

## Supporting Information

### ***p*-block main-group metal-based two-dimensional metal-organic frameworks as efficient electrocatalysts for oxygen reduction reaction**

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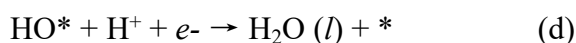
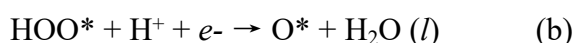
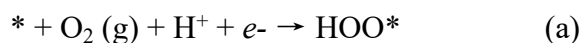
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#### **1. ORR**

The cathodic ORR process follows a four-stage pathway to generate H<sub>2</sub>O product and the four electron reaction paths are defined as equations (a) - (d) as reported in the previous literature<sup>1</sup>:



Where \* represents active sites on the catalyst, (l) and (g) is the liquid and gas phase, respectively, and HOO\*, O\* and HO\* are the corresponding adsorbed intermediates. The Gibbs free energy ( $\Delta G$ ) of each elementary step under the  $U = 0$  and  $\text{pH} = 0$  condition was calculated by the following equations (1a~1d):

$$\Delta G_a = G_{\text{HOO}^*} - G^* - 1/2 G_{\text{H}_2, \text{g}} - \{4.92 \text{eV} + 2G_{\text{H}_2\text{O}, \text{l}} - 2G_{\text{H}_2, \text{g}}\} \quad (1a)$$

$$\Delta G_b = G_{H_2O,l} + G_{O^*} - G_{HOO^*} - 1/2 G_{H_2,g} \quad (1b)$$

$$\Delta G_c = G_{HO^*} - G_{O^*} - 1/2 G_{H_2,g} \quad (1c)$$

$$\Delta G_d = G_{H_2O,l} + G^* - G_{HO^*} - 1/2 G_{H_2,g} \quad (1d)$$

Where we defined  $G_{X^*} = E_{X^*} + ZPE_{X^*} - TS_{X^*}$ , X refers to  $HOO^*$ ,  $O^*$  and  $HO^*$ . Here  $E_{X^*}$  is the DFT total energy of the corresponding  $X^*$  system under the polarization solvent model calculation.  $ZPE_{X^*}$  refers to the zero-point energy of  $X^*$ . Here we only include the zero-point energy of  $X^*$ , while keeping the catalyst  $*$  fixed.  $TS_{X^*}$  is the calculated entropy term of the adsorbed intermediate. Finally,  $G^* = E^*$  is the total energy of catalyst under the DFT solvent model calculation. Due to the poor description of DFT for the high-spin ground state of the  $O_2$ , we used  $G_{O_2,g} + 4G_{H_2,g} - 2G_{H_2O,l} = 4.92$  eV to obtain the free energy of  $O_2$  in the gas phase.<sup>2</sup> It is also difficult to directly calculate the Gibbs free energy of  $H_2O$  in the liquid phase ( $G_{H_2O,l}$ ). It is customary to calculate the liquid phase Gibbs free energy from its vapor phase counterpart at their equilibrium pressure when they have the same Gibbs free energies. Then,  $G_{H_2O,l} = E_{H_2O} + ZPE_{H_2O} - TS_{H_2O}$ . Where,  $E_{H_2O}$  is total energy of  $H_2O$  in the gas phase obtained from the DFT calculation;  $ZPE_{H_2O}$  is the zero point energy;  $TS_{H_2O}$  is the entropy term of the gas phase (in equilibrium with the liquid phase). We took the values of 0.67 eV and 0.41 eV for the  $TS_{H_2O}$  and  $TS_{H_2}$ , respectively.<sup>3</sup> As the most important measure of the catalytic activities for ORR, overpotential  $\eta$  of ORR ( $\eta^{ORR}$ ) was calculated by equation (2):

$$\eta^{ORR} = 1.23 - \frac{\min \{ \Delta G_a, \Delta G_b, \Delta G_c, \Delta G_d \}}{e} \quad (2)$$

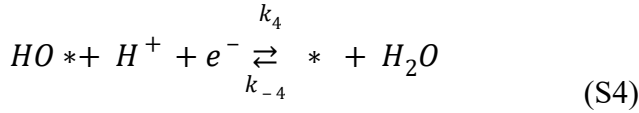
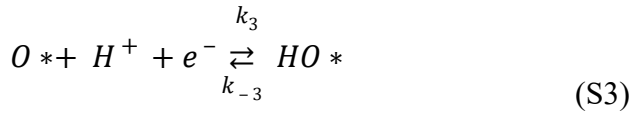
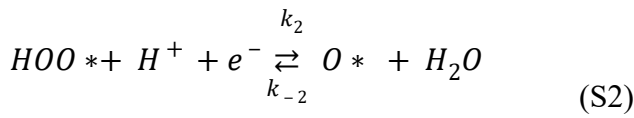
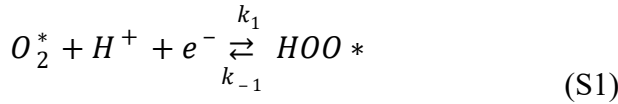
## 2. The catalytic selectivity of the ORR

The rate constant  $k$  can be obtained based on the Arrhenius equation:  $k = A \exp(-\Delta G_{PDS}/k_B T)$ . Here,  $A$ ,  $k_B$  and  $T$  refers to the pre-exponential factor, the Boltzmann constant and the temperature of 298.15 K, respectively. Hence, we can obtain the following equation:  $\ln(k_{sys}/k_{Pt(111)}) = [\Delta G_{PDS}(Pt(111)) - \Delta G_{PDS}(sys)]/k_B T$ . Here,  $k_{sys}$  and  $k_{Pt(111)}$  refer to the rate constant of the ORR on the screened electrocatalysts and ORR on the benchmark catalyst Pt(111), respectively. The selectivity of a certain catalyst can be estimated from the ratio of rate constants  $k_{O_2}$  and  $k_{H_2O_2}$  as shown in the following equation:  $\ln(k_{O_2}/k_{H_2O_2}) = [\Delta G(H_2O_2) - \Delta G(O^*)]/k_B T$ . Here,  $k_{O_2}$  and  $k_{H_2O_2}$  refers to the rate constant of  $O^*$  formation from  $HOO^*$  and

H<sub>2</sub>O<sub>2</sub> formation from HOO\*, respectively.

### 3. The polarization curves simulation of ORR

The ORR polarization curves of PMN<sub>x</sub>O<sub>4-x</sub>-HADQ catalysts were simulated based on the kinetic model developed by Hansen et al.<sup>4</sup> In this work, we focused on the dominating associative mechanism of the ORR. We simplified the above method and considered the corresponding electrochemical reduction steps as shown in the following equations:



Here,  $k_i$  and  $k_{-i}$  refers to the rate constants of reaction and reverse reaction, respectively. Based on the above reaction steps, the corresponding rate equations of intermediates can be calculated by the following equations:

$$\frac{\partial \theta_{HOO^*}}{\partial t} = -k_2 \theta_{HOO^*} + k_{-2} \theta_{O^*} x_{H_2O} + k_1 \theta_{O_2^*} - k_{-1} \theta_{HOO^*} \quad (S5)$$

$$\frac{\partial \theta_{O^*}}{\partial t} = -k_3 \theta_{O^*} + k_{-3} \theta_{HO^*} + k_2 \theta_{HOO^*} - k_{-2} \theta_{O^*} x_{H_2O} \quad (S6)$$

$$\frac{\partial \theta_{HO^*}}{\partial t} = -k_4 \theta_{HO^*} + k_{-4} \theta_{*} x_{H_2O} + k_3 \theta_{O^*} - k_{-3} \theta_{HO^*} \quad (S7)$$

$$\frac{\partial \theta_{*}}{\partial t} = k_4 \theta_{HO^*} - k_{-4} x_{H_2O} \theta_{*} - k_1 \theta_{*} x_{O_2} + k_{-1} \theta_{HOO^*} \quad (S8)$$

Where,  $t$ ,  $\theta$  and  $x$  refers to the time, coverage of intermediates and mole fraction, respectively.

The value of  $x_{H_2O}$  was set as 1, and  $x_{O_2}$  was set as  $2.34 \times 10^{-5}$ , which represents O<sub>2</sub>(g) in equilibrium with O<sub>2</sub>(aq) at 1 atm. The coverages of intermediates on the PM active site should satisfy the following relationship:

$$\theta_* + \theta_{O_2} + \theta_{O*} + \theta_{HO*} + \theta_{HOO*} = 1 \quad (S9)$$

The equilibrium constant ( $K_i$ ) can be calculated by the following equation:

$$K_i = \exp\left[-\frac{e(U - U_i)}{k_b T}\right] \quad (S10)$$

Where,  $k_b$ ,  $T$  and  $U_i$  refers to the Boltzmann constant, the temperature and the reversible potential, respectively. In addition,  $U_i = \Delta G_i/e$ , and  $\Delta G_i$  refers to the Gibbs free energy change.

The rate constant ( $k_i$ ) is calculated by the following equation:

$$k_i = A_i \exp\left[-\frac{\Delta E_{a,i}}{k_b T}\right] \exp\left[-\frac{e\beta_i(U - U_i)}{k_b T}\right] \quad (S11)$$

Where,  $A_i$  refers to the pre-exponential factor set as  $1.23 \times 10^9$  and  $\beta_i$  is the symmetry factor set as 0.5.  $E_{a,i}$  is activation energy. The activation energy values of the electrochemical ORR steps are generally small, ranging from 0.10 to 0.26 eV, as reported in previous literature<sup>5, 6</sup>. Therefore, we used 0.26 eV value of the activation energy for all the electrochemical steps of the ORR in the work.

Moreover, the rate constant of the reverse reaction ( $k_{-i}$ ) can be calculated by the following equation:

$$k_{-i} = \frac{k_i}{K_i} \quad (S12)$$

The current density ( $j$ ) can be calculated by the following equation:

$$j = e\rho T O F_{e-} \quad (S13)$$

where  $\rho$  is the surface density of active sites.

#### 4. Descriptor identification

The considered seven fundamental parameters in this work, including the Pauling electronegativity (PE) of PM atoms, the electron affinity (EA) of PM atoms, the first ionization energy (IP) of PM atoms, the p-electrons (N) of PM atoms, the atomic charge ( $Q_{PM}$ ) of PM atoms before reaction, the distance between PM and N/O atoms (Dis), and the atomic radii (AR) of PM atoms.

The SISSO package<sup>7, 8</sup> was used to identify a simple and accurate descriptor to predict the adsorption Gibbs free energy of the key intermediates  $HO^*$  ( $\Delta G_{HO^*}$ ) according to the below

equation:

$$\Delta G_{HO}^* = -686.07 \times \frac{\exp\left(\frac{EA}{AR}\right) * IP^2}{\exp(PE)} + 0.14 \times \left| \frac{\sqrt[3]{EA} \sqrt{N} * \ln M}{\ln Q_{TM}} - \ln AR * \sqrt[3]{IP} \right| - 0.06 \times \left| \frac{\exp\left(\frac{EA}{AR}\right) * IP^2}{\exp(PE)} \right|$$

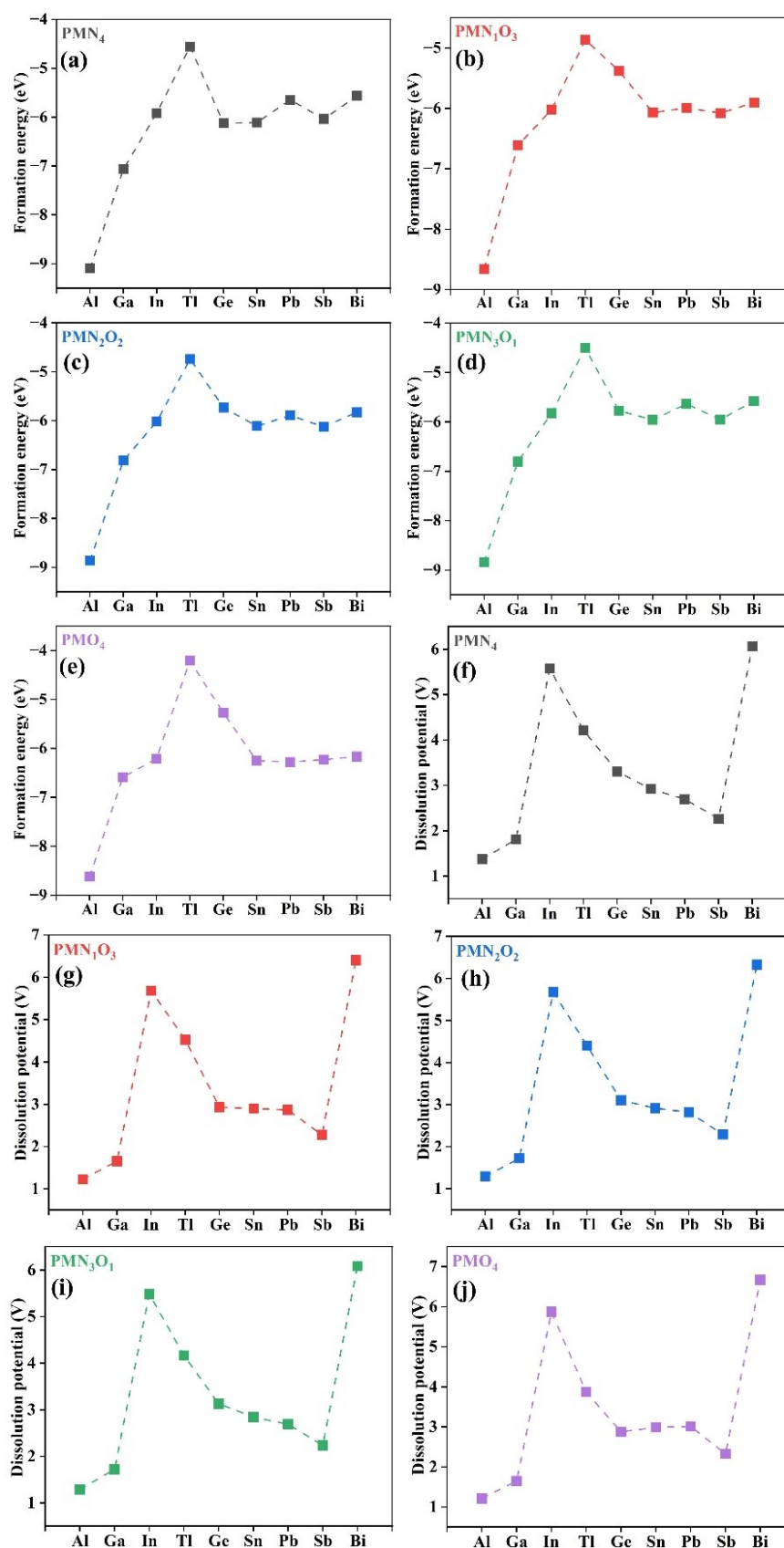
$$\ln N + 3.33$$

## 5. Computational methods

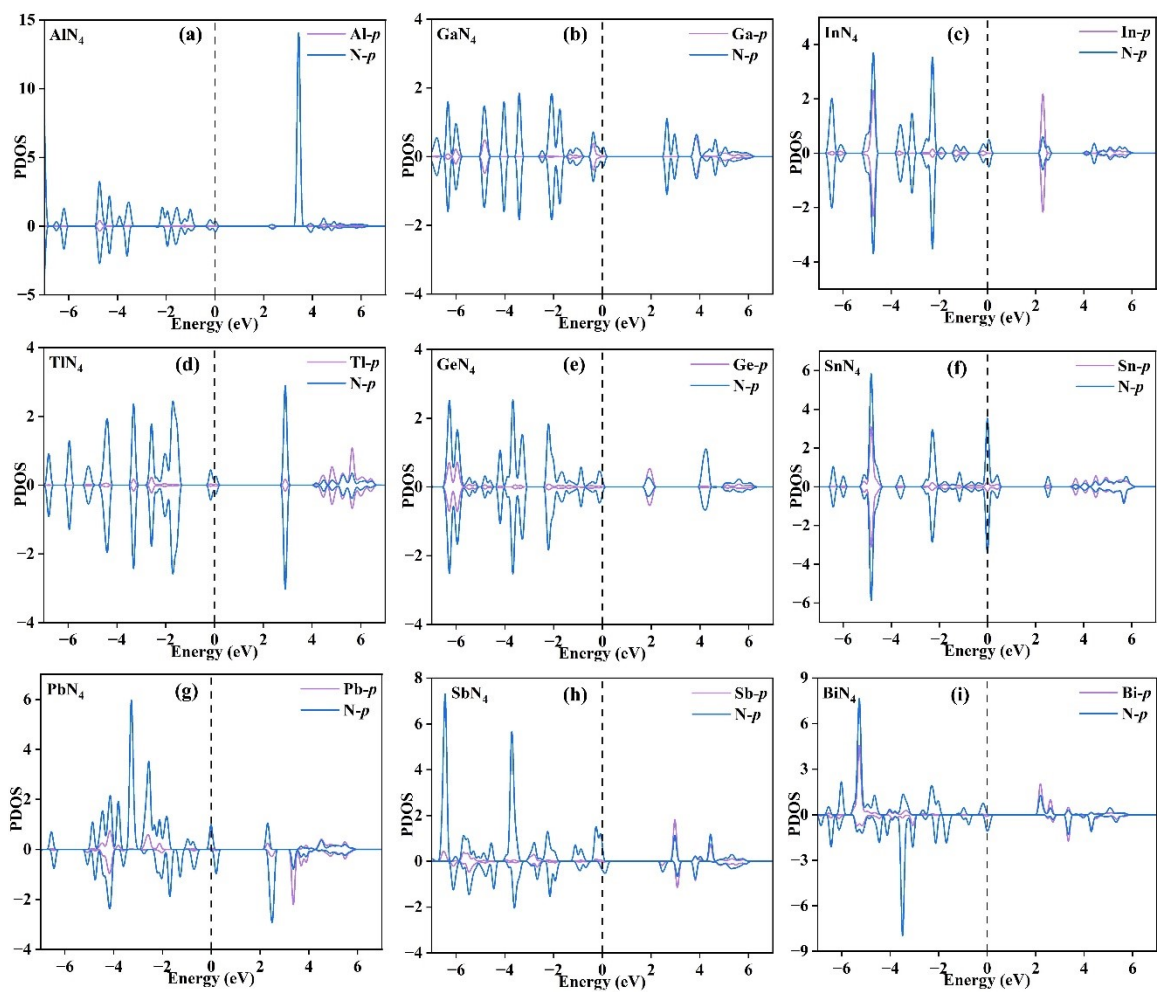
All the spin-polarized density functional theory calculations were carried out by using the Vienna ab initio Simulation Package (VASP).<sup>9-10</sup> The interactions between ion cores and valence electrons were described by using the projector augmented wave (PAW) method.<sup>11</sup> The electronic exchange-correlation interactions were calculated by using the Perdew-Burke-Ernzerhof (PBE)<sup>12</sup> functional of the generalized gradient approximation (GGA).<sup>13</sup> The Van der Waals (vdW) interactions were described by using the dispersion-corrected DFT-D3 method.<sup>14</sup> The plane-wave cutoff energy was set to 500 eV, and the convergence criterion for energy and force during geometrical optimization was set to 10<sup>-5</sup> eV and 10<sup>-2</sup> eV/Å, respectively. The Brillouin zone was sampled using a 3 x 3 x 1 k-point<sup>15</sup> during geometry optimization. The vacuum space of 20 Å was adopted to avoid the interaction between the periodic images. The solvent effect was implicitly considered by using the VASPsol code to simulate the water solvent environment.<sup>16</sup> Ab initio molecular dynamics (AIMD) simulations were performed to demonstrate the thermodynamic stability of catalyst, and the algorithm of the Nose thermostat was carried out to simulate a canonical ensemble<sup>17</sup> for 10 ps with a time step of 1 fs. Bader charge analysis was performed to investigate the charge transfer process.<sup>18</sup> The calculation details for the ORR is listed in the Supporting Information as in our previous study.<sup>19</sup> The adsorption Gibbs free energy is defined as  $G_{ads} = G_{adsorbent+catalyst} - G_{catalyst} - G_{adsorbent}$ , here  $G_{adsorbent+catalyst}$ ,  $G_{catalyst}$ , and  $G_{adsorbent}$  is the Gibbs free energy of the adsorbent on the catalyst, the isolated catalyst, and the isolated adsorbent, respectively.

The  $E_f$  and  $U_{diss}$  defined as  $E_f = (E_{PMN_xO_{4-x}} - E_{N_xO_{4-x}} - 3E_{PM})/3$  and  $U_{diss} = U_{diss}^\circ (\text{bulk}) - E_f/n_e$ , respectively. Where  $E_{PMN_xO_{4-x}}$  and  $E_{N_xO_{4-x}}$  denote the total energies of  $PMN_xO_{4-x}$  system and  $N_xO_{4-x}$  substrate, respectively.  $E_{PM}$  denote the total energy of a metal atom in its most stable bulk structure.  $U_{diss}^\circ (\text{bulk})$  represents the standard dissolution potential of bulk metal,  $n$  refers to the number of electrons involved during the dissolution process. Since  $E_{PM}$  is referenced with respect to its corresponding bulk metal, the designed catalysts with negative values of  $E_f$

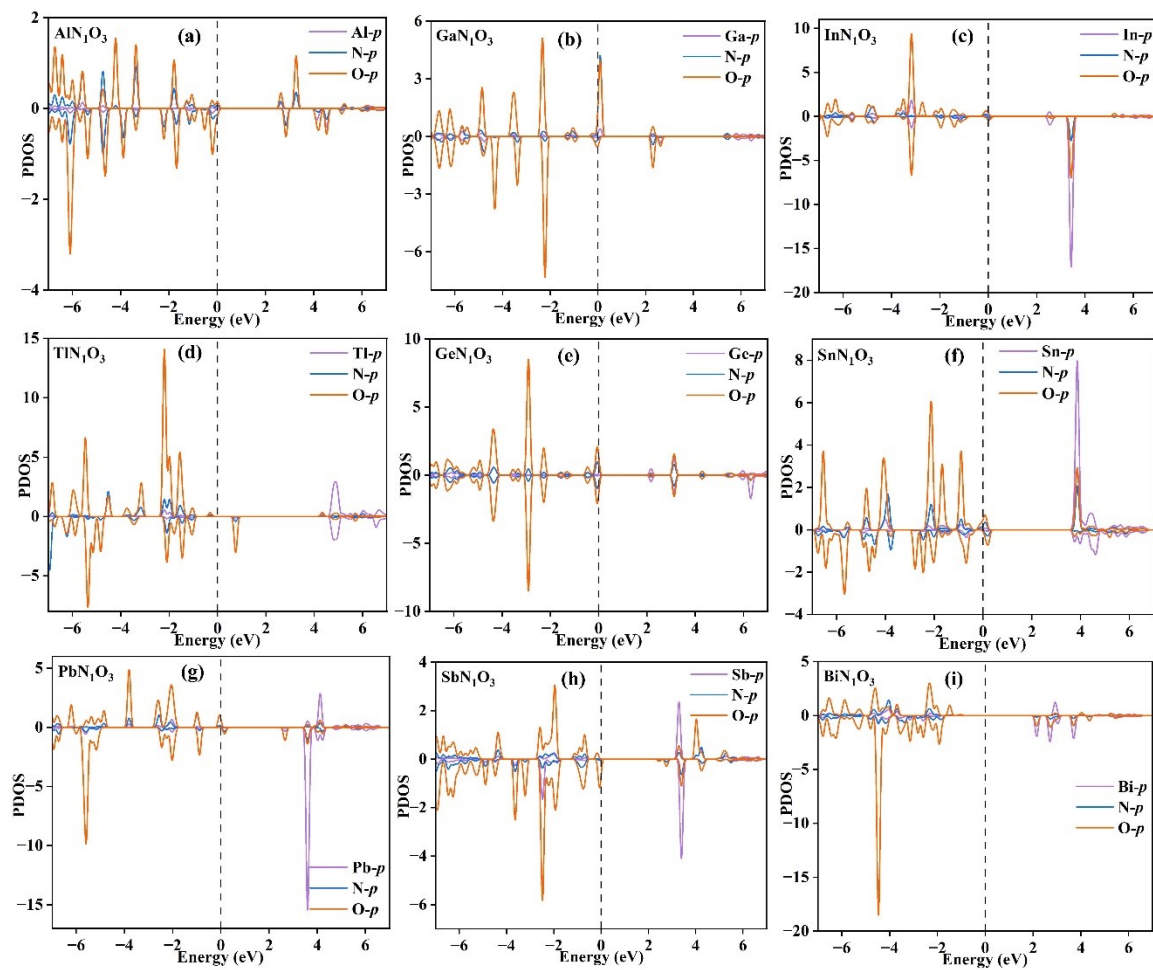
( $E_f < 0$ ) are evaluated to be thermodynamically stable against the clustering of PM atoms. The designed catalysts with positive values of  $U_{\text{diss}}$  ( $U_{\text{diss}} < 0$ ) vs standard hydrogen electrode (SHE) are regarded as electrochemically stable.



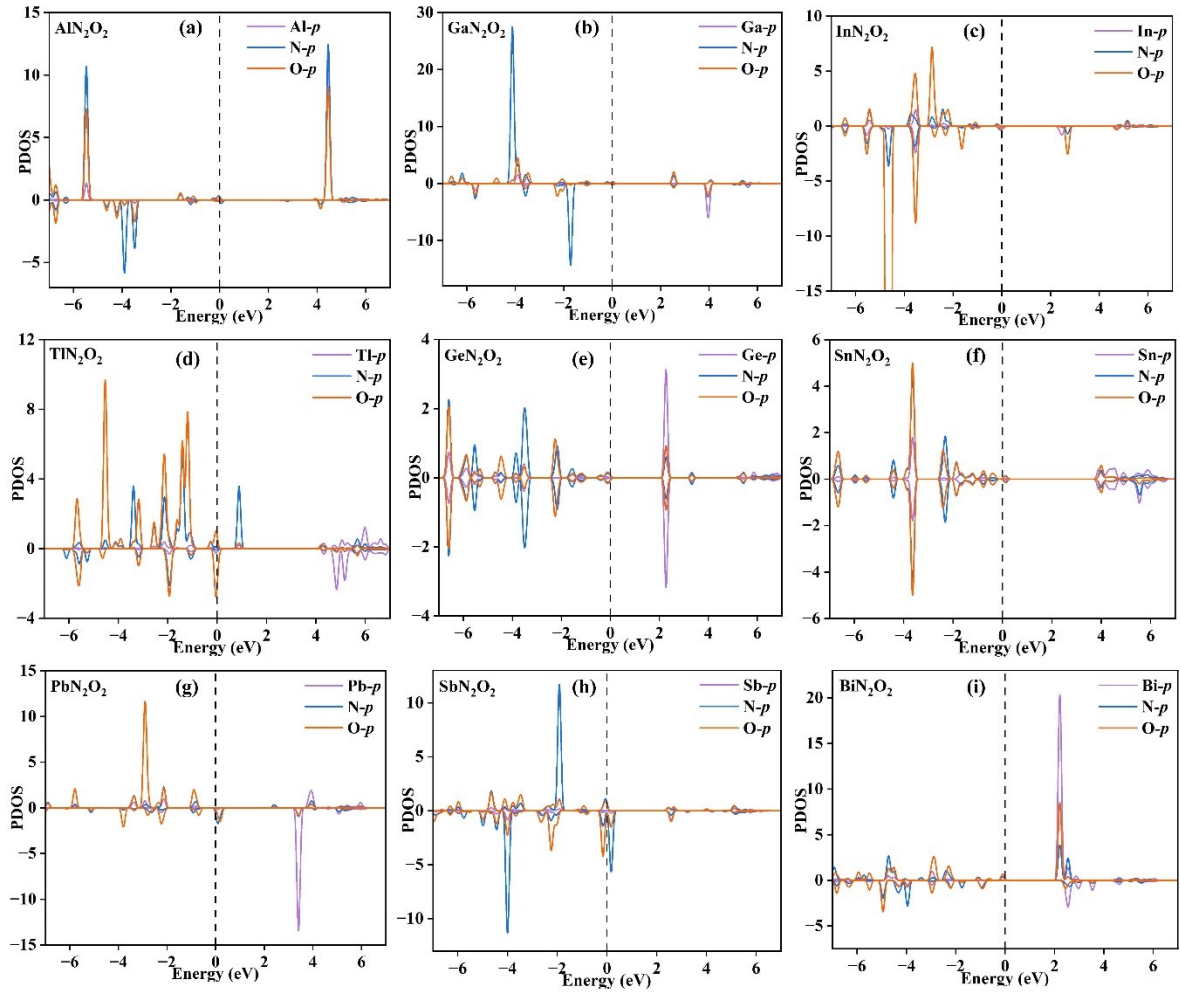
**Fig. S1** Calculated formation energy (a-e) and dissolution potential of metal atoms (f-j) for the designed  $\text{PMN}_x\text{O}_{4-x}$ -HADQ catalysts.



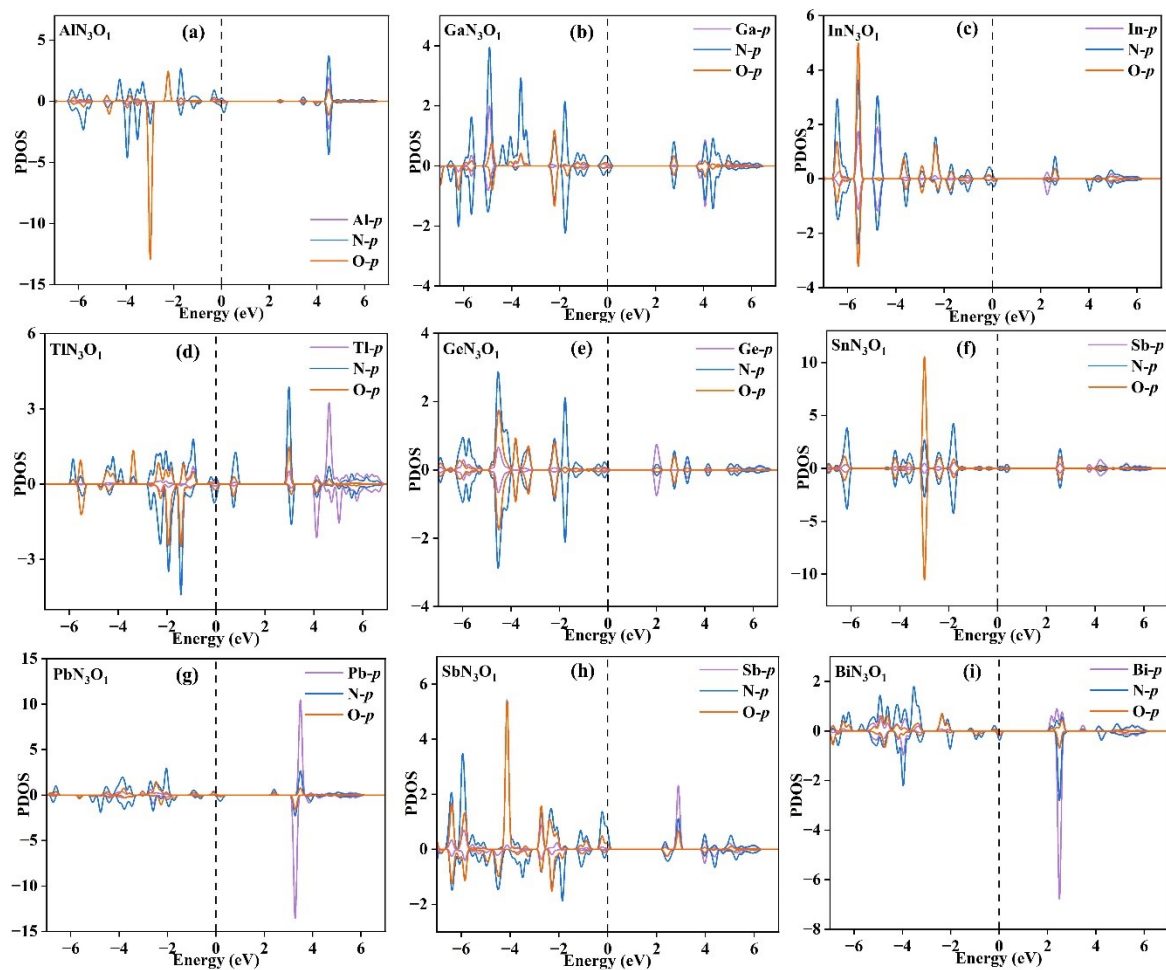
**Fig. S2** Calculated partial density of states (PDOS) for the  $p$  orbitals of N atoms and PM atoms for the designed  $\text{PMN}_4\text{-HADQ}$  catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



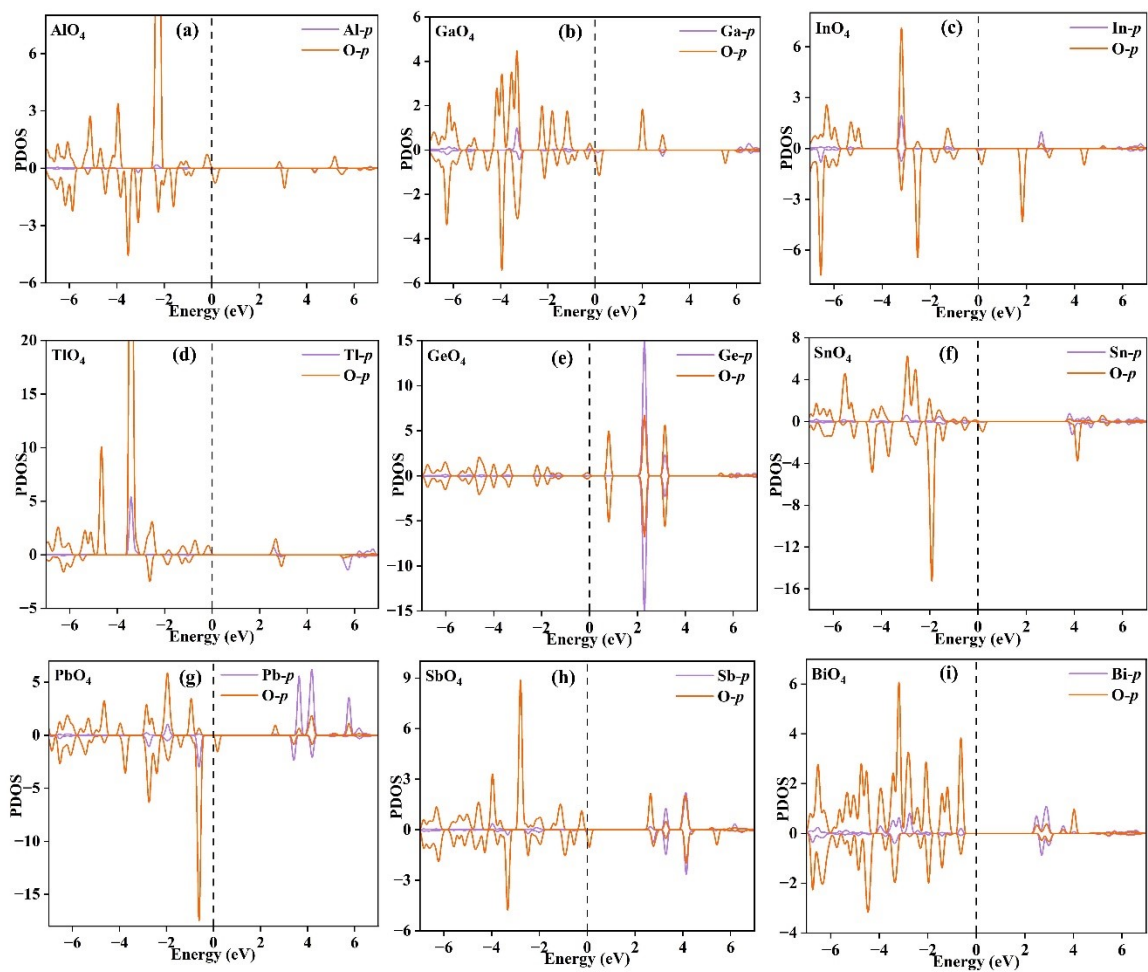
**Fig. S3** Calculated partial density of states (PDOS) for the  $p$  orbitals of N/O atoms and PM atoms for the designed  $\text{PMN}_1\text{O}_3$ -HADQ catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



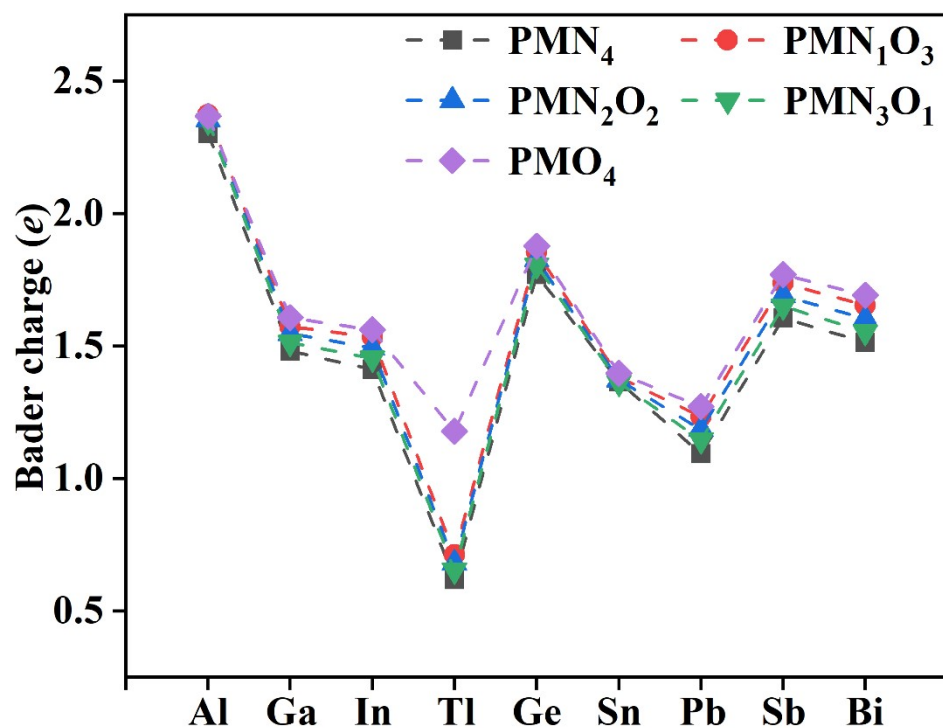
**Fig. S4** Calculated partial density of states (PDOS) for the  $p$  orbitals of N/O atoms and PM atoms for the designed PMN<sub>2</sub>O<sub>2</sub>-HADQ catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



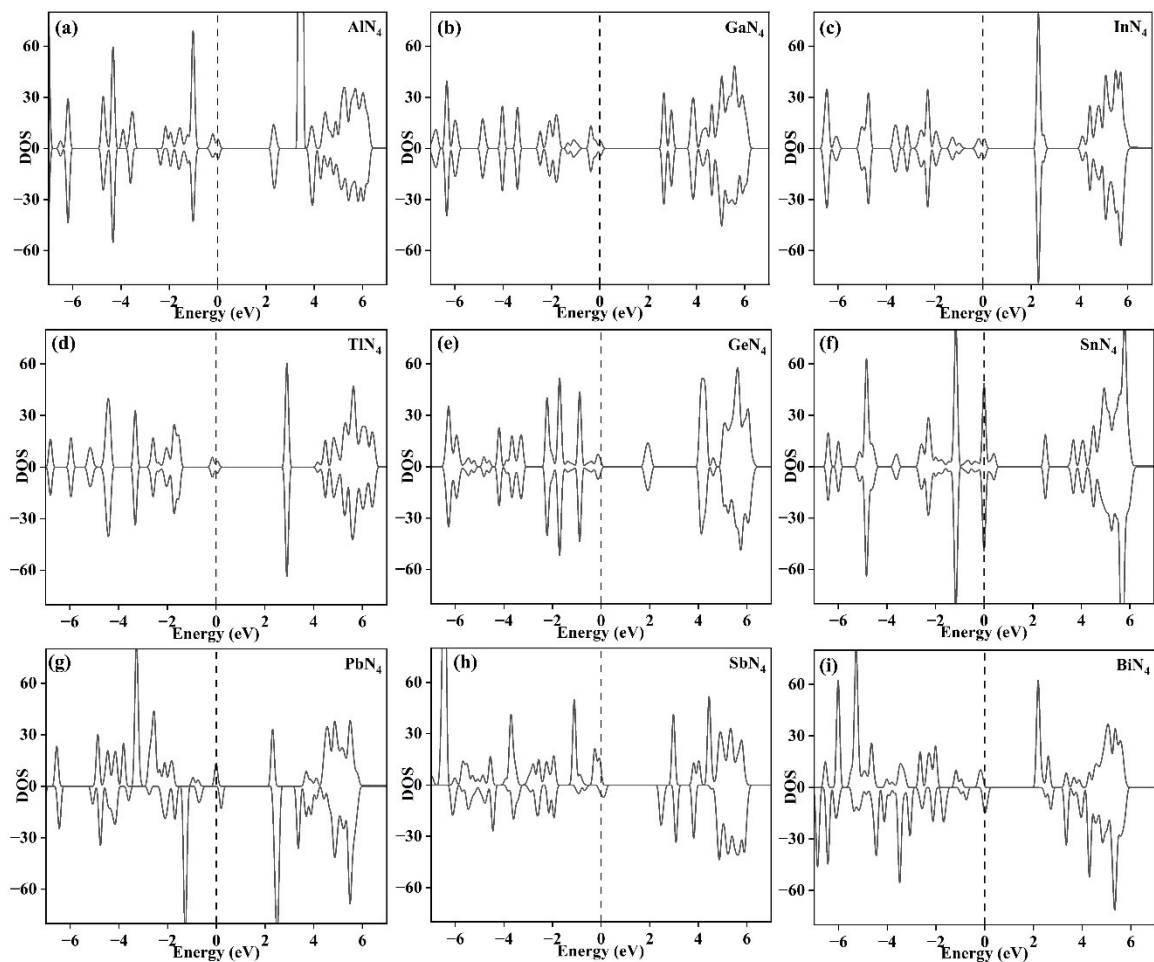
**Fig. S5** Calculated partial density of states (PDOS) for the  $p$  orbitals of N/O atoms and PM atoms for the designed  $\text{PMN}_3\text{O}_1$ -HADQ catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



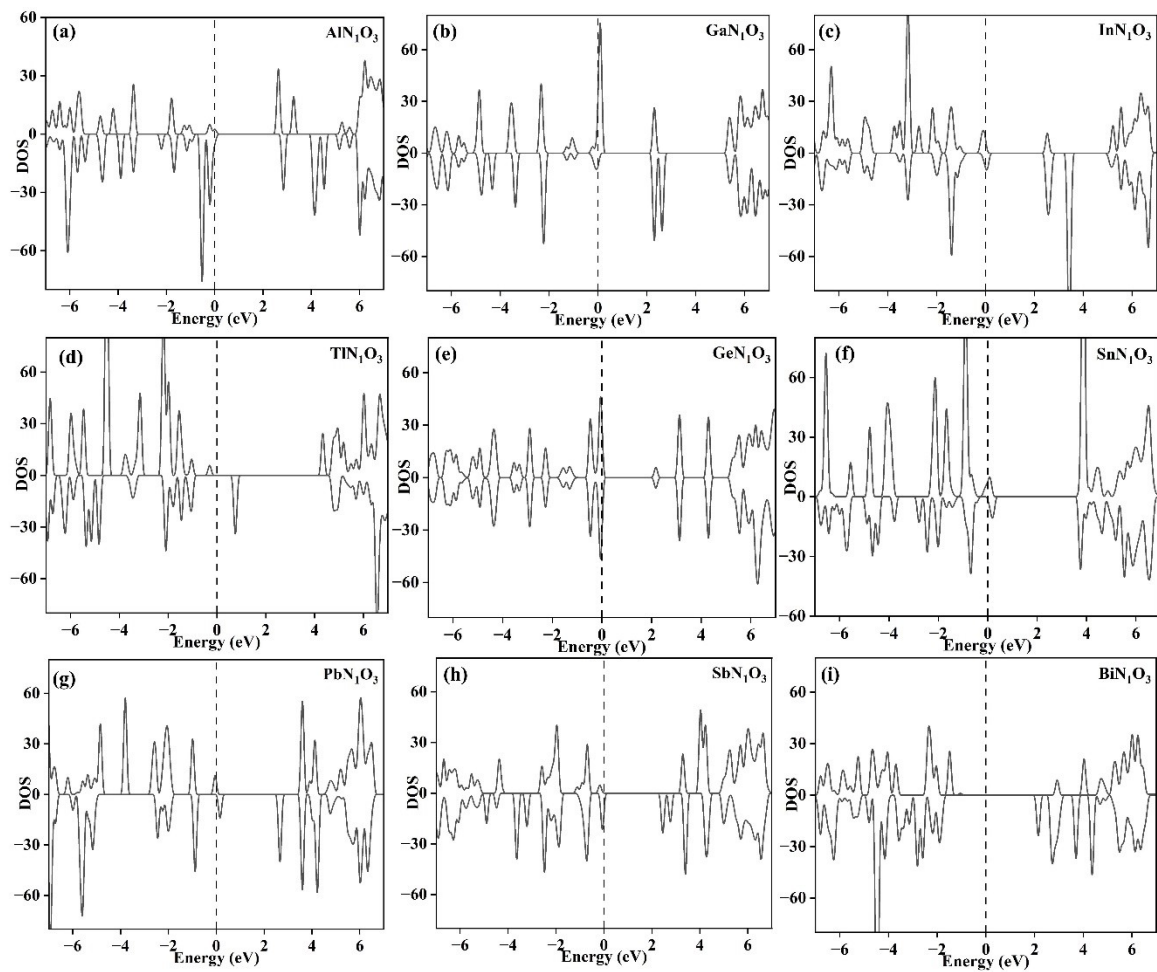
**Fig. S6** Calculated partial density of states (PDOS) for the  $p$  orbitals of O atoms and PM atoms for the designed  $\text{PMO}_4\text{-HADQ}$  catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



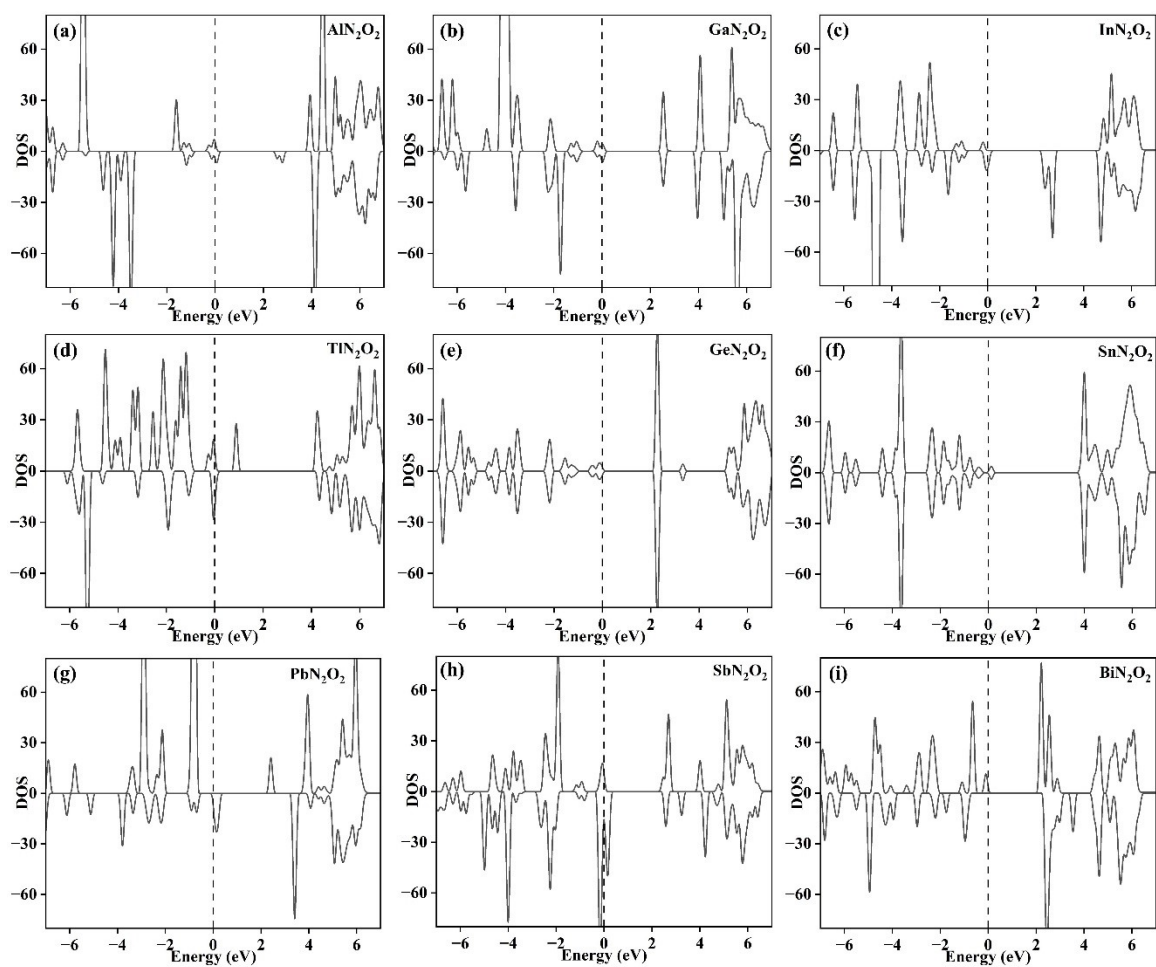
**Fig. S7** Calculated charge transfer from metal atoms to substrates of all the designed PMN<sub>x</sub>O<sub>4-x</sub>-HADQ catalysts based on Bader charge analysis. The positive value of Bader charge suggests that the charge is transferred from metal atoms to the substrates.



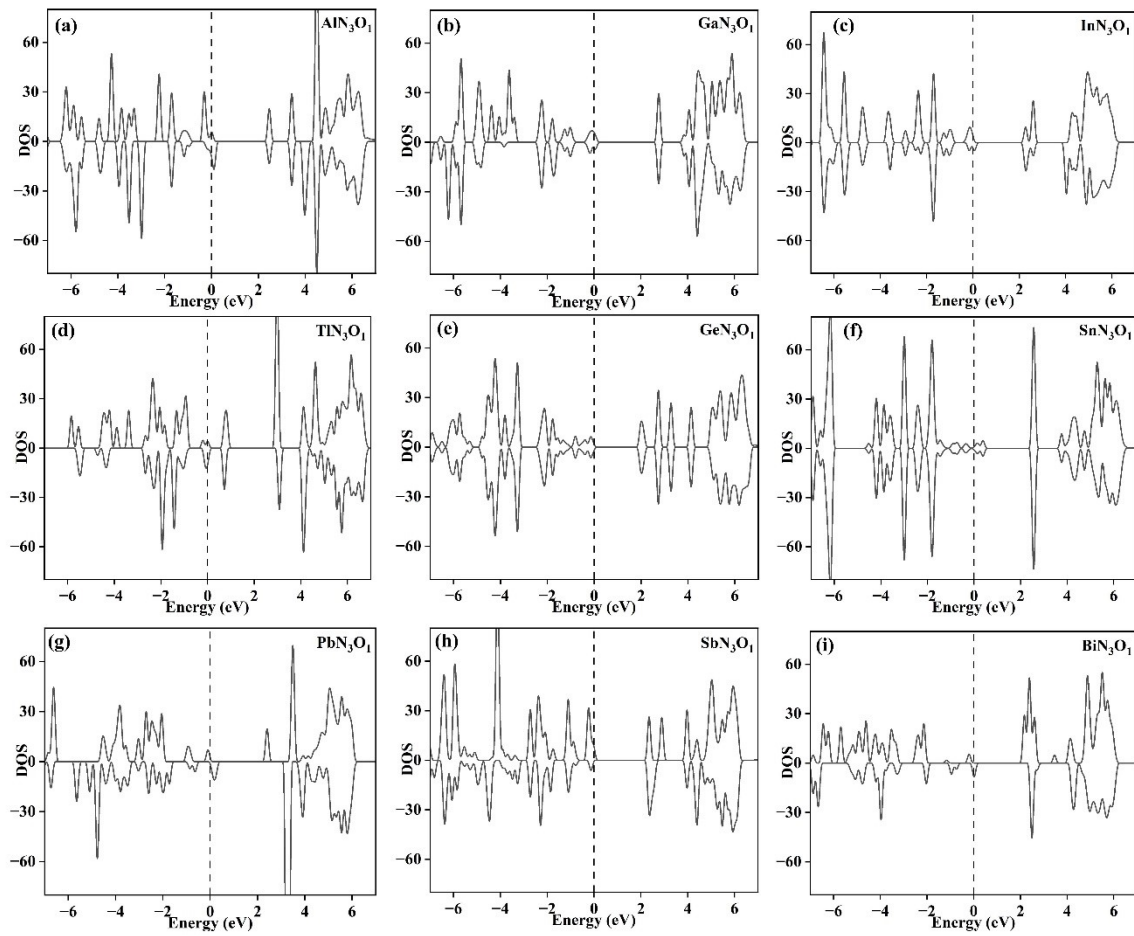
**Fig. S8** Calculated density of states (DOS) for the designed  $\text{PMN}_4$ -HADQ catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



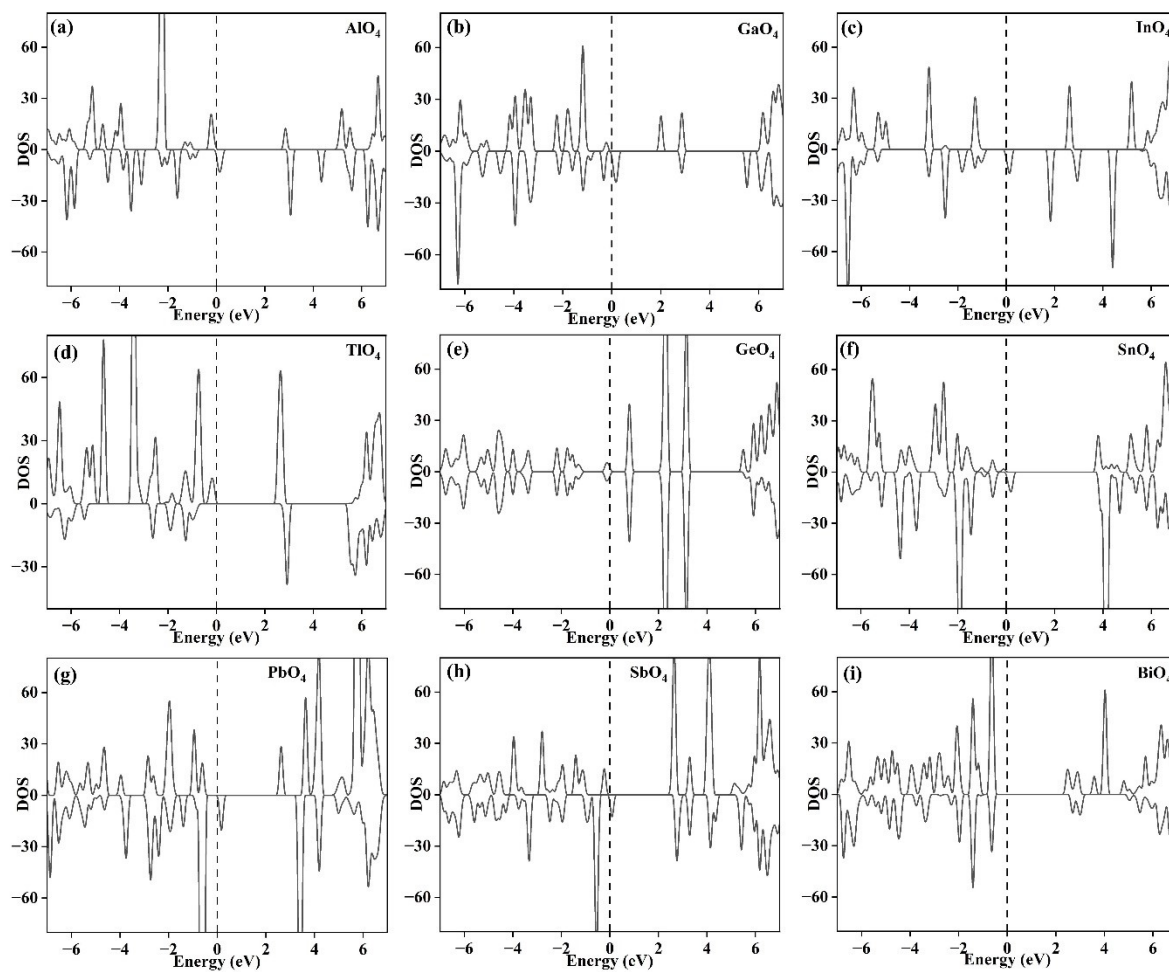
**Fig. S9** Calculated density of states (DOS) for the designed  $\text{PMN}_1\text{O}_3$ -HADQ catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



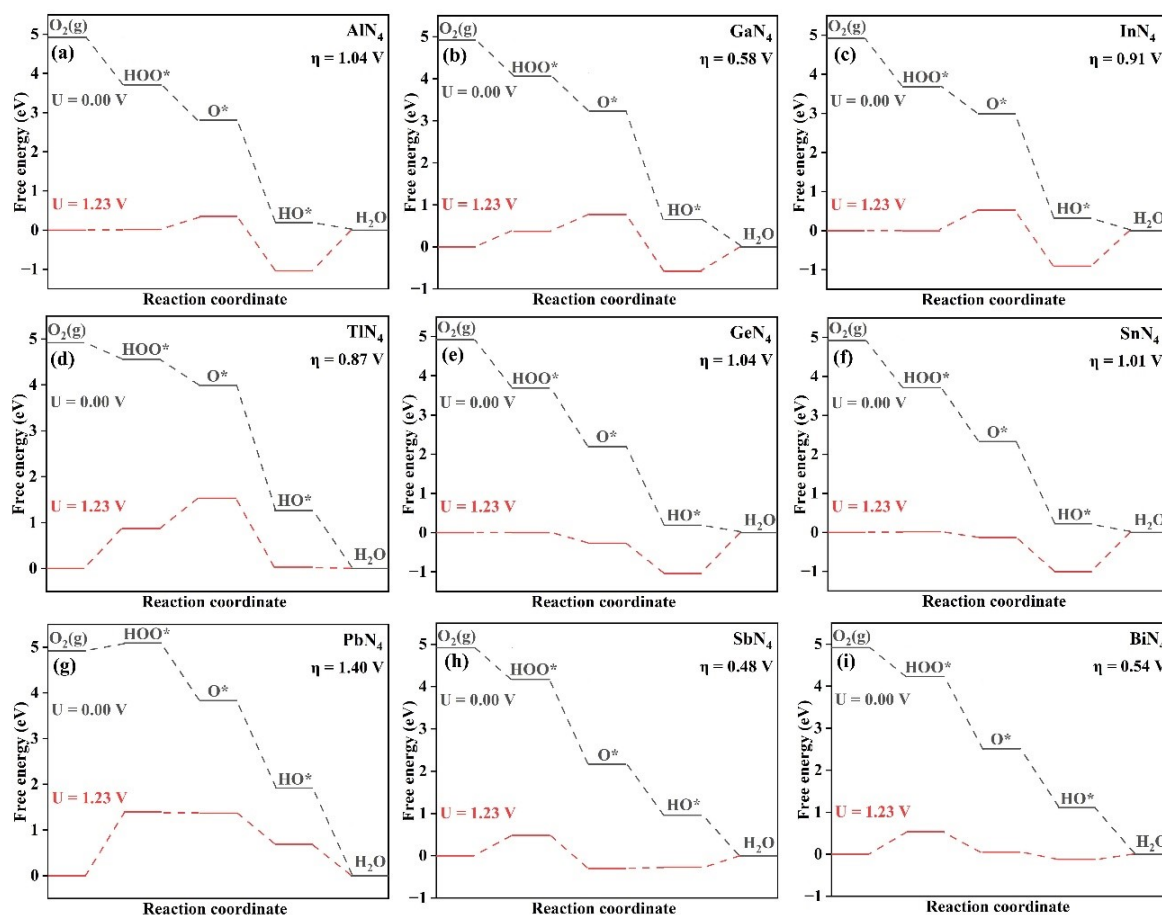
**Fig. S10** Calculated density of states (DOS) for the designed  $\text{PMN}_2\text{O}_2$ -HADQ catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



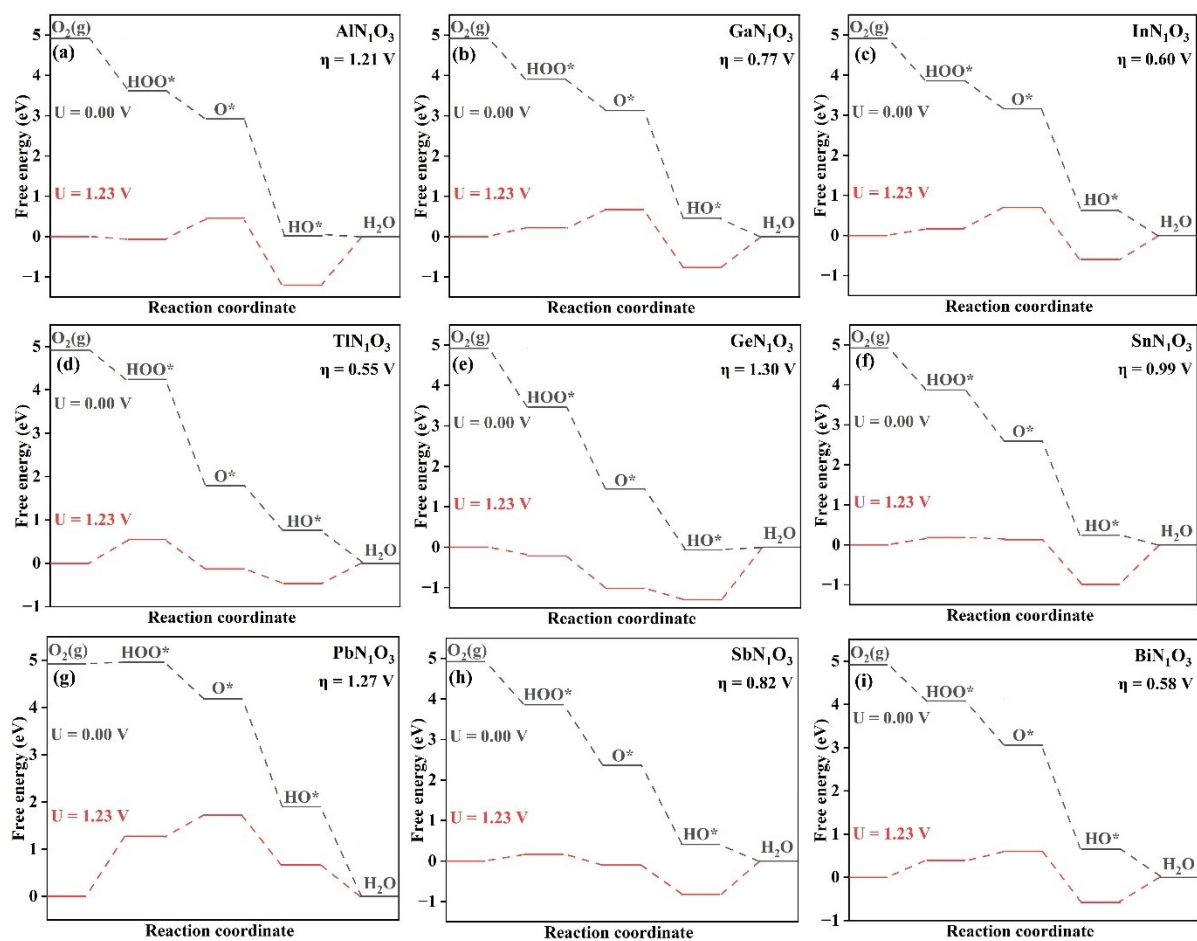
**Fig. S11** Calculated density of states (DOS) for the designed  $\text{PMN}_3\text{O}_1$ -HADQ catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



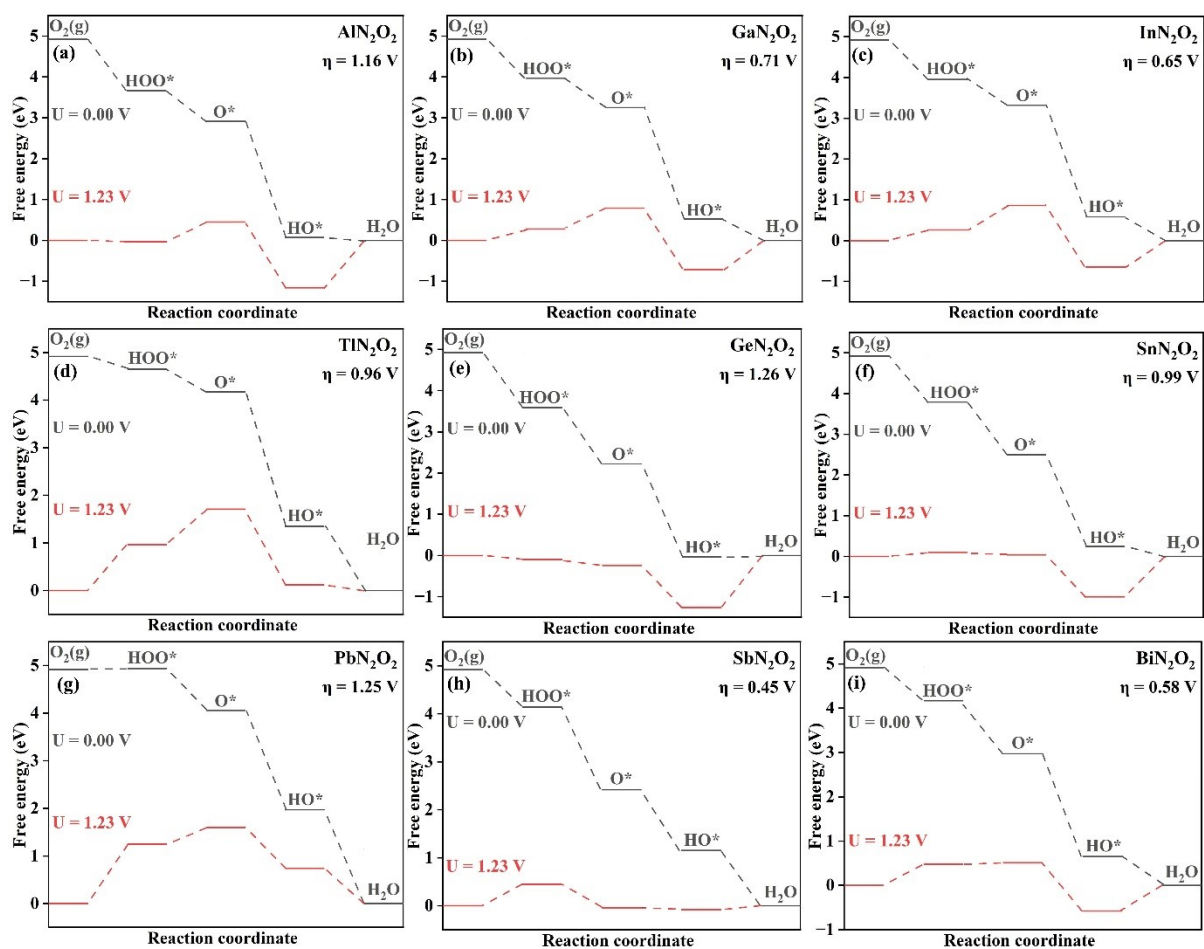
**Fig. S12** Calculated density of states (DOS) for the designed PMO<sub>4</sub>-HADQ catalysts. The Fermi level is set at the zero of energy (dashed line in figures).



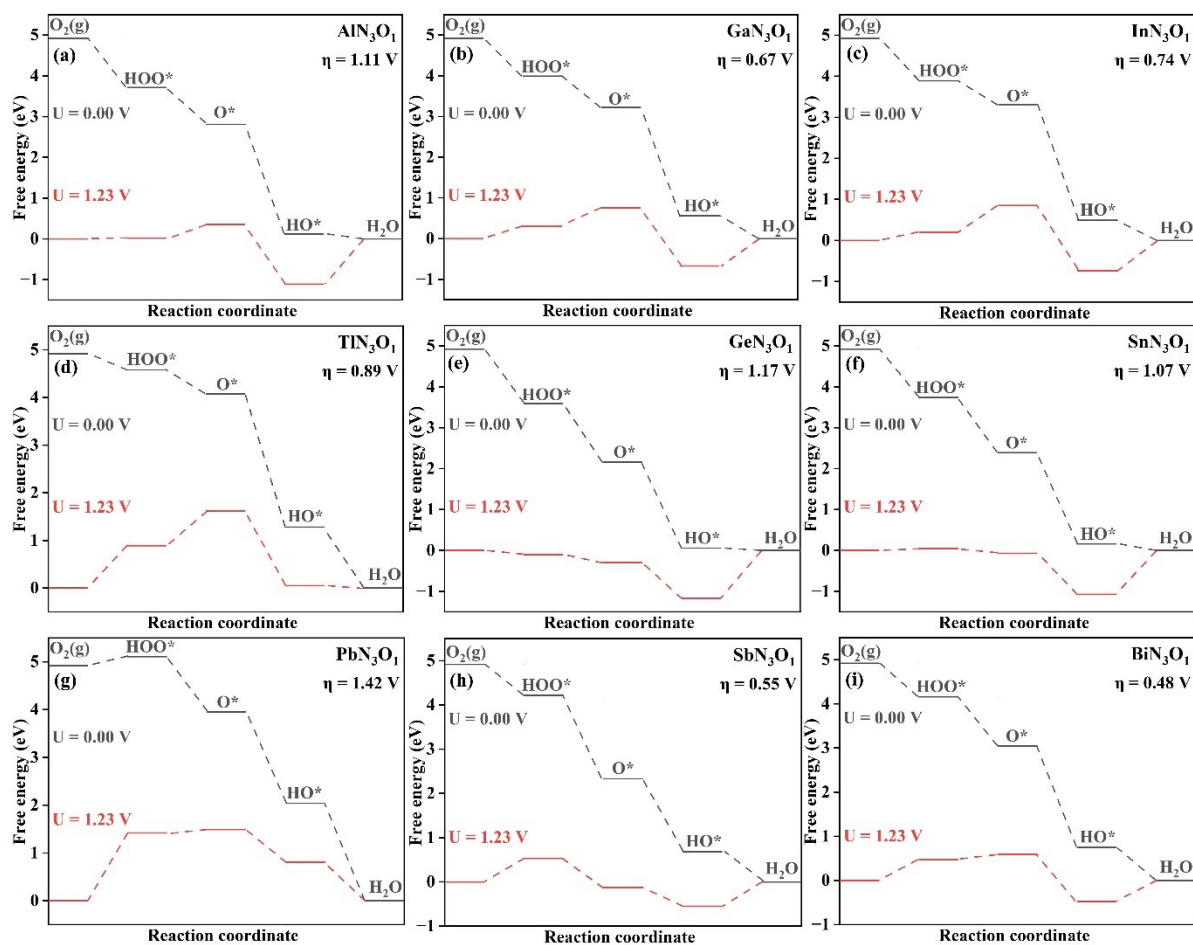
**Fig. S13** Calculated free energy diagrams of ORR on the designed PMN<sub>4</sub>-HADQ catalysts at U = 0 V (grey) and U = 1.23 V (red) under acid conditions.



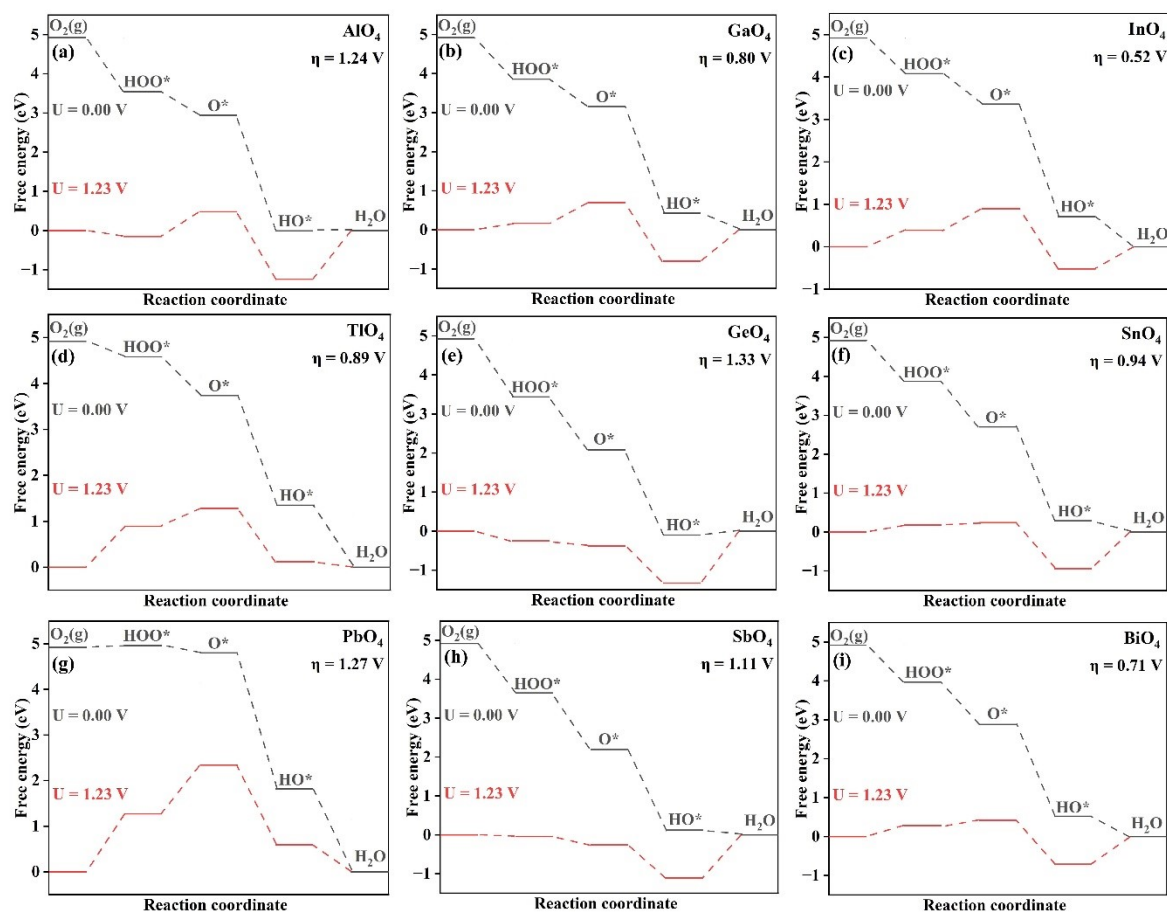
**Fig. S14** Calculated free energy diagrams of ORR on the designed  $PMN_1O_3$ -HADQ catalysts at  $U = 0$  V (grey) and  $U = 1.23$  V (red) under acid conditions.



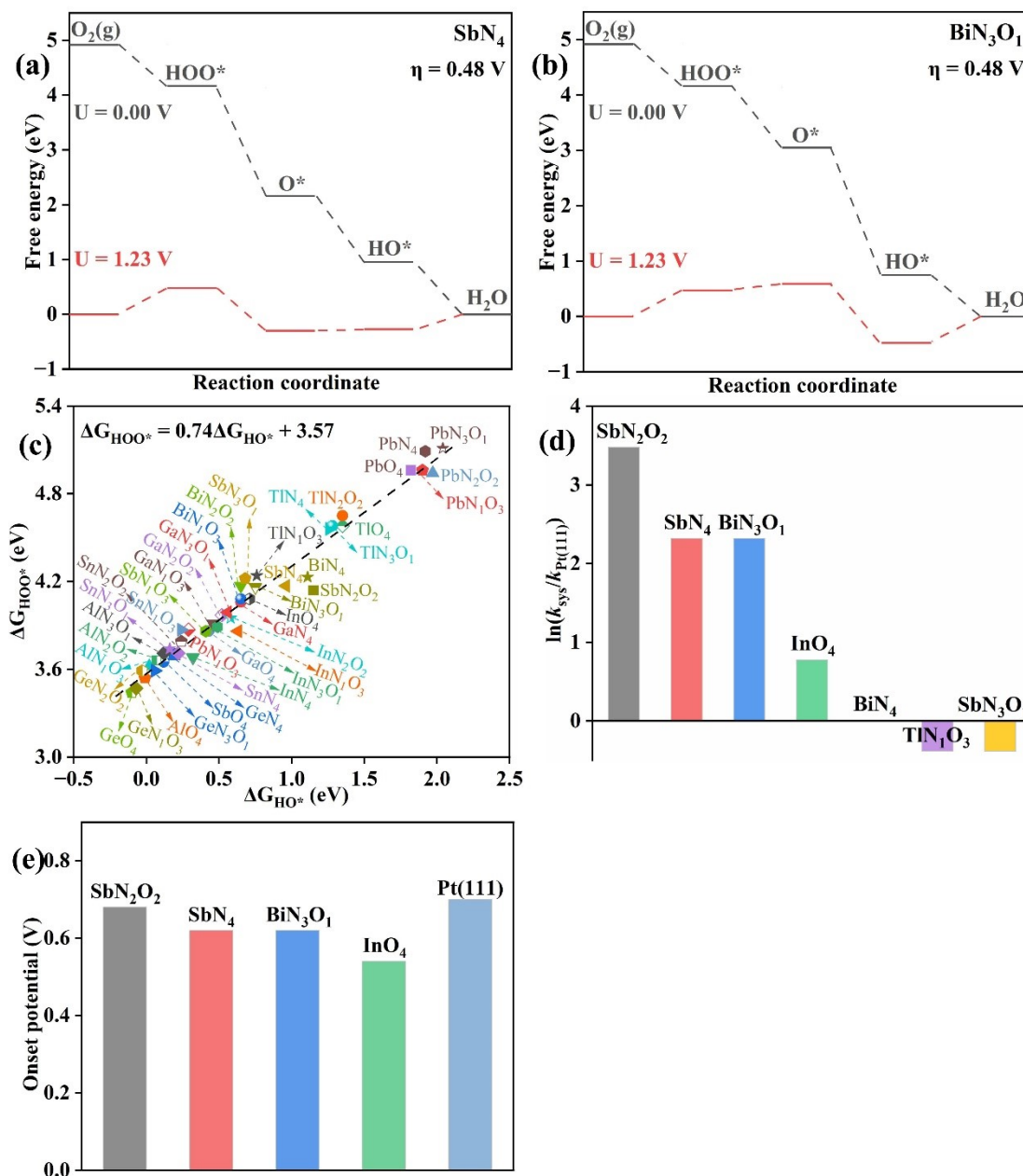
**Fig. S15** Calculated free energy diagrams of ORR on the designed  $\text{PMN}_2\text{O}_2$ -HADQ catalysts at  $U = 0 \text{ V}$  (grey) and  $U = 1.23 \text{ V}$  (red) under acid conditions.



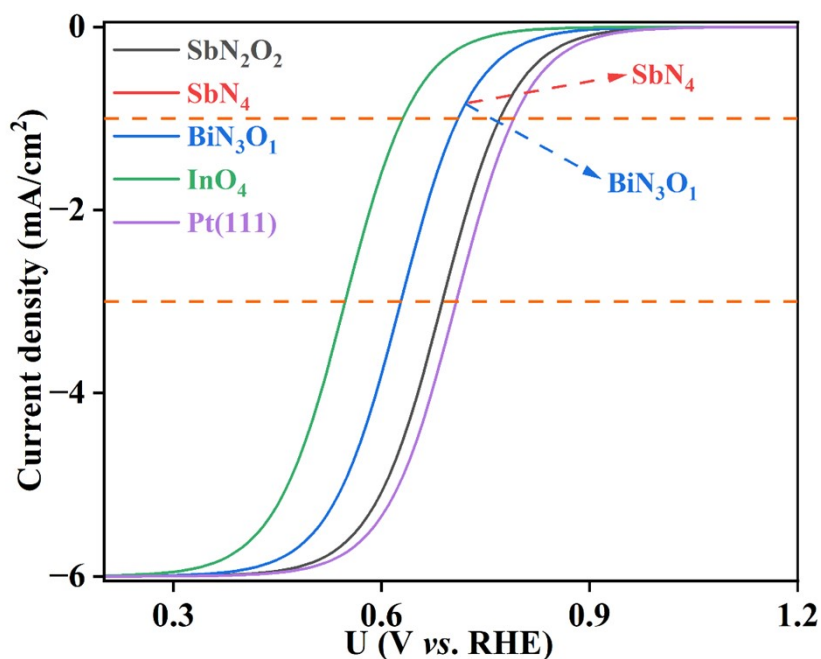
**Fig. S16** Calculated free energy diagrams of ORR on the designed PMN<sub>3</sub>O<sub>1</sub>-HADQ catalysts at U = 0 V (grey) and U = 1.23 V (red) under acid conditions.



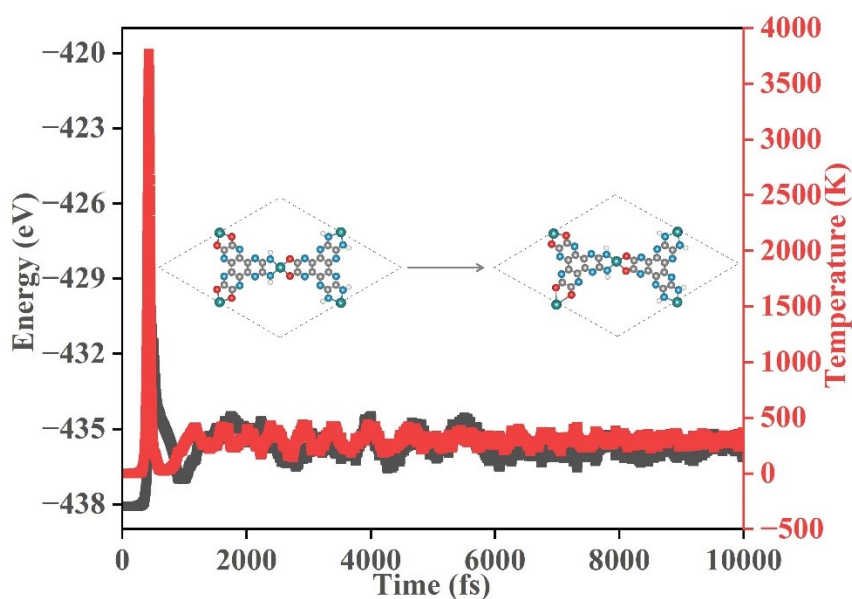
**Fig. S17** Calculated free energy diagrams of ORR on the designed  $PMO_4$ -HADQ catalysts at  $U = 0$  V (grey) and  $U = 1.23$  V (red) under acid conditions.



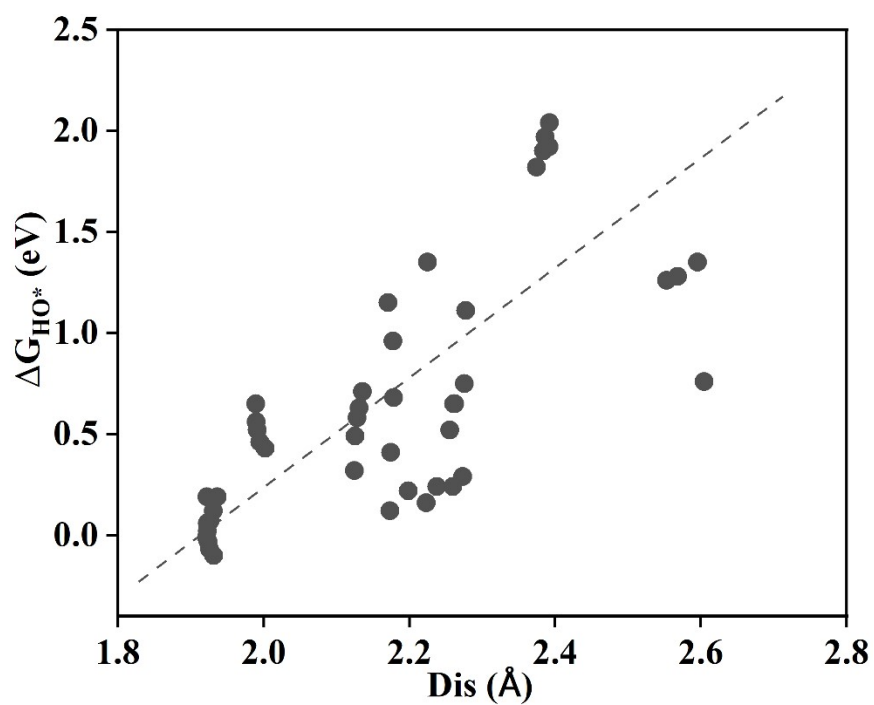
**Fig. S18** Calculated free energy diagrams of promising catalysts for the ORR (a) SbN<sub>4</sub>-HADQ, and (b) BiN<sub>3</sub>O<sub>1</sub>-HADQ, respectively. (c) Scaling relationship between  $\Delta G_{HO^*}$  and  $\Delta G_{HOO^*}$  on all the designed PMN<sub>x</sub>O<sub>4-x</sub>-HADQ catalysts. (d) Variation activity of the potential ORR electrocatalysts. (e) The corresponding half-wave potential of SbN<sub>2</sub>O<sub>2</sub>-HADQ, SbN<sub>4</sub>-HADQ, BiN<sub>3</sub>O<sub>1</sub>-HADQ, InO<sub>4</sub>-HADQ and Pt (111).



**Fig. S19** Theoretical polarization curves of SbN<sub>2</sub>O<sub>2</sub>-HADQ, SbN<sub>4</sub>-HADQ, BiN<sub>3</sub>O<sub>1</sub>-HADQ, InO<sub>4</sub>-HADQ and Pt (111).



**Fig. S20** Evolution of the total energy and temperature for the SbN<sub>2</sub>O<sub>2</sub>-HADQ, the time lasts for 10 ps at 300 K. The initial and final atomic configurations during the AIMD simulation are inserted.



**Fig. S21** Relationship between the adsorption Gibbs free energies of the key intermediate HO\* and the distance between PM and N/O atoms.

**Table S1** The feature values for descriptor identification study.

| System                           | AR   | PE    | Q <sub>PM</sub> | EA    | IP     | N  | Dis   |
|----------------------------------|------|-------|-----------------|-------|--------|----|-------|
| Al-N <sub>4</sub>                | 3.42 | 13.77 | 2.3031          | 0.441 | 64.104 | 13 | 1.936 |
| Ga-N <sub>4</sub>                | 3.6  | 13.97 | 1.4805          | 0.43  | 64.12  | 13 | 1.989 |
| Ge-N <sub>4</sub>                | 3.49 | 14.17 | 1.7704          | 1.23  | 66     | 14 | 1.922 |
| In-N <sub>4</sub>                | 3.8  | 13.94 | 1.4125          | 0.3   | 64.905 | 13 | 2.124 |
| Sn-N <sub>4</sub>                | 3.69 | 14.12 | 1.3646          | 1.11  | 65.462 | 14 | 2.198 |
| Sb-N <sub>4</sub>                | 3.57 | 14.21 | 1.6052          | 1.07  | 66.759 | 15 | 2.177 |
| Tl-N <sub>4</sub>                | 3.8  | 13.78 | 0.6186          | 0.2   | 64.226 | 13 | 2.553 |
| Pb-N <sub>4</sub>                | 3.78 | 14.49 | 1.0929          | 0.36  | 65.535 | 14 | 2.392 |
| Bi-N <sub>4</sub>                | 3.67 | 14.18 | 1.5131          | 0.946 | 65.407 | 15 | 2.277 |
| Al-O <sub>4</sub>                | 3.1  | 15.37 | 2.3677          | 6.285 | 60.44  | 17 | 1.922 |
| Ga-O <sub>4</sub>                | 3.28 | 15.57 | 1.6065          | 6.274 | 60.456 | 17 | 2.002 |
| Ge-O <sub>4</sub>                | 3.17 | 15.77 | 1.8773          | 7.074 | 62.336 | 18 | 1.931 |
| In-O <sub>4</sub>                | 3.48 | 15.54 | 1.5608          | 6.144 | 61.241 | 17 | 2.136 |
| Sn-O <sub>4</sub>                | 3.37 | 15.72 | 1.3969          | 6.954 | 61.798 | 18 | 2.273 |
| Sb-O <sub>4</sub>                | 3.25 | 15.81 | 1.7693          | 6.914 | 63.095 | 19 | 2.173 |
| Tl-O <sub>4</sub>                | 3.48 | 15.38 | 1.1773          | 6.044 | 60.562 | 17 | 2.225 |
| Pb-O <sub>4</sub>                | 3.46 | 16.09 | 1.2712          | 6.204 | 61.871 | 18 | 2.375 |
| Bi-O <sub>4</sub>                | 3.35 | 15.78 | 1.692           | 6.79  | 61.743 | 19 | 2.255 |
| Al-N <sub>1</sub> O <sub>3</sub> | 3.18 | 14.97 | 2.3739          | 4.824 | 61.356 | 16 | 1.923 |
| Ga-N <sub>1</sub> O <sub>3</sub> | 3.36 | 15.17 | 1.5736          | 4.813 | 61.372 | 16 | 1.995 |
| Ge-N <sub>1</sub> O <sub>3</sub> | 3.25 | 15.37 | 1.855           | 5.613 | 63.252 | 17 | 1.926 |
| In-N <sub>1</sub> O <sub>3</sub> | 3.56 | 15.14 | 1.5338          | 4.683 | 62.157 | 16 | 2.131 |
| Sn-N <sub>1</sub> O <sub>3</sub> | 3.45 | 15.32 | 1.3817          | 5.493 | 62.714 | 17 | 2.259 |
| Sb-N <sub>1</sub> O <sub>3</sub> | 3.33 | 15.41 | 1.7376          | 5.453 | 64.011 | 18 | 2.174 |
| Tl-N <sub>1</sub> O <sub>3</sub> | 3.56 | 14.98 | 0.7116          | 4.583 | 61.478 | 16 | 2.604 |
| Pb-N <sub>1</sub> O <sub>3</sub> | 3.54 | 15.69 | 1.2331          | 4.743 | 62.787 | 17 | 2.384 |
| Bi-N <sub>1</sub> O <sub>3</sub> | 3.43 | 15.38 | 1.654           | 5.329 | 62.659 | 18 | 2.261 |

|                                  |      |       |        |       |        |    |       |
|----------------------------------|------|-------|--------|-------|--------|----|-------|
| Al-N <sub>2</sub> O <sub>2</sub> | 3.26 | 14.57 | 2.3533 | 3.363 | 62.272 | 15 | 1.926 |
| Ga-N <sub>2</sub> O <sub>2</sub> | 3.44 | 14.77 | 1.5477 | 3.352 | 62.288 | 15 | 1.991 |
| Ge-N <sub>2</sub> O <sub>2</sub> | 3.33 | 14.97 | 1.8262 | 4.152 | 64.168 | 16 | 1.924 |
| In-N <sub>2</sub> O <sub>2</sub> | 3.64 | 14.74 | 1.4918 | 3.222 | 63.073 | 15 | 2.128 |
| Sn-N <sub>2</sub> O <sub>2</sub> | 3.53 | 14.92 | 1.3723 | 4.032 | 63.63  | 16 | 2.238 |
| Sb-N <sub>2</sub> O <sub>2</sub> | 3.41 | 15.01 | 1.6902 | 3.992 | 64.927 | 17 | 2.171 |
| Tl-N <sub>2</sub> O <sub>2</sub> | 3.64 | 14.58 | 0.6794 | 3.122 | 62.394 | 15 | 2.595 |
| Pb-N <sub>2</sub> O <sub>2</sub> | 3.62 | 15.29 | 1.1846 | 3.282 | 63.703 | 16 | 2.386 |
| Bi-N <sub>2</sub> O <sub>2</sub> | 3.51 | 14.98 | 1.6029 | 3.868 | 63.575 | 17 | 2.262 |
| Al-N <sub>3</sub> O <sub>1</sub> | 3.34 | 14.17 | 2.3492 | 1.902 | 63.188 | 14 | 1.931 |
| Ga-N <sub>3</sub> O <sub>1</sub> | 3.52 | 14.37 | 1.5129 | 1.891 | 63.204 | 14 | 1.989 |
| Ge-N <sub>3</sub> O <sub>1</sub> | 3.41 | 14.57 | 1.8047 | 2.691 | 65.084 | 15 | 1.922 |
| In-N <sub>3</sub> O <sub>1</sub> | 3.72 | 14.34 | 1.4533 | 1.761 | 63.989 | 14 | 2.126 |
| Sn-N <sub>3</sub> O <sub>1</sub> | 3.61 | 14.52 | 1.3613 | 2.571 | 64.546 | 15 | 2.223 |
| Sb-N <sub>3</sub> O <sub>1</sub> | 3.49 | 14.61 | 1.65   | 2.531 | 65.843 | 16 | 2.178 |
| Tl-N <sub>3</sub> O <sub>1</sub> | 3.72 | 14.18 | 0.6528 | 1.661 | 63.31  | 14 | 2.568 |
| Pb-N <sub>3</sub> O <sub>1</sub> | 3.70 | 14.89 | 1.1447 | 1.821 | 64.619 | 15 | 2.392 |
| Bi-N <sub>3</sub> O <sub>1</sub> | 3.59 | 14.58 | 1.5529 | 2.407 | 64.491 | 16 | 2.275 |

### The coordination of the designed promising PMN<sub>x</sub>O<sub>4-x</sub>-HADQ ORR catalysts

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# CRYSTAL DATA

#-----

data\_VESTA\_phase\_1

\_pd\_phase\_name 'SbN2O2'

\_cell\_length\_a 21.89000

\_cell\_length\_b 21.89000

\_cell\_length\_c 20.00000

\_cell\_angle\_alpha 90

\_cell\_angle\_beta 90

\_cell\_angle\_gamma 120

\_symmetry\_space\_group\_name\_H-M 'P 1'

\_symmetry\_Int\_Tables\_number 1

```

loop_
_symmetry_equiv_pos_as_xyz
  'x, y, z'

```

```

loop_
  _atom_site_label
  _atom_site_occupancy
  _atom_site_fract_x
  _atom_site_fract_y
  _atom_site_fract_z
  _atom_site_adp_type
  _atom_site_B_iso_or_equiv
  _atom_site_type_symbol
H1      1.0      0.566107      0.645554      0.202764      Biso  1.000000 H
H2      1.0      0.643847      0.077382      0.202014      Biso  1.000000 H
H3      1.0      0.918924      0.565748      0.203157      Biso  1.000000 H
H4      1.0      0.354556      0.433911      0.202438      Biso  1.000000 H
H5      1.0      0.922591      0.356088      0.201991      Biso  1.000000 H
H6      1.0      0.434232      0.081087      0.203244      Biso  1.000000 H
N1      1.0      0.480950      0.081188      0.200992      Biso  1.000000 N
N2      1.0      0.920780      0.401788      0.200398      Biso  1.000000 N
N3      1.0      0.400782      0.480986      0.200340      Biso  1.000000 N
N4      1.0      0.918776      0.519000      0.200946      Biso  1.000000 N
N5      1.0      0.598132      0.079171      0.200386      Biso  1.000000 N
N6      1.0      0.519065      0.599302      0.200524      Biso  1.000000 N
N7      1.0      0.667492      0.204602      0.195263      Biso  1.000000 N
N8      1.0      0.333138      0.794775      0.195247      Biso  1.000000 N
N9      1.0      0.793777      0.461725      0.195647      Biso  1.000000 N
N10     1.0      0.204224      0.537194      0.196623      Biso  1.000000 N
N11     1.0      0.537511      0.333169      0.196265      Biso  1.000000 N
N12     1.0      0.462440      0.667804      0.195802      Biso  1.000000 N
N13     1.0      0.205391      0.667038      0.195413      Biso  1.000000 N
N14     1.0      0.795354      0.332454      0.195251      Biso  1.000000 N
N15     1.0      0.462913      0.795807      0.196865      Biso  1.000000 N
N16     1.0      0.538213      0.206190      0.195675      Biso  1.000000 N
N17     1.0      0.332231      0.537600      0.195635      Biso  1.000000 N
N18     1.0      0.666622      0.462328      0.196045      Biso  1.000000 N
O1      1.0      0.520092      0.918537      0.201977      Biso  1.000000 O
O2      1.0      0.082987      0.602589      0.200839      Biso  1.000000 O
O3      1.0      0.601496      0.519863      0.201379      Biso  1.000000 O
O4      1.0      0.081484      0.480132      0.201593      Biso  1.000000 O
O5      1.0      0.397677      0.917182      0.200489      Biso  1.000000 O
O6      1.0      0.479938      0.398224      0.201625      Biso  1.000000 O
C1      1.0      0.539140      0.145207      0.197277      Biso  1.000000 C

```

|     |     |          |          |          |      |             |
|-----|-----|----------|----------|----------|------|-------------|
| C2  | 1.0 | 0.461126 | 0.855094 | 0.198129 | Biso | 1.000000 C  |
| C3  | 1.0 | 0.855245 | 0.394007 | 0.197031 | Biso | 1.000000 C  |
| C4  | 1.0 | 0.145248 | 0.605741 | 0.197309 | Biso | 1.000000 C  |
| C5  | 1.0 | 0.605371 | 0.460823 | 0.197648 | Biso | 1.000000 C  |
| C6  | 1.0 | 0.393978 | 0.538944 | 0.197114 | Biso | 1.000000 C  |
| C7  | 1.0 | 0.144959 | 0.539037 | 0.197921 | Biso | 1.000000 C  |
| C8  | 1.0 | 0.854753 | 0.460787 | 0.197264 | Biso | 1.000000 C  |
| C9  | 1.0 | 0.394458 | 0.854867 | 0.197187 | Biso | 1.000000 C  |
| C10 | 1.0 | 0.605924 | 0.144708 | 0.197033 | Biso | 1.000000 C  |
| C11 | 1.0 | 0.461080 | 0.606041 | 0.197197 | Biso | 1.000000 C  |
| C12 | 1.0 | 0.538986 | 0.394409 | 0.197760 | Biso | 1.000000 C  |
| C13 | 1.0 | 0.600424 | 0.266887 | 0.194251 | Biso | 1.000000 C  |
| C14 | 1.0 | 0.400089 | 0.733712 | 0.194720 | Biso | 1.000000 C  |
| C15 | 1.0 | 0.733366 | 0.332965 | 0.193965 | Biso | 1.000000 C  |
| C16 | 1.0 | 0.266604 | 0.665623 | 0.194228 | Biso | 1.000000 C  |
| C17 | 1.0 | 0.665416 | 0.399552 | 0.194518 | Biso | 1.000000 C  |
| C18 | 1.0 | 0.333108 | 0.599829 | 0.194381 | Biso | 1.000000 C  |
| C19 | 1.0 | 0.266363 | 0.600006 | 0.194646 | Biso | 1.000000 C  |
| C20 | 1.0 | 0.733069 | 0.399517 | 0.194221 | Biso | 1.000000 C  |
| C21 | 1.0 | 0.334506 | 0.733532 | 0.194177 | Biso | 1.000000 C  |
| C22 | 1.0 | 0.667001 | 0.266602 | 0.193976 | Biso | 1.000000 C  |
| C23 | 1.0 | 0.400221 | 0.666943 | 0.194445 | Biso | 1.000000 C  |
| C24 | 1.0 | 0.600323 | 0.334467 | 0.194587 | Biso | 1.000000 C  |
| Sb1 | 1.0 | 0.498574 | 0.996819 | 0.240703 | Biso | 1.000000 Sb |
| Sb2 | 1.0 | 0.003126 | 0.501377 | 0.240626 | Biso | 1.000000 Sb |
| Sb3 | 1.0 | 0.501451 | 0.498525 | 0.240719 | Biso | 1.000000 Sb |

#=====

# CRYSTAL DATA

#-----

data\_VESTA\_phase\_1

|                                |          |
|--------------------------------|----------|
| _pd_phase_name                 | 'SbN4'   |
| _cell_length_a                 | 21.89000 |
| _cell_length_b                 | 21.89000 |
| _cell_length_c                 | 20.00000 |
| _cell_angle_alpha              | 90       |
| _cell_angle_beta               | 90       |
| _cell_angle_gamma              | 120      |
| _symmetry_space_group_name_H-M | 'P 1'    |
| _symmetry_Int_Tables_number    | 1        |

loop\_

\_symmetry\_equiv\_pos\_as\_xyz

'x, y, z'

loop\_

\_atom\_site\_label

\_atom\_site\_occupancy

\_atom\_site\_fract\_x

\_atom\_site\_fract\_y

\_atom\_site\_fract\_z

\_atom\_site\_adp\_type

\_atom\_site\_B\_iso\_or\_equiv

\_atom\_site\_type\_symbol

|     |     |          |          |          |      |            |
|-----|-----|----------|----------|----------|------|------------|
| H1  | 1.0 | 0.565046 | 0.645948 | 0.195504 | Biso | 1.000000 H |
| H2  | 1.0 | 0.434946 | 0.354041 | 0.195518 | Biso | 1.000000 H |
| H3  | 1.0 | 0.354004 | 0.919065 | 0.195776 | Biso | 1.000000 H |
| H4  | 1.0 | 0.646015 | 0.080943 | 0.195783 | Biso | 1.000000 H |
| H5  | 1.0 | 0.081057 | 0.434963 | 0.195057 | Biso | 1.000000 H |
| H6  | 1.0 | 0.918977 | 0.565038 | 0.195025 | Biso | 1.000000 H |
| H7  | 1.0 | 0.646056 | 0.565045 | 0.195131 | Biso | 1.000000 H |
| H8  | 1.0 | 0.353913 | 0.434968 | 0.195167 | Biso | 1.000000 H |
| H9  | 1.0 | 0.919109 | 0.354043 | 0.195511 | Biso | 1.000000 H |
| H10 | 1.0 | 0.080865 | 0.645928 | 0.195473 | Biso | 1.000000 H |
| H11 | 1.0 | 0.434955 | 0.080935 | 0.195785 | Biso | 1.000000 H |
| H12 | 1.0 | 0.565061 | 0.919071 | 0.195793 | Biso | 1.000000 H |
| N1  | 1.0 | 0.481294 | 0.080620 | 0.200164 | Biso | 1.000000 N |
| N2  | 1.0 | 0.518716 | 0.919376 | 0.200169 | Biso | 1.000000 N |
| N3  | 1.0 | 0.919404 | 0.400718 | 0.199471 | Biso | 1.000000 N |
| N4  | 1.0 | 0.080591 | 0.599265 | 0.199426 | Biso | 1.000000 N |
| N5  | 1.0 | 0.599368 | 0.518709 | 0.199279 | Biso | 1.000000 N |
| N6  | 1.0 | 0.400611 | 0.481294 | 0.199317 | Biso | 1.000000 N |
| N7  | 1.0 | 0.080675 | 0.481284 | 0.199245 | Biso | 1.000000 N |
| N8  | 1.0 | 0.919336 | 0.518706 | 0.199233 | Biso | 1.000000 N |
| N9  | 1.0 | 0.400656 | 0.919380 | 0.200164 | Biso | 1.000000 N |
| N10 | 1.0 | 0.599361 | 0.080626 | 0.200141 | Biso | 1.000000 N |
| N11 | 1.0 | 0.518669 | 0.599275 | 0.199477 | Biso | 1.000000 N |
| N12 | 1.0 | 0.481320 | 0.400721 | 0.199487 | Biso | 1.000000 N |
| N13 | 1.0 | 0.667789 | 0.205605 | 0.205294 | Biso | 1.000000 N |
| N14 | 1.0 | 0.332219 | 0.794396 | 0.205297 | Biso | 1.000000 N |
| N15 | 1.0 | 0.794378 | 0.462155 | 0.204924 | Biso | 1.000000 N |
| N16 | 1.0 | 0.205636 | 0.537855 | 0.204928 | Biso | 1.000000 N |
| N17 | 1.0 | 0.537810 | 0.332236 | 0.205051 | Biso | 1.000000 N |
| N18 | 1.0 | 0.462186 | 0.667767 | 0.205063 | Biso | 1.000000 N |
| N19 | 1.0 | 0.205568 | 0.667769 | 0.205047 | Biso | 1.000000 N |
| N20 | 1.0 | 0.794426 | 0.332224 | 0.205069 | Biso | 1.000000 N |
| N21 | 1.0 | 0.462158 | 0.794390 | 0.205309 | Biso | 1.000000 N |
| N22 | 1.0 | 0.537840 | 0.205602 | 0.205291 | Biso | 1.000000 N |

|     |     |          |          |          |      |             |
|-----|-----|----------|----------|----------|------|-------------|
| N23 | 1.0 | 0.332213 | 0.537856 | 0.204936 | Biso | 1.000000 N  |
| N24 | 1.0 | 0.667777 | 0.462158 | 0.204926 | Biso | 1.000000 N  |
| C1  | 1.0 | 0.539524 | 0.145678 | 0.203820 | Biso | 1.000000 C  |
| C2  | 1.0 | 0.460484 | 0.854320 | 0.203831 | Biso | 1.000000 C  |
| C3  | 1.0 | 0.854335 | 0.393842 | 0.203247 | Biso | 1.000000 C  |
| C4  | 1.0 | 0.145670 | 0.606152 | 0.203213 | Biso | 1.000000 C  |
| C5  | 1.0 | 0.606182 | 0.460493 | 0.203173 | Biso | 1.000000 C  |
| C6  | 1.0 | 0.393804 | 0.539515 | 0.203193 | Biso | 1.000000 C  |
| C7  | 1.0 | 0.145700 | 0.539513 | 0.203158 | Biso | 1.000000 C  |
| C8  | 1.0 | 0.854308 | 0.460486 | 0.203166 | Biso | 1.000000 C  |
| C9  | 1.0 | 0.393828 | 0.854324 | 0.203825 | Biso | 1.000000 C  |
| C10 | 1.0 | 0.606185 | 0.145679 | 0.203814 | Biso | 1.000000 C  |
| C11 | 1.0 | 0.460473 | 0.606154 | 0.203257 | Biso | 1.000000 C  |
| C12 | 1.0 | 0.539516 | 0.393849 | 0.203251 | Biso | 1.000000 C  |
| C13 | 1.0 | 0.600531 | 0.266900 | 0.207270 | Biso | 1.000000 C  |
| C14 | 1.0 | 0.399470 | 0.733100 | 0.207285 | Biso | 1.000000 C  |
| C15 | 1.0 | 0.733139 | 0.333631 | 0.207178 | Biso | 1.000000 C  |
| C16 | 1.0 | 0.266862 | 0.666375 | 0.207172 | Biso | 1.000000 C  |
| C17 | 1.0 | 0.666349 | 0.399463 | 0.207119 | Biso | 1.000000 C  |
| C18 | 1.0 | 0.333649 | 0.600552 | 0.207127 | Biso | 1.000000 C  |
| C19 | 1.0 | 0.266894 | 0.600553 | 0.207118 | Biso | 1.000000 C  |
| C20 | 1.0 | 0.733112 | 0.399461 | 0.207119 | Biso | 1.000000 C  |
| C21 | 1.0 | 0.333615 | 0.733103 | 0.207281 | Biso | 1.000000 C  |
| C22 | 1.0 | 0.666385 | 0.266897 | 0.207280 | Biso | 1.000000 C  |
| C23 | 1.0 | 0.399499 | 0.666376 | 0.207180 | Biso | 1.000000 C  |
| C24 | 1.0 | 0.600502 | 0.333632 | 0.207164 | Biso | 1.000000 C  |
| Sb1 | 1.0 | 0.500015 | 0.000002 | 0.157572 | Biso | 1.000000 Sb |
| Sb2 | 1.0 | 0.000004 | 0.499984 | 0.156462 | Biso | 1.000000 Sb |
| Sb3 | 1.0 | 0.499993 | 0.500004 | 0.156501 | Biso | 1.000000 Sb |

#=====

# # CRYSTAL DATA

#-----

```

data_VESTA_phase_1
_pd_phase_name          'BiN3O1'
_cell_length_a          21.89000
_cell_length_b          21.89000
_cell_length_c          20.00000
_cell_angle_alpha       90
_cell_angle_beta        90
_cell_angle_gamma       120
_symmetry_space_group_name_H-M  'P 1'
_symmetry_Int_Tables_number  1

```

```

loop_
_symmetry_equiv_pos_as_xyz
  'x, y, z'

```

```

loop_
  _atom_site_label
  _atom_site_occupancy
  _atom_site_fract_x
  _atom_site_fract_y
  _atom_site_fract_z
  _atom_site_adp_type
  _atom_site_B_iso_or_equiv
  _atom_site_type_symbol
H1      1.0      0.435446      0.342734      0.173349      Biso  1.000000 H
H2      1.0      0.340026      0.907002      0.173801      Biso  1.000000 H
H3      1.0      0.093853      0.434151      0.171237      Biso  1.000000 H
H4      1.0      0.639386      0.561683      0.212993      Biso  1.000000 H
H5      1.0      0.362585      0.441927      0.213851      Biso  1.000000 H
H6      1.0      0.918828      0.359506      0.215449      Biso  1.000000 H
H7      1.0      0.075903      0.636373      0.210042      Biso  1.000000 H
H8      1.0      0.439329      0.078471      0.213322      Biso  1.000000 H
H9      1.0      0.558855      0.921406      0.212558      Biso  1.000000 H
N1      1.0      0.486177      0.079489      0.207691      Biso  1.000000 N
N2      1.0      0.511905      0.920809      0.209332      Biso  1.000000 N
N3      1.0      0.919410      0.406367      0.211046      Biso  1.000000 N
N4      1.0      0.077881      0.590853      0.206397      Biso  1.000000 N
N5      1.0      0.593228      0.514650      0.209515      Biso  1.000000 N
N6      1.0      0.408750      0.488704      0.209153      Biso  1.000000 N
N7      1.0      0.087801      0.476806      0.180228      Biso  1.000000 N
N8      1.0      0.388672      0.912875      0.182873      Biso  1.000000 N
N9      1.0      0.478279      0.391383      0.182266      Biso  1.000000 N
N10     1.0      0.671824      0.208747      0.199050      Biso  1.000000 N
N11     1.0      0.325856      0.790422      0.201805      Biso  1.000000 N
N12     1.0      0.792255      0.464833      0.201143      Biso  1.000000 N
N13     1.0      0.210095      0.536886      0.200746      Biso  1.000000 N
N14     1.0      0.537289      0.328099      0.201828      Biso  1.000000 N
N15     1.0      0.464936      0.673893      0.200666      Biso  1.000000 N
N16     1.0      0.202127      0.662090      0.211132      Biso  1.000000 N
N17     1.0      0.795508      0.336950      0.211575      Biso  1.000000 N
N18     1.0      0.458839      0.796962      0.211263      Biso  1.000000 N
N19     1.0      0.540482      0.203827      0.211310      Biso  1.000000 N
N20     1.0      0.338353      0.542242      0.211547      Biso  1.000000 N
N21     1.0      0.663547      0.460744      0.212024      Biso  1.000000 N
O1      1.0      0.912472      0.522978      0.183146      Biso  1.000000 O

```

|     |     |           |          |          |      |             |
|-----|-----|-----------|----------|----------|------|-------------|
| O2  | 1.0 | 0.610632  | 0.088966 | 0.178872 | Biso | 1.000000 O  |
| O3  | 1.0 | 0.524698  | 0.613300 | 0.182921 | Biso | 1.000000 O  |
| C1  | 1.0 | 0.544254  | 0.145275 | 0.205825 | Biso | 1.000000 C  |
| C2  | 1.0 | 0.454670  | 0.855545 | 0.207193 | Biso | 1.000000 C  |
| C3  | 1.0 | 0.854769  | 0.399658 | 0.207944 | Biso | 1.000000 C  |
| C4  | 1.0 | 0.144178  | 0.599733 | 0.205664 | Biso | 1.000000 C  |
| C5  | 1.0 | 0.601345  | 0.457038 | 0.207436 | Biso | 1.000000 C  |
| C6  | 1.0 | 0.401247  | 0.546490 | 0.206995 | Biso | 1.000000 C  |
| C7  | 1.0 | 0.148287  | 0.535444 | 0.196018 | Biso | 1.000000 C  |
| C8  | 1.0 | 0.852760  | 0.465316 | 0.197508 | Biso | 1.000000 C  |
| C9  | 1.0 | 0.386090  | 0.851918 | 0.197567 | Biso | 1.000000 C  |
| C10 | 1.0 | 0.611710  | 0.148009 | 0.194912 | Biso | 1.000000 C  |
| C11 | 1.0 | 0.466172  | 0.614311 | 0.197001 | Biso | 1.000000 C  |
| C12 | 1.0 | 0.536447  | 0.388853 | 0.197529 | Biso | 1.000000 C  |
| C13 | 1.0 | 0.602125  | 0.266108 | 0.210714 | Biso | 1.000000 C  |
| C14 | 1.0 | 0.398044  | 0.734427 | 0.210555 | Biso | 1.000000 C  |
| C15 | 1.0 | 0.733805  | 0.336427 | 0.210256 | Biso | 1.000000 C  |
| C16 | 1.0 | 0.265258  | 0.663919 | 0.211079 | Biso | 1.000000 C  |
| C17 | 1.0 | 0.665047  | 0.399449 | 0.211271 | Biso | 1.000000 C  |
| C18 | 1.0 | 0.337273  | 0.603286 | 0.210609 | Biso | 1.000000 C  |
| C19 | 1.0 | 0.268578  | 0.600155 | 0.208788 | Biso | 1.000000 C  |
| C20 | 1.0 | 0.732002  | 0.401602 | 0.208787 | Biso | 1.000000 C  |
| C21 | 1.0 | 0.329928  | 0.731330 | 0.209223 | Biso | 1.000000 C  |
| C22 | 1.0 | 0.668122  | 0.268268 | 0.207741 | Biso | 1.000000 C  |
| C23 | 1.0 | 0.401191  | 0.669820 | 0.208337 | Biso | 1.000000 C  |
| C24 | 1.0 | 0.600051  | 0.331871 | 0.209376 | Biso | 1.000000 C  |
| Bi1 | 1.0 | 0.500190  | 0.001723 | 0.148770 | Biso | 1.000000 Bi |
| Bi2 | 1.0 | -0.001680 | 0.498526 | 0.148936 | Biso | 1.000000 Bi |
| Bi3 | 1.0 | 0.502012  | 0.504002 | 0.149795 | Biso | 1.000000 Bi |

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