## Supporting information for "Dynamical symmetries and selection rules in high-harmonic generation spectroscopy of nonlinear molecules"

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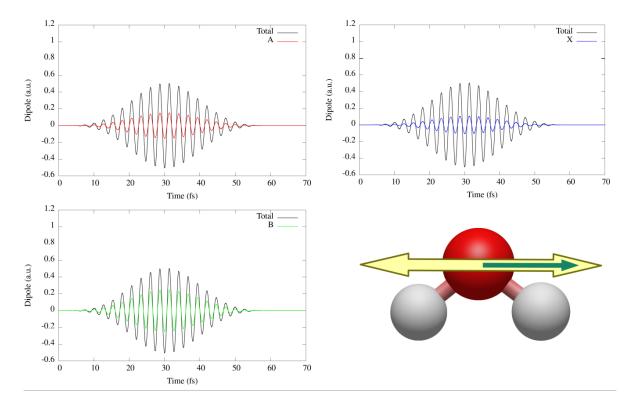


Figure S1: MO decomposition of the time-dependent dipole moment of  $H_2O$ , with laser pulse polarised along the x direction and detection along the same direction, at the RT-TD-CIS level of theory.

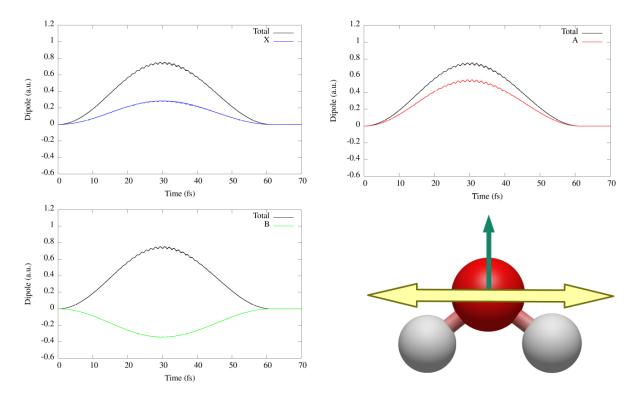


Figure S2: MO decomposition of the time-dependent dipole moment of  $H_2O$ , with laser pulse polarised along the x direction and detection along the z direction, at the RT-TD-CIS level of theory.

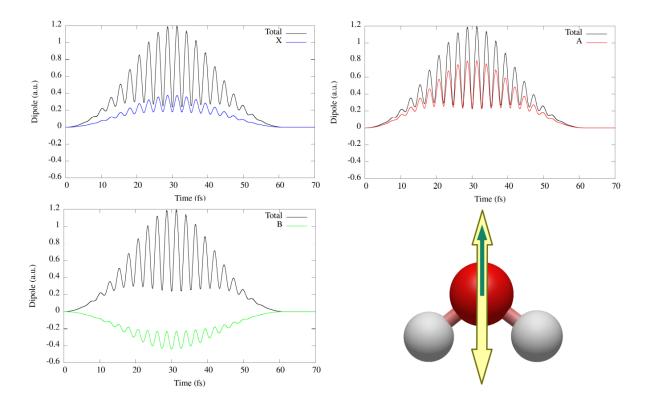


Figure S3: MO decomposition of the time-dependent dipole moment of  $H_2O$ , with laser pulse polarised along the z direction and detection along the same direction, at the RT-TD-CIS level of theory.

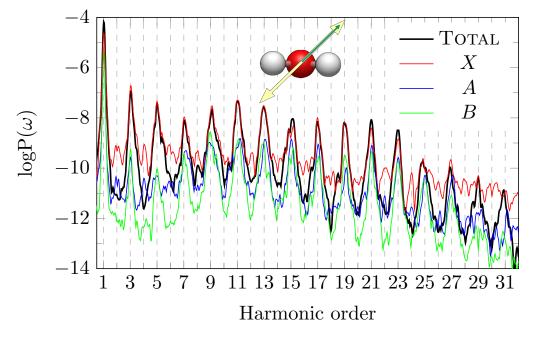


Figure S4: Channel-decomposition of the HHG spectrum, with pulse polarisation and detection in the xy plane, along a direction at  $45^{\circ}$  with respect to the molecular plane. The pulse polarisation is represented by the yellow double arrow, while a green arrow represents the direction of detection of HHG spectra.

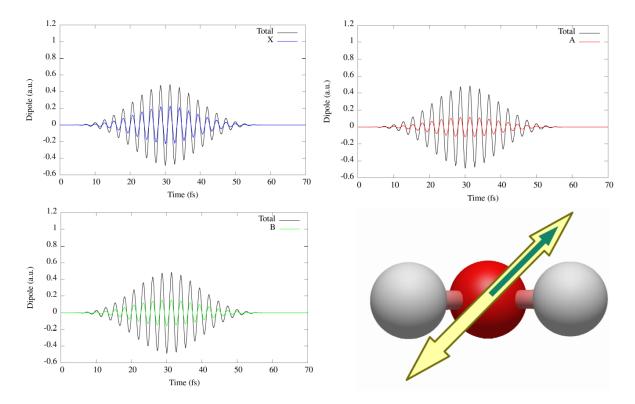


Figure S5: MO decomposition of the time-dependent dipole moment of  $H_2O$ , with laser pulse polarised with an angle of 45° in the xy plane and detection along the same direction, at the RT-TD-CIS level of theory.

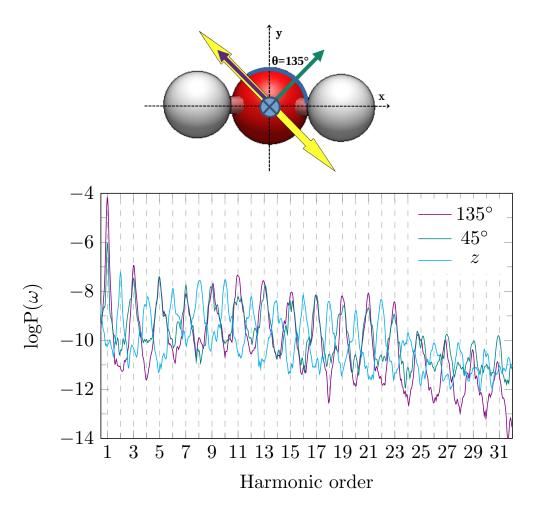


Figure S6: HHG spectra of  $H_2O$  with laser pulse polarized with an angle of  $135^{\circ}$  in the xy plane. The HHG spectra are detected along the pulse polarization ( $135^{\circ}$  in the xy plane), with an angle of  $45^{\circ}$  in the xy plane, and along the z direction. For the detection in the xy plane, only odd harmonics are present, while in the z direction, only even harmonics are allowed.

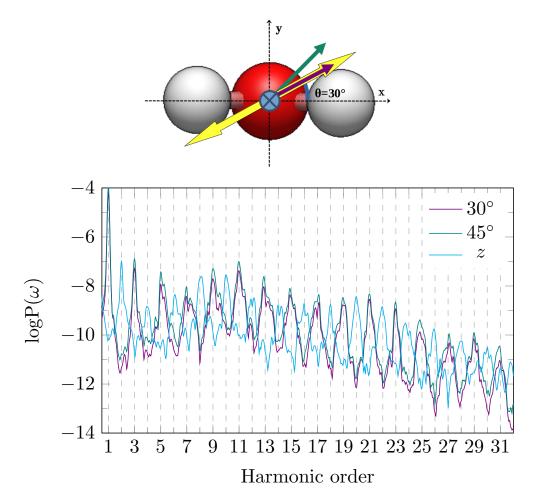


Figure S7: HHG spectra of H<sub>2</sub>O with laser pulse polarized with an angle of 30° in the xy plane. The HHG spectra are detected along the pulse polarization (30° in the xy plane), with an angle of 45° in the xy plane, and along the z direction. Only odd harmonics are present for detection in the xy plane, while only even harmonics are allowed in the z direction.

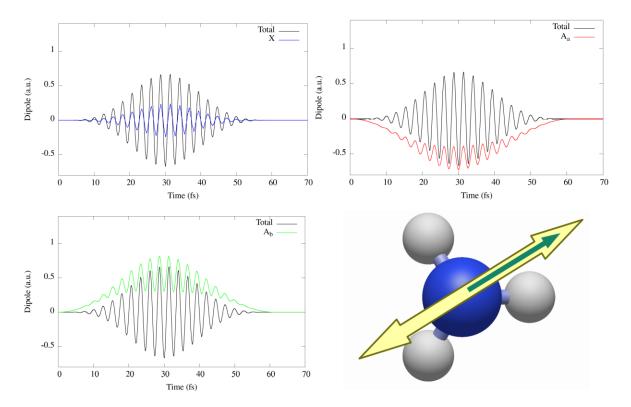


Figure S8: MO decomposition of the time-dependent dipole moment of  $NH_3$ , with laser pulse polarised perpendicular to the  $\sigma'_v$  reflection plane of the  $NH_3$  molecule and detection along the same direction, at the RT-TD-CIS level of theory.

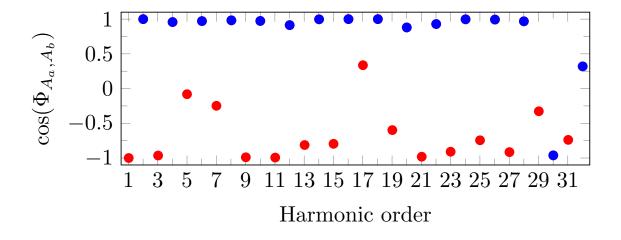


Figure S9: Phase of the interference between  $A_a$  and  $A_b$  channels of NH<sub>3</sub>, with laser pulse polarised perpendicular to the  $\sigma'_v$  reflection plane of the NH<sub>3</sub> molecule and detection along the z direction, at the RT-TD-CIS level of theory.

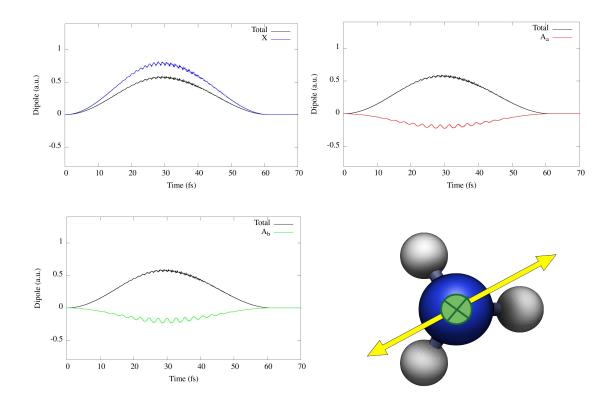


Figure S10: MO decomposition of the time-dependent dipole moment of NH<sub>3</sub>, with laser pulse polarised perpendicular to the  $\sigma'_v$  reflection plane of the NH<sub>3</sub> molecule and detection along the z direction, at the RT-TD-CIS level of theory.

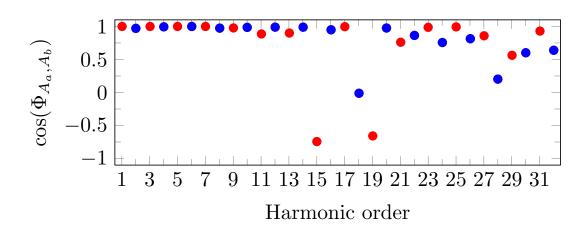


Figure S11: Phase of the interference between  $A_a$  and  $A_b$  channels of NH<sub>3</sub>, with laser pulse along the z axis and detection along the same direction, at the RT-TD-CIS level of theory.

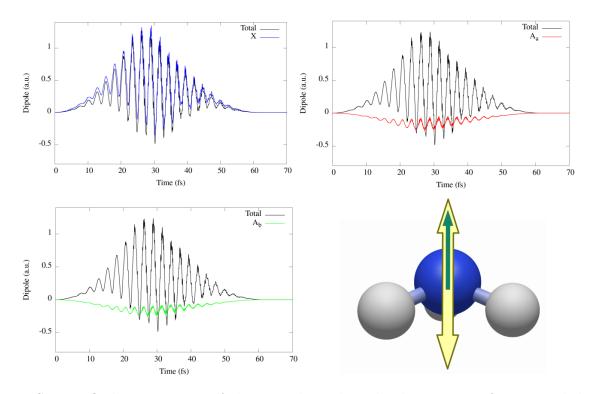


Figure S12: MO decomposition of the time-dependent dipole moment of  $NH_3$ , with laser pulse along the z axis and detection along the same direction, at the RT-TD-CIS level of theory.

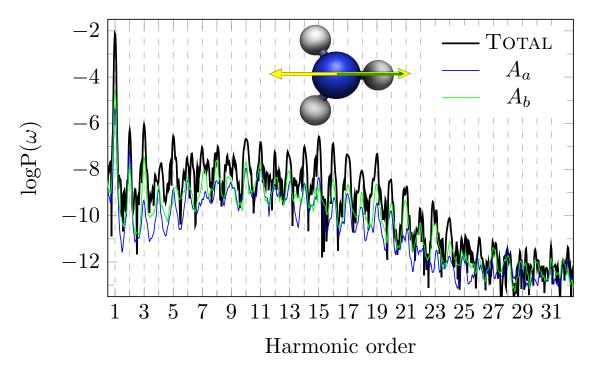


Figure S13: Comparison between  $A_a$  and  $A_b$  channels of NH<sub>3</sub>, with laser pulse along the x axis and detection along the same direction, at the RT-TD-CIS level of theory.