

Supplementary Information for "Revealing the role of ripples in phonon modes for MoS₂ and MoSe₂: Insights from molecular dynamics and machine learning"

4.1 Convergence of DFT Calculations

Our DFT Calculations for MoS₂ and MoSe₂ were properly converged for both the Plane Wave Kinetic Energy and k-points criterion. The energy convergence criterion is shown below. Since we are using Norm-Conserved pseudopotentials, the selected energy cutoff for charge density is always 4 times the cutoff energy for wavefunctions. We conducted convergence tests, which are presented below. Figure S1 shows the energy as a function of the plane-wave cutoff energy for three different k-point grids: 3×3×1, 6×6×1, and 24×24×1. Notably, the energy curves for the 6×6×1 grid overlap with those for the 24×24×1 grid, whereas the 3×3×1 grid shows small deviations. It is noticeable that 6×6×1 and 24×24×1 grid results indicate similar accuracy, within negligible deviations. Figure S2 presents the difference in energy per atom between the 6×6×1 and 24×24×1 grids as a function of cutoff energy. For cutoff values of 40 Ry or higher, the difference stabilizes at approximately 1.4 meV/atom. These results suggest that, for both MoS₂ and MoSe₂, increasing the k-point grid beyond 6×6×1 does not improve energy convergence, particularly when using a plane wave cutoff of at least 40 Ry. The similarity between the 6×6×1 and 24×24×1 results supports the adequacy of our chosen parameters.

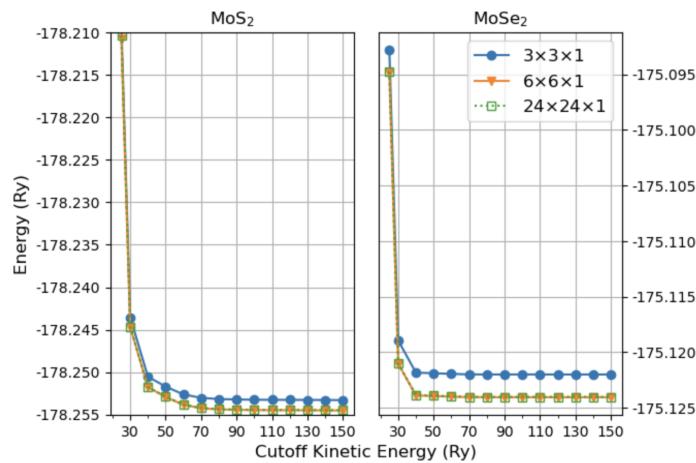


Figure S1 Energy convergence criterion for the plane wave expansion of wavefunctions for several k-points grid.

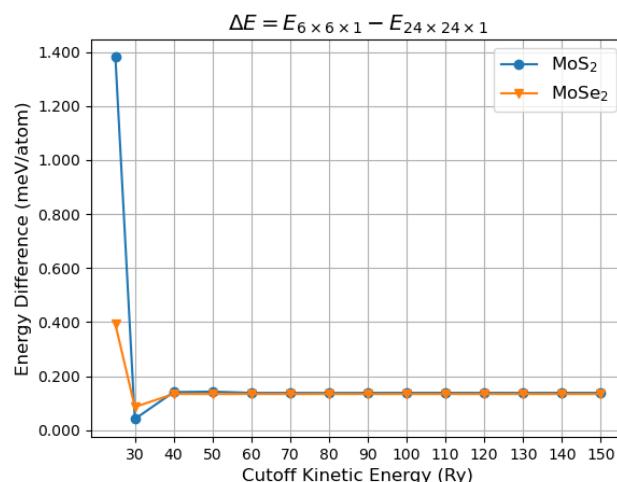


Figure S2 Energy difference for the 6×6×1 and 24×24×1 convergence curves.

As further validation we directly compared energy value per atom results using our chosen cutoff energies, namely 70 Ry for MoS₂ and 40 Ry for MoSe₂ [both with a grid of (6×6×1)], with results from a higher plane-wave cutoff (150 Ry) and a denser k-point sampling (24×24×1). The resulting differences in energy per atom are 1.068 meV for MoS₂ and 0.618 meV for MoSe₂. These values fall within the typical 1–2 meV/atom energy convergence criterion. This choice of parameters allowed that we could generate a DFT dataset of thousand of structures without sacrificing the accuracy and convergence of each DFT structure.

4.2 Accuracy and Validation of MLFF

To check the accuracy of the MLFFs generated in this work on the task of predicting the energies and atomic forces on unseen data we have included Figures S3 and S4. Each one of the subfigures was made with 750 structures of the testing set generated at the time of splitting the reference set between training and testing data. Figure S3a) and b) shows a comparison between the energies per atom and the absolute value for the atomic forces predicted by the MLFF and the reference DFT values on the data set respectively for MoS_2 , with the dashed black line indicating perfect accuracy for the MLFF, i.e., when the MLFF matches DFT without any error. For the structures included in the figure, we obtained a RMSE of 4.1 meV/atom and 286.16 meV/ \AA for the energies and forces respectively. Figure S3 c) shows a histogram of angles between the direction of the MLFF and DFT forces which is a measure of directional error in the sense that the more accurate an MLFF is, the more concentrated at 0° the distribution becomes. Due to the tail of the distribution on angles $\geq 10\%$, we fitted a Lorentz distribution to the histogram. The red dashed line indicates the fitted curve which has a full width half maximum (FWHM) equal to 6.47° and, of all the forces evaluated with the MLFF and included in the histogram, 60.2% of them have their angle with the DFT force within the range of the FWHM and 72.4% of them have this angle within the range of 10° (see inset at Figure S3). The accuracy check of the MLFF for MoSe_2 in Figure S4 with each one of the subfigures being made with the same amount structures of the testing set as in Figure S3. Figure S4a) and b) shows a comparison between the energies per atom and the absolute value for the atomic forces predicted by the MLFF and the reference DFT values on the data set respectively. For the structures included in the figure, we obtained a RMSE of 1.69 meV/atom and 184.11 meV/ \AA for the energies and forces respectively, both being slightly more accurate than the RMSE obtained for MoS_2 . Figure S4 c) shows a histogram of angles between the direction of the MLFF and DFT forces. The red dashed line indicates the Lorentzian fitted to the histogram with a FWHM = 7.23° and, of all the forces evaluated with the MLFF and included in the histogram, 64.7% of them have their angle with the DFT force within the FWHM and 72.1% of them have this angle within the range of 10° . Both figures indicates good agreement between the MLFF and DFT estimates for the force, especially on predicting the direction.

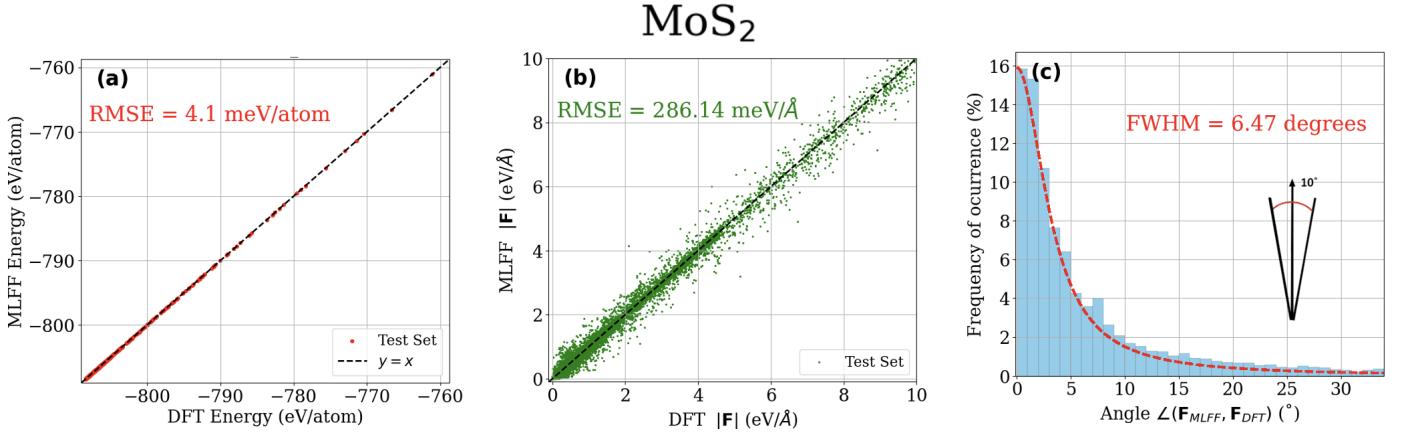


Figure S3 (a,b) Comparison of the energies and lengths of the atomic forces between MLFF and DFT for MoS_2 based respectively.(c) Histogram of the directional errors in the MLFF prediction of the forces. The red dashed line indicates the fitted Lorentzian function.

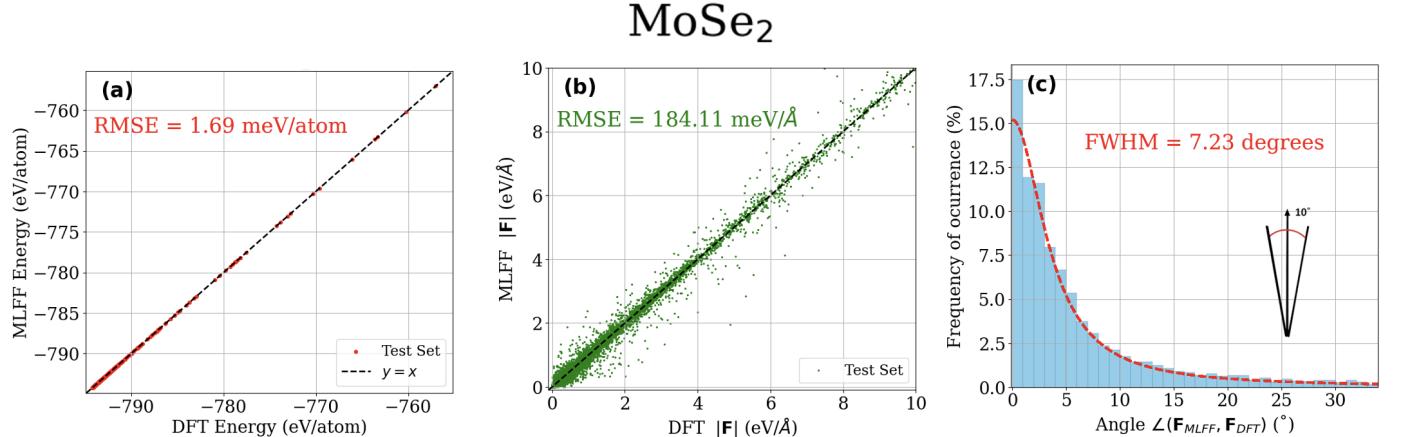


Figure S4 (a,b) Comparison of the energies and lengths of the atomic forces between MLFF and DFT for MoSe_2 based respectively.(c) Histogram of the directional errors in the MLFF prediction of the forces. The red dashed line indicates the fitted Lorentzian function.

The comparison of the MLFF and DFT forces by each component is included here as a complement to the comparison of the force modules and the histogram shown in Figures S3 and S4.

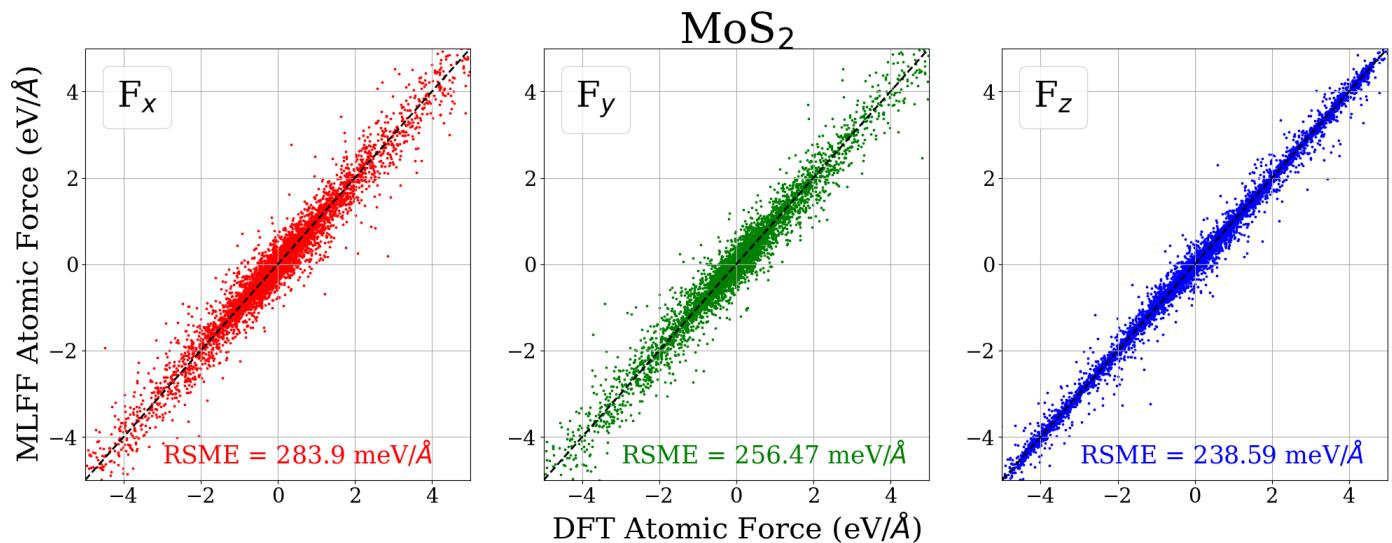


Figure S5 Comparison of the atomic forces Cartesian components between the MLFF developed for MoS_2 and the DFT reference set based on structures included in the testing set exclusively.

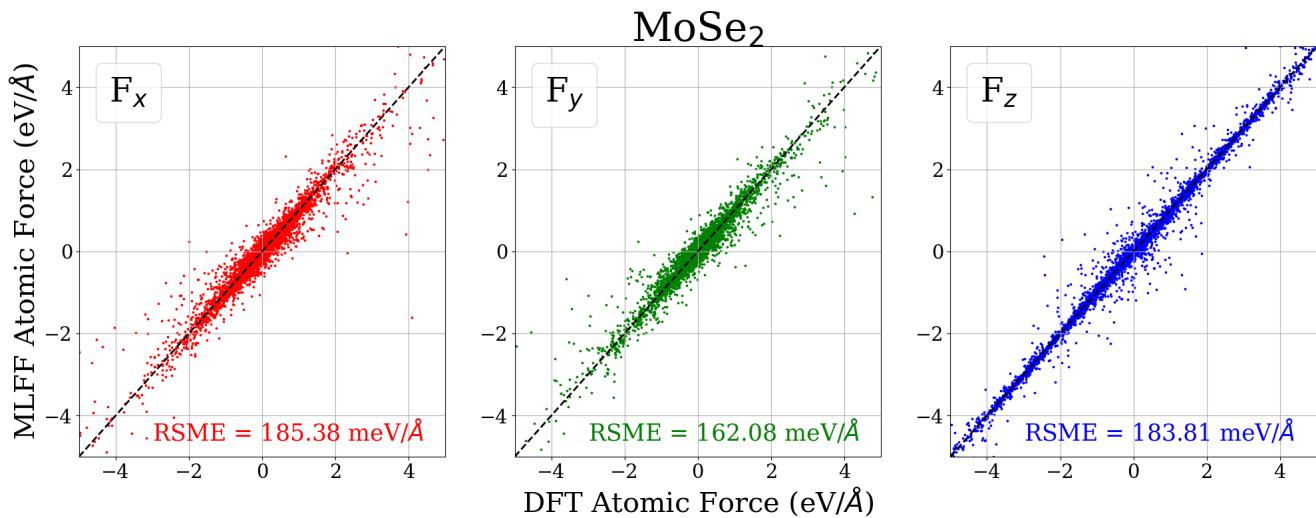


Figure S6 Comparison of the atomic forces Cartesian components between the MLFF developed for MoSe_2 and the DFT reference set based on structures included in the testing set exclusively.

4.3 Dielectric Spectra in Semi-log Plot

Figure S7 shows the imaginary part of dielectric spectra for MoS_2 and MoSe_2 in a semi-log scale, which is more suitable for comparing relative intensities of the observed peaks. Here, since the y axis is in log scale, we have omitted the errorbars for the sake of clarity of the figure.

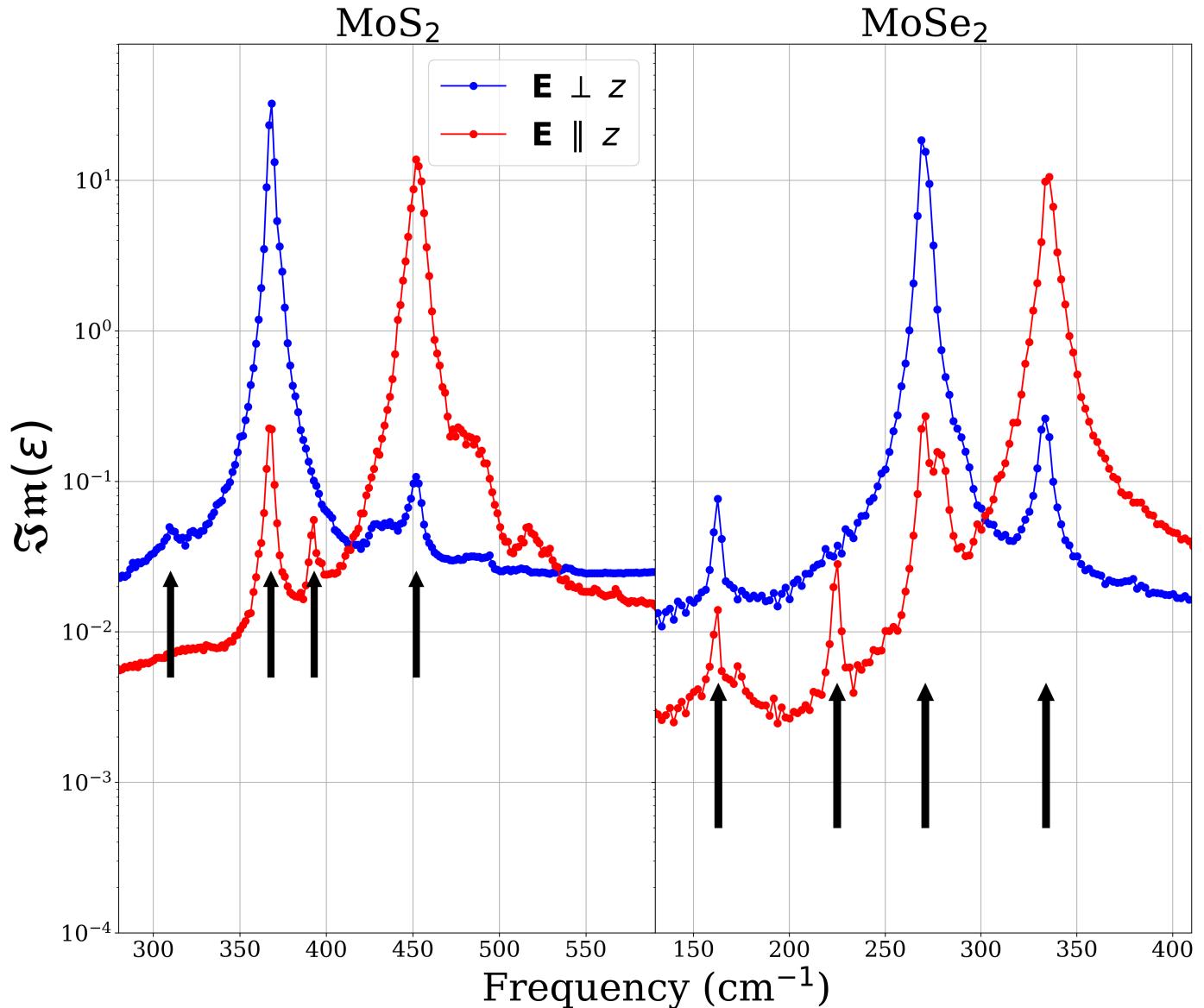


Figure S7 Imaginary part of dielectric spectra for MoS_2 and MoSe_2 at 300K in semi-log scale. Arrows indicate peaks centered at 310(163), 368(225), 393(271) and 452(334) for MoS_2 (MoSe_2) in cm^{-1} .

4.4 Effect of Tensile Strain on Dielectric Spectra

Figure S8 shows the newly identified peaks in the imaginary part of the dielectric spectra for unstrained and strained lattices (1.4% strain relative to the lattice constant). All simulations were performed with constant volume (NVT ensemble) throughout the dynamics which allowed us to assign a strain value to each curve shown. By observing each one of the peaks, it is evident that the application of strain flattens all newly observed peaks, thereby extinguishing the phenomenon observed in the unstrained lattice.

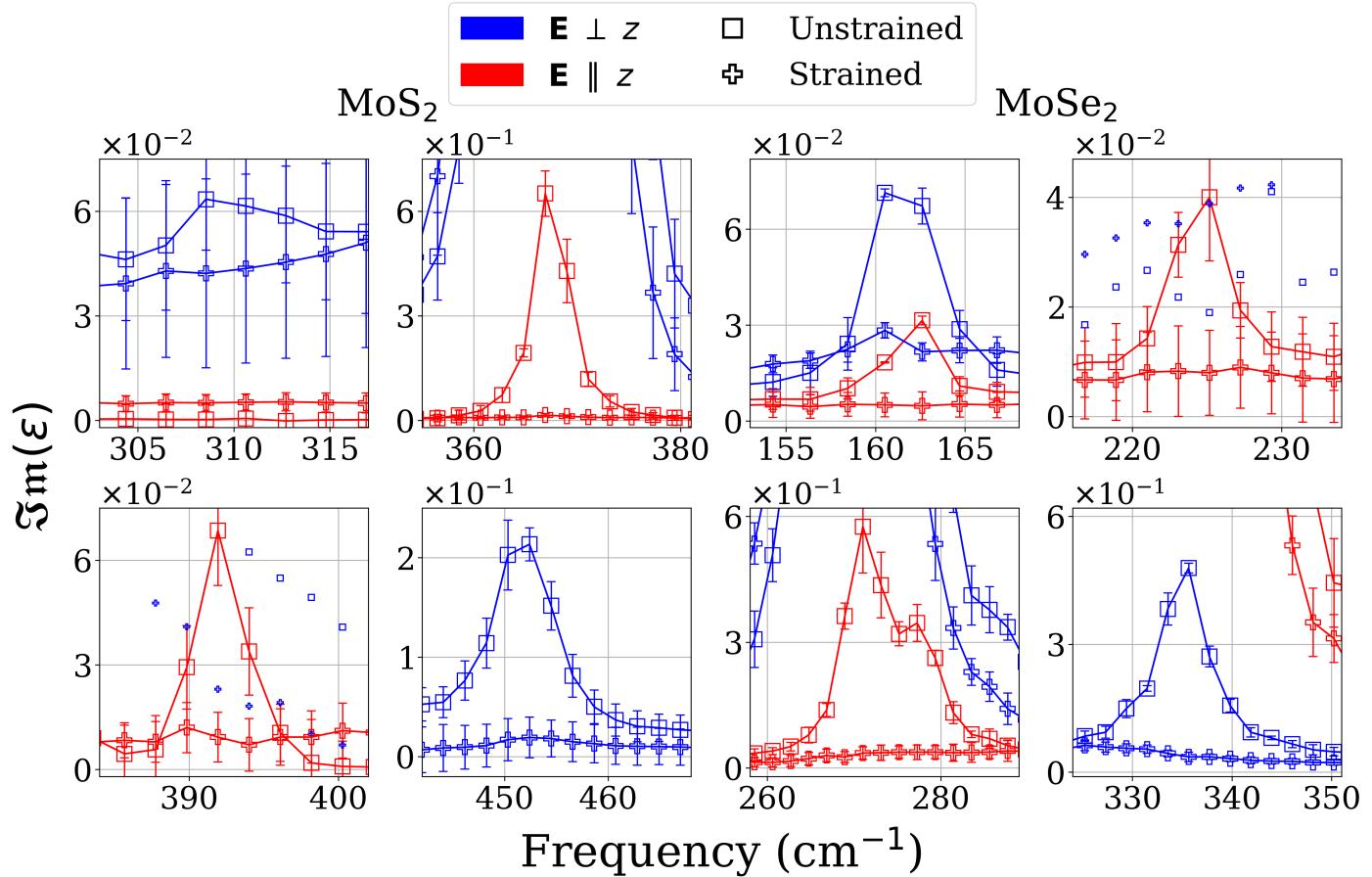


Figure S8 All found low intensity peaks under the effect of strain for MoS_2 and MoSe_2 . In some graphics, blue markers were reduced with the purpose of avoiding visual overload.

4.5 Calculation of Eigenmodes on Rippled Supercell

The supercell used on the calculation of eigenmodes is included in Figure S9 and was used for both MoS₂ and MoSe₂. This cell was constructed by the replication of the rectangular unit cell of MoS(Se)₂ (see green rectangle at Figure 1 at main manuscript). The unit cell was replicated 17 times in the direction of \mathbf{a}_1 and 10 times in the direction of \mathbf{a}_2 , resulting on a approximately square cell with a total of 1020 atoms. In order to model the ripple, an overall sine function with wave vector parallel to the zig-zag direction (referred as \mathbf{x} in the main manuscript) and peak-to-peak amplitude of 1Å were added to the z component of each atom of the supercell:

$$\Delta z_i = (0.5 \text{ \AA}) \times \sin\left(\frac{2\pi}{17a_0}x_i\right).$$

The amplitude was chosen so that the deformed system is very similar to the original, but the perturbation allows a qualitative investigation of any new peaks in the spectra without losing correspondence of peaks between the perturbed and original systems. After adding the deformation, the energy of the model cell must be minimized to ensure that the dynamical matrix is being calculated at a local minimum of the energy. Minimization usually does not significantly affect the model structure and can eliminate strain in the \mathbf{x} direction. After minimization, the dimensions for each cell were 54.26 Å × 55.28 Å for MoS₂ and 56.46 Å × 57.53 Å for MoSe₂. Alamode detected that this supercell can be assigned to a primitive cell with 102 atoms shown in Figure S10. Therefore, the calculation resulted in a total of 306 eigenmodes, some of which were mentioned in the main manuscript.

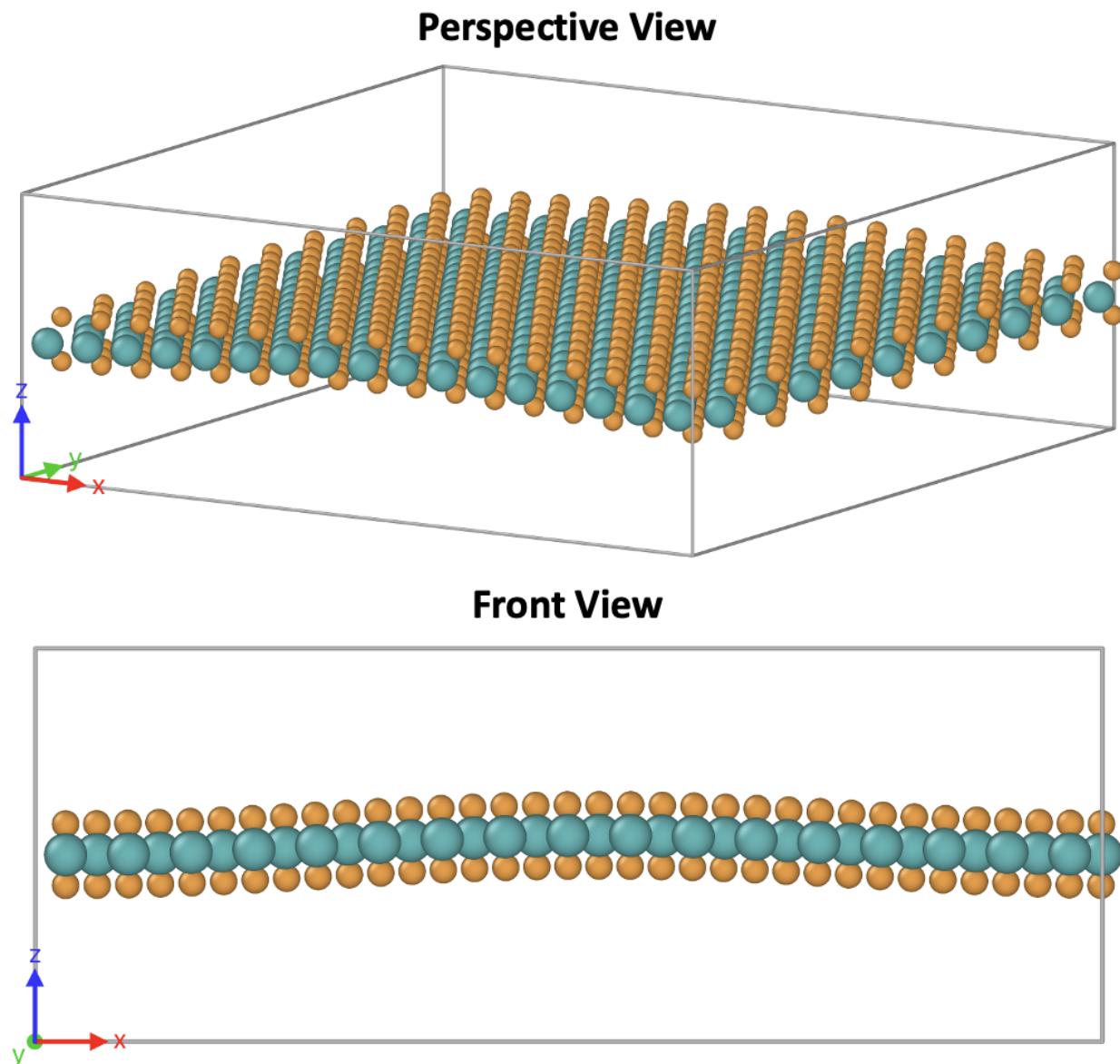


Figure S9 Supercell of 1020 atoms containing a sinusoidal wave in the x direction used in the calculation made by finite displacements.

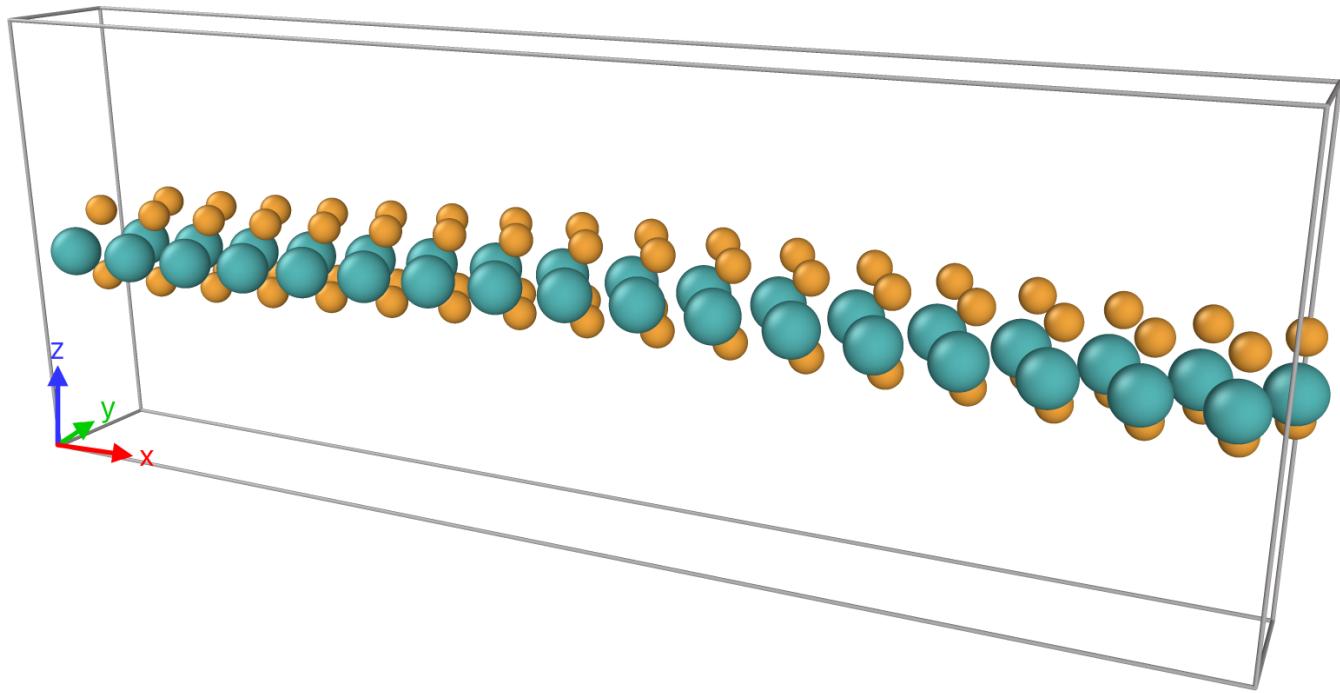


Figure S10 Primitive rippled cell of 102 atoms. The supercell at Figure S9 is made by 10 units of this primitive cell repeated on the y (armchair) direction

The calculated frequencies and IR intensities (see Figures 20 and 21 in the main manuscript) for the modes of these models are listed in the following tables for both compounds:

Table S1 Frequencies (in cm^{-1}) and IR intensities (in arb. units) calculated for the MoS₂ rippled supercell (continued on next page)

#	Frequency	$f_{xy}(\omega_j)$	$f_z(\omega_j)$	#	Frequency	$f_{xy}(\omega_j)$	$f_z(\omega_j)$
1	0.0000	0.0000e+00	0.0000e+00	77	178.1703	0.0000e+00	0.0000e+00
2	0.0000	0.0000e+00	0.0000e+00	78	194.6444	0.0000e+00	0.0000e+00
3	0.0000	0.0000e+00	0.0000e+00	79	194.6508	0.0000e+00	0.0000e+00
4	0.3004	1.5000e-09	0.0000e+00	80	207.1886	0.0000e+00	0.0000e+00
5	1.8919	2.9843e-06	0.0000e+00	81	207.2135	0.0000e+00	0.0000e+00
6	9.7114	0.0000e+00	0.0000e+00	82	210.7835	6.2832e-11	0.0000e+00
7	9.7339	0.0000e+00	1.9521e-09	83	210.7954	1.6482e-11	0.0000e+00
8	28.1362	0.0000e+00	0.0000e+00	84	211.9602	1.7368e-09	0.0000e+00
9	28.2301	0.0000e+00	1.3760e-06	85	211.9632	4.9071e-10	0.0000e+00
10	30.3155	7.8702e-12	0.0000e+00	86	214.3197	0.0000e+00	0.0000e+00
11	30.3498	4.6923e-11	0.0000e+00	87	214.3218	0.0000e+00	0.0000e+00
12	41.9107	0.0000e+00	1.2716e-06	88	218.6117	0.0000e+00	0.0000e+00
13	41.9859	0.0000e+00	0.0000e+00	89	218.6140	2.6231e-11	0.0000e+00
14	53.1230	3.3736e-07	0.0000e+00	90	222.7617	0.0000e+00	0.0000e+00
15	53.2314	2.6503e-08	0.0000e+00	91	222.7675	0.0000e+00	0.0000e+00
16	60.3363	0.0000e+00	0.0000e+00	92	227.7333	0.0000e+00	0.0000e+00
17	60.3553	0.0000e+00	7.9234e-10	93	227.7431	0.0000e+00	0.0000e+00
18	73.1519	0.0000e+00	0.0000e+00	94	229.2407	0.0000e+00	0.0000e+00
19	73.1689	0.0000e+00	0.0000e+00	95	229.2421	0.0000e+00	0.0000e+00
20	81.7425	2.3890e-07	0.0000e+00	96	229.2629	0.0000e+00	0.0000e+00
21	81.8700	2.5765e-07	0.0000e+00	97	229.3726	1.1092e-11	0.0000e+00
22	82.8899	1.6798e-09	0.0000e+00	98	229.6204	0.0000e+00	1.2724e-11
23	82.9214	7.7406e-10	0.0000e+00	99	232.0023	0.0000e+00	0.0000e+00
24	88.2026	0.0000e+00	0.0000e+00	100	232.0219	0.0000e+00	0.0000e+00
25	88.2153	0.0000e+00	0.0000e+00	101	236.0732	0.0000e+00	0.0000e+00
26	93.7257	5.9053e-10	0.0000e+00	102	236.1080	2.1504e-11	0.0000e+00
27	93.7349	9.3762e-11	0.0000e+00	103	273.2504	0.0000e+00	2.7727e-06
28	118.3505	1.2801e-10	0.0000e+00	104	273.2724	0.0000e+00	0.0000e+00
29	118.3634	4.6785e-11	0.0000e+00	105	273.4864	1.6840e-04	0.0000e+00
30	122.0125	0.0000e+00	2.7460e-09	106	273.5141	1.4075e-05	0.0000e+00
31	122.0369	0.0000e+00	0.0000e+00	107 *E"(x)	273.7792	4.4171e-04	0.0000e+00
32	124.4398	0.0000e+00	7.7146e-11	108	273.8270	4.8997e-05	0.0000e+00
33	124.4455	0.0000e+00	0.0000e+00	109	274.0492	0.0000e+00	3.6610e-06
34	139.7821	1.9723e-11	0.0000e+00	110	274.4042	0.0000e+00	0.0000e+00
35	139.7829	0.0000e+00	0.0000e+00	111	275.3041	0.0000e+00	1.4193e-08
36	141.1141	0.0000e+00	0.0000e+00	112	275.3100	0.0000e+00	0.0000e+00
37	141.1176	0.0000e+00	0.0000e+00	113	276.5469	1.5850e-05	0.0000e+00
38	146.7319	0.0000e+00	0.0000e+00	114 *E"(y)	276.8662	7.4914e-04	0.0000e+00
39	146.7371	0.0000e+00	0.0000e+00	115	278.5667	4.0210e-10	0.0000e+00
40	146.7722	0.0000e+00	0.0000e+00	116	278.5677	0.0000e+00	0.0000e+00
41	147.4916	0.0000e+00	0.0000e+00	117	282.8495	0.0000e+00	1.0258e-09
42	147.4994	2.3797e-11	0.0000e+00	118	282.8622	0.0000e+00	0.0000e+00
43	148.8470	0.0000e+00	0.0000e+00	119	283.5313	0.0000e+00	0.0000e+00
44	148.8540	0.0000e+00	0.0000e+00	120	283.5965	0.0000e+00	5.9290e-08
45	150.4327	0.0000e+00	3.2671e-11	121	287.6733	1.5370e-08	0.0000e+00
46	150.4336	0.0000e+00	0.0000e+00	122	287.6948	2.0589e-10	0.0000e+00
47	156.3055	0.0000e+00	0.0000e+00	123	291.9335	5.2952e-10	0.0000e+00
48	156.3070	3.4823e-11	0.0000e+00	124	291.9499	2.0494e-10	0.0000e+00
49	157.6091	3.6204e-11	0.0000e+00	125	292.2277	0.0000e+00	3.3894e-10
50	157.7530	2.4539e-11	0.0000e+00	126	292.2542	0.0000e+00	0.0000e+00
51	158.3782	0.0000e+00	0.0000e+00	127	292.3891	0.0000e+00	0.0000e+00
52	158.3796	0.0000e+00	0.0000e+00	128	292.4098	0.0000e+00	2.2970e-11
53	159.1099	0.0000e+00	0.0000e+00	129	293.7746	0.0000e+00	0.0000e+00
54	159.1399	0.0000e+00	0.0000e+00	130	293.7807	0.0000e+00	1.3956e-10
55	161.6504	0.0000e+00	0.0000e+00	131	293.9443	1.2764e-08	0.0000e+00
56	161.6510	0.0000e+00	0.0000e+00	132	293.9559	2.0135e-09	0.0000e+00
57	162.7385	5.4753e-11	0.0000e+00	133	294.7139	1.6856e-11	0.0000e+00
58	162.7441	0.0000e+00	0.0000e+00	134	294.7309	1.4578e-10	0.0000e+00
59	163.0493	2.1695e-09	0.0000e+00	135	294.9363	1.4523e-10	0.0000e+00
60	163.0657	3.4835e-09	0.0000e+00	136	294.9548	1.4455e-09	0.0000e+00
61	164.8681	2.2028e-11	0.0000e+00	137	297.5955	0.0000e+00	0.0000e+00
62	164.8754	2.0751e-11	0.0000e+00	138	297.6363	0.0000e+00	0.0000e+00
63	168.7493	0.0000e+00	0.0000e+00	139	300.1429	2.2061e-10	0.0000e+00
64	168.7521	4.4227e-11	0.0000e+00	140	300.2090	3.7842e-10	0.0000e+00
65	172.0617	0.0000e+00	0.0000e+00	141	302.9717	0.0000e+00	5.5150e-10
66	172.0736	0.0000e+00	0.0000e+00	142	303.0660	0.0000e+00	0.0000e+00
67	174.9430	0.0000e+00	0.0000e+00	143	304.5511	5.2804e-11	0.0000e+00
68	174.9444	0.0000e+00	9.1010e-12	144	306.0252	0.0000e+00	8.7459e-11
69	175.0726	5.7227e-11	0.0000e+00	145	306.0271	0.0000e+00	0.0000e+00
70	175.0895	2.1084e-11	0.0000e+00	146	316.7751	0.0000e+00	9.8539e-11
71	175.1134	0.0000e+00	0.0000e+00	147	316.7796	0.0000e+00	0.0000e+00
72	175.2960	0.0000e+00	0.0000e+00	148	318.3125	5.5392e-10	0.0000e+00
73	177.3062	9.9039e-11	0.0000e+00	149	318.3265	1.2964e-11	0.0000e+00
74	177.3329	4.8577e-11	0.0000e+00	150	320.8214	1.3012e-09	0.0000e+00
75	177.3987	1.1791e-11	0.0000e+00	151	321.6145	0.0000e+00	0.0000e+00
76	178.1685	0.0000e+00	0.0000e+00	152	321.8978	0.0000e+00	1.2098e-10

#	Frequency	$f_{xy}(\omega_j)$	$f_z(\omega_j)$	#	Frequency	$f_{xy}(\omega_j)$	$f_z(\omega_j)$
153	323.7785	2.9885e-09	0.0000e+00	230	367.5009	0.0000e+00	0.0000e+00
154	323.7843	2.1762e-09	0.0000e+00	231	367.9259	1.7025e-04	0.0000e+00
155	323.8573	1.2087e-09	0.0000e+00	232	367.9354	4.7225e-04	0.0000e+00
156	323.9123	1.5143e-10	0.0000e+00	233	369.2067	0.0000e+00	0.0000e+00
157	326.3453	0.0000e+00	3.9333e-11	234 *E(z)	369.3800	0.0000e+00	2.7172e-03
158	326.3629	0.0000e+00	0.0000e+00	235	369.4637	4.4660e-07	0.0000e+00
159	328.0523	1.7098e-09	0.0000e+00	236	369.5608	2.1461e-08	0.0000e+00
160	328.0574	4.3551e-10	0.0000e+00	237	372.2349	0.0000e+00	0.0000e+00
161	328.2593	0.0000e+00	2.9334e-11	238	372.2480	0.0000e+00	1.3568e-09
162	328.2600	0.0000e+00	0.0000e+00	239	372.4870	0.0000e+00	0.0000e+00
163	328.9067	2.8267e-10	0.0000e+00	240	372.6904	0.0000e+00	3.0859e-06
164	328.9304	1.0511e-10	0.0000e+00	241	372.9135	0.0000e+00	0.0000e+00
165	329.1346	0.0000e+00	1.2178e-09	242	372.9165	0.0000e+00	9.1110e-10
166	329.1574	0.0000e+00	0.0000e+00	243	373.6371	1.2882e-06	0.0000e+00
167	329.1876	3.8037e-10	0.0000e+00	244	373.6807	1.1691e-05	0.0000e+00
168	329.2029	9.0030e-10	0.0000e+00	245	374.0959	0.0000e+00	1.2271e-09
169	329.2486	0.0000e+00	1.9500e-09	246	374.4536	1.0000e+00	0.0000e+00
170	329.2655	0.0000e+00	0.0000e+00	247	374.5136	9.9534e-01	0.0000e+00
171	331.8733	6.7552e-11	0.0000e+00	248	374.6015	0.0000e+00	0.0000e+00
172	331.8759	1.5611e-09	0.0000e+00	249	375.9753	7.3998e-07	0.0000e+00
173	333.1575	0.0000e+00	0.0000e+00	250	379.3993	0.0000e+00	0.0000e+00
174	333.1576	0.0000e+00	8.3908e-12	251	379.4022	0.0000e+00	2.5619e-09
175	335.7557	2.1390e-09	0.0000e+00	252	379.9541	7.2983e-09	0.0000e+00
176	335.7563	2.1324e-09	0.0000e+00	253	379.9597	8.9618e-08	0.0000e+00
177	339.8761	0.0000e+00	0.0000e+00	254	381.4096	8.5213e-08	0.0000e+00
178	339.8789	0.0000e+00	3.7071e-10	255	381.4148	5.0836e-09	0.0000e+00
179	343.8019	0.0000e+00	0.0000e+00	256	382.6173	0.0000e+00	0.0000e+00
180	343.8043	0.0000e+00	7.6687e-11	257	382.6258	0.0000e+00	1.0278e-09
181	344.9890	3.2593e-10	0.0000e+00	258	383.2061	1.6449e-08	0.0000e+00
182	344.9989	1.3071e-09	0.0000e+00	259	383.2096	1.2353e-07	0.0000e+00
183	347.3096	4.6152e-10	0.0000e+00	260	388.5925	2.9772e-09	0.0000e+00
184	347.3193	4.9868e-10	0.0000e+00	261	388.5935	1.6798e-08	0.0000e+00
185	347.4101	0.0000e+00	2.1975e-11	262	389.1419	0.0000e+00	0.0000e+00
186	347.4224	0.0000e+00	0.0000e+00	263	389.1479	0.0000e+00	5.7520e-09
187	347.5440	0.0000e+00	4.5060e-11	264	389.9698	0.0000e+00	1.1090e-09
188	347.5689	0.0000e+00	0.0000e+00	265	390.5062	8.0234e-08	0.0000e+00
189	348.9126	1.7356e-09	0.0000e+00	266	390.6240	2.0980e-09	0.0000e+00
190	348.9159	1.5788e-10	0.0000e+00	267	390.7729	0.0000e+00	3.2572e-10
191	349.6935	1.3006e-08	0.0000e+00	268	390.7914	0.0000e+00	0.0000e+00
192	349.6964	3.6542e-11	0.0000e+00	269	393.3133	0.0000e+00	2.9506e-07
193	350.7227	0.0000e+00	5.7332e-10	270	393.3258	0.0000e+00	0.0000e+00
194	350.7237	0.0000e+00	0.0000e+00	271	393.9653	4.0190e-05	0.0000e+00
195	351.2465	0.0000e+00	0.0000e+00	272	394.8126	4.3183e-10	0.0000e+00
196	351.2995	0.0000e+00	1.2422e-11	273	394.8171	2.0629e-09	0.0000e+00
197	352.4320	0.0000e+00	0.0000e+00	274	395.3889	2.5018e-08	0.0000e+00
198	352.4344	0.0000e+00	1.1743e-09	275	395.4002	2.4750e-08	0.0000e+00
199	353.2188	8.9671e-10	0.0000e+00	276	396.0900	0.0000e+00	6.9752e-08
200	353.6687	1.7246e-08	0.0000e+00	277	396.1195	0.0000e+00	0.0000e+00
201	354.2405	0.0000e+00	0.0000e+00	278	398.0295	0.0000e+00	0.0000e+00
202	354.8236	2.7183e-08	0.0000e+00	279	398.0300	0.0000e+00	1.0573e-09
203	354.8381	1.7413e-07	0.0000e+00	280	399.6199	0.0000e+00	0.0000e+00
204	354.9018	0.0000e+00	0.0000e+00	281 *A ₁ (z)	399.7048	0.0000e+00	2.0318e-03
205	356.6375	3.7176e-08	0.0000e+00	282	402.2895	8.5086e-10	0.0000e+00
206	357.0515	5.0216e-09	0.0000e+00	283	402.2957	1.5012e-08	0.0000e+00
207	357.3550	5.9509e-09	0.0000e+00	284	402.4346	6.3738e-06	0.0000e+00
208	357.3573	1.9804e-08	0.0000e+00	285	402.4905	1.2283e-07	0.0000e+00
209	358.3473	9.9374e-09	0.0000e+00	286	403.9095	0.0000e+00	0.0000e+00
210	358.3497	2.9031e-10	0.0000e+00	287	403.9191	0.0000e+00	1.4563e-07
211	358.5896	0.0000e+00	3.2640e-10	288	404.7318	0.0000e+00	1.3542e-08
212	358.5918	0.0000e+00	0.0000e+00	289	404.7337	0.0000e+00	0.0000e+00
213	360.3862	0.0000e+00	0.0000e+00	290	405.9482	7.0984e-09	0.0000e+00
214	360.3869	0.0000e+00	9.7288e-10	291	405.9501	5.7378e-10	0.0000e+00
215	360.5574	1.9365e-07	0.0000e+00	292	407.1525	8.2134e-09	0.0000e+00
216	360.5581	1.3874e-10	0.0000e+00	293	407.1640	6.3367e-09	0.0000e+00
217	360.5696	1.1635e-08	0.0000e+00	294	408.8301	0.0000e+00	6.5091e-10
218	360.5861	2.8598e-08	0.0000e+00	295	408.8305	0.0000e+00	0.0000e+00
219	361.8122	0.0000e+00	3.6359e-07	296	411.3898	6.1117e-09	0.0000e+00
220	361.8282	0.0000e+00	0.0000e+00	297	411.3927	6.8111e-11	0.0000e+00
221	361.9944	0.0000e+00	1.9516e-09	298	426.8635	0.0000e+00	0.0000e+00
222	362.0135	0.0000e+00	0.0000e+00	299	426.8718	0.0000e+00	6.3928e-08
223	365.4927	9.4691e-10	0.0000e+00	300	441.8104	7.7818e-08	0.0000e+00
224	365.5025	2.9297e-08	0.0000e+00	301	441.8264	2.5173e-09	0.0000e+00
225	365.8672	4.2517e-06	0.0000e+00	302	452.8761	0.0000e+00	0.0000e+00
226	365.8877	1.9735e-05	0.0000e+00	303	452.8877	0.0000e+00	1.3630e-04
227	365.9394	0.0000e+00	3.6662e-10	304 *A ₂ (x)	458.9485	5.2085e-03	0.0000e+00
228	366.0330	0.0000e+00	0.0000e+00	305	459.1162	9.4335e-06	0.0000e+00
229	367.4811	0.0000e+00	6.5958e-06	306	460.8882	0.0000e+00	9.9646e-01

Table S2 Frequencies (in cm^{-1}) and IR intensities (in arb. units) calculated for the MoSe₂ rippled supercell (continued on next page)

#	Frequency	$f_{xy}(\omega_j)$	$f_z(\omega_j)$	#	Frequency	$f_{xy}(\omega_j)$	$f_z(\omega_j)$
1	-2.6629	0.0000e+00	5.6698e-09	77	125.8856	0.0000e+00	0.0000e+00
2	-2.5117	0.0000e+00	0.0000e+00	78	125.8858	0.0000e+00	0.0000e+00
3	-1.9646	0.0000e+00	0.0000e+00	79	126.3839	0.0000e+00	0.0000e+00
4	-1.1047	6.9404e-07	0.0000e+00	80	126.3923	0.0000e+00	0.0000e+00
5	0.0000	0.0000e+00	0.0000e+00	81	128.3717	0.0000e+00	0.0000e+00
6	0.0000	0.0000e+00	0.0000e+00	82	128.7002	0.0000e+00	0.0000e+00
7	0.0000	0.0000e+00	0.0000e+00	83	128.7004	0.0000e+00	0.0000e+00
8	14.6863	0.0000e+00	0.0000e+00	84	135.4425	0.0000e+00	0.0000e+00
9	14.7134	0.0000e+00	0.0000e+00	85	135.4438	0.0000e+00	0.0000e+00
10	16.1746	0.0000e+00	8.7662e-07	86	136.8321	0.0000e+00	0.0000e+00
11	16.2030	0.0000e+00	0.0000e+00	87	136.8321	0.0000e+00	0.0000e+00
12	27.7563	0.0000e+00	9.1173e-07	88	139.5283	0.0000e+00	0.0000e+00
13	27.8300	0.0000e+00	0.0000e+00	89	139.5284	0.0000e+00	0.0000e+00
14	35.2782	2.0900e-08	0.0000e+00	90	141.6707	0.0000e+00	0.0000e+00
15	35.2825	0.0000e+00	0.0000e+00	91	141.6716	0.0000e+00	0.0000e+00
16	36.1774	0.0000e+00	0.0000e+00	92	141.9819	0.0000e+00	0.0000e+00
17	36.1873	0.0000e+00	0.0000e+00	93	141.9840	0.0000e+00	0.0000e+00
18	51.5443	3.1899e-09	0.0000e+00	94	142.8326	0.0000e+00	0.0000e+00
19	51.5474	0.0000e+00	0.0000e+00	95	142.8335	0.0000e+00	0.0000e+00
20	57.6149	0.0000e+00	0.0000e+00	96	146.1858	0.0000e+00	0.0000e+00
21	57.6172	0.0000e+00	0.0000e+00	97	146.1861	0.0000e+00	0.0000e+00
22	61.6297	0.0000e+00	0.0000e+00	98	149.4763	0.0000e+00	0.0000e+00
23	61.6347	0.0000e+00	0.0000e+00	99	149.4803	0.0000e+00	0.0000e+00
24	71.8869	0.0000e+00	0.0000e+00	100	152.3675	0.0000e+00	0.0000e+00
25	71.8898	0.0000e+00	3.8190e-09	101	152.5578	0.0000e+00	0.0000e+00
26	76.2994	0.0000e+00	0.0000e+00	102	153.7746	0.0000e+00	0.0000e+00
27	76.2999	0.0000e+00	0.0000e+00	103	164.2998	2.3023e-07	0.0000e+00
28	85.0401	0.0000e+00	0.0000e+00	104	164.3019	5.7435e-08	0.0000e+00
29	85.0459	0.0000e+00	0.0000e+00	105	164.5174	0.0000e+00	1.1348e-07
30	89.6306	0.0000e+00	0.0000e+00	106	164.5176	0.0000e+00	0.0000e+00
31	89.6307	0.0000e+00	0.0000e+00	107	165.2054	8.1132e-07	0.0000e+00
32	95.2070	0.0000e+00	0.0000e+00	108 *E"(x)	165.2447	4.0016e-05	0.0000e+00
33	95.2091	0.0000e+00	0.0000e+00	109	165.3773	0.0000e+00	3.9538e-09
34	102.0082	0.0000e+00	0.0000e+00	110	165.3780	0.0000e+00	0.0000e+00
35	102.0091	0.0000e+00	0.0000e+00	111	165.5665	0.0000e+00	6.3685e-07
36	102.1693	0.0000e+00	0.0000e+00	112	165.5727	0.0000e+00	0.0000e+00
37	102.1704	0.0000e+00	0.0000e+00	113 *E"(y)	166.2991	1.1501e-04	0.0000e+00
38	107.6967	0.0000e+00	0.0000e+00	114	166.3314	1.1228e-06	0.0000e+00
39	110.3673	0.0000e+00	0.0000e+00	115	168.0348	0.0000e+00	0.0000e+00
40	110.6988	0.0000e+00	0.0000e+00	116	168.0371	0.0000e+00	0.0000e+00
41	112.1514	0.0000e+00	0.0000e+00	117	168.8408	0.0000e+00	2.3263e-09
42	112.1516	0.0000e+00	0.0000e+00	118	168.8453	0.0000e+00	0.0000e+00
43	112.4234	0.0000e+00	0.0000e+00	119	172.0236	0.0000e+00	0.0000e+00
44	112.4247	0.0000e+00	0.0000e+00	120	172.0241	0.0000e+00	0.0000e+00
45	112.4459	0.0000e+00	0.0000e+00	121	173.5651	2.7199e-08	0.0000e+00
46	112.4512	0.0000e+00	0.0000e+00	122	173.5659	0.0000e+00	0.0000e+00
47	114.1139	0.0000e+00	0.0000e+00	123	176.5753	0.0000e+00	0.0000e+00
48	114.1156	0.0000e+00	0.0000e+00	124	176.5777	0.0000e+00	0.0000e+00
49	114.6704	0.0000e+00	0.0000e+00	125	179.5178	0.0000e+00	0.0000e+00
50	114.6712	0.0000e+00	0.0000e+00	126	180.2997	0.0000e+00	0.0000e+00
51	115.2674	0.0000e+00	0.0000e+00	127	180.3003	0.0000e+00	0.0000e+00
52	115.2681	0.0000e+00	0.0000e+00	128	180.8233	0.0000e+00	0.0000e+00
53	115.9309	0.0000e+00	0.0000e+00	129	180.8240	0.0000e+00	0.0000e+00
54	115.9312	0.0000e+00	0.0000e+00	130	182.2798	0.0000e+00	0.0000e+00
55	117.2375	0.0000e+00	0.0000e+00	131	182.6072	0.0000e+00	0.0000e+00
56	117.2377	0.0000e+00	0.0000e+00	132	184.1532	0.0000e+00	0.0000e+00
57	117.8539	0.0000e+00	0.0000e+00	133	184.1554	0.0000e+00	0.0000e+00
58	117.8549	0.0000e+00	0.0000e+00	134	186.1518	0.0000e+00	0.0000e+00
59	119.8634	0.0000e+00	0.0000e+00	135	186.1523	0.0000e+00	0.0000e+00
60	119.8636	0.0000e+00	0.0000e+00	136	186.5818	0.0000e+00	0.0000e+00
61	120.0330	0.0000e+00	0.0000e+00	137	186.5829	0.0000e+00	0.0000e+00
62	120.0342	0.0000e+00	0.0000e+00	138	186.7730	0.0000e+00	0.0000e+00
63	120.1289	0.0000e+00	0.0000e+00	139	186.7735	0.0000e+00	0.0000e+00
64	120.1342	0.0000e+00	0.0000e+00	140	187.1726	0.0000e+00	0.0000e+00
65	120.2579	0.0000e+00	0.0000e+00	141	187.1764	0.0000e+00	0.0000e+00
66	120.2622	0.0000e+00	0.0000e+00	142	187.7026	0.0000e+00	0.0000e+00
67	120.6842	0.0000e+00	0.0000e+00	143	187.7034	0.0000e+00	0.0000e+00
68	120.6883	0.0000e+00	0.0000e+00	144	188.2704	0.0000e+00	0.0000e+00
69	120.8324	0.0000e+00	0.0000e+00	145	188.2707	0.0000e+00	0.0000e+00
70	120.8331	0.0000e+00	0.0000e+00	146	188.4532	0.0000e+00	0.0000e+00
71	121.7699	0.0000e+00	0.0000e+00	147	188.4541	0.0000e+00	0.0000e+00
72	121.7716	0.0000e+00	0.0000e+00	148	192.2173	0.0000e+00	0.0000e+00
73	122.6488	0.0000e+00	0.0000e+00	149	192.2174	0.0000e+00	0.0000e+00
74	122.6497	0.0000e+00	0.0000e+00	150	192.4596	0.0000e+00	0.0000e+00
75	123.8163	0.0000e+00	0.0000e+00	151	192.4606	0.0000e+00	0.0000e+00
76	123.8170	0.0000e+00	0.0000e+00	152	194.5190	0.0000e+00	0.0000e+00

#	Frequency	$f_{xy}(\omega_j)$	$f_z(\omega_j)$	#	Frequency	$f_{xy}(\omega_j)$	$f_z(\omega_j)$
153	194.5268	0.0000e+00	0.0000e+00	230	277.2789	5.7531e-03	0.0000e+00
154	194.5273	0.0000e+00	0.0000e+00	231	277.2791	6.0488e-03	0.0000e+00
155	194.5752	0.0000e+00	0.0000e+00	232	277.4235	0.0000e+00	0.0000e+00
156	194.5758	0.0000e+00	0.0000e+00	233	277.4882	0.0000e+00	1.3966e-04
157	194.5888	0.0000e+00	0.0000e+00	234	277.7334	9.9393e-01	0.0000e+00
158	194.6389	0.0000e+00	0.0000e+00	235	277.8259	9.9558e-01	0.0000e+00
159	194.9594	0.0000e+00	0.0000e+00	236	278.8554	0.0000e+00	9.8602e-09
160	194.9616	0.0000e+00	0.0000e+00	237	278.8563	0.0000e+00	0.0000e+00
161	194.9821	0.0000e+00	0.0000e+00	238	279.2194	2.3366e-07	0.0000e+00
162	194.9920	0.0000e+00	0.0000e+00	239	279.2202	1.2872e-07	0.0000e+00
163	195.0167	0.0000e+00	0.0000e+00	240	281.2949	0.0000e+00	0.0000e+00
164	195.0168	0.0000e+00	0.0000e+00	241	281.2958	0.0000e+00	0.0000e+00
165	196.1237	0.0000e+00	0.0000e+00	242	282.0133	3.1367e-09	0.0000e+00
166	196.1242	0.0000e+00	0.0000e+00	243	282.0137	0.0000e+00	0.0000e+00
167	196.1625	0.0000e+00	0.0000e+00	244	283.5714	0.0000e+00	0.0000e+00
168	196.1636	0.0000e+00	0.0000e+00	245	283.6668	5.5553e-08	0.0000e+00
169	196.3572	0.0000e+00	0.0000e+00	246	284.0780	0.0000e+00	0.0000e+00
170	196.3587	0.0000e+00	0.0000e+00	247	284.0787	0.0000e+00	0.0000e+00
171	196.8589	0.0000e+00	0.0000e+00	248	284.3158	0.0000e+00	0.0000e+00
172	196.8613	0.0000e+00	0.0000e+00	249	284.3165	0.0000e+00	0.0000e+00
173	198.2623	0.0000e+00	0.0000e+00	250	284.7569	0.0000e+00	0.0000e+00
174	198.2641	0.0000e+00	0.0000e+00	251	284.7606	0.0000e+00	0.0000e+00
175	200.8625	0.0000e+00	0.0000e+00	252	285.0748	0.0000e+00	0.0000e+00
176	200.8627	0.0000e+00	0.0000e+00	253	285.6463	1.8453e-08	0.0000e+00
177	201.9206	0.0000e+00	0.0000e+00	254	285.6464	0.0000e+00	0.0000e+00
178	201.9208	0.0000e+00	0.0000e+00	255	285.7199	0.0000e+00	0.0000e+00
179	202.4013	0.0000e+00	0.0000e+00	256	285.7221	0.0000e+00	0.0000e+00
180	202.4016	0.0000e+00	0.0000e+00	257	285.9973	0.0000e+00	0.0000e+00
181	202.6970	0.0000e+00	0.0000e+00	258	285.9975	4.0972e-09	0.0000e+00
182	202.6971	0.0000e+00	0.0000e+00	259	286.3782	0.0000e+00	2.4080e-09
183	203.5375	0.0000e+00	0.0000e+00	260	286.3802	0.0000e+00	0.0000e+00
184	203.5389	0.0000e+00	0.0000e+00	261 *E'(z)	286.3858	0.0000e+00	1.1638e-03
185	206.3360	0.0000e+00	0.0000e+00	262	286.4566	0.0000e+00	0.0000e+00
186	206.3453	0.0000e+00	0.0000e+00	263	286.5439	3.9181e-09	0.0000e+00
187	207.7706	0.0000e+00	0.0000e+00	264	286.5444	0.0000e+00	0.0000e+00
188	211.8350	0.0000e+00	0.0000e+00	265	286.9856	2.6576e-08	0.0000e+00
189	211.8353	0.0000e+00	0.0000e+00	266	286.9861	0.0000e+00	0.0000e+00
190	217.1501	0.0000e+00	0.0000e+00	267	287.3942	0.0000e+00	0.0000e+00
191	217.1509	0.0000e+00	0.0000e+00	268	287.3954	0.0000e+00	0.0000e+00
192	218.5335	0.0000e+00	0.0000e+00	269	288.0934	0.0000e+00	0.0000e+00
193	218.5344	0.0000e+00	0.0000e+00	270	288.0967	0.0000e+00	0.0000e+00
194	219.0516	0.0000e+00	0.0000e+00	271	288.9074	0.0000e+00	0.0000e+00
195	219.0535	0.0000e+00	0.0000e+00	272	288.9085	0.0000e+00	0.0000e+00
196	219.9614	0.0000e+00	0.0000e+00	273	289.3836	0.0000e+00	0.0000e+00
197	219.9623	0.0000e+00	0.0000e+00	274	289.3837	2.4984e-09	0.0000e+00
198	222.2880	0.0000e+00	4.8598e-09	275	289.6797	0.0000e+00	0.0000e+00
199	222.2904	0.0000e+00	0.0000e+00	276	289.7007	0.0000e+00	0.0000e+00
200	226.1703	8.3005e-06	0.0000e+00	277	290.7716	0.0000e+00	0.0000e+00
201	226.1705	4.9376e-06	0.0000e+00	278	290.7867	3.1457e-09	0.0000e+00
202	230.6795	0.0000e+00	0.0000e+00	279	290.7873	0.0000e+00	0.0000e+00
203 *A'_1(z)	230.7519	0.0000e+00	1.2680e-05	280	291.0347	0.0000e+00	0.0000e+00
204	233.4271	1.8821e-05	0.0000e+00	281	291.3793	0.0000e+00	0.0000e+00
205	249.4671	0.0000e+00	0.0000e+00	282	291.5225	0.0000e+00	0.0000e+00
206	249.4673	0.0000e+00	0.0000e+00	283	291.5239	0.0000e+00	0.0000e+00
207	250.5295	1.2693e-09	0.0000e+00	284	292.0997	0.0000e+00	0.0000e+00
208	250.5298	0.0000e+00	0.0000e+00	285	292.1013	0.0000e+00	0.0000e+00
209	255.3279	1.2084e-09	0.0000e+00	286	294.8619	0.0000e+00	0.0000e+00
210	255.3289	0.0000e+00	0.0000e+00	287	294.8656	0.0000e+00	0.0000e+00
211	256.9785	0.0000e+00	0.0000e+00	288	296.6353	0.0000e+00	0.0000e+00
212	256.9785	0.0000e+00	0.0000e+00	289	296.6354	0.0000e+00	1.0003e-08
213	264.6738	0.0000e+00	0.0000e+00	290	298.1685	1.9924e-06	0.0000e+00
214	264.6739	0.0000e+00	0.0000e+00	291	298.1707	2.6434e-06	0.0000e+00
215	265.3222	0.0000e+00	0.0000e+00	292	300.0483	0.0000e+00	0.0000e+00
216	265.3223	0.0000e+00	0.0000e+00	293	300.0488	0.0000e+00	0.0000e+00
217	267.9888	0.0000e+00	0.0000e+00	294	305.3310	0.0000e+00	0.0000e+00
218	267.9892	0.0000e+00	0.0000e+00	295	305.3354	0.0000e+00	0.0000e+00
219	269.2317	0.0000e+00	0.0000e+00	296	310.4386	0.0000e+00	0.0000e+00
220	269.8267	0.0000e+00	0.0000e+00	297	310.4386	0.0000e+00	0.0000e+00
221	269.8267	0.0000e+00	0.0000e+00	298	315.8700	0.0000e+00	1.4546e-09
222	269.8656	0.0000e+00	0.0000e+00	299	315.8747	0.0000e+00	0.0000e+00
223	269.8658	0.0000e+00	0.0000e+00	300	322.6883	6.4744e-09	0.0000e+00
224	270.1820	0.0000e+00	0.0000e+00	301	322.6889	5.3295e-09	0.0000e+00
225	270.1820	0.0000e+00	0.0000e+00	302	331.0249	0.0000e+00	1.9422e-04
226	270.5389	1.2482e-09	0.0000e+00	303	331.0312	0.0000e+00	0.0000e+00
227	270.5956	0.0000e+00	0.0000e+00	304 *A''_2(x)	338.4135	1.4042e-03	0.0000e+00
228	270.9801	0.0000e+00	0.0000e+00	305	338.6413	1.1579e-04	0.0000e+00
229	270.9818	0.0000e+00	0.0000e+00	306	341.6002	0.0000e+00	1.0000e+00