

**Supplementary information for
“Dual-Surface Functionalization of Graphene beyond DFT Limits: Nanoscale Insights
into Flat Bands and Optical Behavior”**

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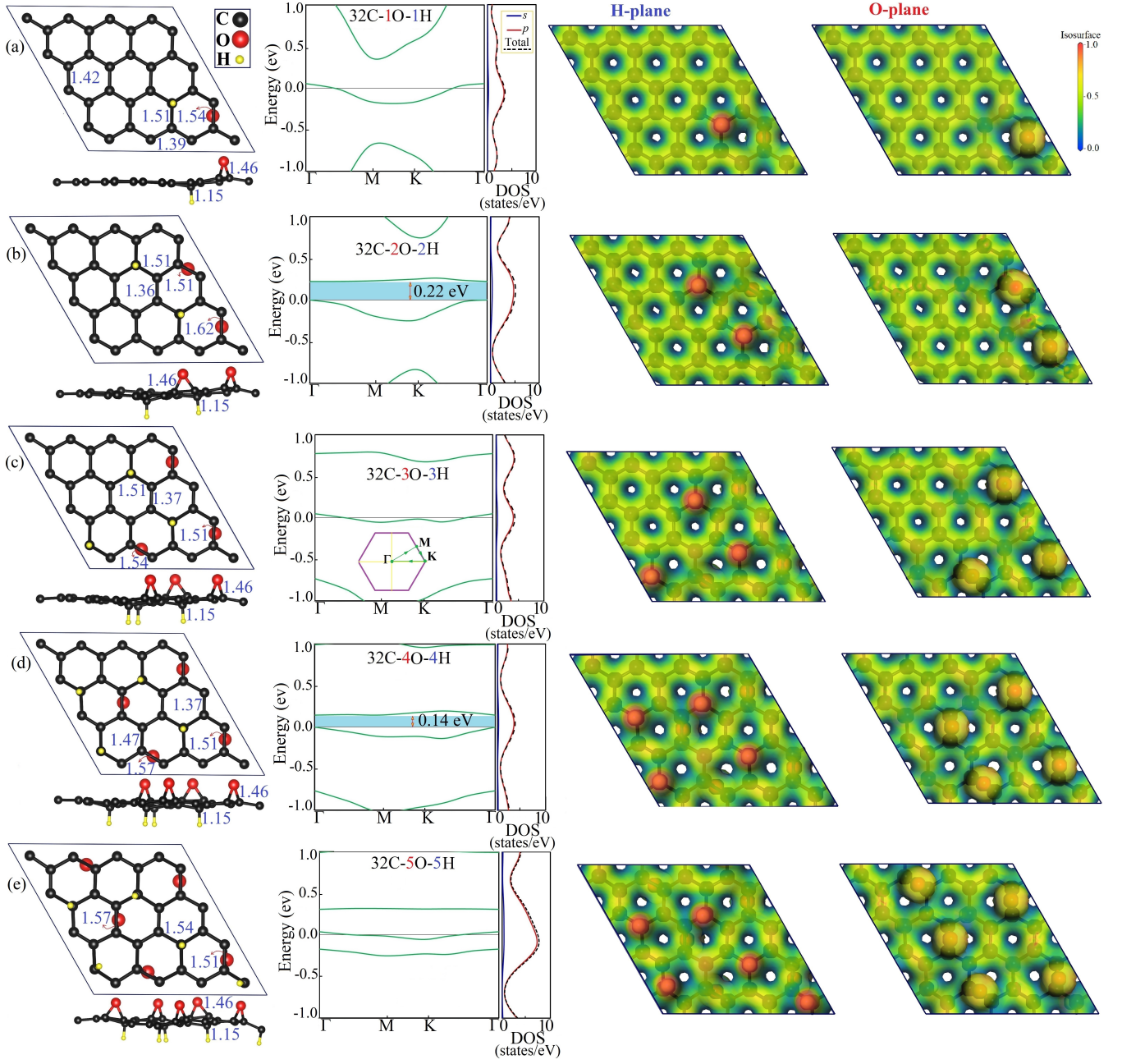


FIG. S1. The computed properties of $z\text{C}-x\text{H}-y\text{O}$ ($z=32$, $x, y=1-5$): (Left) Top and side views of the optimized supercell. The bond lengths are in Å. (Middle) The electronic band structure and the electronic density of states (DOS). The panel shows the First Brillouin zone (FBZ). (Right) Electron localization function (ELF) from top views of planes containing H and O atoms.

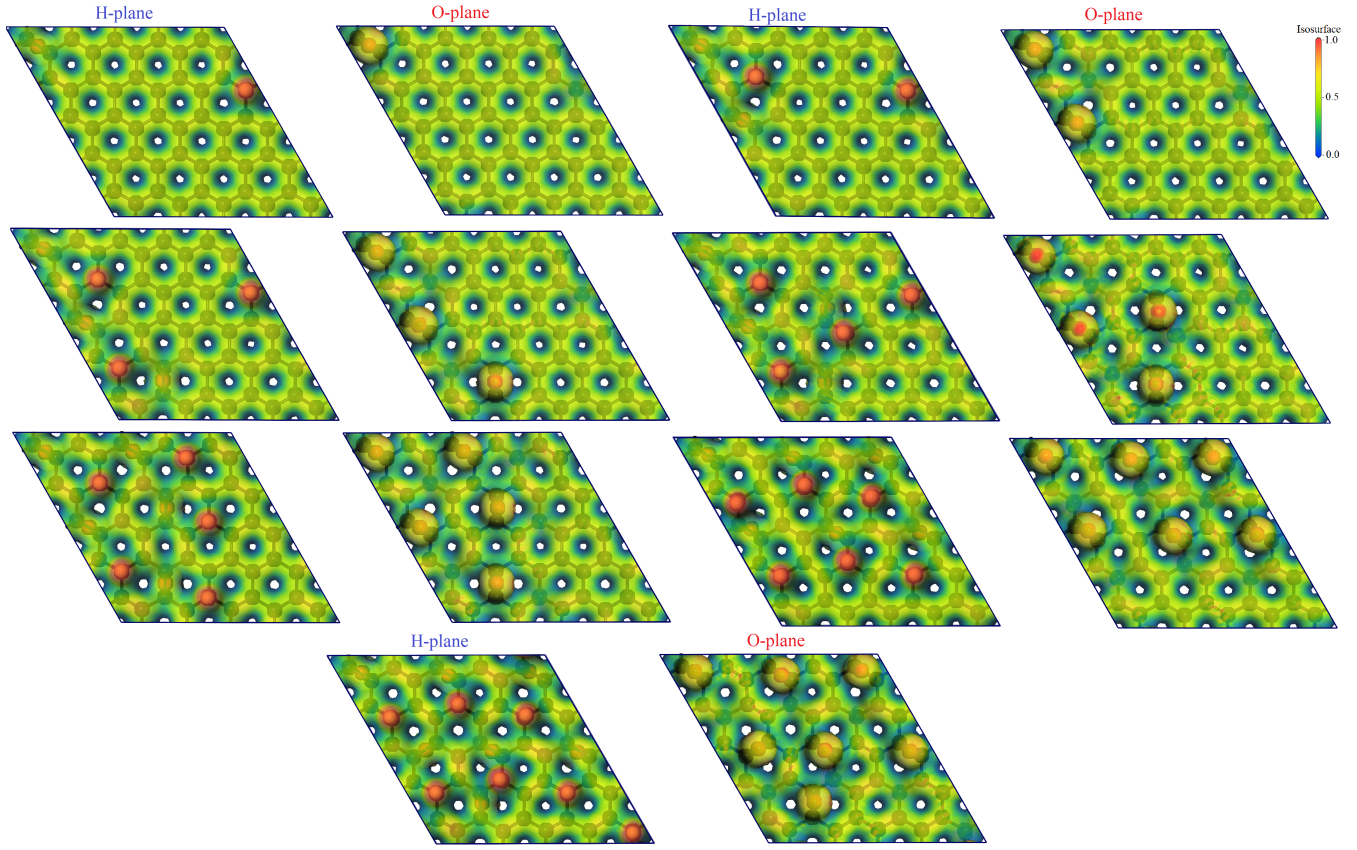


FIG. S2. Electron localization function (ELF) from top views of planes containing H and O atoms of the $z\text{C-}x\text{H-}y\text{O}$ ($z=50$, $x, y= 1-7$) structures.

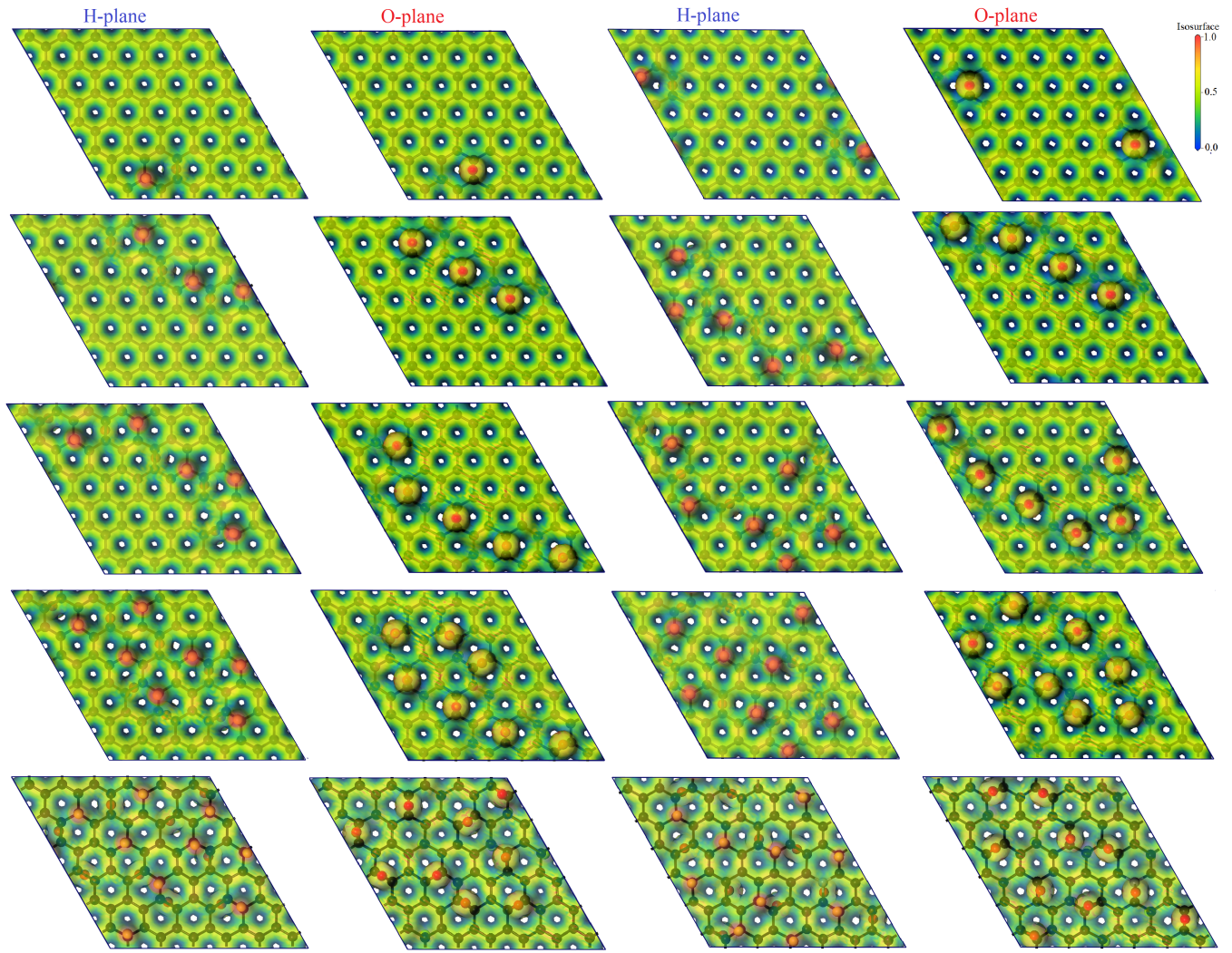


FIG. S3. Electron localization function (ELF) from top views of planes containing H and O atoms of the $z\text{C}-x\text{H}-y\text{O}$ ($z=72$, $x, y=1-10$) structures.

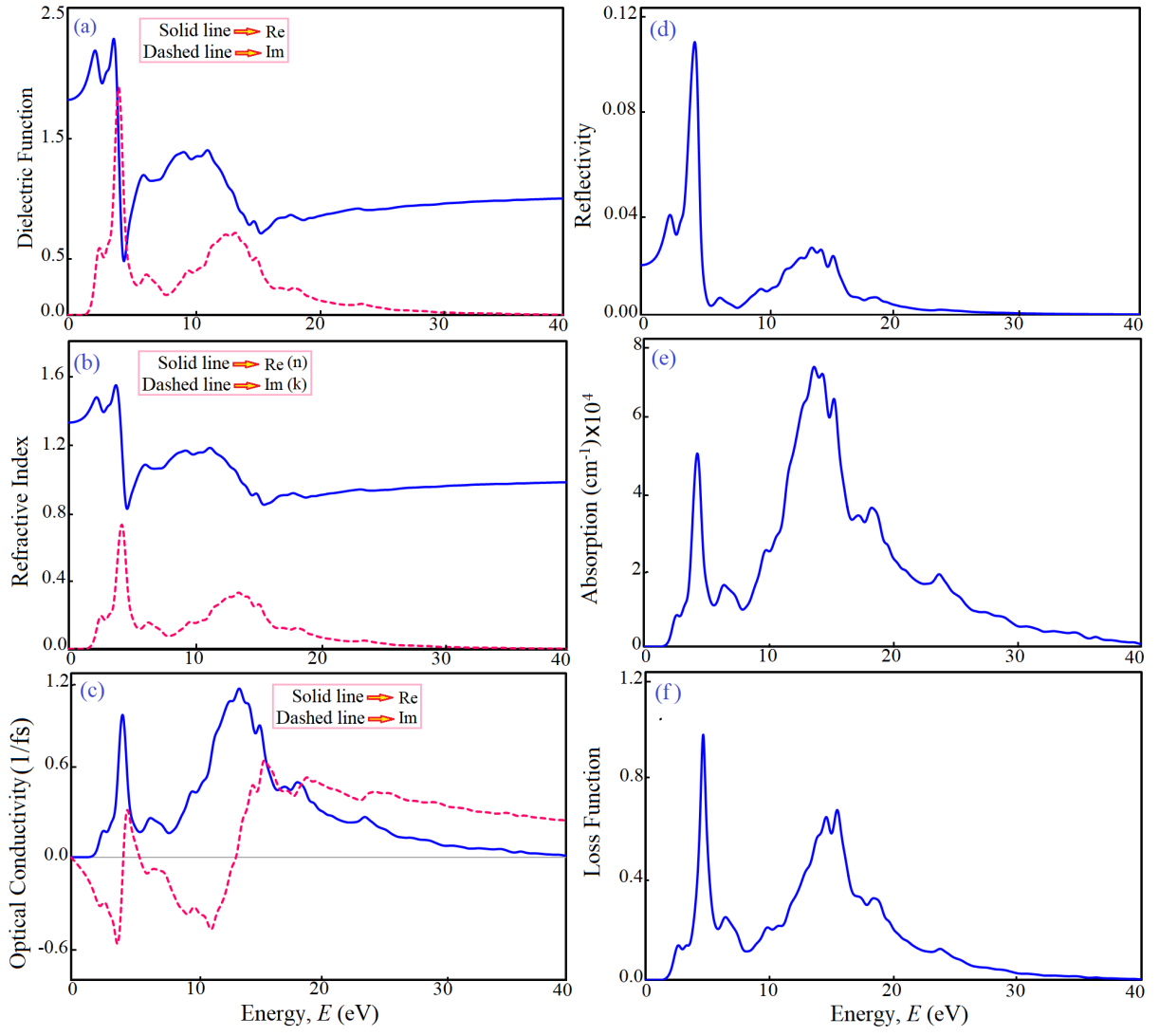


FIG. S4. (a) Dielectric function, (b) refractive index, (c) optical conductivity, (d) reflectivity, (e) Absorption, and (f) loss function of the $z\text{C-}x\text{H-}y\text{O}$ ($z=8$) structures.

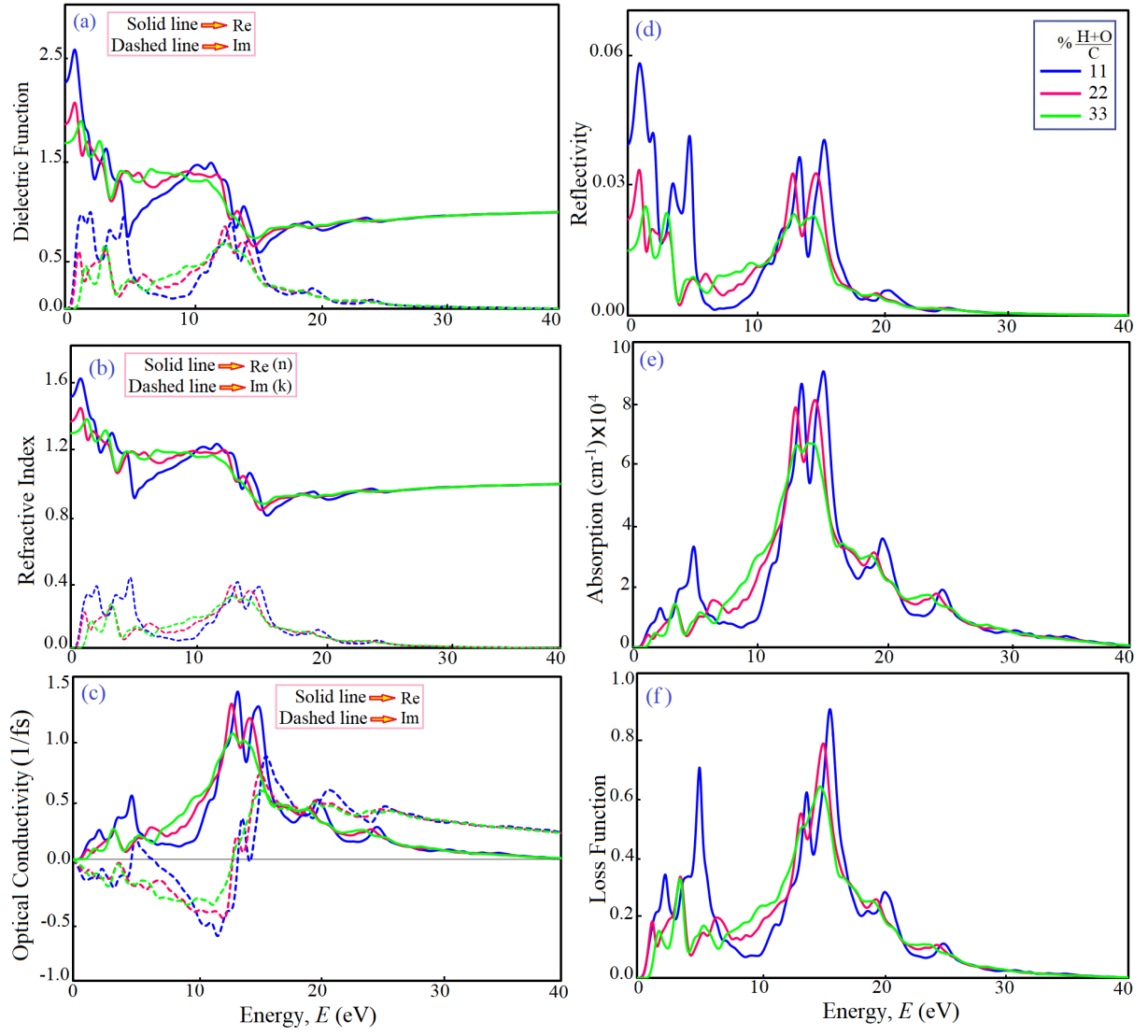


FIG. S5. (a) Dielectric function, (b) refractive index, (c) optical conductivity, (d) reflectivity, (e) Absorption, and (f) loss function of the $z\text{C-}x\text{H-}y\text{O}$ ($z=18$) structures.

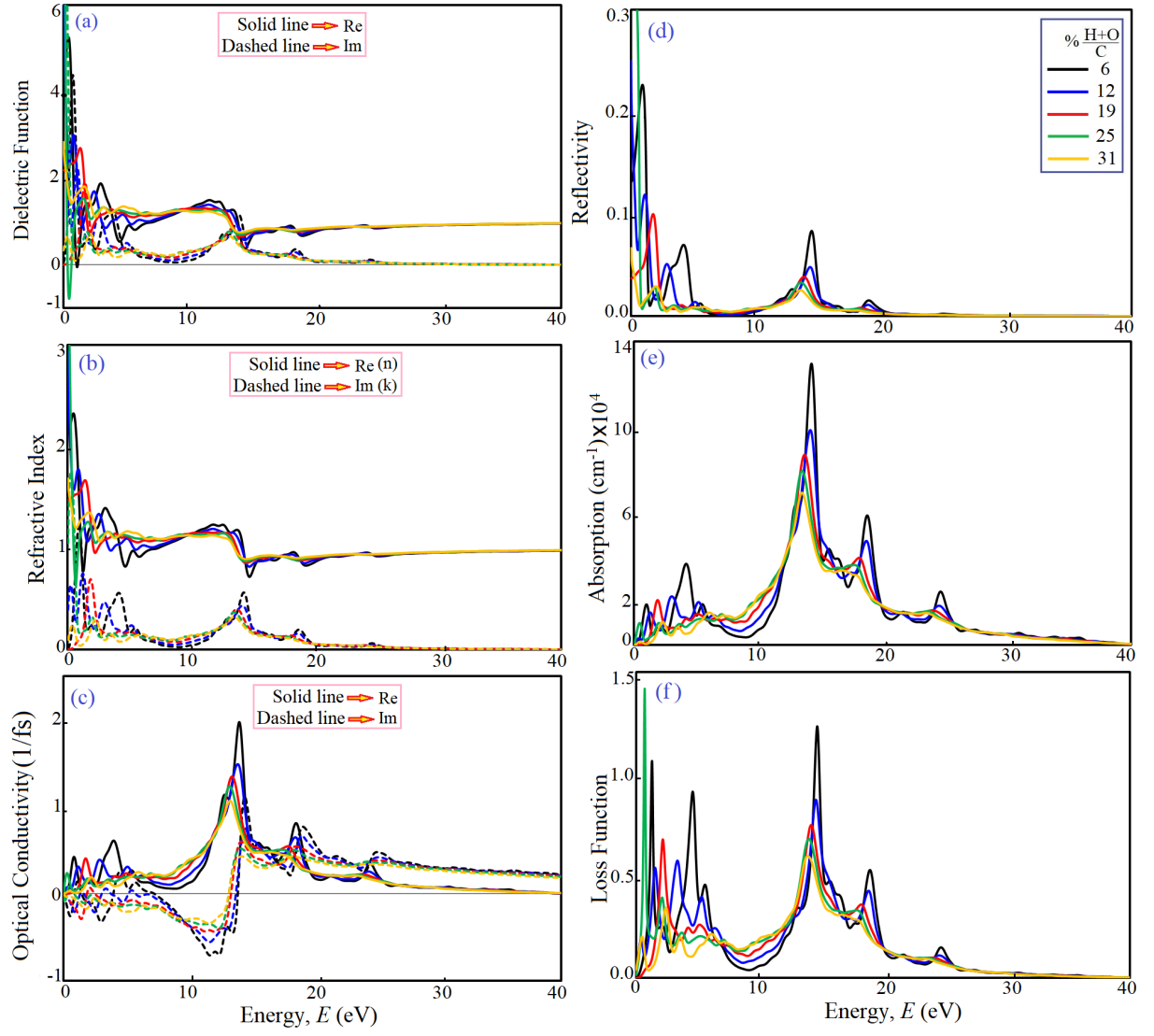


FIG. S6. (a) Dielectric function, (b) refractive index, (c) optical conductivity, (d) reflectivity, (e) Absorption, and (f) loss function of the $z\text{C}-x\text{H}-y\text{O}$ ($z=32$) structures.

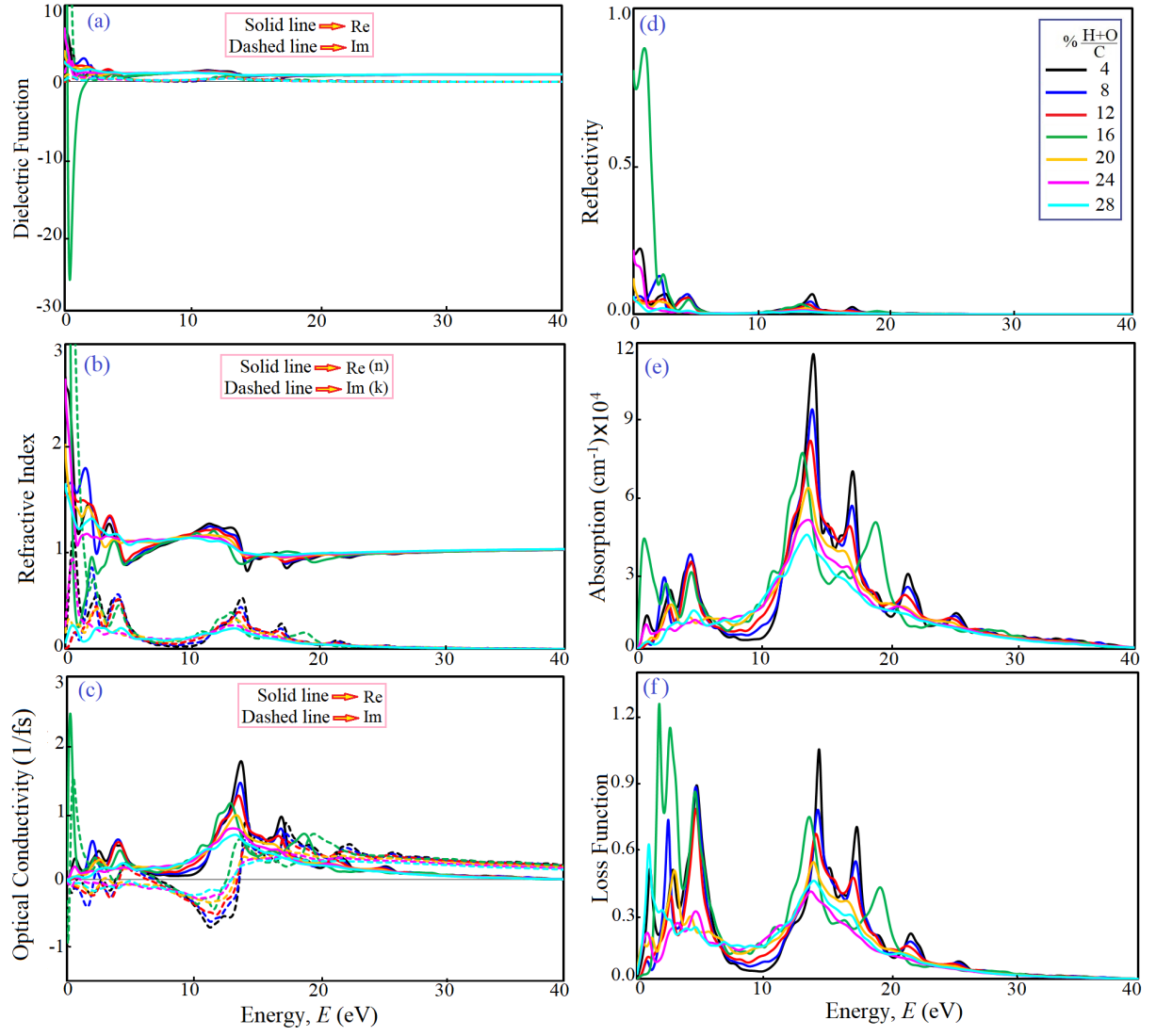


FIG. S7. (a) Dielectric function, (b) refractive index, (c) optical conductivity, (d) reflectivity, (e) Absorption, and (f) loss function of the $z\text{C}-x\text{H}-y\text{O}$ ($z=50$) structures.