

## Supporting materials

### Catalyst-free oxidation of nitrogen fixation by underwater bubble discharge: performance optimization and mechanism exploration

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## Bubble Characterization Methodology

Bubble size was determined by taking photographs of bubbles emerging from a coaxial discharge reactor in an optically transparent quartz vessel. The captured bubble images were processed using Fiji (Fiji Is Just ImageJ) image processing software by enhancing the contrast between the glowing bubbles and the background for size analysis using the Weka plug-in in the software.

The Weka Segmentation machine learning algorithms were trained to classify the illuminated bubbles and backgrounds as separate segments. Bubbles are then manually adjusted to eliminate any misidentified bubbles caused by multiple bubbles overlapping or visual artefacts in the photo.

The frequency of each bubble diameter from 0-5 mm in diameter was divided into 0.1 mm increments and the distribution was analyzed to characterize a total of 1500 bubbles between 15 images and The Sauter mean diameter (SMD) following equation S1 was used to represent the mean diameter of the characterized bubbles.

$$SMD = \frac{\sum_{i=1}^N n_i d_i^3}{\sum_{i=1}^N n_i d_i^2} \quad (S1)$$

SMD= Sauter Mean Diameter (mm)

N= Total number of bubbles characterised

$n_i$ = Number of bubbles in size range i

$d_i$ = Diameter of bubble in size range i (mm)

At flow rates above 1 SLM occasional coalescence of adjacent micro-bubbles ( $\varnothing > 1.6$  mm) was observed. The resulting enlargement and breakup of bubbles modulated the instantaneous gap length, leading to small (< 5 %) fluctuations in

discharge current but no sustained instability. This behavior accounts for the slight reduction in  $\text{NO}_x^-$  yield at the highest flow rates (Fig. 4a) and confirms that bubble-size control is beneficial for maintaining a steady spark channel.

### The reduced electric field in the bubble discharge

To ensure stable functionality in ZDPlaskin simulations, it is necessary to adopt an approximation wherein the reduced electric field and electron density are assumed to be constant. This simplification can result in an overestimation of ion densities, sometimes exceeding the electron density. Nevertheless, if ion-related reactions do not significantly influence the overall reaction mechanism, this approximation has a negligible impact on the accuracy of the simulation outcomes. We solve for this using the following equation(S2)

$$\frac{E}{N} = \frac{1}{N} \bullet \sqrt{\frac{P(t)}{\sigma}} \quad (\text{S2})$$

Electron conductivity ( $\sigma$ ) can be calculated as a function of electron density and electron mobility, the latter of which can be obtained from BOLSIG+.

### Zero-D plasma chemistry modelling

The model takes into account parameters of the reactor structure such as the diameter of the high-voltage electrodes, and the solution volume to self-consistently calculate the reduced electric field based on the voltage-current waveforms measured in various discharge modes (Fig. S2) and is used as an input parameter to reveal the

transient plasma properties with a reasonable computational load.

**Table S1.** Summarized important gas phase reactions in N<sub>2</sub>/O<sub>2</sub> plasma system; the gas temperature T<sub>gas</sub>

Process	Rate coefficient [cm <sup>3</sup> s <sup>-1</sup> ] [cm <sup>6</sup> s <sup>-1</sup> ] <sup>‡</sup>	Ref.
<u>Deactivation of O metastable</u>		
R1      O(1D) + O <sub>2</sub> => O + O <sub>2</sub>	6.4d-12 * exp(67.0d0/T <sub>gas</sub> )	[1]
R2      O(1D) + O <sub>2</sub> => O + O <sub>2</sub> (a1)	1.0d-12	[1]
R3      O(1D) + O <sub>2</sub> => O + O <sub>2</sub> (b1)	2.6d-11 * exp(67.0d0/T <sub>gas</sub> )	[1]
R4      O(1D) + N <sub>2</sub> => O + N <sub>2</sub>	2.3d-11	[1]
R5      O(1D) + O <sub>3</sub> => O <sub>2</sub> + O + O	1.2d-10	[1]
R6      O(1D) + O <sub>3</sub> => O <sub>2</sub> + O <sub>2</sub>	1.2d-10	[1]
R7      O(1D) + NO => O <sub>2</sub> + N	1.7d-10	[1]
R8      O(1D) + N <sub>2</sub> O => NO + NO	7.2d-11	[1]
R9      O(1D) + N <sub>2</sub> O => O <sub>2</sub> + N <sub>2</sub>	4.4d-11	[1]
R10     O(1S) + O => O + O	5.0d-11 * exp(-73.0d0/T <sub>gas</sub> )	[1]
R11     O(1S) + N => O + N	1.0d-12	[2]
R12     O(1S) + N => O + N	1.0d-12	[1]
R13     O(1S) + O <sub>2</sub> => O(1D) + O <sub>2</sub>	1.24d-12 * exp(-208.0d0/T <sub>gas</sub> )	[1]
R14     O(1S) + O <sub>2</sub> => O + O + O	3.0d-12 * exp(-850.0d0/T <sub>gas</sub> )	[1]
R15     O(1S) + O <sub>2</sub> => O + O <sub>2</sub> (4.5eV)	2.76d-12 * exp(-208.0d0/T <sub>gas</sub> )	[1]
R16     O(1S) + N <sub>2</sub> => O + N <sub>2</sub>	5.0d-17	[1]
R17     O(1S) + NO => O + NO	2.9d-10	[1]
R18     O(1S) + NO => O(1D) + NO	5.1d-10	[1]
R19     O(1S) + O <sub>3</sub> => O <sub>2</sub> + O <sub>2</sub>	2.9d-10	[1]
R20     O(1S) + N <sub>2</sub> O => O + N <sub>2</sub> O	6.3d-12	[1]
R21     O(1D) + O => O + O	8.0d-12	[1]
R22     O(1S) + O => O + O	7.5d-12	[3,4]
<u>Bimolecular nitrogen-oxygen reactions</u>		
R23     N + NO => O + N <sub>2</sub>	1.8d-11 * (T <sub>gas</sub> /300.0)*0.5	[1]
R24     N + O <sub>2</sub> => O + NO	3.2d-12 * (T <sub>gas</sub> /300.0) * exp(-3150.0d0/T <sub>gas</sub> )	[1]
R25     N + NO <sub>2</sub> => O + O + N <sub>2</sub>	9.1d-13	[1]
R26     N + NO <sub>2</sub> => O + N <sub>2</sub> O	3.0d-12	[1]
R27     N + NO <sub>2</sub> => N <sub>2</sub> + O <sub>2</sub>	7.0d-13	[5]
R28     N + NO <sub>2</sub> => NO + NO	2.3d-12	[1]
R28     O + N <sub>2</sub> => N + NO	3.0d-10 * exp(-38370.0d0/T <sub>gas</sub> )	[1]
R29     O + NO => N + O <sub>2</sub>	7.5d-12 * (T <sub>gas</sub> /300.0) * exp(-19500.0d0/T <sub>gas</sub> )	[1]
R30     O + NO => NO <sub>2</sub>	4.2d-18	[1]
R31     O + N <sub>2</sub> O => N <sub>2</sub> + O <sub>2</sub>	8.3d-12 * exp(-14000.0d0/T <sub>gas</sub> )	[1]
R32     N <sub>2</sub> + O <sub>2</sub> => O + N <sub>2</sub> O	2.5d-10 * exp(-50390.0d0/T <sub>gas</sub> )	
R33     NO + NO => O + N <sub>2</sub> O	2.2d-12 * exp(-32100.0d0/T <sub>gas</sub> )	
R34     NO + O <sub>2</sub> => O + NO <sub>2</sub>	2.8d-12 * exp(-23400.0d0/T <sub>gas</sub> )	
R35     NO + N <sub>2</sub> O => N <sub>2</sub> + NO <sub>2</sub>	4.6d-10 * exp(-25170.0d0/T <sub>gas</sub> )	
R36     NO <sub>2</sub> + NO <sub>2</sub> => NO + NO + O <sub>2</sub>	3.3d-12 * exp(-13500.0d0/T <sub>gas</sub> )	
R37     NO <sub>3</sub> + O <sub>2</sub> => NO <sub>2</sub> + O <sub>3</sub>	1.5d-12 * exp(-15020.0d0/T <sub>gas</sub> )	
R38     NO <sub>3</sub> + NO <sub>3</sub> => O <sub>2</sub> + NO <sub>2</sub> + NO <sub>2</sub>	4.3d-12 * exp(-3850.0d0/T <sub>gas</sub> )	
<u>Dissociation of nitrogen-oxygen molecules</u>		
R39     N <sub>2</sub> + @M => N + N + @M @M = N <sub>2</sub> O <sub>2</sub> NO    O    N @R = 1.0d0   6.6d0	5.4d-8 * (1.0d0-exp(-3354.0d0/T <sub>gas</sub> )) * exp(-113200.0d0/T <sub>gas</sub> ) * @R	
R40     O <sub>2</sub> + @M => O + O + @M @M = N <sub>2</sub> O <sub>2</sub> O    N    NO @R = 1.0d0   5.9d0   21.0d0   1.0d0	6.1d-9 * (1.0d0-exp(-2240.0d0/T <sub>gas</sub> )) * exp(-59380.0d0/T <sub>gas</sub> ) * @R	[1]
R41     NO + @M => N + O + @M @M = N <sub>2</sub> O <sub>2</sub> O    N    NO @R = 1.0d0   20.0d0	8.7d-9 * exp(-75994.0d0/T <sub>gas</sub> ) * @R	[1]
R42     O <sub>3</sub> + @M => O <sub>2</sub> + O + @M @M = N <sub>2</sub> O <sub>2</sub> N @R = 1.0d0   0.38d0	6.6d-10 * exp(-11600.0d0/T <sub>gas</sub> ) * @R	[1]

R43	$N_2O + @M \Rightarrow N_2 + O + @M$ @M = N <sub>2</sub> O <sub>2</sub> NO N <sub>2</sub> O @R = 1.0d0 2.0d0 4.0d0	1.2d-8 * (300.0d0/T <sub>gas</sub> ) * exp(-29000.0d0/T <sub>gas</sub> ) * @R	[1]
R44	$NO_2 + @M \Rightarrow NO + O + @M$ @M = N <sub>2</sub> O <sub>2</sub> NO NO <sub>2</sub> @R = 1.0d0 0.78d0 7.8d0 5.9d0	6.8d-6 * (300.0d0/T <sub>gas</sub> ) * 2 * exp(-36180.0d0/T <sub>gas</sub> ) * @R	[1]
R45	$NO_3 + @M \Rightarrow NO_2 + O + @M$ @M = N <sub>2</sub> O <sub>2</sub> NO N O @R = 1.0d0 10.0d0	3.1d-5 * (300.0d0/T <sub>gas</sub> ) * 2 * exp(-25000.0d0/T <sub>gas</sub> ) * @R	[1]
R46	$NO_3 + @M \Rightarrow NO + O_2 + @M$ @M = N <sub>2</sub> O <sub>2</sub> NO N O @R = 1.0d0 12.0d0	6.2d-5 * (300.0d0/T <sub>gas</sub> ) * 2 * exp(-25000.0d0/T <sub>gas</sub> ) * @R	[1]

#### Negative ion reactions

R47	$O^{\cdot-} + O_2(a1) \Rightarrow O_2^{\cdot-} + O$	1.0d-10	[1]
R48	$O^{\cdot-} + O_3 \Rightarrow O_3^{\cdot-} + O$	8.0d-10	[1]
R49	$O^{\cdot-} + NO_2 \Rightarrow NO_2^{\cdot-} + O$	1.2d-9	[1]
R50	$O^{\cdot-} + N_2O \Rightarrow NO^{\cdot-} + NO$	2.0d-10	[1]
R51	$O^{\cdot-} + N_2O \Rightarrow N_2O^{\cdot-} + O$	2.0d-12	[1]
R52	$O_2^{\cdot-} + O \Rightarrow O^{\cdot-} + O_2$	3.3d-10	[1]
R53	$O_2^{\cdot-} + O_3 \Rightarrow O_3^{\cdot-} + O_2$	3.5d-10	[1]
R54	$O_2^{\cdot-} + NO_2 \Rightarrow NO_2^{\cdot-} + O_2$	7.0d-10	[1]
R55	$O_2^{\cdot-} + NO_3 \Rightarrow NO_3^{\cdot-} + O_2$	5.0d-10	[1]
R56	$O_3^{\cdot-} + O \Rightarrow O_2^{\cdot-} + O_2$	1.0d-11	[1]
R57	$O_3^{\cdot-} + NO \Rightarrow NO_3^{\cdot-} + O$	1.0d-11	[1]
R58	$O_3^{\cdot-} + NO \Rightarrow NO_2^{\cdot-} + O_2$	2.6d-12	[1]
R59	$NO^{\cdot-} + N_2O \Rightarrow NO_2^{\cdot-} + N_2$	2.8d-14	[1]
R60	$NO_2^{\cdot-} + NO_3 \Rightarrow NO_3^{\cdot-} + NO_2$	5.0d-10	[1]

All 3-body reactions are in the unit of [cm<sup>6</sup> s<sup>-1</sup>], 2.d0=2e0

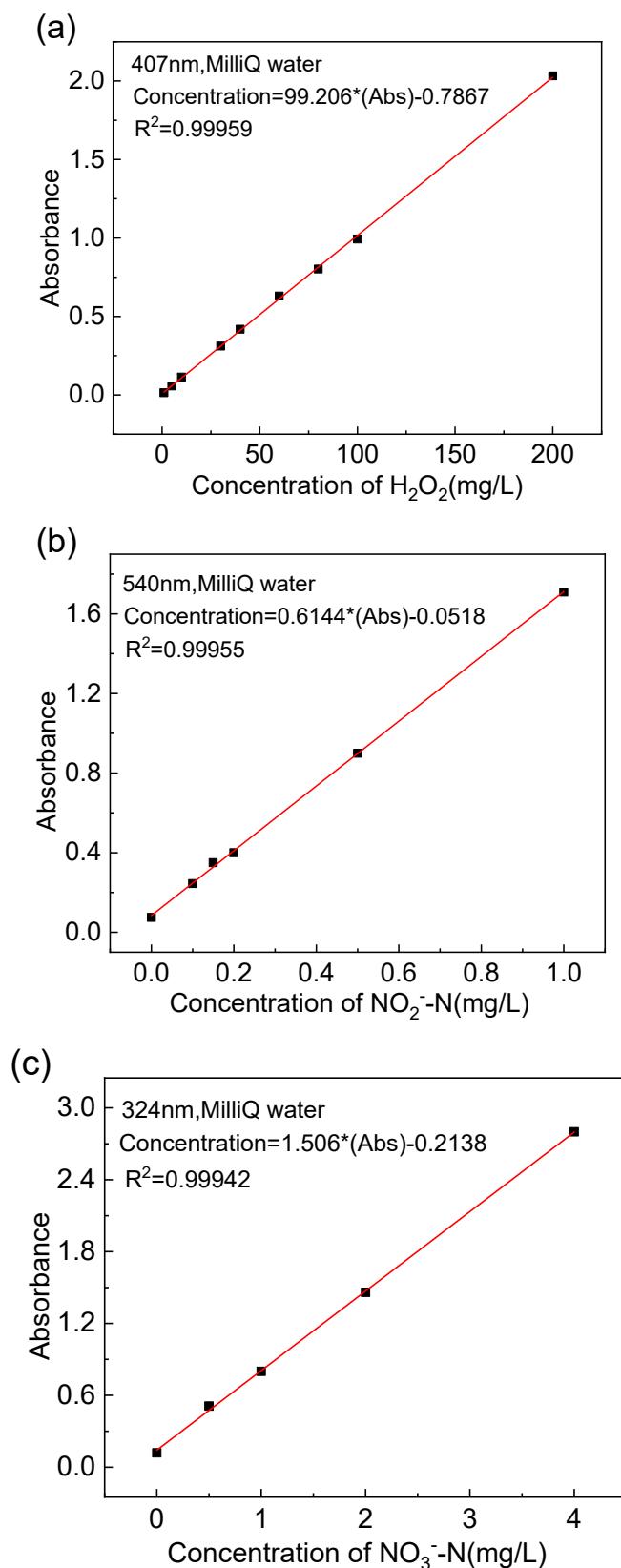
**Table S2.** Summarized important liquid phase reactions in N<sub>2</sub>/O<sub>2</sub>/H<sub>2</sub>O plasma system

Process	Rate coefficient [cm <sup>3</sup> s <sup>-1</sup> ] [cm <sup>6</sup> s <sup>-1</sup> ] <sup>†</sup>	Ref.
<u>Ions</u>		
R1	e(aq) + H <sub>2</sub> O(aq) => H <sub>2</sub> O(aq) <sup>·-</sup>	5.e-15
R2	N <sub>2</sub> (aq) <sup>·+</sup> + H <sub>2</sub> O(aq) => H <sub>2</sub> O(aq) <sup>·+</sup> + N <sub>2</sub> (aq)	1.0e-12
R3	N(aq) <sup>·+</sup> + H <sub>2</sub> O(aq) => H <sub>2</sub> O(aq) <sup>·+</sup> + N(aq)	5.e-15
R4	O <sub>2</sub> (aq) <sup>·+</sup> + H <sub>2</sub> O(aq) => H <sub>2</sub> O(aq) <sup>·+</sup> + O <sub>2</sub> (aq)	5.e-15
R5	NO(aq) <sup>·+</sup> + H <sub>2</sub> O(aq) => H <sub>2</sub> O(aq) <sup>·+</sup> + NO(aq)	5.e-15
R6	H <sub>2</sub> (aq) <sup>·+</sup> + H <sub>2</sub> O(aq) => H <sub>2</sub> O(aq) <sup>·+</sup> + H <sub>2</sub> (aq)	5.e-15
R7	NO <sub>2</sub> (aq) <sup>·+</sup> + H <sub>2</sub> O(aq) => H <sub>2</sub> O(aq) <sup>·+</sup> + NO <sub>2</sub> (aq)	5.e-15
R8	N <sub>4</sub> (aq) <sup>·+</sup> + H <sub>2</sub> O(aq) => H <sub>2</sub> O(aq) <sup>·+</sup> + N <sub>2</sub> (aq) + N <sub>2</sub> (aq)	5.e-15
R9	H(aq) <sup>·+</sup> + H <sub>2</sub> O(aq) => H <sub>3</sub> O(aq) <sup>·+</sup>	5.e-15
R10	H(aq) <sup>·-</sup> + H <sub>2</sub> O(aq) => H <sub>2</sub> O(aq) <sup>·-</sup> + H(aq)	5.e-15
R11	O(aq) <sup>·-</sup> + H <sub>2</sub> O(aq) => OH(aq) <sup>·-</sup> + OH(aq)	3.e-15
<u>Acid dissociation</u>		
R12	ONOOH(aq) + H <sub>2</sub> O(aq) => H <sub>3</sub> O(aq) <sup>·+</sup> + ONOO(aq) <sup>·-</sup>	5.e-15
R13	ONOO(aq) <sup>·-</sup> + H <sub>3</sub> O(aq) <sup>·+</sup> => H <sub>2</sub> O(aq) + ONOOH(aq)	1.75e-6
R14	HO <sub>2</sub> (aq) + H <sub>2</sub> O(aq) => H <sub>3</sub> O(aq) <sup>·+</sup> + O <sub>2</sub> (aq) <sup>·-</sup>	1.43e-17
R15	H <sub>3</sub> O(aq) <sup>·+</sup> + O <sub>2</sub> (aq) <sup>·-</sup> => HO <sub>2</sub> (aq) + H <sub>2</sub> O(aq)	5.e-11
R16	HNO <sub>2</sub> (aq) + H <sub>2</sub> O(aq) => H <sub>3</sub> O(aq) <sup>·+</sup> + NO <sub>2</sub> (aq) <sup>·-</sup>	5.e-15
R17	H <sub>3</sub> O(aq) <sup>·+</sup> + NO <sub>2</sub> (aq) <sup>·-</sup> => HNO <sub>2</sub> (aq) + H <sub>2</sub> O(aq)	6.81e-10
R18	HNO <sub>3</sub> (aq) + H <sub>2</sub> O(aq) => H <sub>3</sub> O(aq) <sup>·+</sup> + NO <sub>3</sub> (aq) <sup>·-</sup>	3.e-8
R19	H <sub>3</sub> O(aq) <sup>·+</sup> + NO <sub>3</sub> (aq) <sup>·-</sup> => HNO <sub>3</sub> (aq) + H <sub>2</sub> O(aq)	7.e-16
R20	HO <sub>2</sub> NO <sub>2</sub> (aq) + H <sub>2</sub> O(aq) => O <sub>2</sub> NO <sub>2</sub> (aq) <sup>·-</sup> + H <sub>3</sub> O(aq) <sup>·+</sup>	5.e-15
R21	O <sub>2</sub> NO <sub>2</sub> (aq) <sup>·-</sup> + H <sub>3</sub> O(aq) <sup>·+</sup> => HO <sub>2</sub> NO <sub>2</sub> (aq) + H <sub>2</sub> O(aq)	1.05e-7
<u>Reactive oxygen species</u>		
R22	OH(aq) + H(aq) => H <sub>2</sub> O(aq)	3.e-11

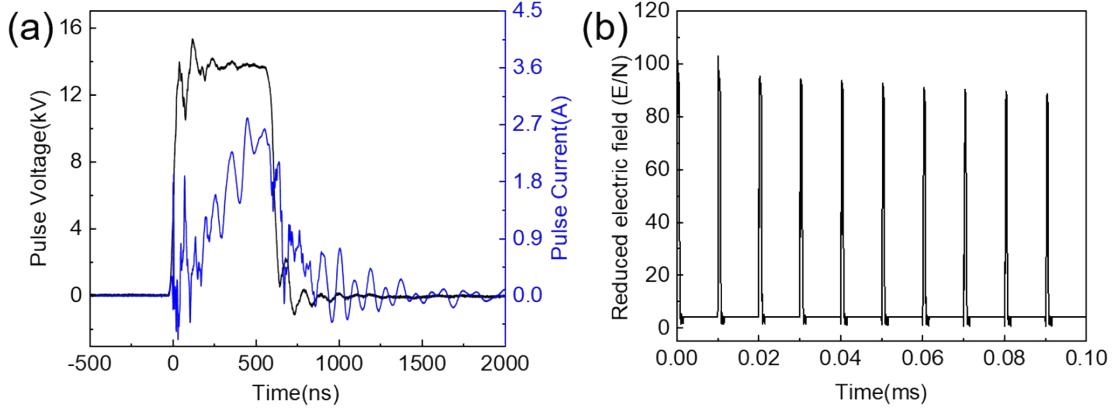
R23	$\text{H}_2\text{O}(\text{aq})^{\wedge-} + \text{O}(\text{aq}) \Rightarrow \text{O}(\text{aq})^{\wedge-} + \text{H}_2\text{O}(\text{aq})$	3.e-11	[1]
R24	$\text{H}_2\text{O}(\text{aq})^{\wedge-} + \text{O}_2(\text{aq}) \Rightarrow \text{O}_2(\text{aq})^{\wedge-} + \text{H}_2\text{O}(\text{aq})$	3.e-11	[1]
R25	$\text{H}_2\text{O}(\text{aq})^{\wedge-} + \text{OH}(\text{aq}) \Rightarrow \text{OH}(\text{aq})^{\wedge-} + \text{H}_2\text{O}(\text{aq})$	5.e-11	[1]
R26	$\text{H}_2\text{O}(\text{aq})^{\wedge-} + \text{H}_2\text{O}_2(\text{aq}) \Rightarrow \text{OH}(\text{aq}) + \text{OH}(\text{aq})^{\wedge-} + \text{H}_2\text{O}(\text{aq})$	2.e-11	[5]
R27	$\text{H}_2\text{O}(\text{aq})^{\wedge-} + \text{O}(\text{aq})^{\wedge-} \Rightarrow \text{OH}(\text{aq})^{\wedge-} + \text{OH}(\text{aq})^{\wedge-}$	2.e-11	[1]
R28	$\text{H}_2\text{O}(\text{aq})^{\wedge-} + \text{H}_2\text{O}(\text{aq})^{\wedge-} \Rightarrow \text{H}_2(\text{aq}) + \text{OH}(\text{aq})^{\wedge-} + \text{OH}(\text{aq})^{\wedge-}$	1.e-11	[1]
R29	$\text{H}_3\text{O}(\text{aq})^{\wedge+} + \text{OH}(\text{aq})^{\wedge-} \Rightarrow \text{H}(\text{aq}) + \text{OH}(\text{aq}) + \text{H}_2\text{O}(\text{aq})$	1.e-10	[1]
R30	$\text{H}_2\text{O}(\text{aq}) \Rightarrow \text{H}_2\text{O}(\text{aq})^{\wedge+} + \text{e}(\text{aq})$	1.e-20	
R31	$\text{H}_2\text{O}(\text{aq}) \Rightarrow \text{OH}(\text{aq}) + \text{H}(\text{aq})$	1.e-20	
R32	$\text{OH}(\text{aq}) + \text{OH}(\text{aq}) \Rightarrow \text{H}_2\text{O}_2(\text{aq})$	1.7e-11	
R33	$\text{OH}(\text{aq}) + \text{H}_2(\text{aq}) \Rightarrow \text{H}(\text{aq}) + \text{H}_2\text{O}(\text{aq})$	6.e-14	
R34	$\text{OH}(\text{aq}) + \text{HO}_2(\text{aq}) \Rightarrow \text{O}_2(\text{aq}) + \text{H}_2\text{O}(\text{aq})$	2.e-11	
R35	$\text{OH}(\text{aq}) + \text{H}_2\text{O}_2(\text{aq}) \Rightarrow \text{HO}_2(\text{aq}) + \text{H}_2\text{O}(\text{aq})$	1.e-13	
R36	$\text{OH}(\text{aq}) + \text{OH}(\text{aq})^{\wedge-} \Rightarrow \text{O}(\text{aq})^{\wedge-} + \text{H}_2\text{O}(\text{aq})$	8.e-12	
R37	$\text{OH}(\text{aq}) + \text{O}(\text{aq})^{\wedge-} \Rightarrow \text{HO}_2(\text{aq})^{\wedge-}$	4.e-11	
R38	$\text{OH}(\text{aq}) + \text{O}_2(\text{aq})^{\wedge-} \Rightarrow \text{O}_2(\text{aq}) + \text{OH}(\text{aq})^{\wedge-}$	1.5e-11	
R39	$\text{OH}(\text{aq}) + \text{HO}_2(\text{aq})^{\wedge-} \Rightarrow \text{HO}_2(\text{aq}) + \text{OH}(\text{aq})^{\wedge-}$	1.5e-11	
R40	$\text{H}(\text{aq}) + \text{H}_2\text{O}(\text{aq}) \Rightarrow \text{H}_2(\text{aq}) + \text{OH}(\text{aq})$	1.5e-21	
R41	$\text{H}(\text{aq}) + \text{H}(\text{aq}) \Rightarrow \text{H}_2(\text{aq})$	1.5e-11	
R42	$\text{H}(\text{aq}) + \text{HO}_2(\text{aq}) \Rightarrow \text{H}_2\text{O}_2(\text{aq})$	3.e-11	
R43	$\text{H}(\text{aq}) + \text{H}_2\text{O}_2(\text{aq}) \Rightarrow \text{OH}(\text{aq}) + \text{H}_2\text{O}(\text{aq})$	1.5e-13	
R44	$\text{O}_3(\text{aq}) \Rightarrow \text{O}_2(\text{aq}) + \text{O}(\text{aq})$	3.e-6	
R45	$\text{O}_3(\text{aq}) + \text{OH}(\text{aq})^{\wedge-} \Rightarrow \text{O}_2(\text{aq})^{\wedge-} + \text{HO}_2(\text{aq})$	1.16e-19	
R46	$\text{O}_3(\text{aq}) + \text{O}_2(\text{aq})^{\wedge-} \Rightarrow \text{O}_3(\text{aq})^{\wedge-} + \text{O}_2(\text{aq})$	2.66e-12	

#### Reactive nitrogen species

R47	$\text{N}(\text{aq}) + \text{N}(\text{aq}) \Rightarrow \text{N}_2(\text{aq})$	5.e-14	[1]
R48	$\text{N}(\text{aq}) + \text{H}_2\text{O}(\text{aq}) \Rightarrow \text{NH}(\text{aq}) + \text{OH}(\text{aq})$	6.93e-39	[1]
R49	$\text{NH}(\text{aq}) + \text{NO}(\text{aq}) \Rightarrow \text{N}_2\text{O}(\text{aq}) + \text{H}(\text{aq})$	1.3e-12	[1]
R50	$\text{O}(\text{aq})^{\wedge+} + \text{N}_2(\text{aq}) \Rightarrow \text{NO}(\text{aq})^{\wedge+} + \text{N}(\text{aq})$	1.2e-12	[1]
R51	$\text{NO}(\text{aq}) + \text{NO}(\text{aq}) + \text{O}_2(\text{aq}) \Rightarrow \text{NO}_2(\text{aq}) + \text{NO}_2(\text{aq})$	6.28e-36	[1]
R52	$\text{NO}(\text{aq}) + \text{NO}_2(\text{aq}) + \text{H}_2\text{O}(\text{aq}) \Rightarrow \text{HNO}_2(\text{aq}) + \text{HNO}_2(\text{aq})$	5.55e-34	[1]
R53	$\text{NO}_3(\text{aq}) + \text{H}_2\text{O}(\text{aq}) \Rightarrow \text{HNO}_3(\text{aq}) + \text{OH}(\text{aq})$	4.8e-14	[1]
R54	$\text{NO}(\text{aq}) + \text{HO}_2(\text{aq}) \Rightarrow \text{HNO}_3(\text{aq})$	5.33e-12	[1]
R55	$\text{OH}(\text{aq}) + \text{HNO}_3(\text{aq}) \Rightarrow \text{NO}_3(\text{aq}) + \text{H}_2\text{O}(\text{aq})$	2.17e-13	[1]
R56	$\text{N}_2\text{O}_4(\text{aq}) + \text{H}_2\text{O}(\text{aq}) \Rightarrow \text{HNO}_2(\text{aq}) + \text{HNO}_3(\text{aq})$	1.33e-18	[1]
R57	$\text{N}_2\text{O}_5(\text{aq}) + \text{H}_2\text{O}(\text{aq}) \Rightarrow \text{NO}_2(\text{aq}) + \text{NO}_3(\text{aq}) + \text{H}_2\text{O}(\text{aq})$	1.4e-19	[1]
R58	$\text{N}_2\text{O}_5(\text{aq}) + \text{H}_2\text{O}(\text{aq}) \Rightarrow \text{HNO}_3(\text{aq}) + \text{HNO}_3(\text{aq})$	2.e-21	[1]
R59	$\text{NO}_2(\text{aq})^{\wedge-} + \text{N}_2\text{O}(\text{aq}) \Rightarrow \text{NO}_3(\text{aq})^{\wedge-} + \text{N}_2(\text{aq})$	5.e-13	
R60	$\text{HO}_2\text{NO}_2(\text{aq}) + \text{HNO}_2(\text{aq}) \Rightarrow \text{HNO}_3(\text{aq}) + \text{HNO}_3(\text{aq})$	1.99e-20	
R61	$\text{HO}_2\text{NO}_2(\text{aq}) \Rightarrow \text{HNO}_2(\text{aq}) + \text{O}_2(\text{aq})$	7.e-4	
R62	$\text{HO}_2\text{NO}_2(\text{aq}) \Rightarrow \text{HO}_2(\text{aq}) + \text{NO}_2(\text{aq})$	4.6e-3	
R63	$\text{N}_2\text{O}_5(\text{aq}) + \text{H}_2\text{O}(\text{aq}) \Rightarrow \text{ONOOH}(\text{aq}) + \text{ONOOH}(\text{aq})$	2.e-21	[1]
R64	$\text{ONOOH}(\text{aq}) + \text{H}_2\text{O}(\text{aq}) \Rightarrow \text{H}_3\text{O}(\text{aq})^{\wedge+} + \text{NO}_3(\text{aq})^{\wedge-}$	2.9e-23	[1]

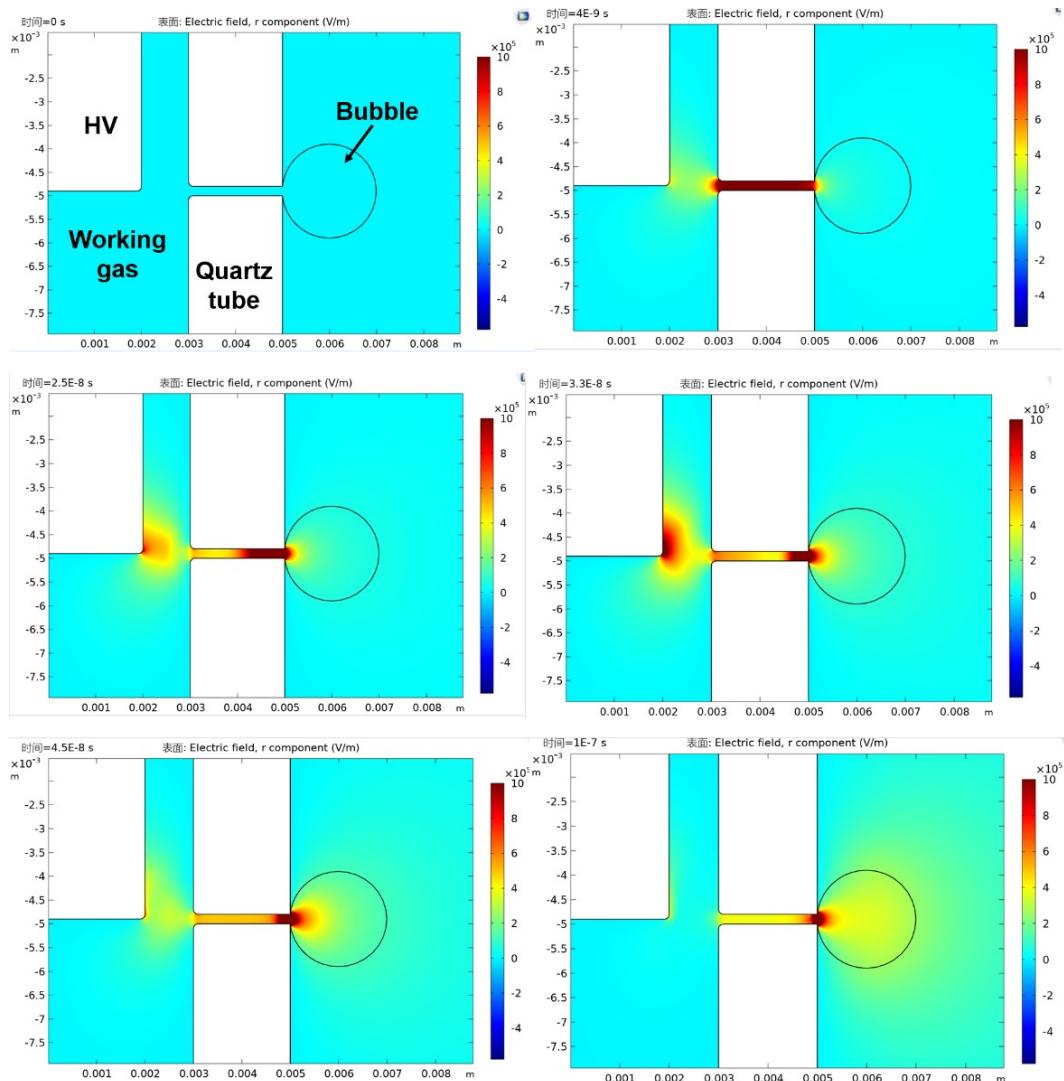


**Fig. S1.** (a) Standard curve for  $\text{H}_2\text{O}_2$  detection using titanium salt photometry; (b) Standard curve for  $\text{NO}_2^-$  detection using ethylenediamine photometry; (c) Standard curve for  $\text{NO}_3^-$  detection using 2,6-dimethylphenol photometry

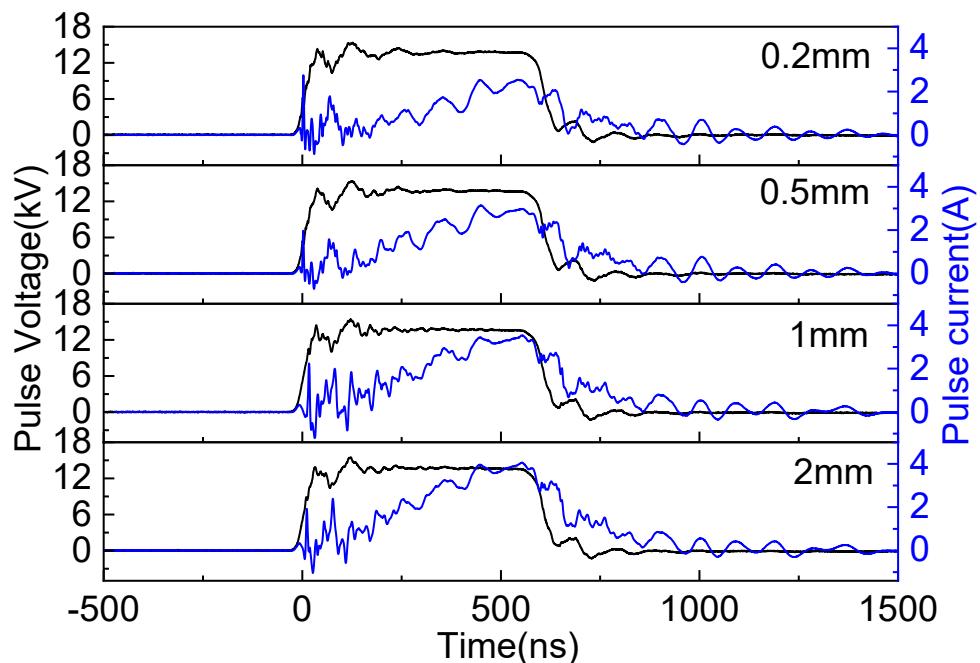


**Fig. S2.** (a) Voltage-current waveform of underwater bubble discharge; (b) Self-consistently derived corresponding the reduced electric field

In order to have a clearer understanding of the electric field distribution in the bubble discharge, the COMSOL transient electric field module was used without considering the plasma formation in order to analyze in depth the temporal and spatial evolution of the electric field, as shown in Fig. S3. In our reactor model, the tip edge of the high-voltage electrode is horizontally aligned with the air holes, which is also the same as the actual experimental configuration. With the addition of the applied voltage, affected by the pressure difference between the inside and outside, a potential difference of  $1 \times 10^6$  V/m is first formed inside the air holes, which is followed by a rapid spreading to the edge of the high-voltage electrode, and then gradually develops inside the bubbles, resulting in the formation of spark bubble discharge.

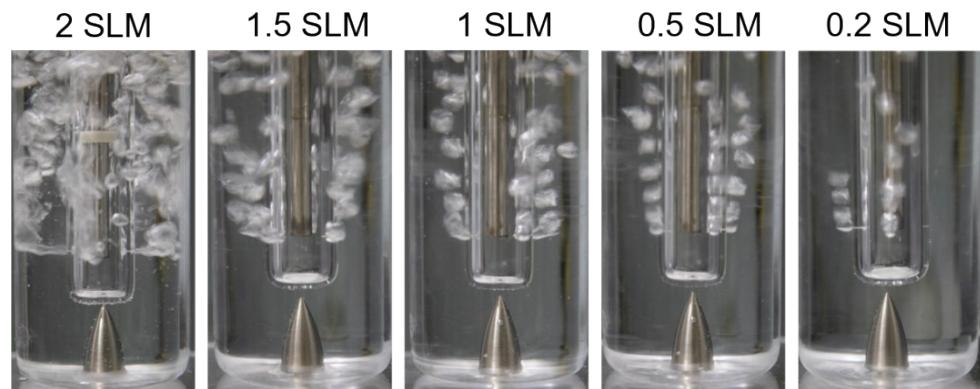


**Fig. S3.** Simulated electric field distribution in the bubble column reactor configuration.



**Fig. S4.** Comparison of voltage and current waveforms with different pore diameters.

In order to clearly demonstrate the morphology of the bubbles at different air flow rates, we photographed the outgassing when they were not under discharge, and the bubbles show irregular channels at larger flow rates, which corresponds to lower gas-liquid mass transfer efficiencies, and that the bubbles at smaller flow rates can demonstrate a complete morphology while possessing lower diameters.



**Fig. S5.** Variation of bubble diffusion at different air flow rates (exposure time 1/125s)

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