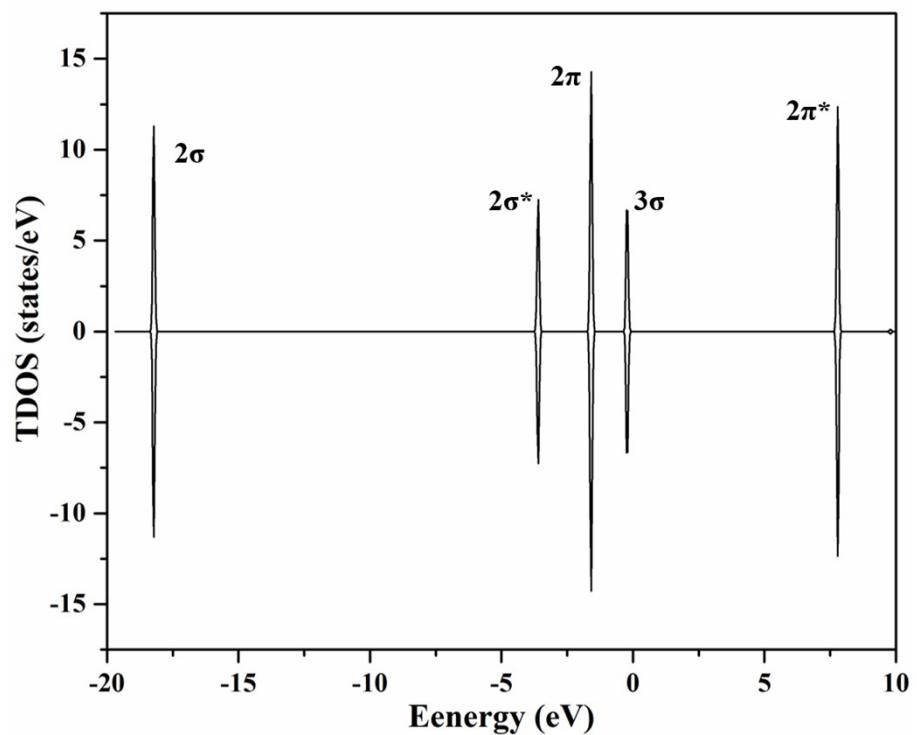


Fig. S8 Total density of states for free N_2 molecule.

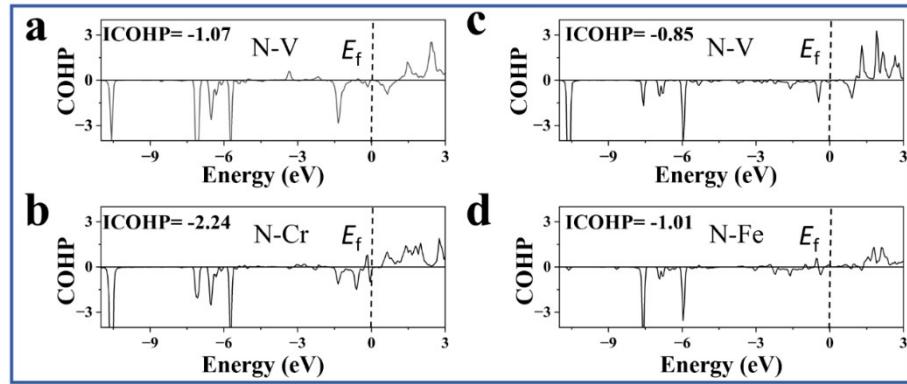


Fig. S9 COHP for the interactions between N of adsorbed N_2 and its bonded V and Cr atoms for N_2 adsorbed V-Cr@GDY (a-b), and V and Fe for N_2 adsorbed V-Fe@GDY (c-d).

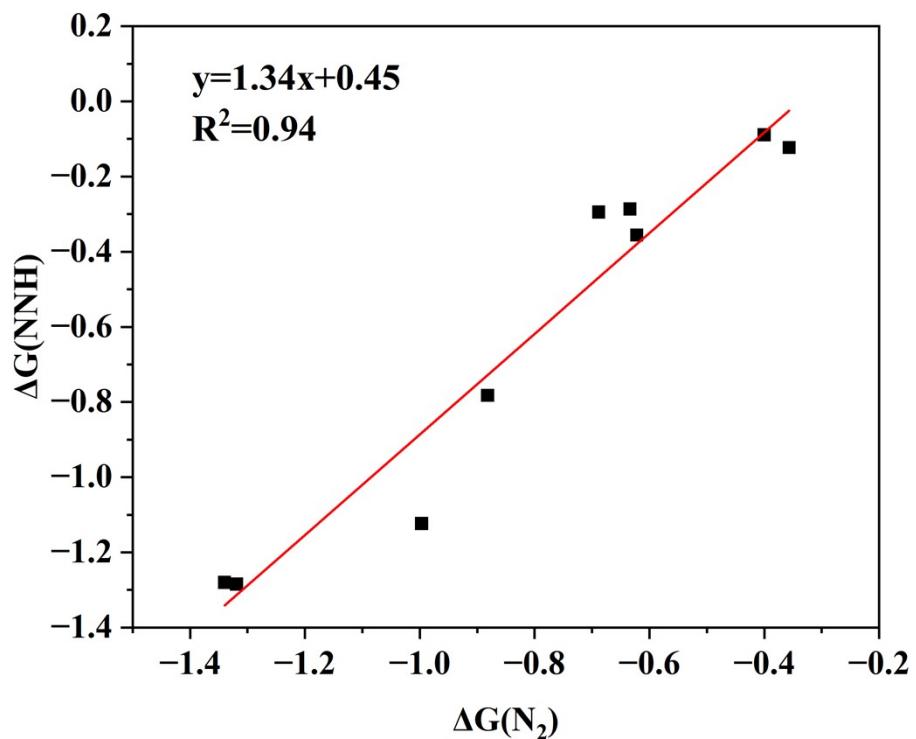


Fig. S10 The NNH adsorption free energy ($\Delta G(\text{NNH})$) versus the corresponding N_2 adsorption free energy ($\Delta G(\text{N}_2)$).

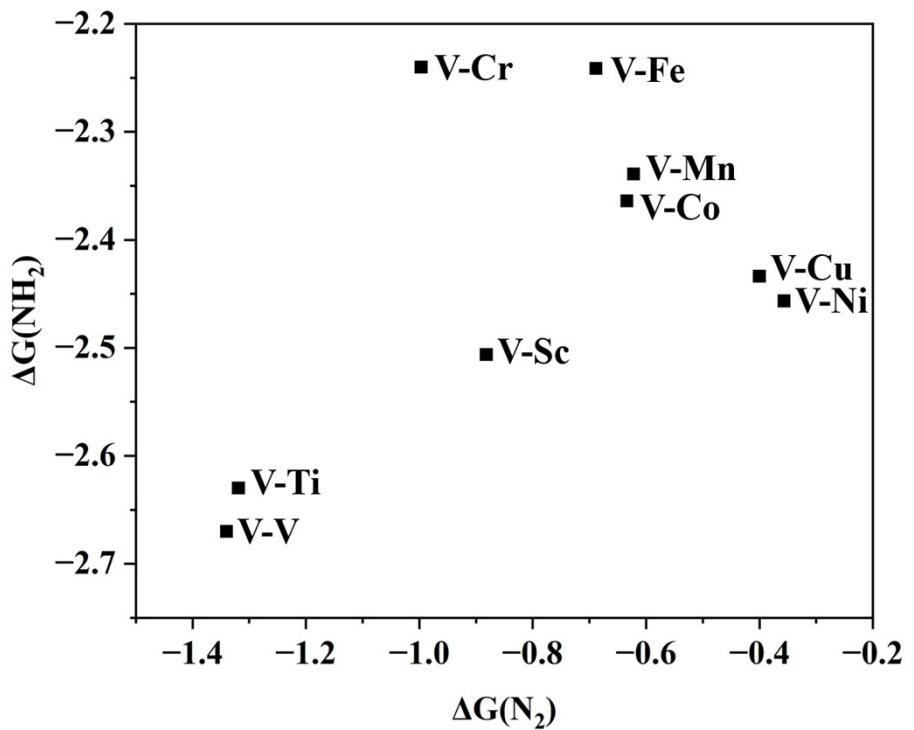


Fig. S11 The NH_2 adsorption free energy ($\Delta G(\text{NH}_2)$) versus the corresponding N_2 adsorption free energy ($\Delta G(\text{N}_2)$).

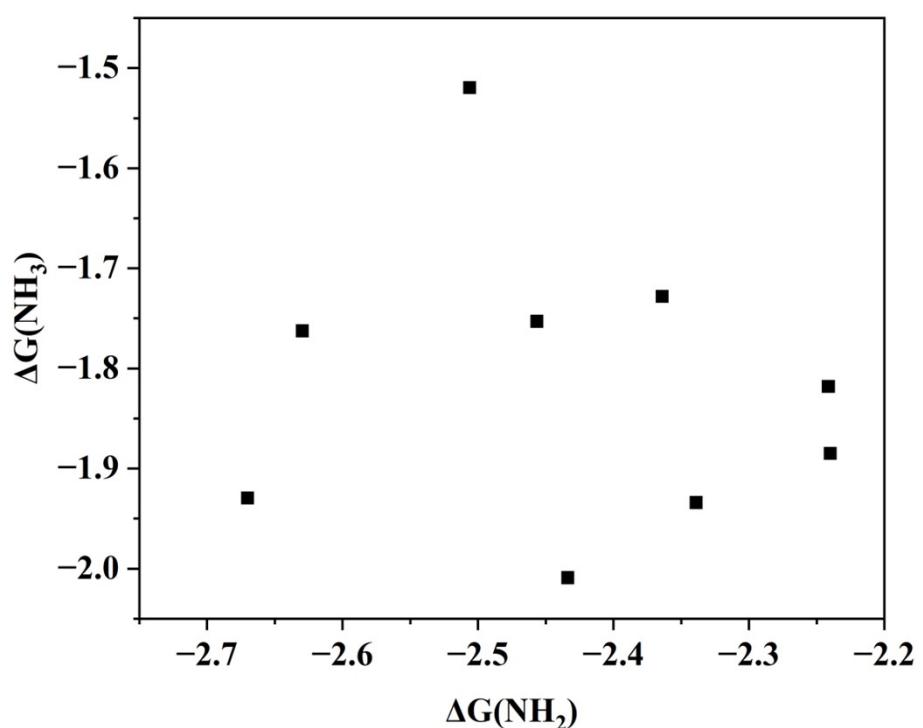


Fig. S12 The NH_3 adsorption free energy ($\Delta G(\text{NH}_3)$) versus the corresponding NH_2 adsorption free energy ($\Delta G(\text{NH}_2)$).

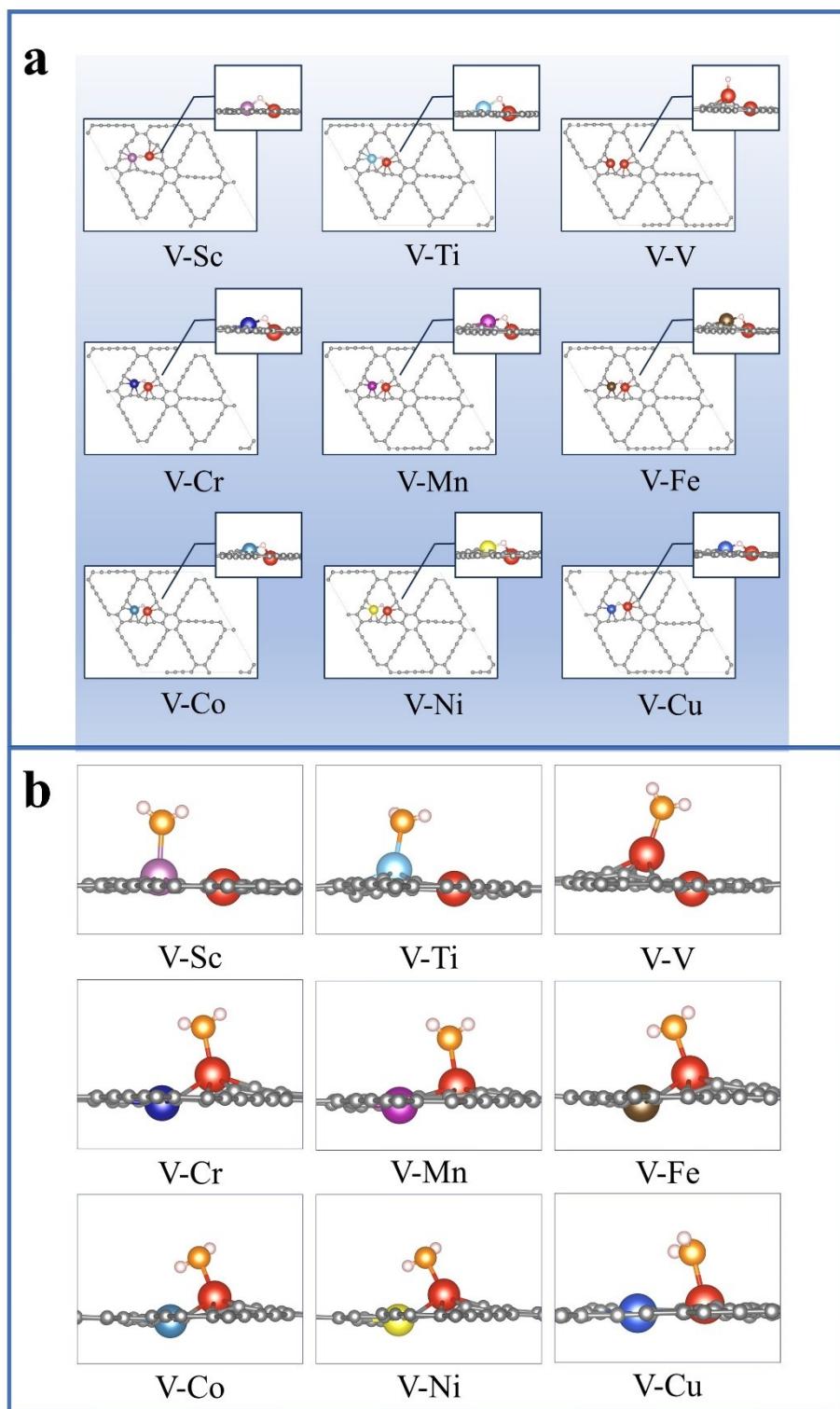


Fig. S13 Optimized H (a) and H₂O (b) adsorption configurations on V-TM@GDY (TM = Sc to Cu).

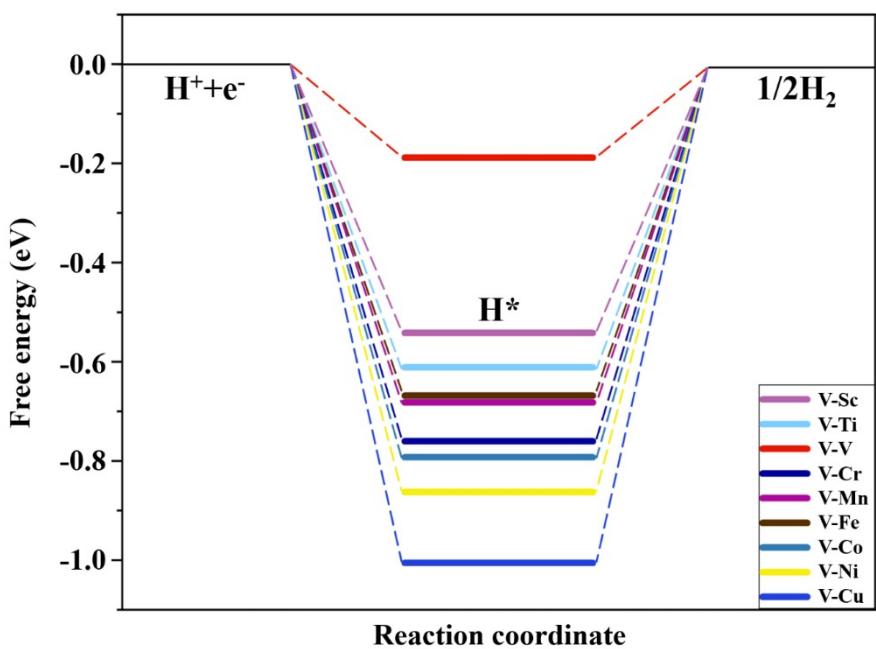


Fig. S14 Free energy diagram of HER for V-TM@GDY.

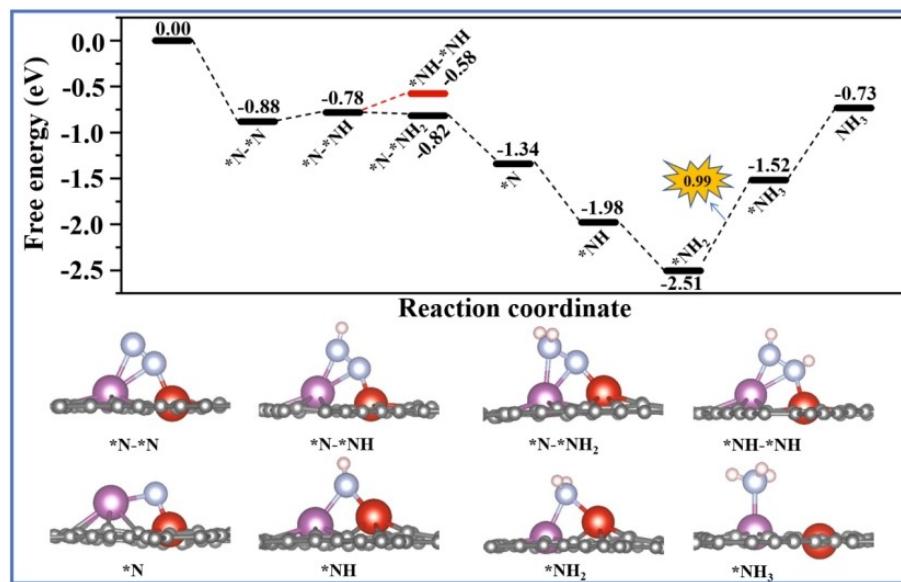


Fig. S15 Free energy diagrams and corresponding reaction intermediates for NRR via a consecutive pathway on V-Sc@GDY.

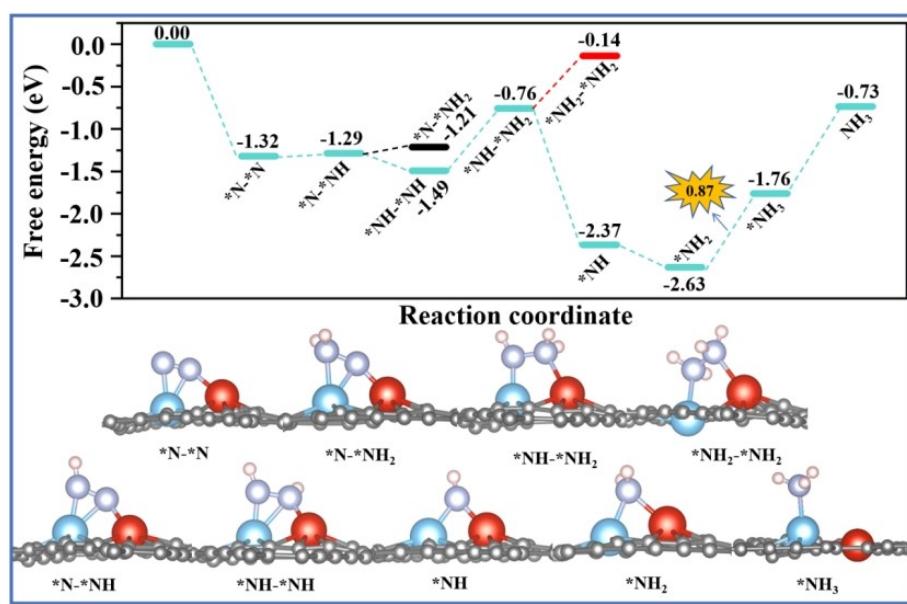


Fig. S16 Free energy diagrams and corresponding reaction intermediates for NRR via a mixed pathway on V-Ti@GDY.

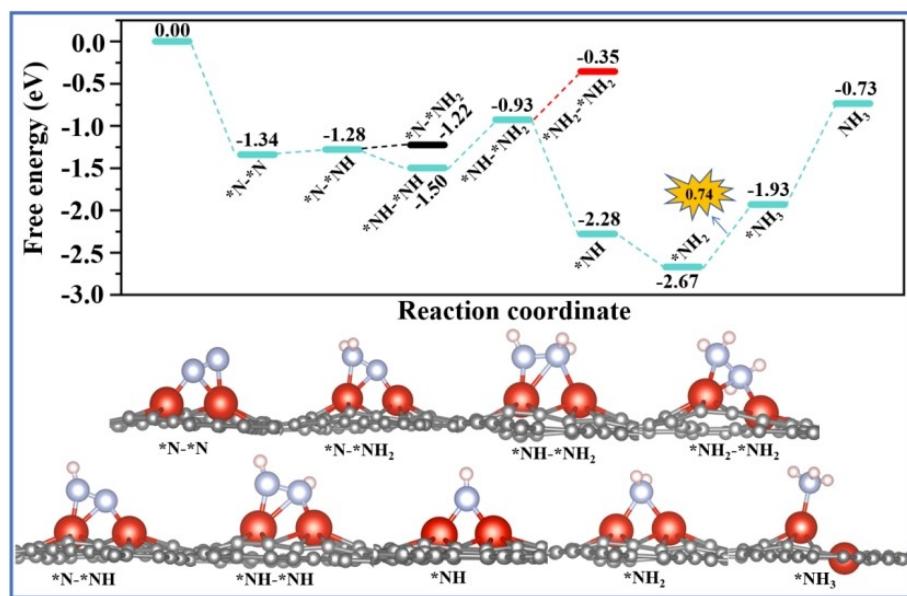


Fig. S17 Free energy diagrams and corresponding reaction intermediates for NRR via a mixed pathway on V-V@GDY.

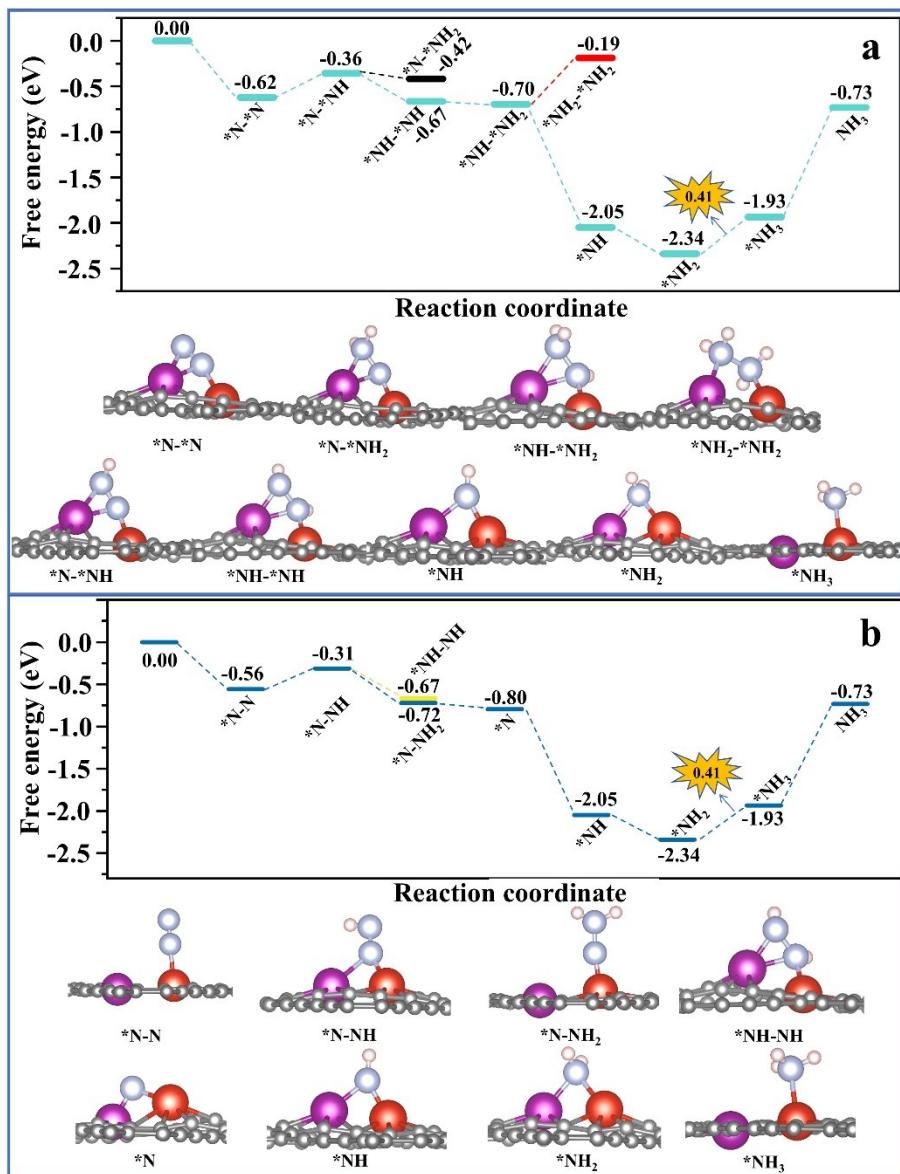


Fig. S18 Free energy diagrams and corresponding reaction intermediates for NRR via a mixed pathway on V-Mn@GDY(a) and distal pathway (b).

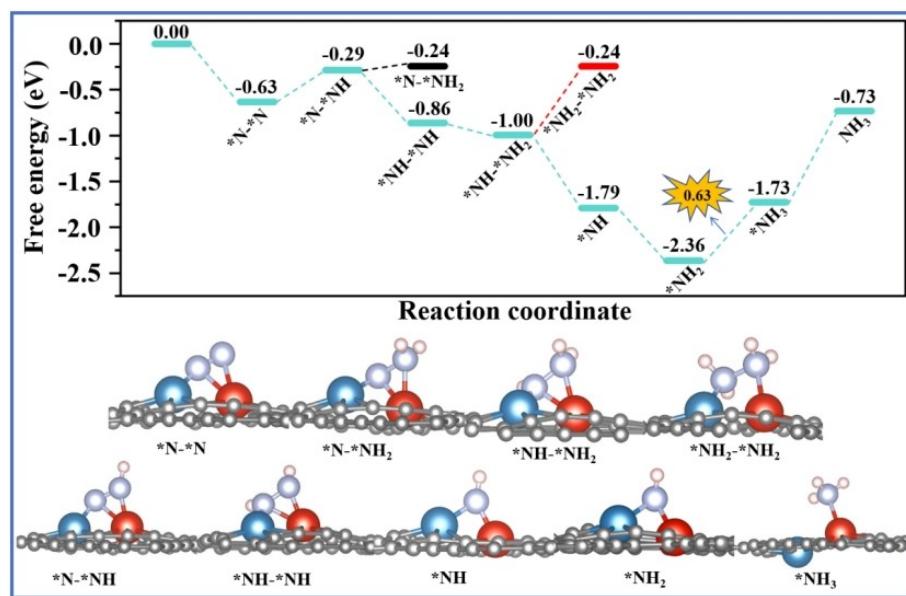


Fig. S19 Free energy diagrams and corresponding reaction intermediates for NRR via a mixed pathway on V-Co@GDY.

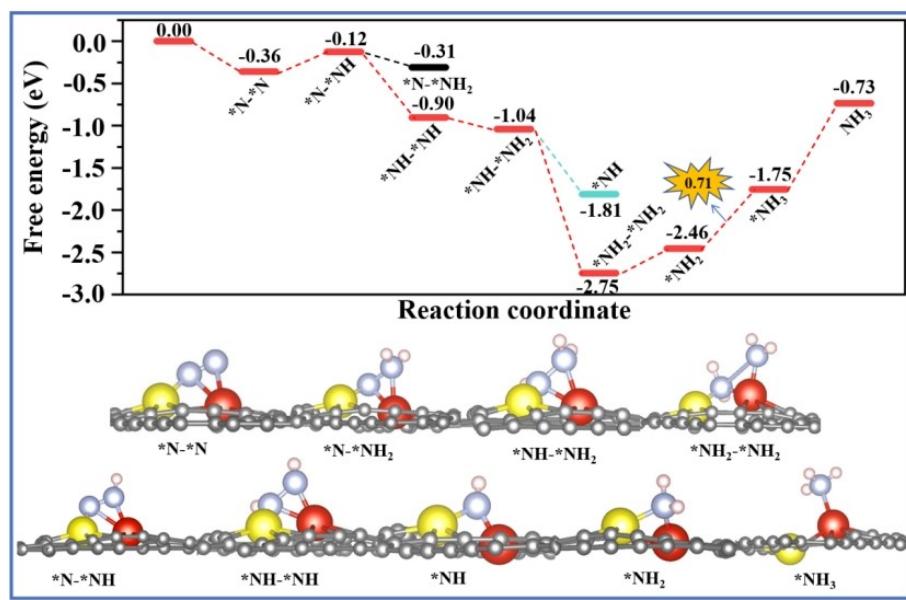


Fig. S20 Free energy diagrams and corresponding reaction intermediates for NRR via an enzymatic pathway on V-Ni@GDY.

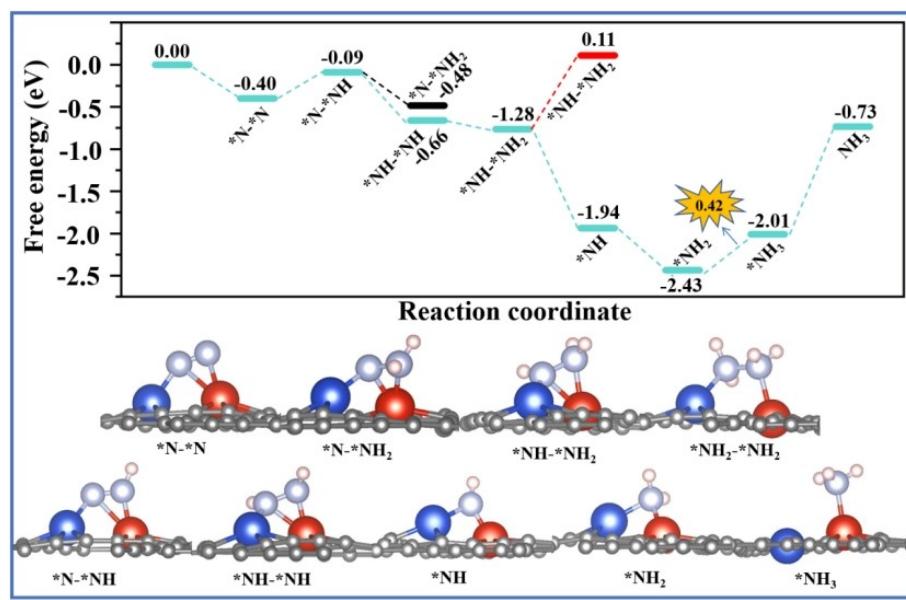


Fig. S21 Free energy diagrams and corresponding reaction intermediates for NRR via a mixed pathway on V-Cu@GDY.

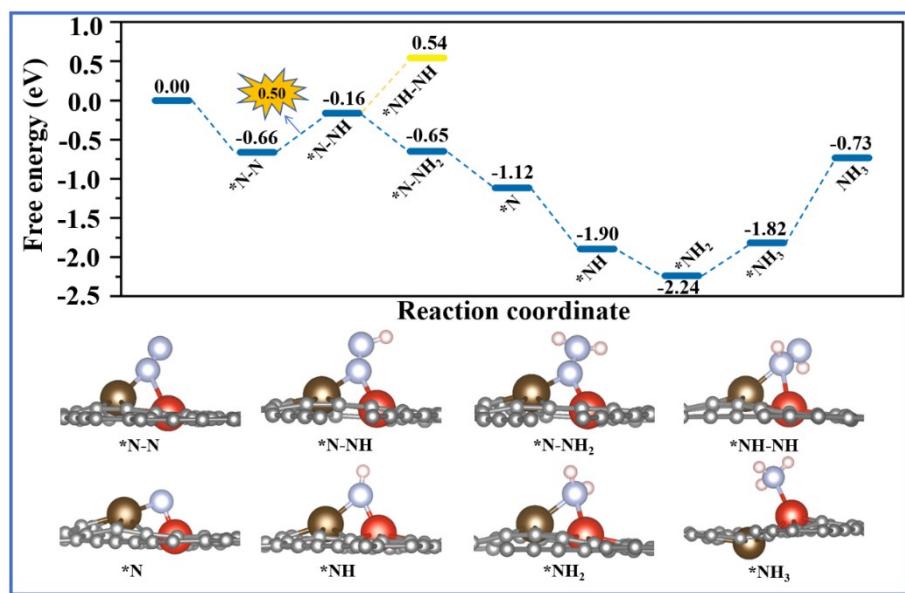


Fig. S22 Free energy diagrams and corresponding reaction intermediates for NRR via a distal pathway on V-Fe@GDY.

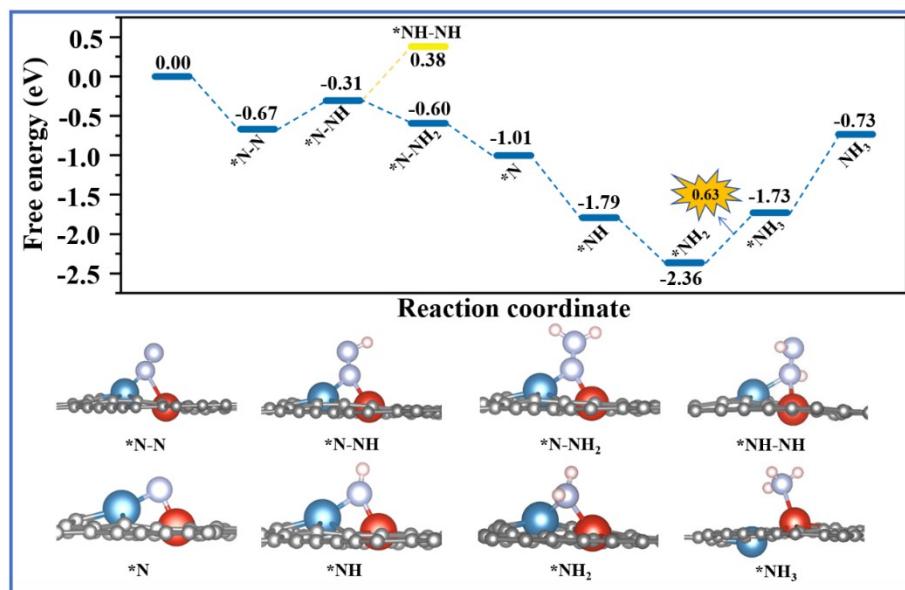


Fig. S23 Free energy diagrams and corresponding reaction intermediates for NRR via a distal pathway on V-Co@GDY.

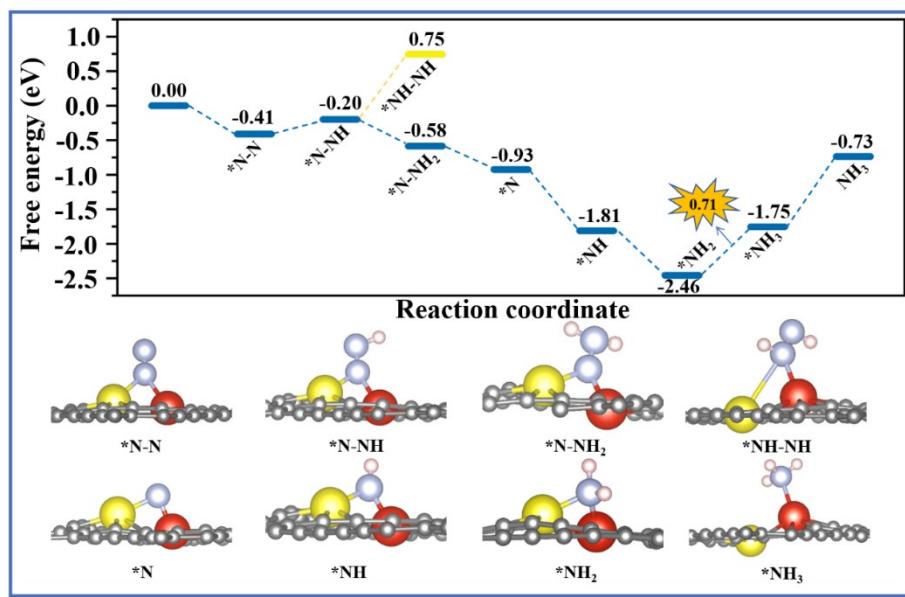


Fig. S24 Free energy diagrams and corresponding reaction intermediates for NRR via a distal pathway on V-Ni@GDY.

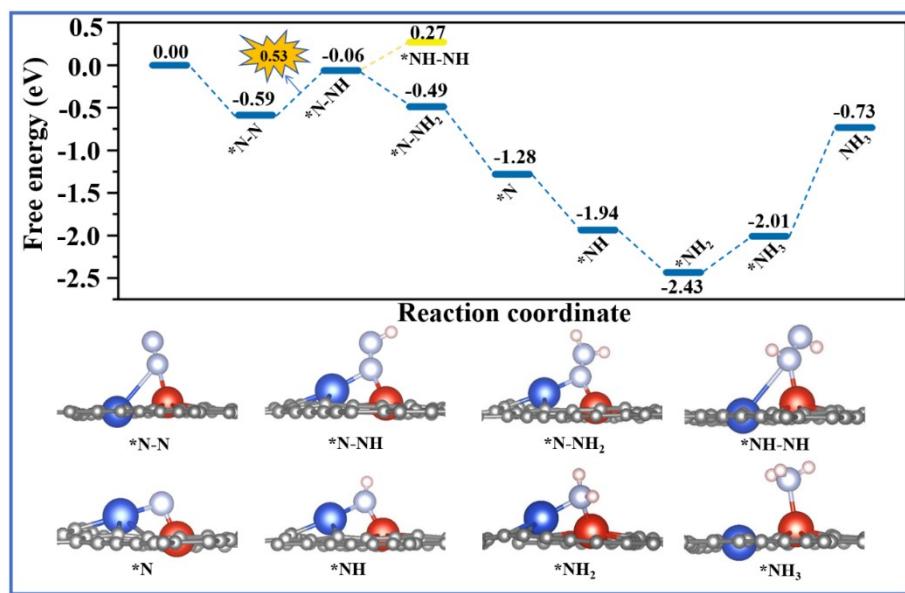


Fig. S25 Free energy diagrams and corresponding reaction intermediates for NRR via a distal pathway on V-Cu@GDY.

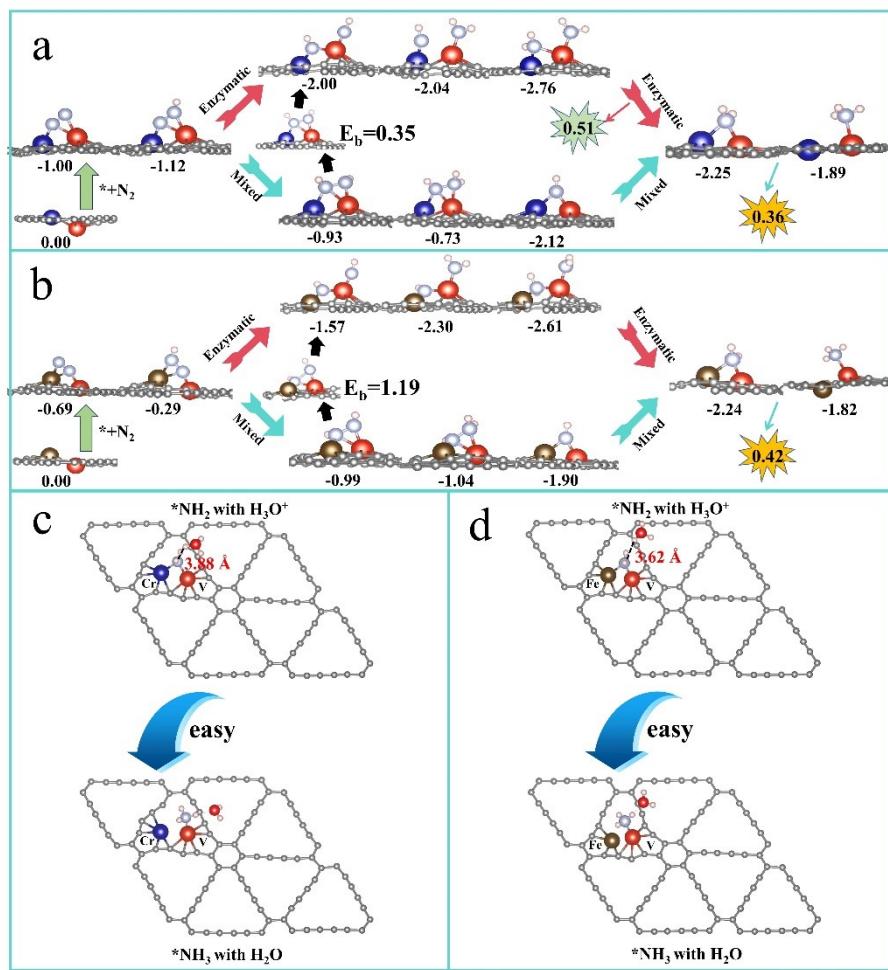


Fig. S26 The intermediates and the free energy changes (in eV) for the NRR on V-Cr@GDY (a) and V-Fe@GDY (b). Easy protonation of $*\text{NH}_2$ to $*\text{NH}_3$ by H_3O^+ under acidic conditions for V-Cr@GDY (c) and V-Fe@GDY (d). E_b denotes the energy barrier (in eV) for the dissociation of the adsorbed species.

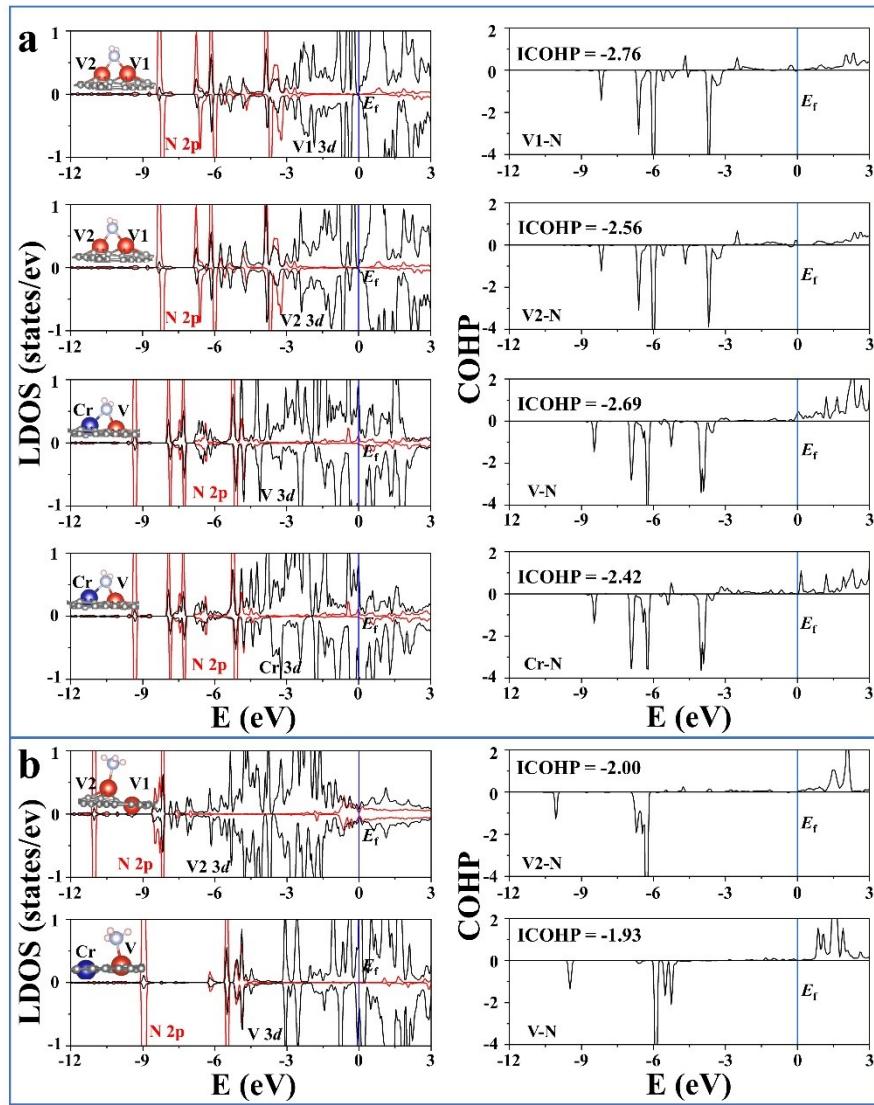


Fig. S27 The LDOS projected on the N atom of the adsorbed NH_2 species and its bonded TM atoms, and the relevant pCOHP and ICOHP (a), and The LDOS projected on the N atom of the adsorbed NH_3 species and its bonded TM atoms, and the relevant pCOHP and ICOHP (b).

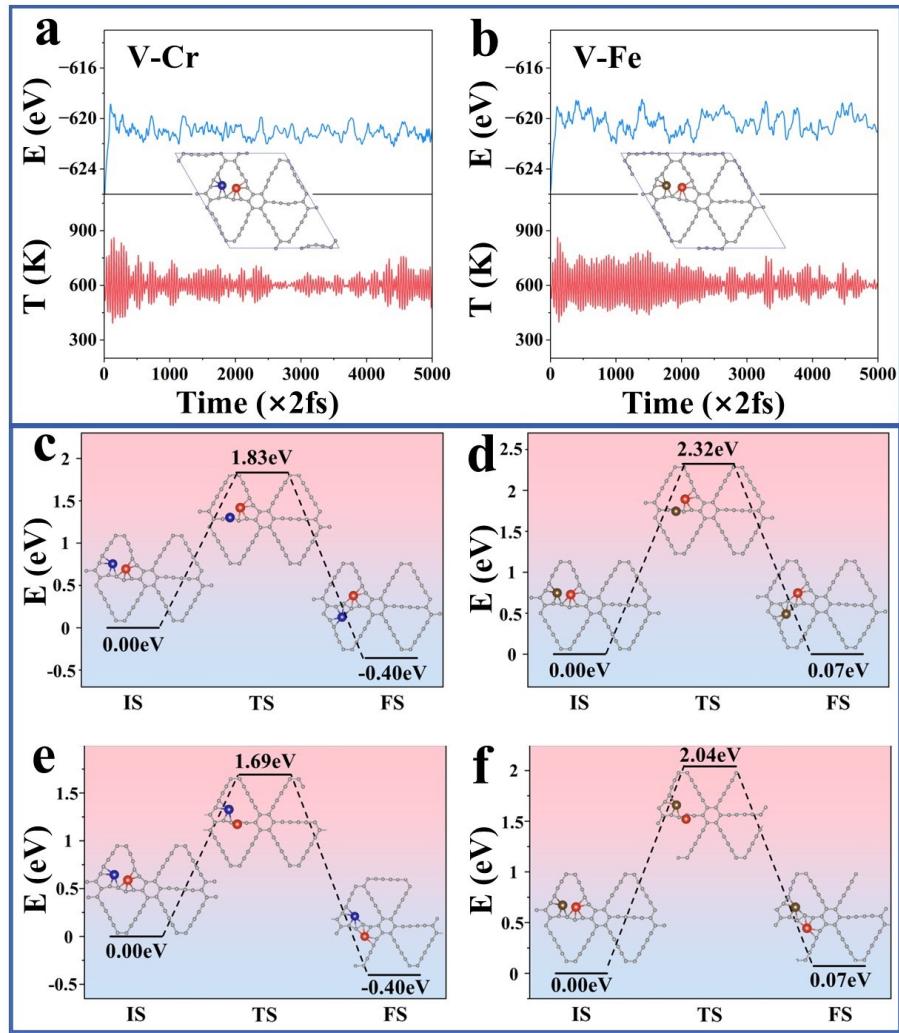


Fig. S28 Energy and temperature fluctuations against the time in AIMD simulations over 10 ps at 600 K for V-Cr@GDY (a), V-Fe@GDY (b). Optimized structures of the initial state (IS), transition state (TS), final state (FS), and the energy barrier for the dissociation of the V-Cr pair in V-Cr@GDY (b-c) and the V-Fe pair in V-Fe@GDY (d-e), leading to the formation of separated single atoms.

Reference

1. X. Guo; J. Gu; S. Lin; S. Zhang; Z. Chen; S. Huang, Tackling the Activity and Selectivity Challenges of Electrocatalysts toward the Nitrogen Reduction Reaction Via Atomically Dispersed Biatom Catalysts, *J. Am. Chem. Soc.*, 2020, **142**, 5709-5721.
2. W. Zhao; L. Zhang; Q. Luo; Z. Hu; W. Zhang; S. Smith; J. Yang, Single

Mo₁(Cr₁) Atom on Nitrogen-Doped Graphene Enables Highly Selective Electrocatalysis of Nitrogen into Ammonia, *ACS Catal.*, 2019, **9**, 3419-3425.

3. X. Liu; Y. Jiao; Y. Zheng; M. Jaroniec; S.-Z. Qiao, Building up a Picture of the Electrocatalytic Nitrogen Reduction Activity of Transition Metal Single-Atom Catalysts, *J. Am. Chem. Soc.*, 2019, **141**, 9664-9672.
4. X. Wang; Q. Zhang; W. Hao; C. Fang; J. Zhou; J. Xu, A Novel Porous Graphitic Carbon Nitride (G-C₇n₃) Substrate: Prediction of Metal-Based Π -D Conjugated Nanosheets toward the Highly Active and Selective Electrocatalytic Nitrogen Reduction Reaction, *J. Mater. Chem. A.*, 2022, **10**, 15036-15050.
5. [Http://Webbook.Nist.Gov/Chemistry/](http://Webbook.Nist.Gov/Chemistry/).
6. Z. Feng; Y. Tang; W. Chen; Y. Li; R. Li; Y. Ma; X. Dai, Graphdiyne Coordinated Transition Metals as Single-Atom Catalysts for Nitrogen Fixation, *Phys. Chem. Chem. Phys.*, 2020, **22**, 9216-9224.