

## Supplementary Information

### First-Principles Investigation of Lithium Ion First-In-First-Out Behavior during Delithiation and Lithiation Processes in $\text{Li}_2\text{MnO}_3$ Lithium-Rich Cathode Material

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Fig. S1 and Fig. S2 show the comparison of voltage curves and electronic structures of  $\text{Li}_2\text{MnO}_3$  based on the SCAN+rVV10 and PBE+D3 exchange–correlation functionals. The voltage profiles obtained using the SCAN+rVV10 and PBE+D3 exchange–correlation functionals show that SCAN+rVV10 predicts a lower initial delithiation voltage, which is also closer to the experimental value. In the later stages of delithiation, SCAN+rVV10 yields a slightly higher voltage window compared with PBE+D3. Overall, the higher-level SCAN+rVV10 functional produces a larger difference between the initial voltage and the voltage window, resulting in a description that agrees more closely with experimental observations and offers improved accuracy. The electronic-structure results show that both functionals exhibit consistent overall trends in the density of states of oxygen and manganese. However, the band gap calculated using SCAN+rVV10 is approximately 1.4 eV, whereas PBE+D3 yields a slightly smaller value of around 1.1 eV. Since the GGA-based PBE functional is known to underestimate band gaps, applying a +U correction can partially mitigate this deviation. In summary, the higher-level SCAN+rVV10 functional provides more accurate predictions of both the voltage profiles and electronic structure, while the PBE+D3 method with a +U correction offers a computationally more efficient approach that still provides reasonable and meaningful interpretations for the system studied in this work.

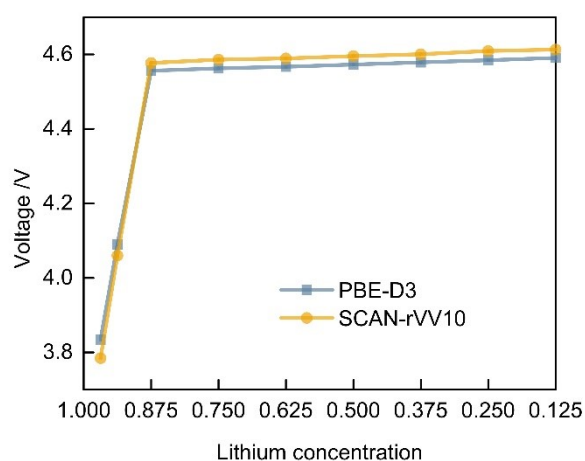


Fig. S1 Simulated voltage curves of  $\text{Li}_2\text{MnO}_3$  based on the SCAN+rVV10 and PBE+D3 pseudopotentials.

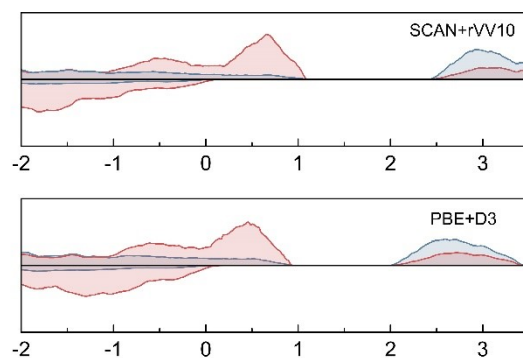


Fig. S2 Partial density of states of Mn and O from 75% lithium structure based on the SCAN+rVV10 and PBE+D3 pseudopotentials.

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Fig. S3 to Fig. S32 show thirty computationally stable structures with different lithium contents and distributions. The CIF files obtained from VASP calculations are provided in the attachment.

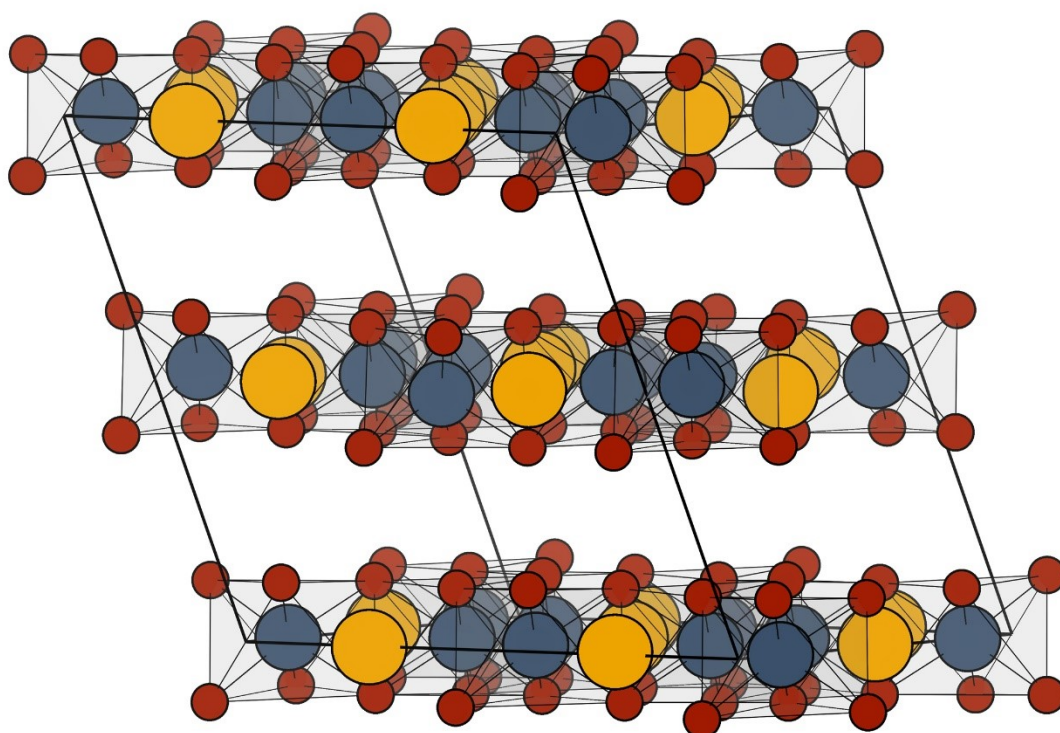


Fig S3 Calculated structure of  $\text{Li}_0(\text{Li-layer})\text{Li}_8(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

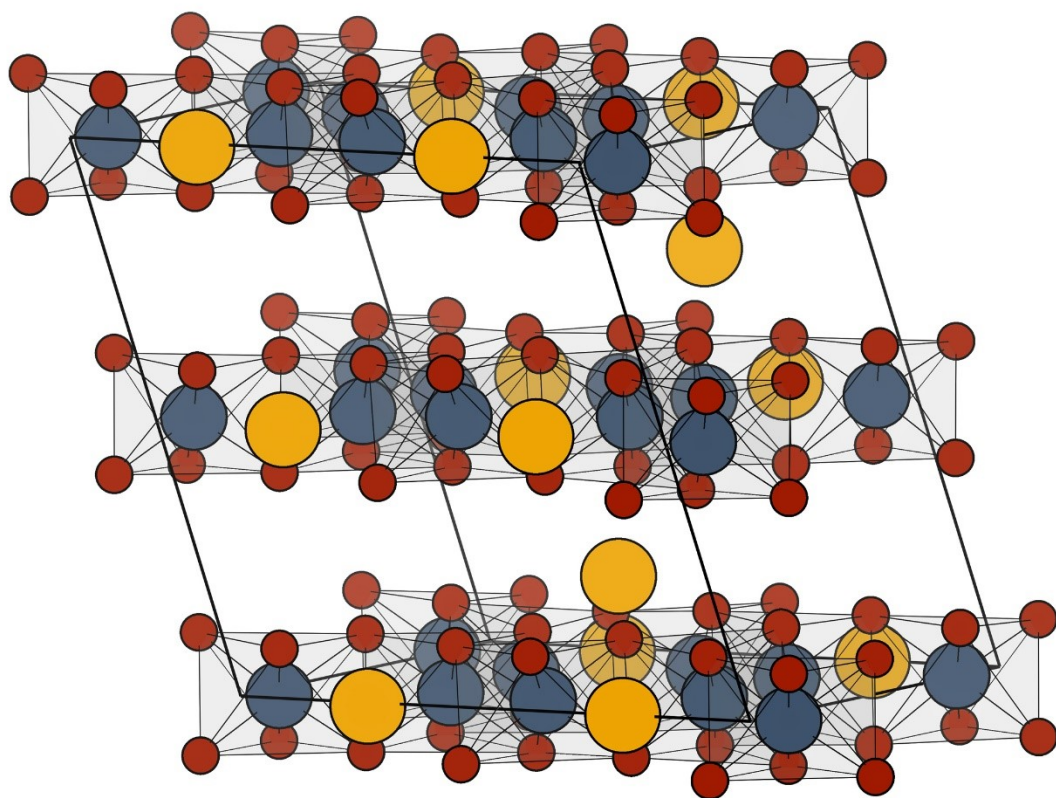


Fig S4 Calculated structure of  $\text{Li}_2(\text{Li-layer})\text{Li}_6(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$



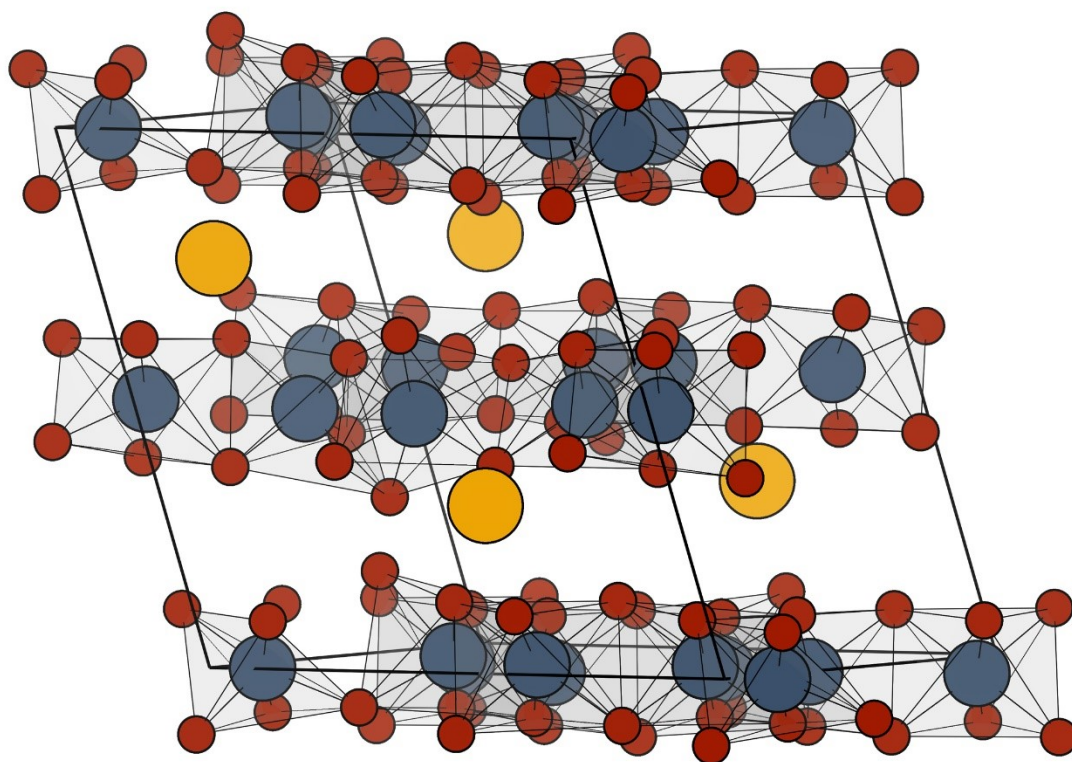


Fig S5 Calculated structure of  $\text{Li}_4(\text{Li-layer})\text{Li}_0(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

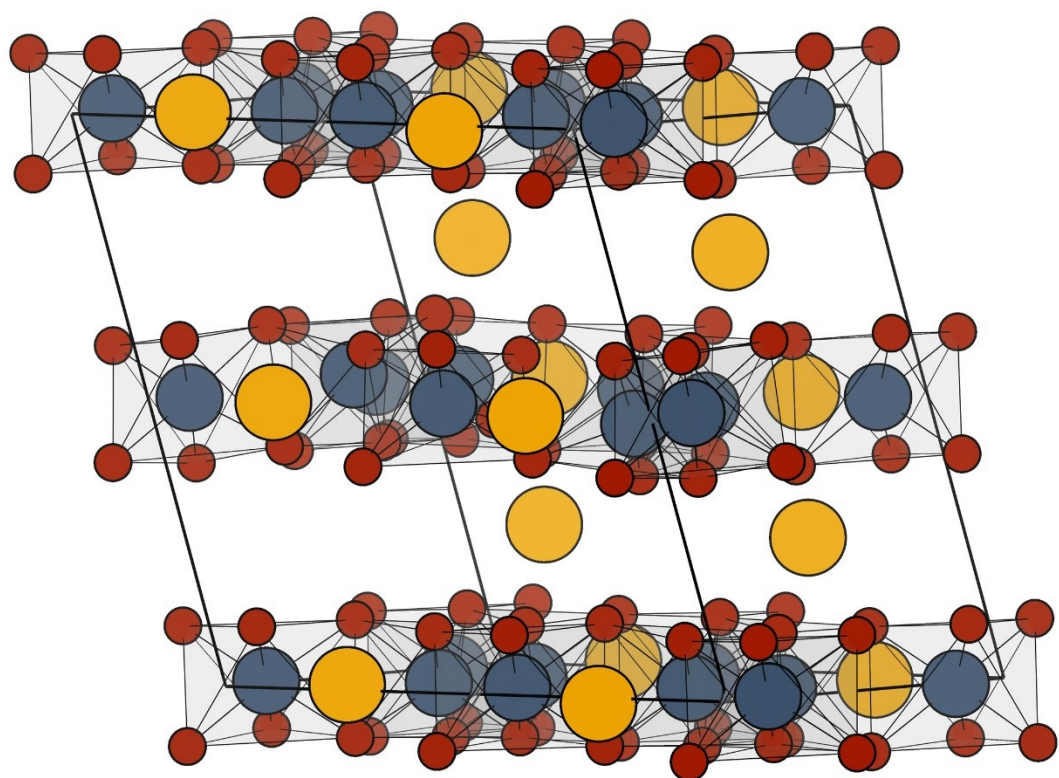


Fig S6 Calculated structure of  $\text{Li}_4(\text{Li-layer})\text{Li}_4(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

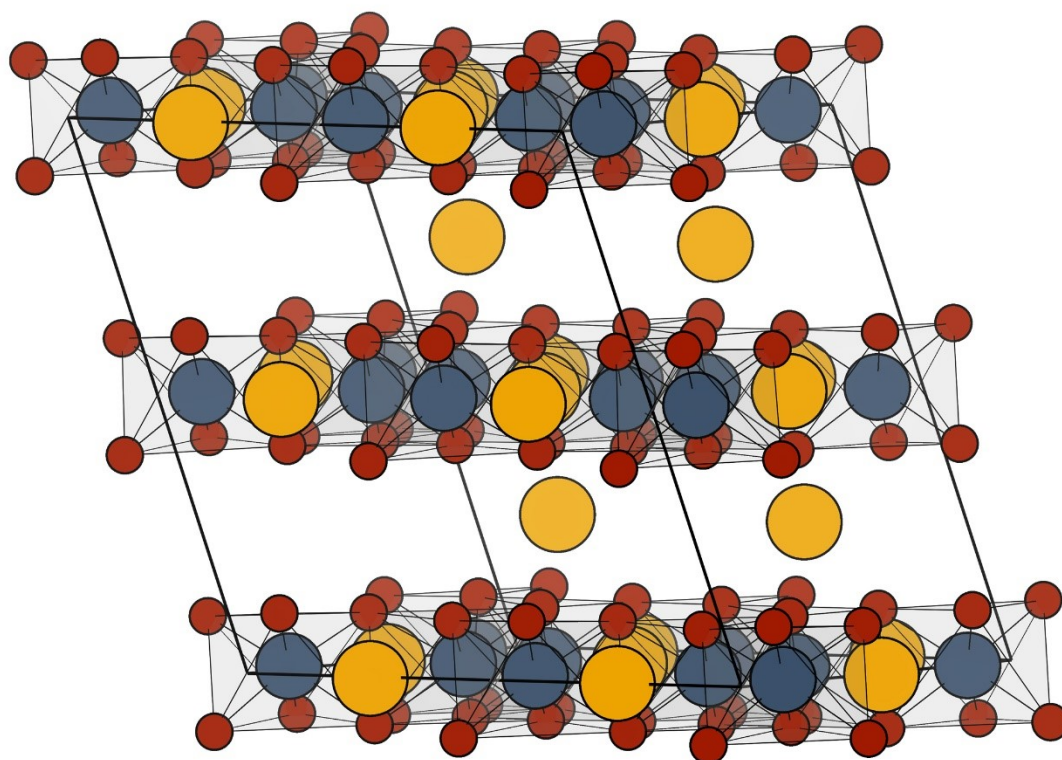


Fig S7 Calculated structure of  $\text{Li}_4(\text{Li-layer})\text{Li}_8(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

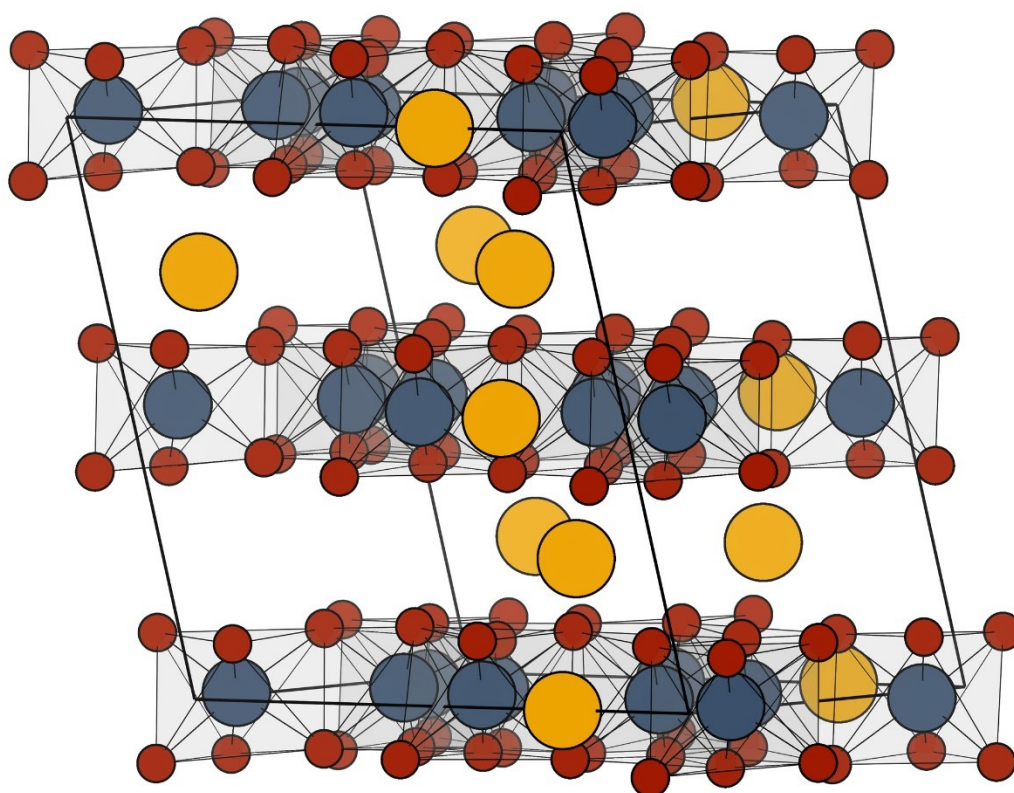


Fig S8 Calculated structure of  $\text{Li}_6(\text{Li-layer})\text{Li}_2(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

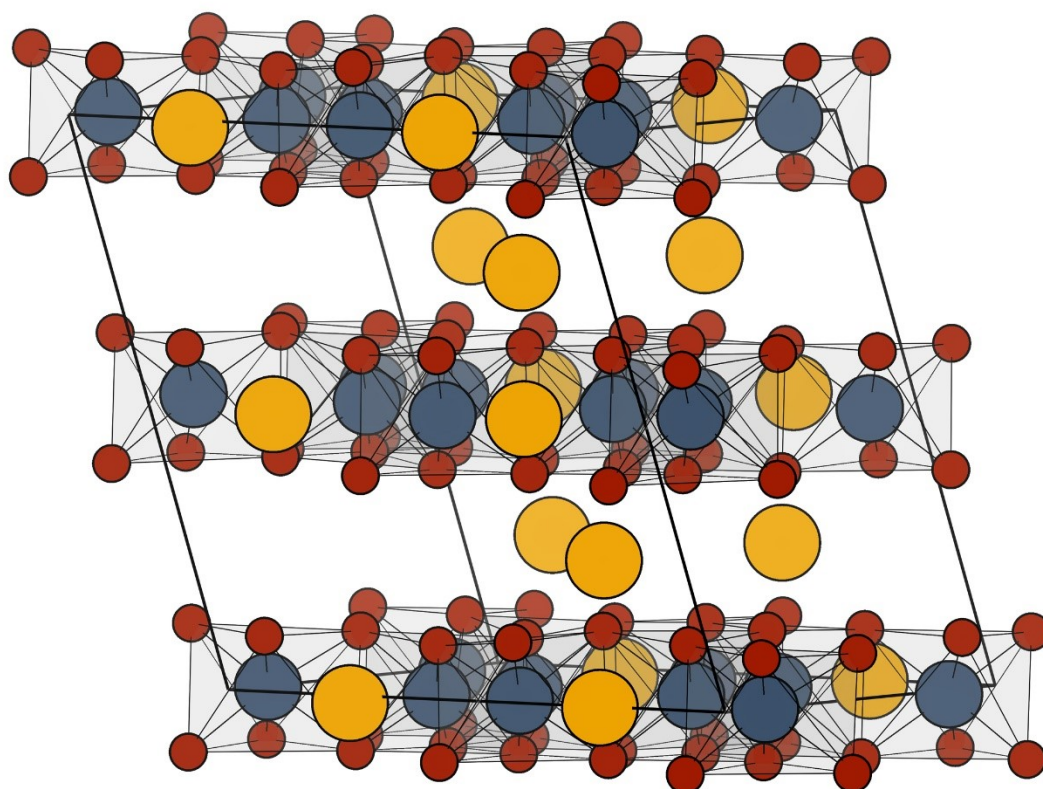


Fig S9 Calculated structure of  $\text{Li}_6(\text{Li-layer})\text{Li}_6(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$



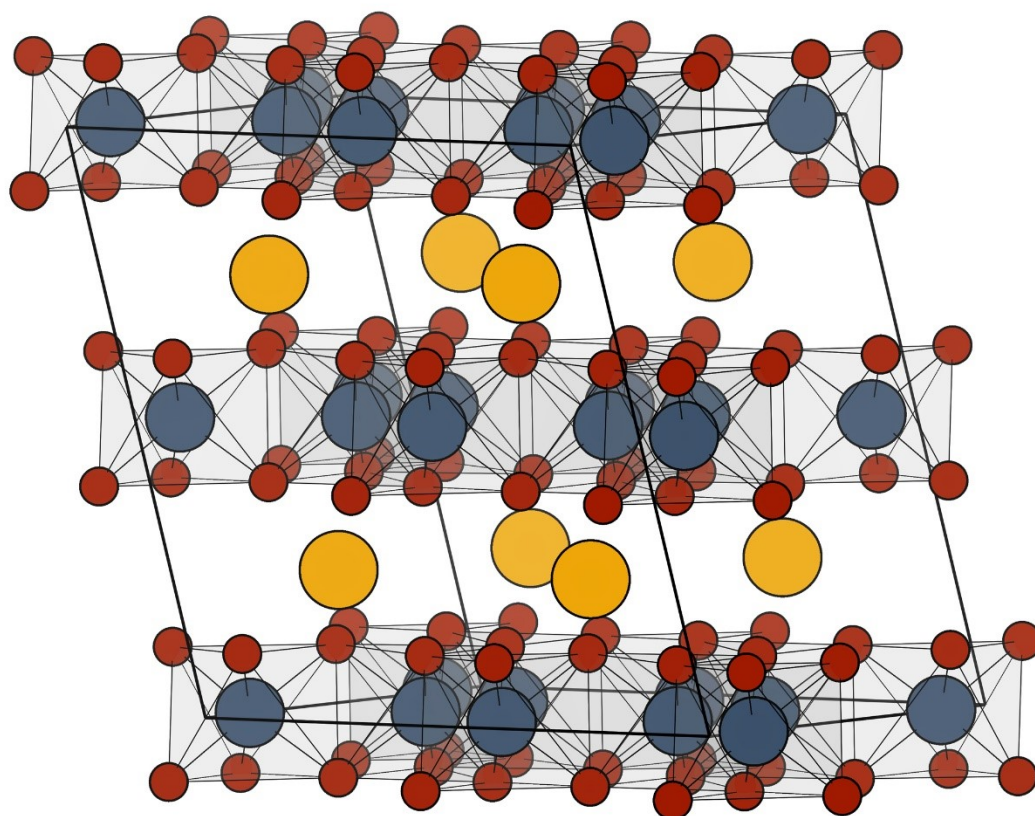


Fig S10 Calculated structure of  $\text{Li}_8(\text{Li-layer})\text{Li}_0(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

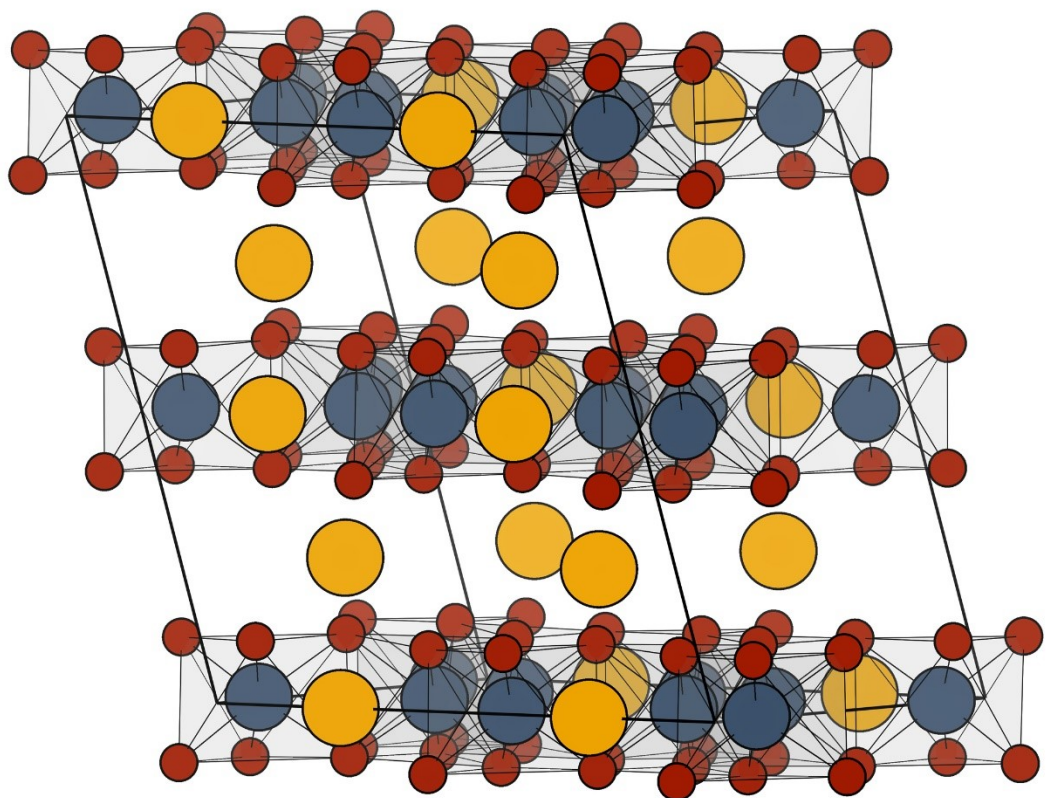


Fig S11 Calculated structure of  $\text{Li}_8(\text{Li-layer})\text{Li}_4(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$



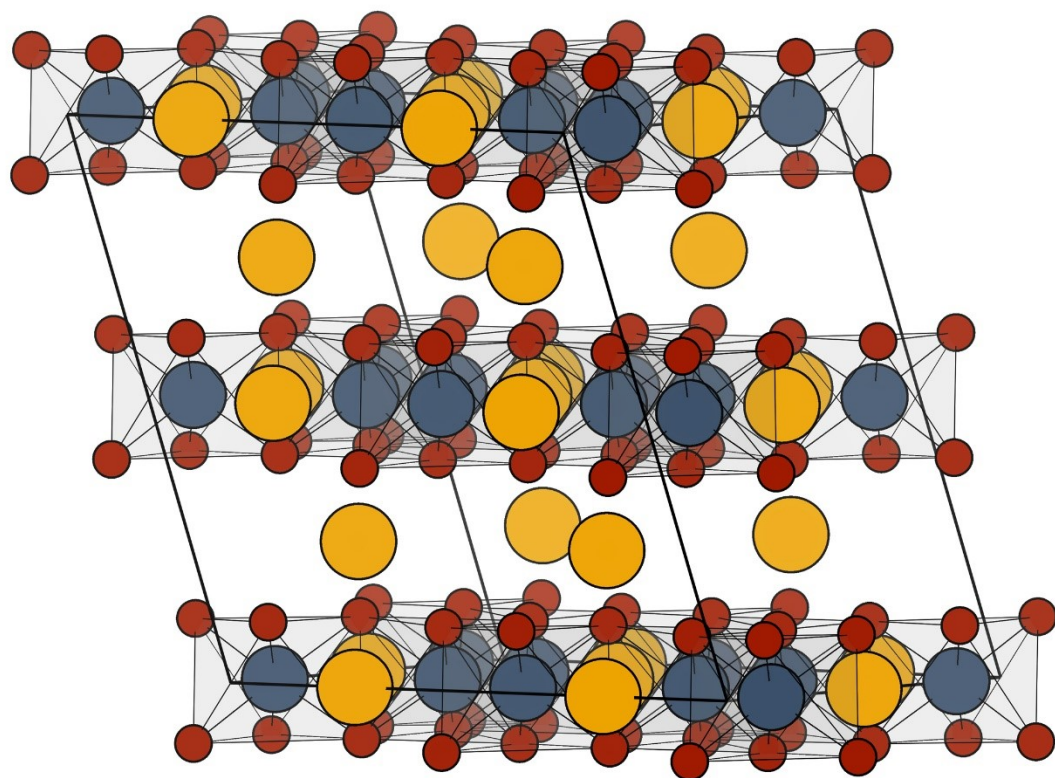


Fig S12 Calculated structure of  $\text{Li}_8(\text{Li-layer})\text{Li}_8(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

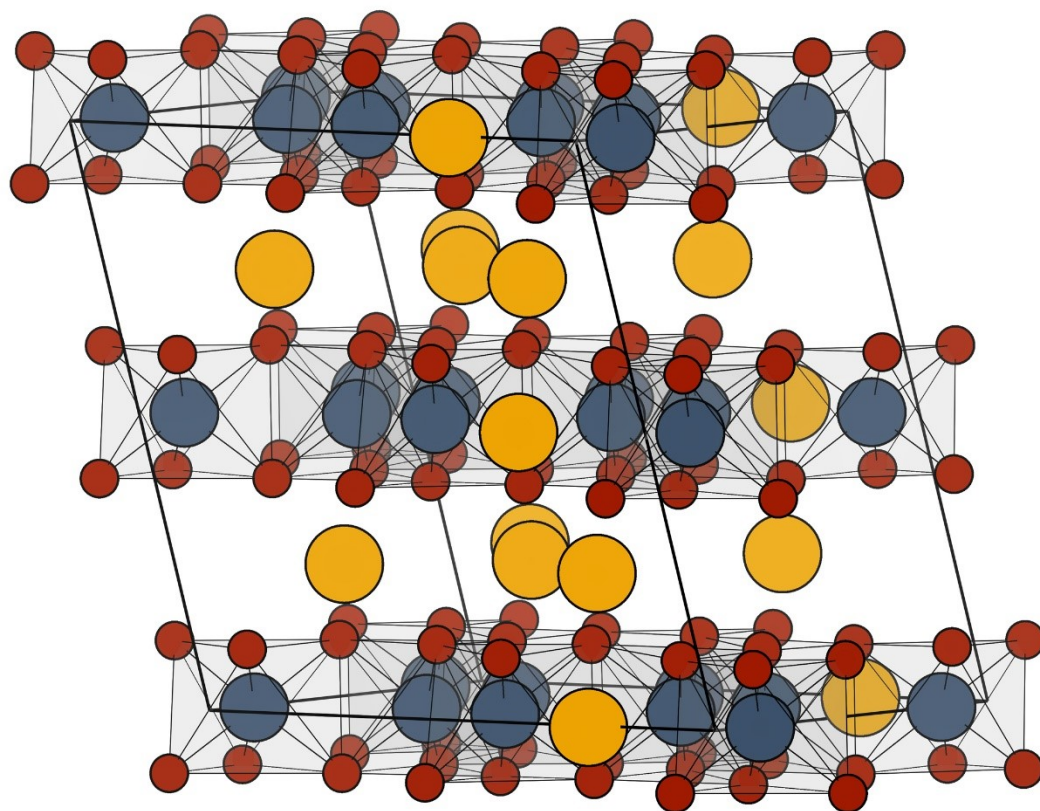


Fig S13 Calculated structure of  $\text{Li}_{10}(\text{Li-layer})\text{Li}_2(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

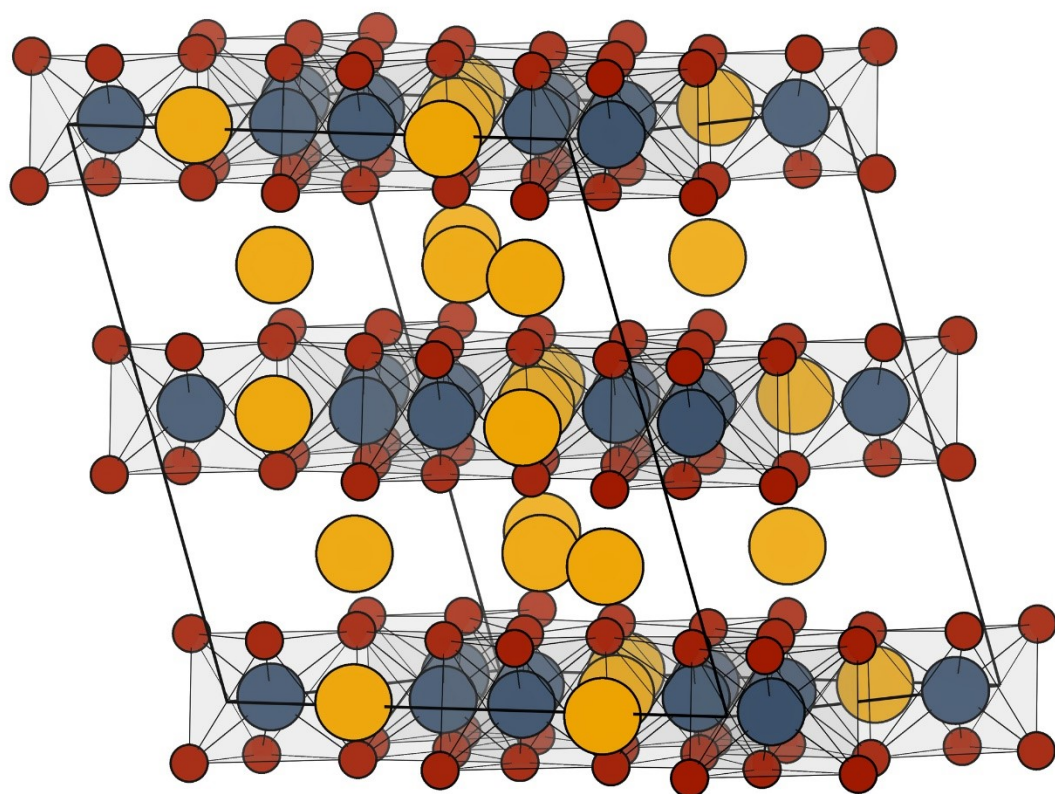


Fig S14 Calculated structure of  $\text{Li}_{10}(\text{Li-layer})\text{Li}_6(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

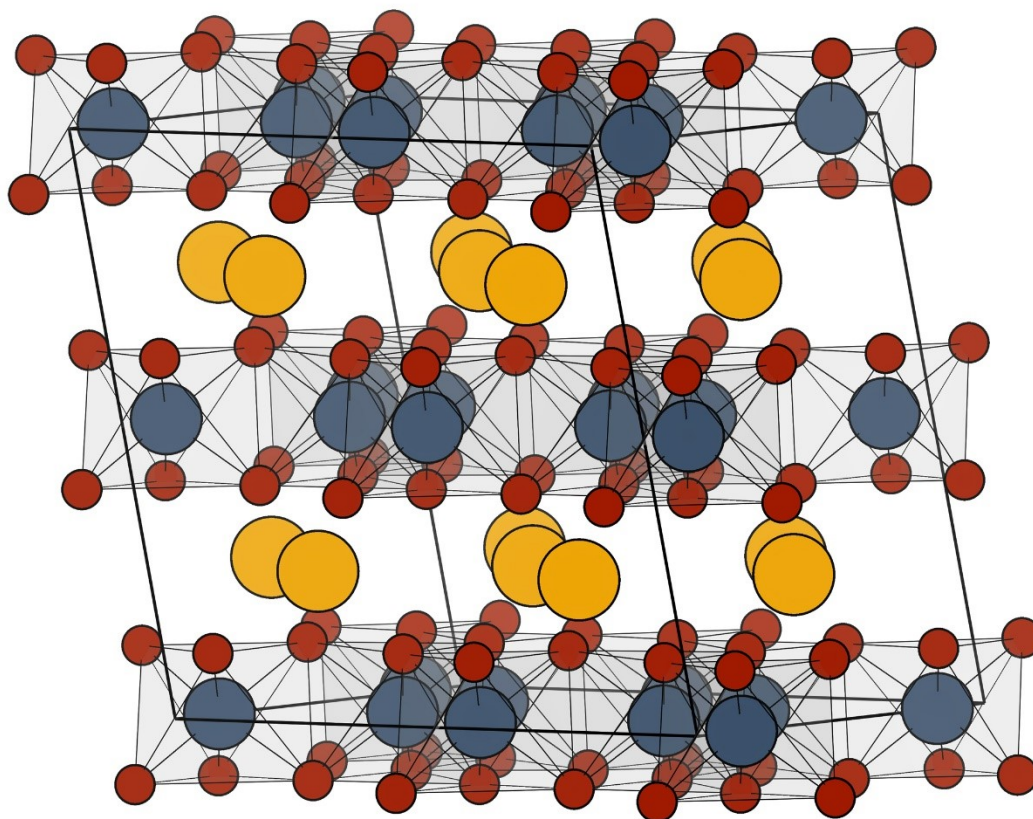


Fig S15 Calculated structure of  $\text{Li}_{12}(\text{Li-layer})\text{Li}_0(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$



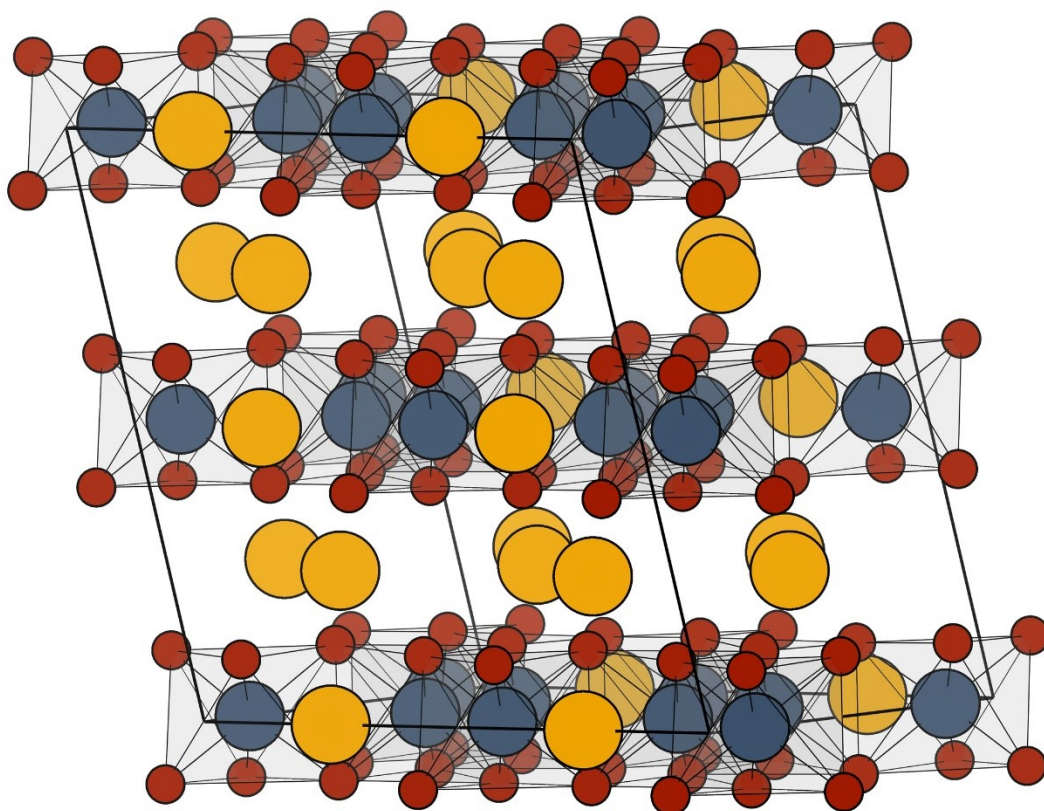


Fig S16 Calculated structure of  $\text{Li}_{12}(\text{Li-layer})\text{Li}_4(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

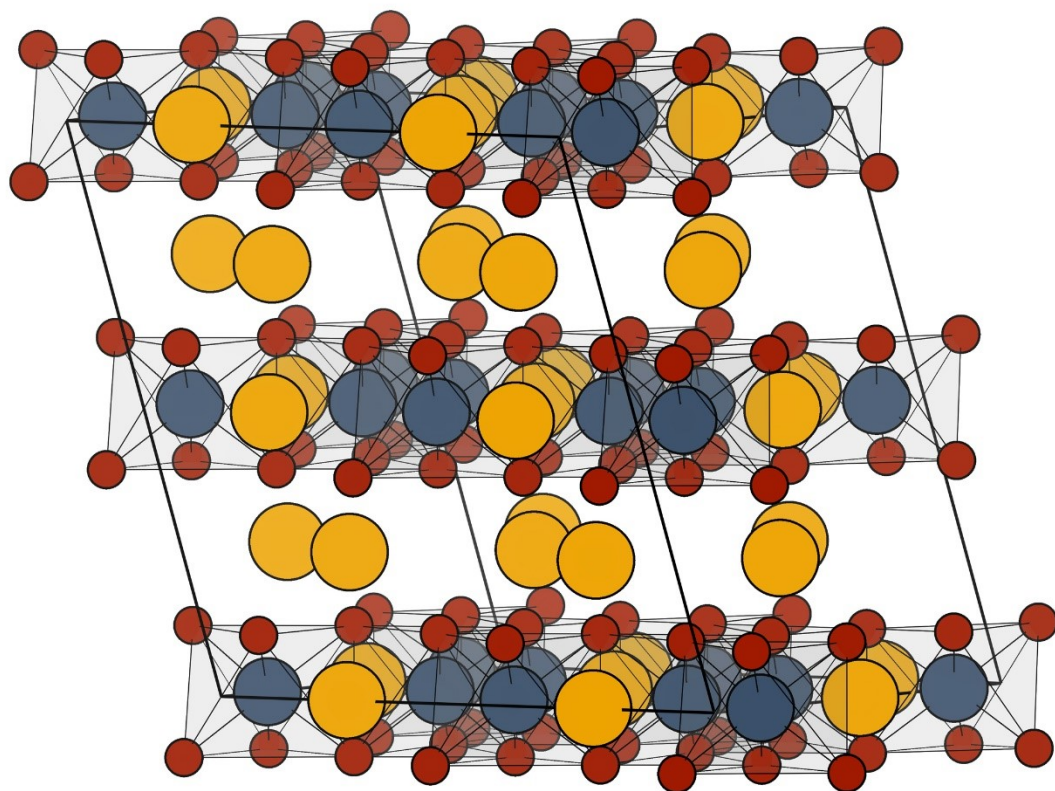


Fig S17 Calculated structure of  $\text{Li}_{12}(\text{Li-layer})\text{Li}_8(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

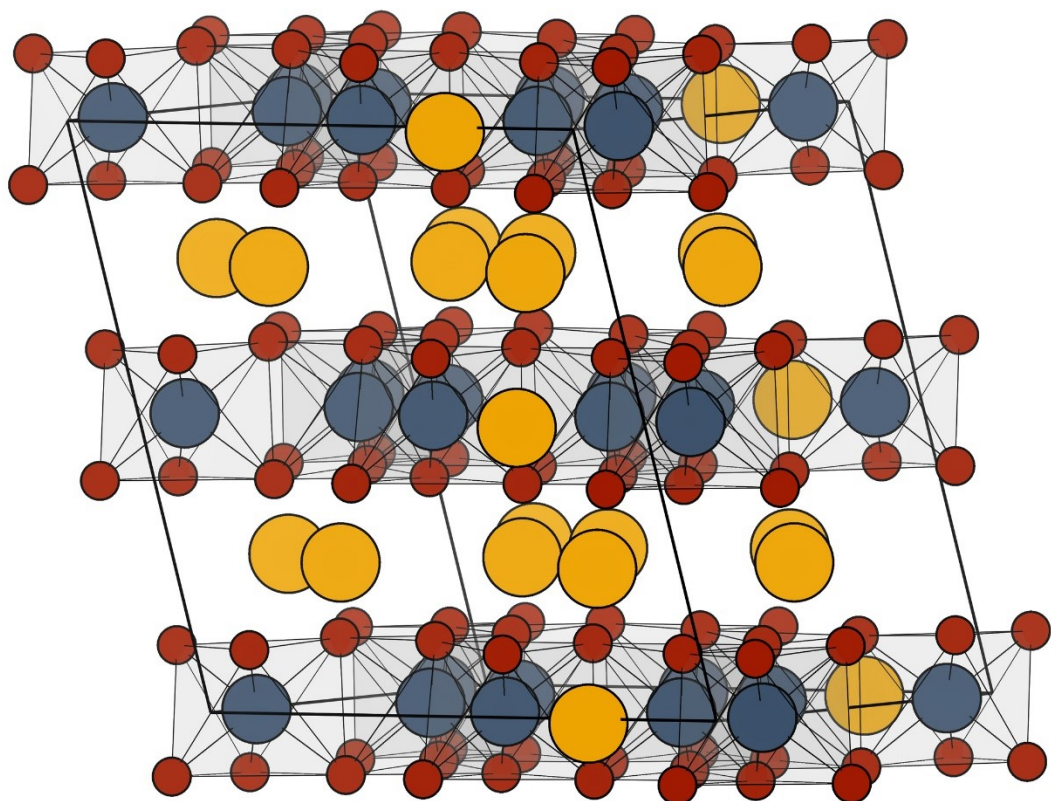


Fig S18 Calculated structure of  $\text{Li}_{14}(\text{Li-layer})\text{Li}_2(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$



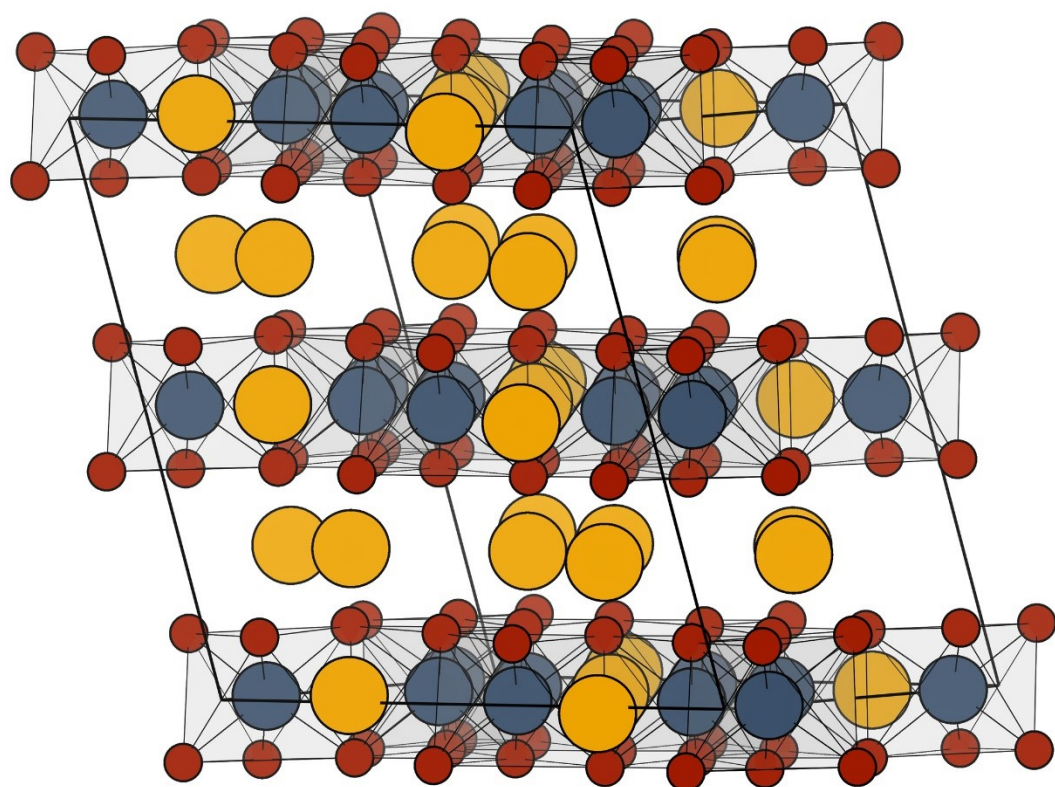


Fig S19 Calculated structure of  $\text{Li}_{14}(\text{Li-layer})\text{Li}_6(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

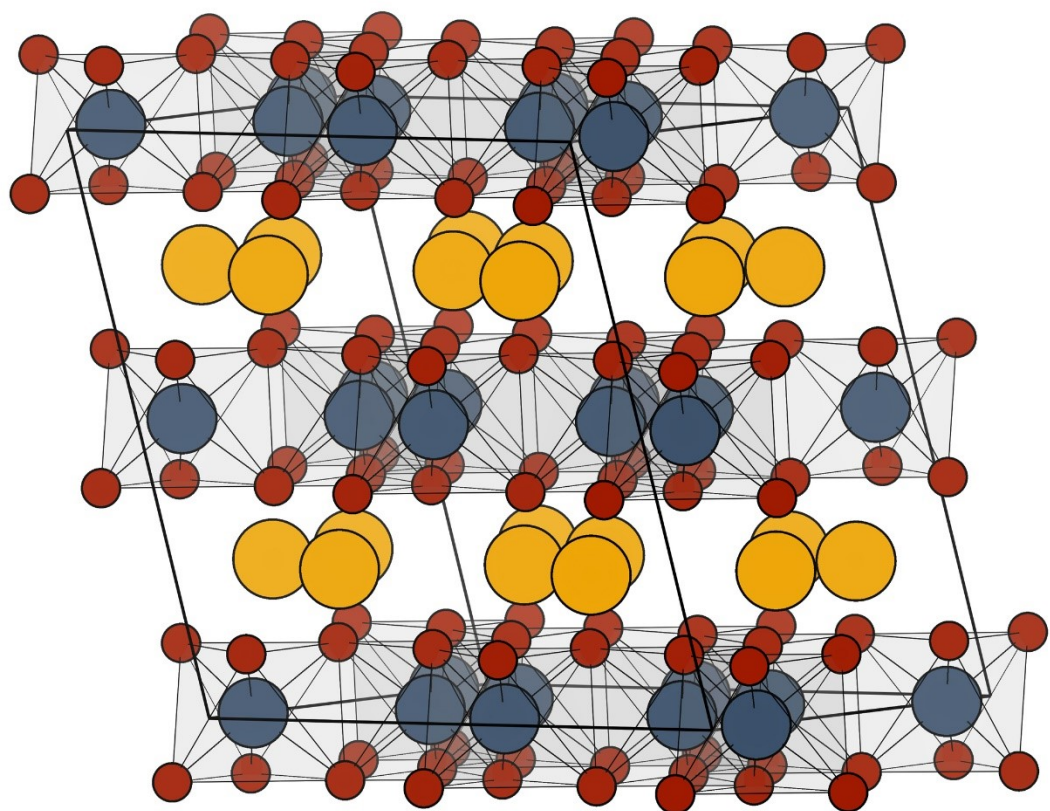


Fig S20 Calculated structure of  $\text{Li}_{16}(\text{Li-layer})\text{Li}_0(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

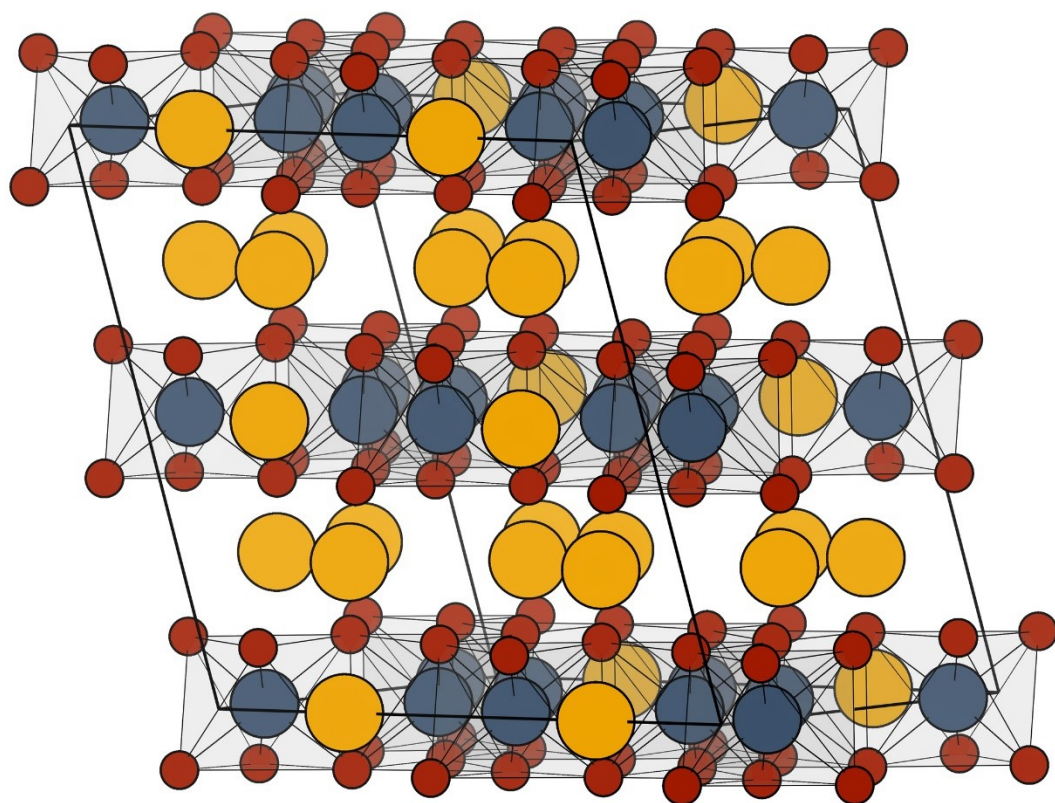


Fig S21 Calculated structure of  $\text{Li}_{16}(\text{Li-layer})\text{Li}_4(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

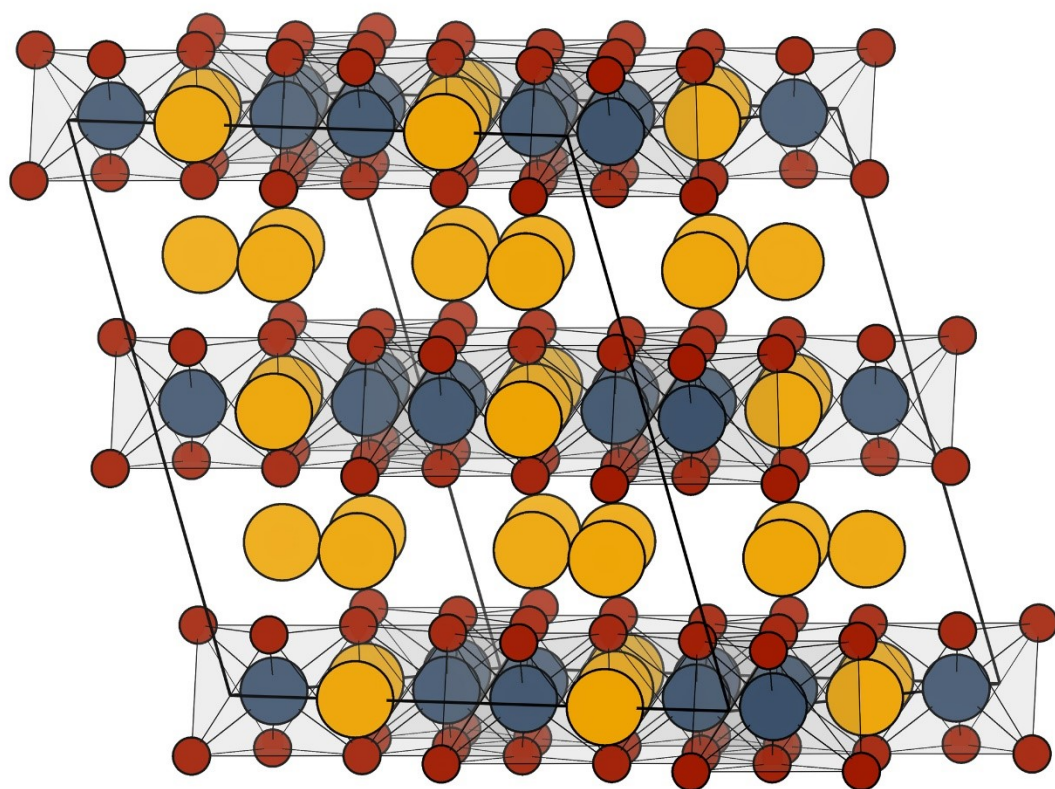


Fig S22 Calculated structure of  $\text{Li}_{16}(\text{Li-layer})\text{Li}_8(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$



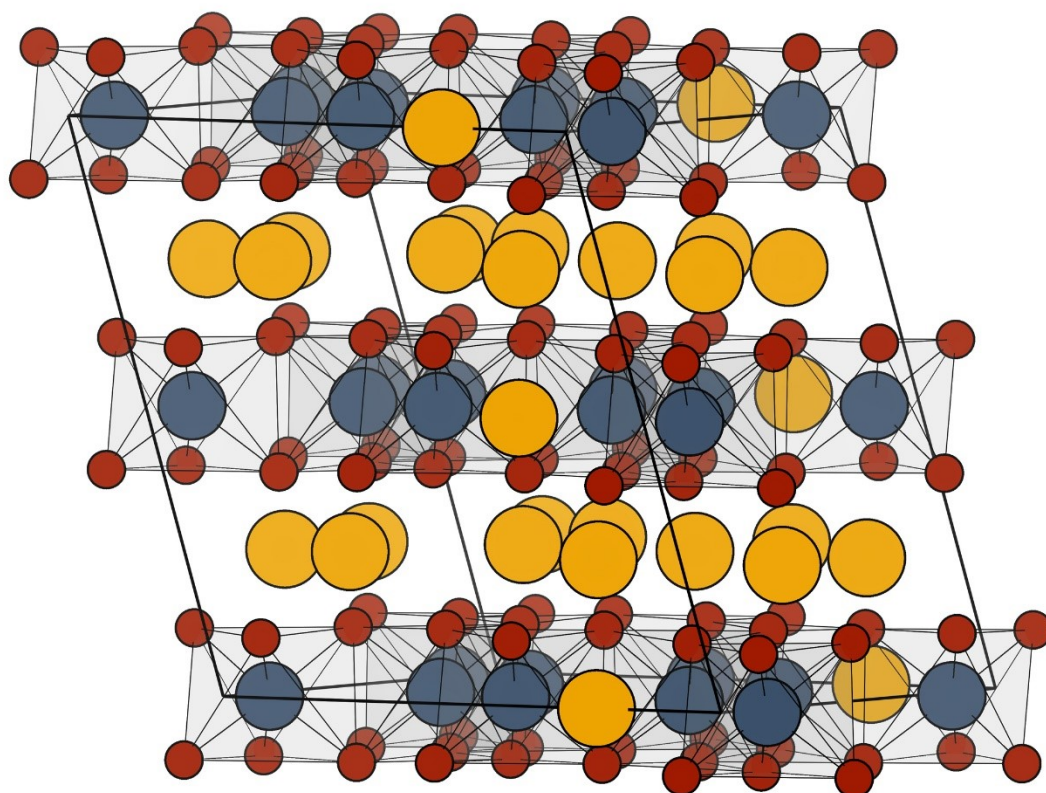


Fig S23 Calculated structure of  $\text{Li}_{18}(\text{Li-layer})\text{Li}_2(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

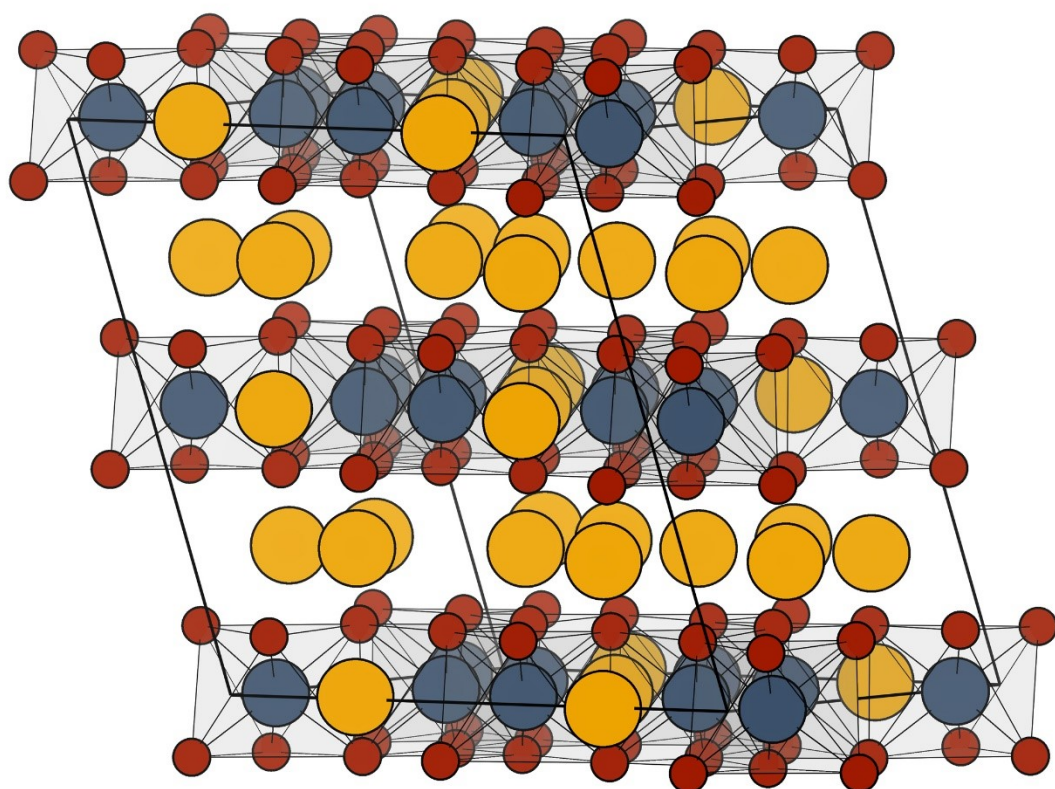


Fig S24 Calculated structure of  $\text{Li}_{18}(\text{Li-layer})\text{Li}_6(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

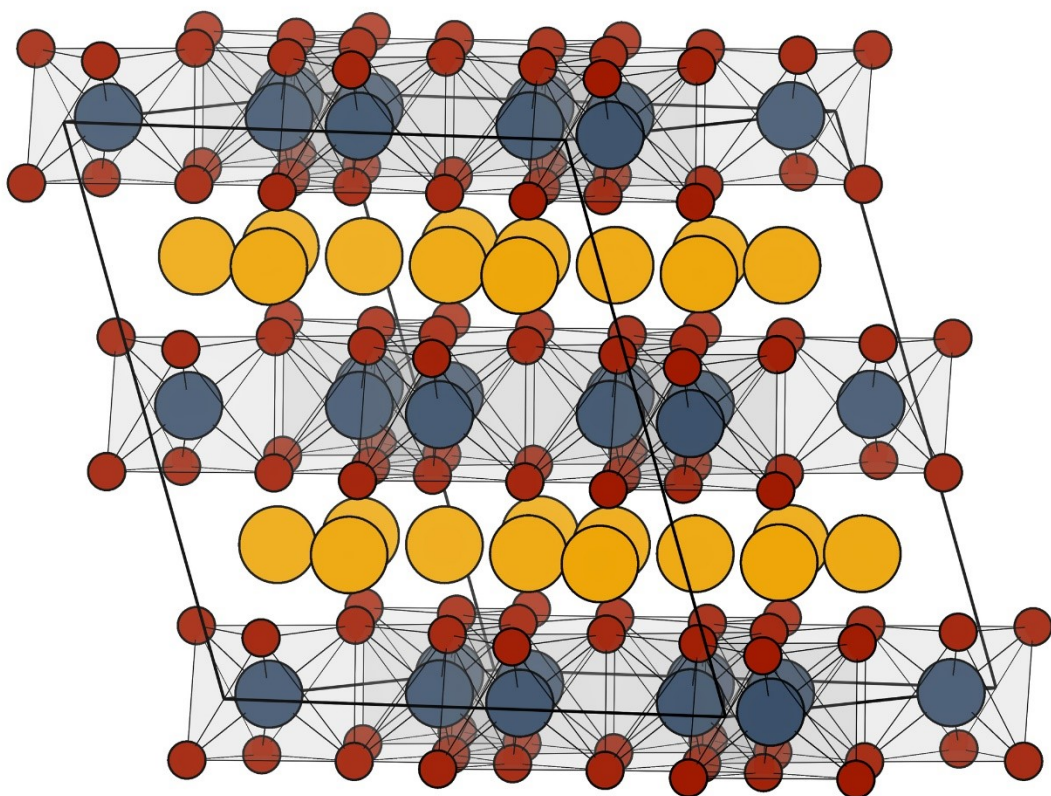


Fig S25 Calculated structure of  $\text{Li}_{20}(\text{Li-layer})\text{Li}_0(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$



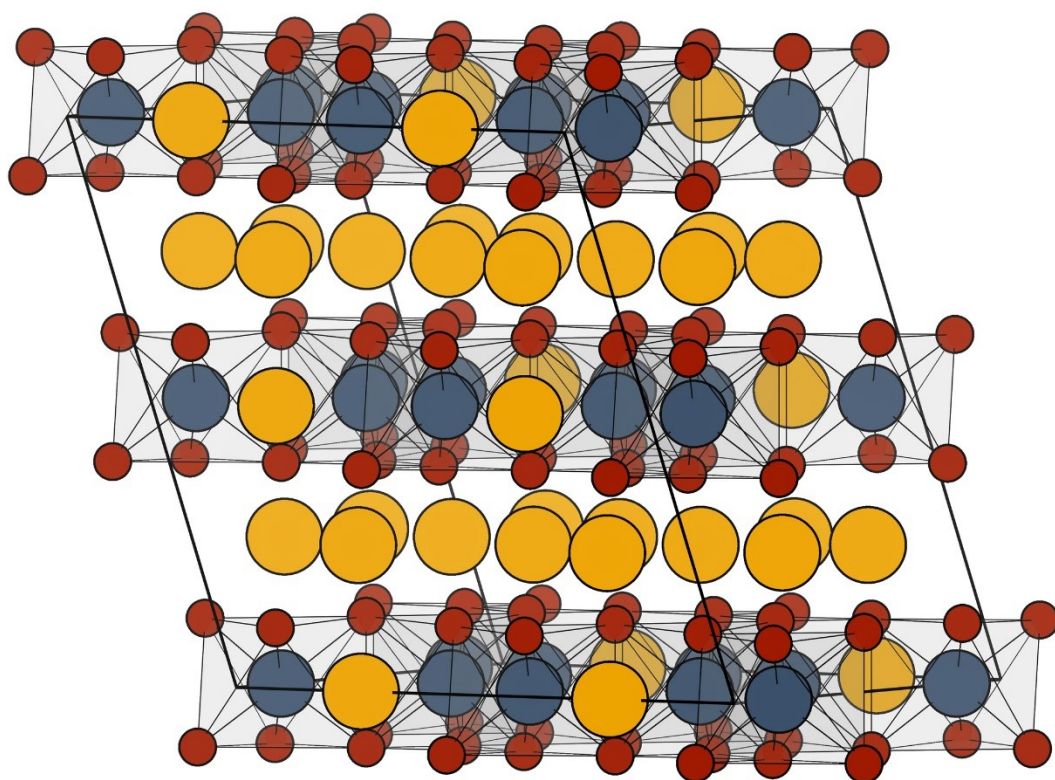


Fig S26 Calculated structure of  $\text{Li}_{20}(\text{Li-layer})\text{Li}_4(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

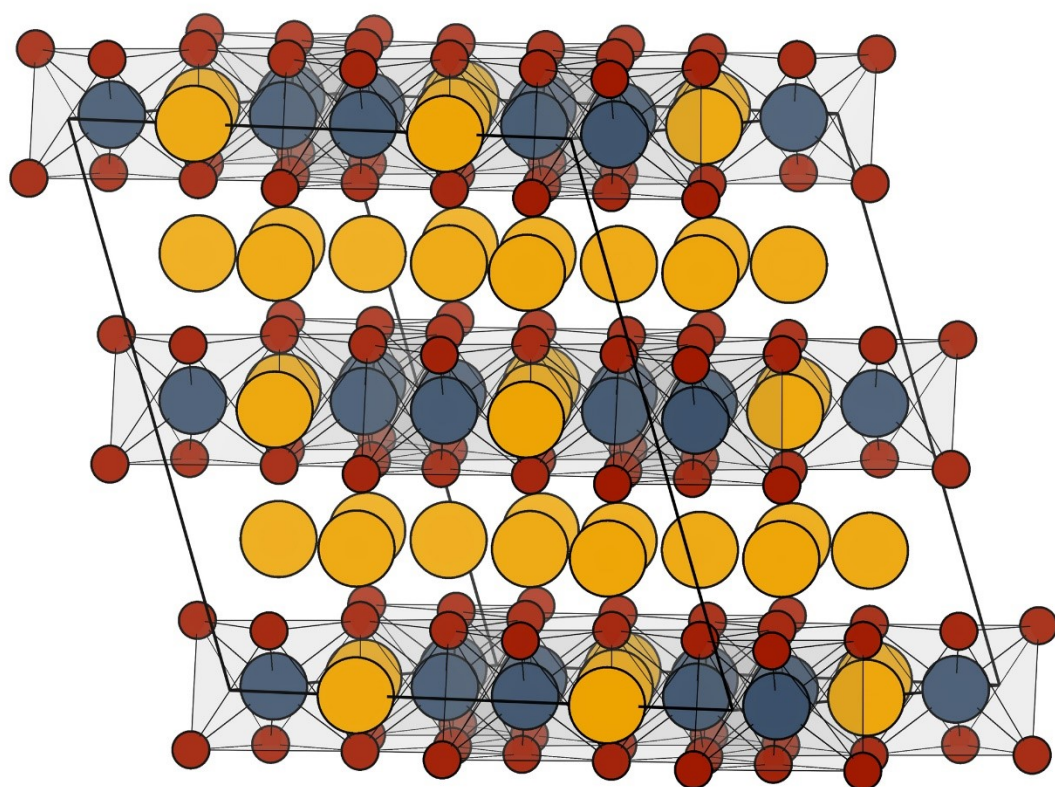


Fig S27 Calculated structure of  $\text{Li}_{20}(\text{Li-layer})\text{Li}_8(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

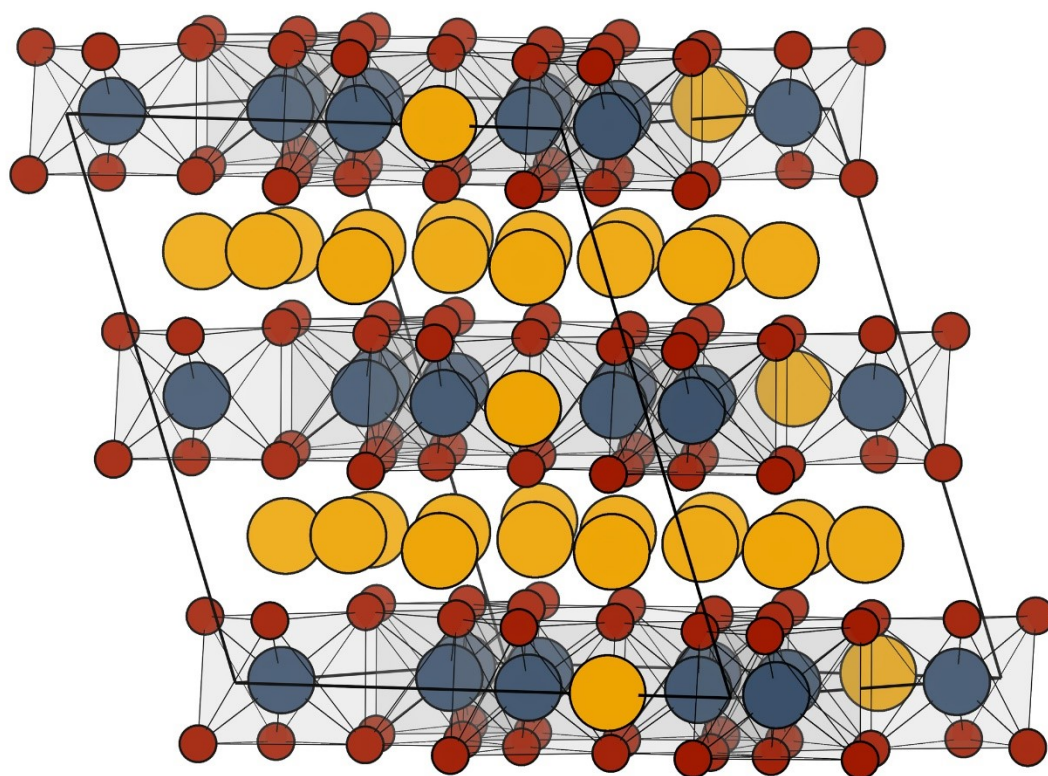


Fig S28 Calculated structure of  $\text{Li}_{22}(\text{Li-layer})\text{Li}_2(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

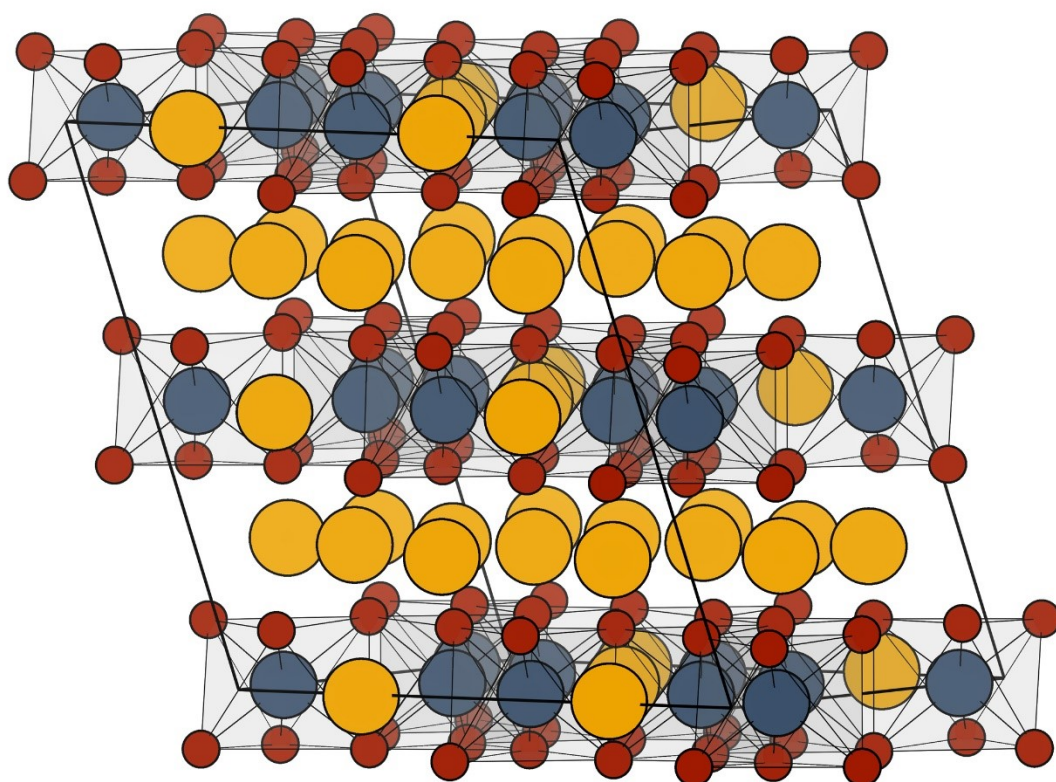


Fig S29 Calculated structure of  $\text{Li}_{22}(\text{Li-layer})\text{Li}_6(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$



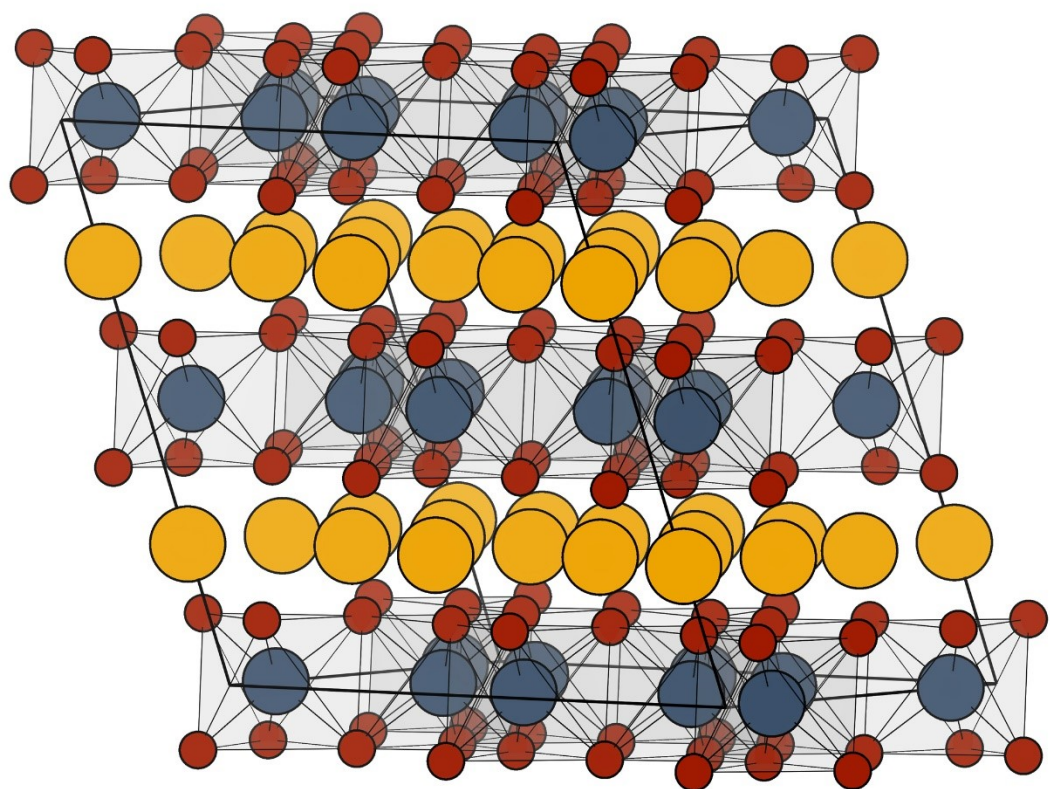


Fig S30 Calculated structure of  $\text{Li}_{24}(\text{Li-layer})\text{Li}_0(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

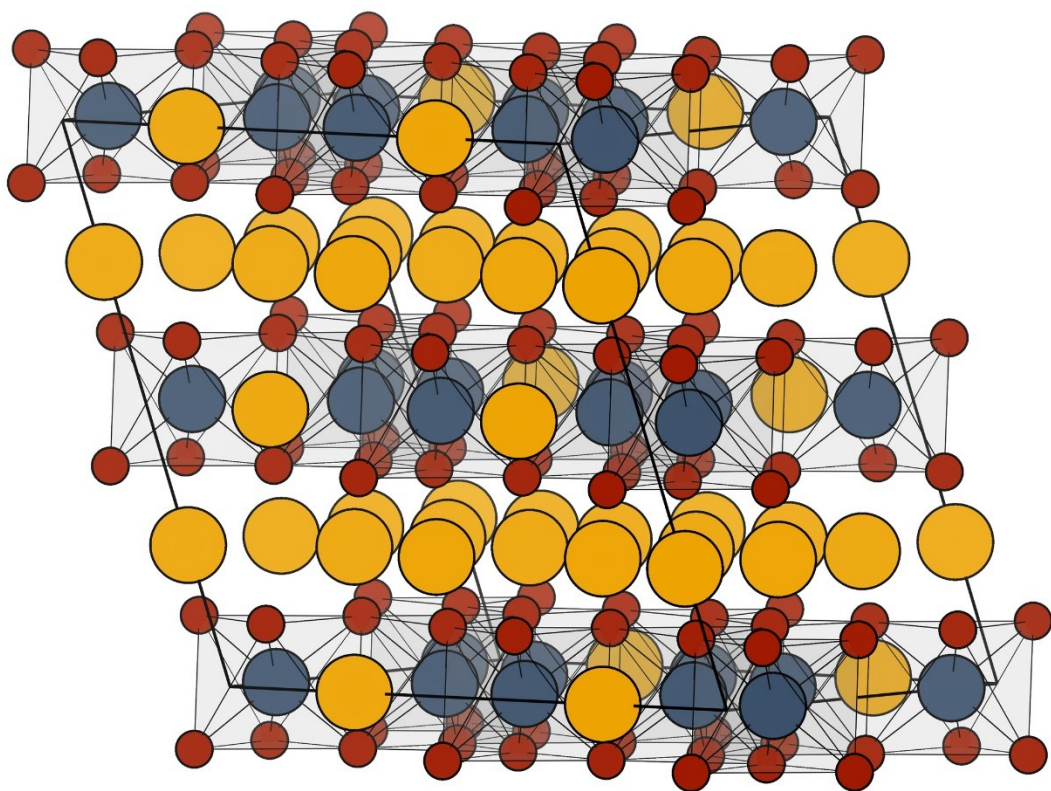


Fig S31 Calculated structure of  $\text{Li}_{24}(\text{Li-layer})\text{Li}_4(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$

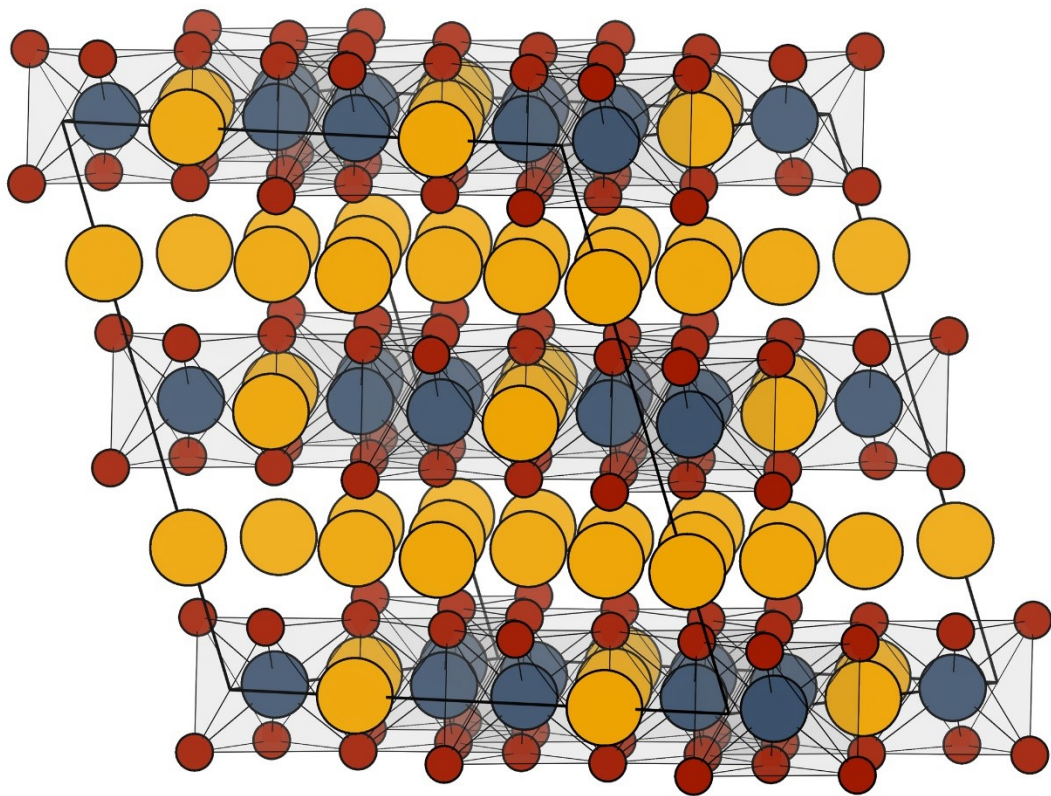


Fig S32 Calculated structure of  $\text{Li}_{24}(\text{Li-layer})\text{Li}_8(\text{Mn-layer})\text{Mn}_{16}\text{O}_{48}$