Supporting Information

Novel mixed topological state in monolayer MnSbO3

Yanzhao Wu^a, Li Deng^a, Junwei Tong^b, Xiang Yin^a, Gaowu Qin^a and Xianmin Zhang^{a*} ^aKey Laboratory for Anisotropy and Texture of Materials (Ministry of Education), School of Material Science and Engineering, Northeastern University, Shenyang, 110819, China ^bDepartment of Physics, Freie Universität Berlin, Berlin, 14195, Germany

*E-mail: zhangxm@atm.neu.edu.cn

To evaluate the its stability, the phonon spectra, ab initio molecular dynamics (AIMD) simulation at 300 K and formation energy of monolayer MnSbO₃ are calculated. As shown in Figure S1(a), the absence of imaginary frequencies in the phonon spectra confirms the dynamical stability of the material. During the AIMD simulations, the total energy fluctuates within a small range, as demonstrated in Figure S1(b). Furthermore, the inset of Figure S1(b) shows that after 6 ps of AIMD simulations, the structure of monolayer MnSbO₃ remains intact, indicating its thermal stability. Furthermore, the formation energy of the monolayer MnSbO₃ is also studied, which is defined as $E_f = E_{total} - 2E_{Mn} - 2E_{Sb} - 6E_0$. Here, E_{total} is the ground state energy of monolayer MnSbO₃ in the primitive cell. E_{Mn} , E_{Sb} and E_0 is the energy per atom of Mn, Sb and O in their most stable phases, respectively. The calculated values of E_f for monolayer MnSbO₃ is -15.69 eV (shown in Table S1), which is lower than that of monolayer NiAsO₃ (-10.62 eV) [1] and MnAsO₃ (-11.12 eV) [2], demonstrating that monolayer MnSbO₃ have a good thermodynamical stability against the elemental phases.



Figure S1. (a) Phonon spectrum of monolayer MnSbO₃. (b) Total energy fluctuation of the AIMD simulations for monolayer MnSbO₃. Inset is the structure of monolayer MnSbO₃ at 6 ps.

Table S1. The values of E_{f_1} , E_{total_1} , E_{Mn_1} , E_{Sb} and E_{O} for monolayer MnSbO₃.

Material	E_{total} (eV)	E_{Mn} (eV)	E_{Sb} (eV)	E_{0} (eV)	E_{f} (eV)
MnSbO ₃	-22.39	-5.87	-4.15	-1.91	-15.69

Figure S2 displays one ferromagnetic (FM) and three antiferromagnetic (AFM1, AFM2 and AFM3) configurations of monolayer MnSbO₃.



Figure S2. One ferromagnetic (FM) and three antiferromagnetic (AFM1, AFM2 and AFM3) configurations of monolayer MnSbO₃.

At $\varphi = 5^{\circ}$, 10°, 15°, 20° and 25° in xy plane, topological gap of monolayer MnSbO₃ decreases gradually, as shown in Figures S3(a)-S3(e). As $\varphi = 90^{\circ}$, monolayer MnSbO₃ presents a half metal state, as indicated in Figure S3(f). Under $\varphi = 120^{\circ}$ case, monolayer MnSbO₃ recovers the QAH states, as described in Figure S3(g). At $\varphi = 150^{\circ}$ and 180°, monolayer MnSbO₃ behaves as a half metal and QAH insulators, respectively, as shown in Figures S3(h) and S3(i).



Figure S3. Orbital-resolved energy bands of monolayer MnSbO3 as M direction varies in xy plane.

Figure S4 shows the orbital-resolved energy bands of monolayer $MnSbO_3$ as the M direction varies in xz plane. As θ changes from 30° to 180°, the topological band gap of monolayer $MnSbO_3$ increases first, and then decreases, as shown in Figures S4(a)-S4(f).



Figure S4. Orbital-resolved energy bands of monolayer MnSbO3 as the M varies in xz plane.

As shown in Figure S5, under -5% ~ 5% strains, monolayer MnSbO₃ exhibits a QAH state as the M direction along $\varphi = 0^{\circ}$. Moreover, during this progress, the topological band gap of monolayer MnSbO₃ gradually decreases from 9.6 to 6.7 meV.



Figure S5. The orbital-resolved energy bands of monolayer MnSbO₃ under different strains as the M direction along $\phi = 0^{\circ}$, respectively.

As drawn in Figures S6, under -5% ~ 5% strains, monolayer MnSbO₃ behaves as a QAH insulator as the M direction along $\theta = 0^{\circ}$. Moreover, throughout the strains, the topological band gap of monolayer MnSbO₃ also reduces from 26.9 to 24.9 meV.



Figure S6. The orbital-resolved energy bands of monolayer MnSbO₃ under different strains as the M direction along $\theta = 0^{\circ}$, respectively.

As shown in Figures S7(a)-S7(f), under $0 \sim 5$ eV U values, monolayer MnSbO₃ exhibits a QAH state as the M direction along $\varphi = 0^{\circ}$. Moreover, during this progress, the topological band gap of monolayer MnSbO₃ gradually decreases from 9.2 to 7.9 meV. As drawn in Figures S7(g)-S7(l), under $0 \sim 5$ eV U values, monolayer MnSbO₃ behaves as a QAH insulator as the M direction along $\theta = 0^{\circ}$. Moreover, throughout the strains, the topological band gap of monolayer MnSbO₃ also reduces from 38.3 to 24.2 meV. Therefore, the QAH property of monolayer MnSbO₃ is robust for strains and U values.



Figure S7. The orbital-resolved energy bands of monolayer MnSbO₃ under different U values as the M direction along $\phi = 0^{\circ}$ and $\theta = 0^{\circ}$, respectively.

References

- Z. Y. Li, Y. L. Han, Z. H. Qiao. Chern number tunable quantum anomalous Hall effect in monolayer transitional metal oxides via manipulating magnetization orientation. *Phys. Rev. Lett.* **129**, 036801 (2022).
- [2] H. Chen, J.n Lu, N. Wang, X. Zhao, G. Hu, X. Yuan, and J. Ren, Strain-induced high-Chern-number spin-unlocked edge states in monolayer MnAsO₃ with intrinsic quantum anomalous Hall effect, *Appl. Phys. Lett.* **124**, 153101 (2024).