## **Supplementary Information:**

## A Molecular Dynamics Study of Enhanced CO<sub>2</sub> Separation via Boron Nitride Nanotubes Embedded in a Silicon Nitride Membrane

Winarto,<sup>a,\*</sup> Lilis Yuliati,<sup>a</sup> Khairul Anam,<sup>a</sup> Paul E. Brumby,<sup>b</sup> and Kenji Yasuoka<sup>b</sup>

 <sup>a</sup> Department of Mechanical Engineering, Faculty of Engineering, Brawijaya University, Jl. MT Haryono 167, Malang 65145, Indonesia
<sup>b</sup> Department of Mechanical Engineering, Keio University, 3-14-1 Hiyoshi, Kohoku-ku, Yokohama 223-8522, Japan

\*E-mail: winarto@ub.ac.id

Figure S1A and B display the simulation system of (18, 18) and (20, 20) BNNTs embedded in a silicon nitride (Si<sub>3</sub>N<sub>4</sub>) membrane, respectively. Dimension of the Si<sub>3</sub>N<sub>4</sub> membrane is  $3.80 \times 3.95 \text{ nm}^2$  and the diameters of (18, 18) and (20, 20) BNNTs are 2.5 nm and 2.8 nm, respectively.



Figure S1 Simulation systems of: (A) (18, 18) BNNT-Si<sub>3</sub>N<sub>4</sub> and (B) (20, 20) BNNT-Si<sub>3</sub>N<sub>4</sub>

Figure S2A and B show distribution of the non-uniform electric fields inside the (18, 18) and (20, 20) BNNTs. The electric fields are generated by the positive charges of silicon atoms and the negative charges of nitrogen atoms in the Si<sub>3</sub>N<sub>4</sub> membrane.



**Figure S2** Distribution of electric field in the systems of: (A) (18, 18) BNNT-Si<sub>3</sub>N<sub>4</sub> and (B) (20, 20) BNNT-Si<sub>3</sub>N<sub>4</sub>

Figure S3A represents the structure of CO<sub>2</sub> molecules in the (18, 18) BNNT system while Figure S3B and C are snapshots of the CO<sub>2</sub> structures in (18, 18) BNNT-Si<sub>3</sub>N<sub>4</sub> systems. The structure in Figure S3B was obtained from simulation with normal condition where there are positive and negative charges on the silicon and nitrogen atoms of the Si<sub>3</sub>N<sub>4</sub> membrane, respectively. Meanwhile, the structure in Figure 3C was obtained from simulation without charges on the Si<sub>3</sub>N<sub>4</sub> membrane. The charges in the membrane were removed to clarify the effect of the electric fields induced by the charges on the CO<sub>2</sub> structure. Structures in Figure S3A and B are obviously different. This means that the Si<sub>3</sub>N<sub>4</sub> membrane affects the CO<sub>2</sub> structure. The CO<sub>2</sub> structure in Figure S3C differs from that in Figure S3B. However, the structure of Figure S3C is similar to that in Figure S3A. The results suggest that the charges of the Si<sub>3</sub>N<sub>4</sub> membrane play an important role on the changing of the CO<sub>2</sub> structure. As explained before, the charges induce non-uniform electric fields and subsequently influences the CO<sub>2</sub> structure.



**Figure S3** Structures of CO<sub>2</sub> molecules in the system of: (A) (18, 18) BNNT, (B) (18, 18) BNNT-Si<sub>3</sub>N<sub>4</sub>, and (C) (18, 18) BNNT-Si<sub>3</sub>N<sub>4</sub> without charges.

Figure S4 shows distribution of the Lennard-Jones (LJ) potential energy of  $CO_2$  molecule inside the BNNT system and inside the BNNT-Si<sub>3</sub>N<sub>4</sub> system. The LJ potential energy comes from the interaction between  $CO_2$  with BNNT wall for the BNNT system or between  $CO_2$  with BNNT and Si3N4 wall for the BNNT-Si<sub>3</sub>N<sub>4</sub> system.



Figure S4 Distribution of the Lennard-Jones (LJ) potential energy of CO<sub>2</sub> in the BNNT system (upper) and in the BNNT-Si<sub>3</sub>N<sub>4</sub> system (lower) using: (A) (10, 10), (B) (12, 12), and (C) (15, 15) BNNTs. PDF on the vertical axis means the probability distribution function.

Distributions of the Coulomb potential energy of the  $CO_2$  molecule inside the (10, 10), (12, 12), and (15, 15) BNNT-Si<sub>3</sub>N<sub>4</sub> systems are displayed in Figure S5. The potential energy is from the electrostatic interaction between the  $CO_2$  with the Si<sub>3</sub>N<sub>4</sub> membrane.



**Figure S5** The Coulomb potential energy of the interaction between CO<sub>2</sub> molecules inside the (10, 10), (12, 12), and (15, 15) BNNTs with the Si<sub>3</sub>N<sub>4</sub> membrane.

Potential energies within the  $CO_2$  structure inside the (10, 10), (12, 12), and (15, 15) BNNTs of the BNNT system and BNNT-Si3N4 system are shown in Figure S6. The potential energy consists of the van der Waals (or the Lennard-Jones) interactions and the electrostatic interactions within the  $CO_2$  structure.



**Figure S6** Potential energy within the CO<sub>2</sub> structure inside the BNNT system (upper) and inside the BNNT-Si<sub>3</sub>N<sub>4</sub> system (lower) using: (A) (10, 10), (B) (12, 12), and (C) (15, 15) BNNTs.