Supplementary information

Visualization of trap distribution in SrAl<sub>2</sub>O<sub>4</sub>:Eu<sup>2+</sup>,Dy<sup>3+</sup> revealed by simulations of luminescence change in charging and emission of persistent luminescence and thermoluminescence based on a random walk model

Ryusuke Koizumi, Ryoya Takahashi, Shigeki Yamada, Shingo Hattori, Kazuteru Shinozaki<sup>\*</sup>

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#### S-1. Experimental

### Preparation of PersL SAOED<sub>x</sub> (x = 2, 4, 5, 6, 8, 10)

 $Sr_{0.9}Al_2O_4:Eu^{2+}_{0.01x},Dy^{3+}_{(0.1-0.01x)}$  (x = 2, 4, 5, 6, 8, 10), SAOED<sub>x</sub>, were synthesized according to the procedure described in the literature.<sup>s1</sup> To a mixture of SrCO<sub>3</sub> and Al<sub>2</sub>O<sub>3</sub> powders in the molar ratio 0.9 : 1.0, Eu<sub>2</sub>O<sub>3</sub> and Dy<sub>2</sub>O<sub>3</sub> powders were added so as to be the molar ratios of 0.02 : 0.08, 0.04 : 0.06, 0.05 : 0.05, 0.06 : 0.04, 0.08 : 0.02, or 0.10 : 0.00. After grinding for 1 h with a mortar and a pestle, the resulting powders were pressed under 2 t for 15 min to become pellet-like solid. The pellets of SAOED<sub>x</sub> were placed in a SILICONIT electric furnace TEXSH-530 under argon atmosphere containing 1% hydrogen gas and heated up from room temperature to 1500 °C for over 5 h. The temperature of the electric furnace was maintained at 1500 °C for 2 h and then decreased to room temperature over one night.

#### Reference

 R. M. Calderón-Olvera, E. A. Albanés-Ojeda, M. García-Hipólito, J. M. Hernández-Alcántara, M. A. Álvarez-Perez, C. Falcony, O. Álvarez-Fregoso, *Ceram. Int.*, 2018, 44, 7917.

#### Measurement

PL and PeasL of SAOED<sub>x</sub> (x = 2, 4, 5, 6, 8, 10) were recorded on a JASCO spectrofluorometer FP-6500. PXRD measurements were performed using a Bruker AXS NEW D8 ADVANCE with the Cu K $\alpha$  radiation (1.5406 Å) at 40 kV and 40 mA for SAOED<sub>x</sub> powders obtained by griding with mortar and pestle. We employed an Oxford microstat N equipped with a thermo-controller Oxford ITC502 for the temperature control for TL spectra. The temperature of SAOED<sub>x</sub> powders increased at a rate of ca. 1 K/s from 200 K to 500 K. TL spectra were depicted against temperature corresponding to time from the beginning of the observation. For the TL measurement, after the samples were heated at 500 K for de-trapping under the dark and cooled to 200 K by liquid nitrogen, they were excited with 370 nm (10 W) LED light for 10 min and left to stand in the dark.

S-2. PL emission and excitation spectra of  $SAOED_x$  (x = 2, 4, 5, 6, 8, 10)

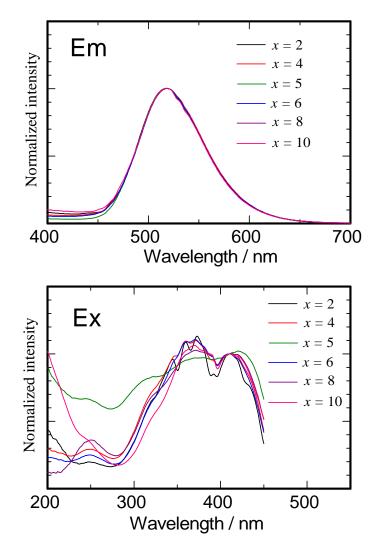
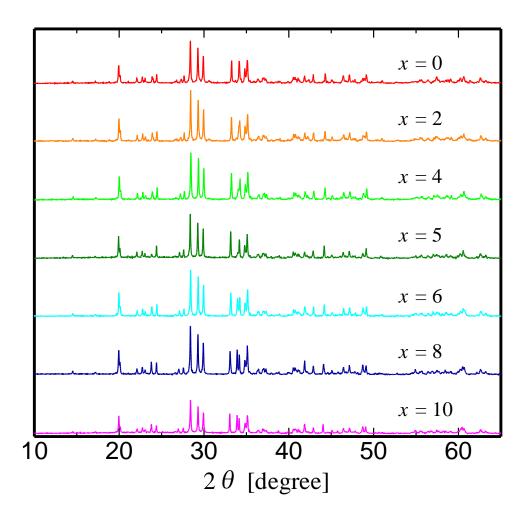


Figure S1. PL emission spectra (top) and excitation spectra (bottom) of  $SAOED_x$  (x = 2 (red), 4 (orange), 5 (green), 6 (dark green), 8 (cyan), 10 (blue).

S-3. PXRD of SAOED<sub>x</sub> (x = 2, 4, 5, 6, 8, 10)



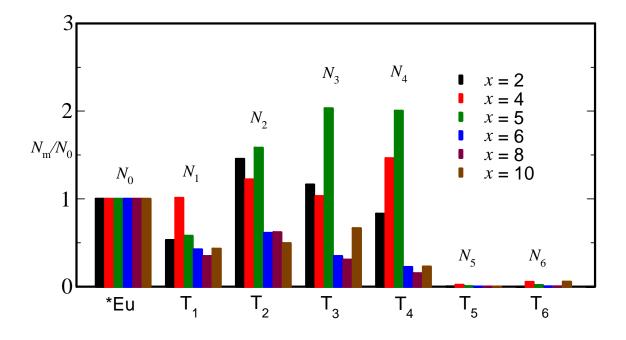
**Figure S2**. PXRD patterns of SAOED<sub>*x*</sub>, where x = 0 (red), 2 (orange), 4 (green), 5 (dark green), 6 (cyan), 8 (blue), 10 (purple).

## S-4. Lattice constants $(a, b, c, \beta)$ for SAOED<sub>x</sub> (x = 2, 4, 5, 6, 8, 10) crystals

**Table S1**. Lattice constants  $(a, b, c, \beta)$  for SAOED<sub>x</sub> in the monoclinic crystal system evaluated from the PXRD patterns using the Bragg's equation.

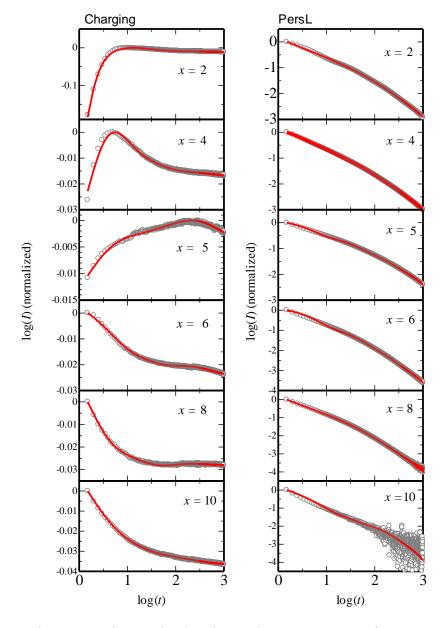
x	<i>a</i> / Å	<i>b</i> /Å	<i>c</i> /Å	β /°
0	8.384	8.887	5.198	93.403
2	8.381	8.879	5.193	93.400
4	8.367	8.870	5.188	93.396
5	8.380	8.904	5.208	93.406
6	8.374	8.887	5.198	93.401
8	8.382	8.887	5.191	93.257
10	8.383	8.887	5.186	93.298

S-5. Electron populations in reservoirs  $N_m$  (m = 0-6) for SAOED<sub>x</sub> (x = 2, 4, 5, 6, 8, 10)



**Figure S3.** Electron populations in reservoirs  $N_m$  (m = 0–6) for SAOED<sub>x</sub> (x = 2, 4, 5, 6, 8, 10) predicted by the simulation of charging and PersL processes based on RWM.

# S-6. Luminescence changes in charging and PersL processes for $SAOED_x$ (x = 2, 4, 5, 6, 8, 10)



**Figure S4.** Luminescence changes in charging and PersL processes for SAOED<sub>x</sub> (x = 2, 4, 5, 6, 8, 10). The red lines are the best fits for the curve fitting using equations  $I_c = I_{c1}\exp(-t/\tau_{c1}) + I_{c2}\exp(-t/\tau_{c2}) - I_{c3}\exp(-t/\tau_{c3}) + I_{c0}$  for the charging (left) and  $I_p = I_{p1}\exp(-t/\tau_{p1}) + I_{p2}\exp(-t/\tau_{p2}) + I_{p3}\exp(-t/\tau_{p3})$  for PersL (right).

# S-7. Parameters determined through the simulation of the luminescence changes in charging and PersL for SAOED<sub>x</sub> (x = 2, 4, 5, 6, 8, 10)

**Table S2.** Parameters determined through the simulation of the luminescence changes in charging and PersL for SAOED<sub>x</sub> (x = 2, 4, 5, 6, 8, 10) using equations  $I_c = I_{c1}exp(-t/\tau_{c1}) + I_{c2}exp(-t/\tau_{c2}) + I_{c3}exp(-t/\tau_{c3}) + I_{c0}$  for the charging and  $I_p = I_{p1}exp(-t/\tau_{p1}) + I_{p2}exp(-t/\tau_{p2}) + I_{p3}exp(-t/\tau_{p3})$ .

Charging		PersI	
	44 -		5.0 -
			$\tau_{p1} = 5.0 \text{ s}$
	$\tau_{c2} = 51000 \text{ s}$		$\tau_{p2} = 65 \text{ s}$
	$\tau_{c3} = 1.3 \text{ s}$	$I_{p3} = 1\%$	$\tau_{p3} = 430 \text{ s}$
$I_{c1} = 0.040$	$\tau_{c1} = 23 \ s$	$I_{\rm p1} = 89\%$	$\tau_{p1} = 7.3 \text{ s}$
$I_{c2} = 0.26$	$\tau_{c2} = 61000 \text{ s}$	$I_{\rm p2} = 9\%$	$\tau_{p2} = 71 \text{ s}$
$I_{c3} = -0.46$	$\tau_{c3} = 0.74 \text{ s}$	$I_{p3} = 1\%$	$\tau_{p3} = 450 \text{ s}$
$I_{\rm c0} = 0.70$	•5		P
$I_{c1} = 0.019$	$\tau_{c1} = 2600 \text{ s}$	$I_{\rm p1} = 92\%$	$\tau_{p1} = 3.7 \text{ s}$
$I_{c2} = -0.025$	$\tau_{c2} = 3.0 \text{ s}$	$I_{p2} = 7\%$	$\tau_{p2} = 49 \text{ s}$
$I_{c3} = -0.0083$	•2	$I_{p3} = 1\%$	$\tau_{p3} = 450 \text{ s}$
$I_{\rm c0} = 0.98$		1	tps lete b
$I_{c1} = 490$	$\tau_{c1} = 8.0 \text{ s}$	$I_{\rm p1} = 90\%$	$\tau_{p1} = 2.6 \text{ s}$
$I_{c2} = 0.017$	$\tau_{c2} = 1400 \text{ s}$	$I_{p2} = 9\%$	$\tau_{p2} = 27 \text{ s}$
$I_{c3} = 6.3 \times 10^{-6}$		$I_{p3} = 1\%$	$\tau_{p3} = 170 \text{ s}$
$I_{\rm c0} = 0.94$	100005	1	<b>Up</b> 5 1705
$I_{c1} = 0.098$	$\tau_{c1} = 1.5 \text{ s}$	$I_{\rm p1} = 91\%$	$\tau_{p1} = 4.9 \text{ s}$
$I_{c2} = 0.029$	$\tau_{c2} = 8.5 \text{ s}$	$I_{p2} = 8\%$	$\tau_{p2} = 57 \text{ s}$
$I_{c3} = 1.9 \times 10^{-5}$		$I_{p3} = 1\%$	$\tau_{p3} = 380 \text{ s}$
$I_{c0} = 0.94$	•0, 0,00		•p5 500 5
$I_{c1} = 0.079$	$\tau_{c1} = 1.9 \text{ s}$	$I_{p1} = 93\%$	$\tau_{p1} = 3.2 \text{ s}$
$I_{c2} = 0.035$		$I_{p2} = 6\%$	$\tau_{p2} = 49 \text{ s}$
			$\tau_{p3} = 270 \text{ s}$
-	1703	r-	ups 2703
	$I_{c3} = -0.46$ $I_{c0} = 0.70$ $I_{c1} = 0.019$ $I_{c2} = -0.025$ $I_{c3} = -0.0083$ $I_{c0} = 0.98$ $I_{c1} = 490$ $I_{c2} = 0.017$ $I_{c3} = 6.3 \times 10^{-6}$ $I_{c0} = 0.94$ $I_{c1} = 0.098$ $I_{c2} = 0.029$ $I_{c3} = 1.9 \times 10^{-5}$ $I_{c0} = 0.94$ $I_{c1} = 0.079$	$\begin{array}{c c} I_{c1} = 0.025 & & \tau_{c1} = 44 \text{ s} \\ I_{c2} = 0.26 & & \tau_{c2} = 51000 \text{ s} \\ I_{c3} = -1.1 & & \tau_{c3} = 1.3 \text{ s} \\ \hline I_{c0} = 0.72 & & \tau_{c1} = 23 \text{ s} \\ I_{c2} = 0.26 & & \tau_{c2} = 61000 \text{ s} \\ I_{c3} = -0.46 & & \tau_{c3} = 0.74 \text{ s} \\ \hline I_{c1} = 0.019 & & \tau_{c1} = 2600 \text{ s} \\ I_{c2} = -0.025 & & \tau_{c2} = 3.0 \text{ s} \\ I_{c3} = -0.0083 & & \tau_{c3} = 70 \text{ s} \\ \hline I_{c1} = 490 & & \tau_{c1} = 8.0 \text{ s} \\ I_{c2} = 0.017 & & \tau_{c2} = 1400 \text{ s} \\ I_{c3} = 6.3 \times 10^{-6} & & \tau_{c3} = 10000 \text{ s} \\ \hline I_{c1} = 0.098 & & \tau_{c1} = 1.5 \text{ s} \\ I_{c2} = 0.029 & & \tau_{c2} = 8.5 \text{ s} \\ I_{c3} = 1.9 \times 10^{-5} & & \tau_{c3} = 590 \text{ s} \\ \hline I_{c1} = 0.079 & & \tau_{c1} = 1.9 \text{ s} \\ I_{c2} = 0.013 & & \tau_{c3} = 190 \text{ s} \\ \end{array}$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $