

# From Adiabatic to Diabatic Representation: An ab initio Investigation of the LiS Molecule

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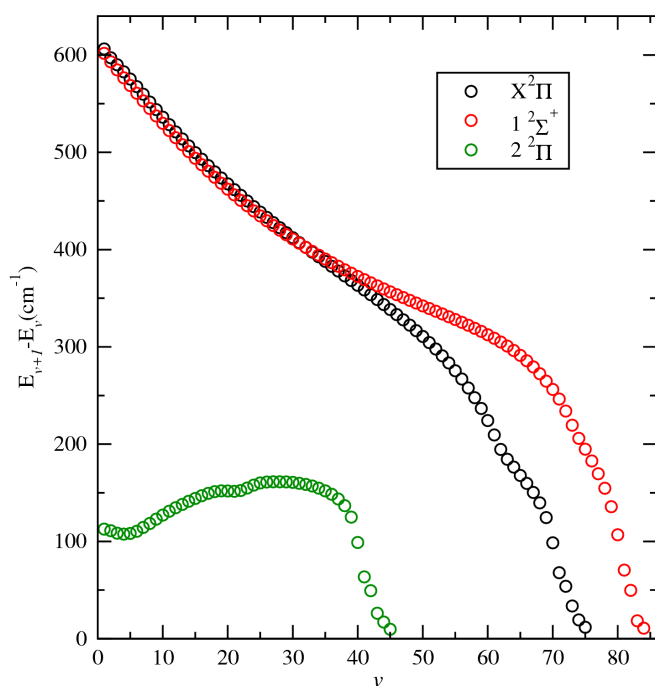


FIG. 1. Vibrational energy levels of LiS.

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TABLE I. Vibrational energy levels for the  $X^2\Pi$ ,  $A^2\Sigma^+$  and  $2^2\Pi$  electronic states of LiS.

| $v$ | $E(X^2\Pi)$ | $\Delta E(X^2\Pi)$ | $E(A^2\Sigma^+)$ | $\Delta E(A^2\Sigma^+)$ | $E(2^2\Pi)$ | $\Delta E(2^2\Pi)$ |
|-----|-------------|--------------------|------------------|-------------------------|-------------|--------------------|
| 0   | -26730.9    |                    | -30456.8         |                         | -5770.6     |                    |
| 1   | -26124.6    | 606.3              | -29855.1         | 601.7                   | -5657.9     | 112.7              |
| 2   | -25527.4    | 597.2              | -29262.1         | 593.0                   | -5547.0     | 110.9              |
| 3   | -24937.4    | 589.9              | -28677.3         | 584.8                   | -5438.6     | 108.4              |
| 4   | -24354.7    | 582.8              | -28100.7         | 576.6                   | -5331.1     | 107.5              |
| 5   | -23779.3    | 575.3              | -27532.1         | 568.6                   | -5222.9     | 108.2              |
| 6   | -23211.8    | 567.5              | -26971.4         | 560.7                   | -5112.5     | 110.4              |
| 7   | -22652.2    | 559.6              | -26418.5         | 552.8                   | -4998.1     | 114.4              |
| 8   | -22100.5    | 551.7              | -25873.5         | 545.0                   | -4879.6     | 118.5              |
| 9   | -21556.6    | 543.9              | -25336.1         | 537.4                   | -4756.7     | 122.9              |
| 10  | -21020.5    | 536.1              | -24806.3         | 529.8                   | -4629.6     | 127.0              |
| 11  | -20492.0    | 528.4              | -24283.9         | 522.3                   | -4498.7     | 130.9              |
| 12  | -19971.0    | 521.0              | -23768.9         | 515.0                   | -4364.0     | 134.7              |
| 13  | -19457.3    | 513.7              | -23261.1         | 507.8                   | -4225.9     | 138.0              |
| 14  | -18950.7    | 506.6              | -22760.4         | 500.8                   | -4084.7     | 141.2              |
| 15  | -18451.0    | 499.7              | -22266.5         | 493.9                   | -3940.6     | 144.2              |
| 16  | -17958.1    | 492.9              | -21779.3         | 487.2                   | -3793.6     | 146.9              |
| 17  | -17471.7    | 486.3              | -21298.7         | 480.6                   | -3644.2     | 149.4              |
| 18  | -16991.9    | 479.9              | -20824.4         | 474.3                   | -3493.0     | 151.2              |
| 19  | -16518.3    | 473.6              | -20356.3         | 468.1                   | -3341.0     | 152.0              |
| 20  | -16050.7    | 467.5              | -19894.2         | 462.1                   | -3189.2     | 151.9              |
| 21  | -15589.1    | 461.6              | -19437.9         | 456.3                   | -3037.7     | 151.5              |
| 22  | -15133.4    | 455.7              | -18987.4         | 450.6                   | -2885.3     | 152.3              |
| 23  | -14683.5    | 449.9              | -18542.2         | 445.1                   | -2730.4     | 154.9              |
| 24  | -14239.3    | 444.2              | -18102.5         | 439.8                   | -2572.5     | 157.9              |
| 25  | -13800.7    | 438.5              | -17667.9         | 434.6                   | -2412.4     | 160.1              |
| 26  | -13367.7    | 433.1              | -17238.3         | 429.6                   | -2251.3     | 161.1              |
| 27  | -12939.9    | 427.7              | -16813.7         | 424.7                   | -2090.1     | 161.3              |
| 28  | -12517.4    | 422.5              | -16393.7         | 419.9                   | -1928.7     | 161.3              |
| 29  | -12100.0    | 417.3              | -15978.3         | 415.4                   | -1767.5     | 161.2              |
| 30  | -11687.8    | 412.2              | -15567.4         | 410.9                   | -1606.8     | 160.7              |
| 31  | -11280.7    | 407.1              | -15160.9         | 406.5                   | -1447.0     | 159.8              |
| 32  | -10878.5    | 402.2              | -14758.6         | 402.3                   | -1288.4     | 158.6              |
| 33  | -10481.0    | 397.4              | -14360.4         | 398.2                   | -1131.5     | 156.9              |
| 34  | -10088.4    | 392.6              | -13966.2         | 394.2                   | -976.7      | 154.8              |
| 35  | -9700.6     | 387.8              | -13575.9         | 390.3                   | -824.7      | 152.0              |
| 36  | -9317.7     | 382.9              | -13189.3         | 386.5                   | -676.2      | 148.5              |
| 37  | -8939.8     | 377.9              | -12806.5         | 382.8                   | -532.6      | 143.6              |
| 38  | -8566.8     | 372.9              | -12427.3         | 379.2                   | -395.9      | 136.7              |
| 39  | -8198.7     | 368.1              | -12051.5         | 375.8                   | -270.9      | 124.9              |
| 40  | -7835.3     | 363.3              | -11679.1         | 372.4                   | -171.9      | 98.9               |
| 41  | -7476.8     | 358.5              | -11310.1         | 369.0                   | -108.4      | 63.5               |
| 42  | -7123.3     | 353.6              | -10944.3         | 365.8                   | -59.0       | 49.4               |
| 43  | -6774.7     | 348.6              | -10581.6         | 362.6                   | -32.9       | 26.2               |
| 44  | -6431.1     | 343.5              | -10222.1         | 359.5                   | -15.8       | 17.1               |
| 45  | -6092.7     | 338.4              | -9865.5          | 356.5                   | -6.2        | 9.6                |
| 46  | -5759.5     | 333.2              | -9511.9          | 353.6                   |             |                    |
| 47  | -5431.7     | 327.8              | -9161.3          | 350.7                   |             |                    |
| 48  | -5109.3     | 322.3              | -8813.5          | 347.8                   |             |                    |
| 49  | -4792.8     | 316.6              | -8468.5          | 344.9                   |             |                    |

TABLE II. Continued

| $v$ | $E(X^2\Pi)$ | $\Delta E(X^2\Pi)$ | $E(A^2\Sigma^+)$ | $\Delta E(1^2\Sigma^+)$ | $E(2^2\Pi)$ | $\Delta E(2^2\Pi)$ |
|-----|-------------|--------------------|------------------|-------------------------|-------------|--------------------|
| 50  | -4482.1     | 310.6              | -8126.4          | 342.2                   |             |                    |
| 51  | -4177.7     | 304.4              | -7786.9          | 339.4                   |             |                    |
| 52  | -3879.9     | 297.8              | -7450.4          | 336.6                   |             |                    |
| 53  | -3589.1     | 290.8              | -7116.6          | 333.8                   |             |                    |
| 54  | -3305.7     | 283.4              | -6785.6          | 330.9                   |             |                    |
| 55  | -3030.2     | 275.5              | -6457.5          | 328.1                   |             |                    |
| 56  | -2763.2     | 266.9              | -6132.3          | 325.2                   |             |                    |
| 57  | -2505.5     | 257.7              | -5810.1          | 322.2                   |             |                    |
| 58  | -2257.8     | 247.7              | -5490.9          | 319.1                   |             |                    |
| 59  | -2021.1     | 236.7              | -5175.1          | 315.9                   |             |                    |
| 60  | -1796.9     | 224.2              | -4862.6          | 312.5                   |             |                    |
| 61  | -1587.5     | 209.4              | -4553.7          | 308.9                   |             |                    |
| 62  | -1392.9     | 194.6              | -4248.7          | 304.9                   |             |                    |
| 63  | -1208.4     | 184.4              | -3947.9          | 300.8                   |             |                    |
| 64  | -1032.1     | 176.4              | -3651.7          | 296.3                   |             |                    |
| 65  | -864.3      | 167.8              | -3360.4          | 291.3                   |             |                    |
| 66  | -704.7      | 159.6              | -3074.7          | 285.7                   |             |                    |
| 67  | -554.4      | 150.3              | -2795.3          | 279.4                   |             |                    |
| 68  | -414.8      | 139.6              | -2522.9          | 272.4                   |             |                    |
| 69  | -290.3      | 124.5              | -2258.2          | 264.7                   |             |                    |
| 70  | -191.8      | 98.5               | -2001.9          | 256.2                   |             |                    |
| 71  | -123.9      | 67.8               | -1755.6          | 246.4                   |             |                    |
| 72  | -70.1       | 53.8               | -1521.6          | 233.9                   |             |                    |
| 73  | -36.5       | 33.6               | -1302.2          | 219.4                   |             |                    |
| 74  | -17.2       | 19.3               | -1096.2          | 206.0                   |             |                    |
| 75  | -5.5        | 11.7               | -901.4           | 194.8                   |             |                    |
| 76  |             |                    | -718.7           | 182.7                   |             |                    |
| 77  |             |                    | -549.2           | 169.5                   |             |                    |
| 78  |             |                    | -394.5           | 154.7                   |             |                    |
| 79  |             |                    | -258.9           | 135.7                   |             |                    |
| 80  |             |                    | -152.1           | 106.8                   |             |                    |
| 81  |             |                    | -81.5            | 70.5                    |             |                    |
| 82  |             |                    | -31.8            | 49.7                    |             |                    |
| 83  |             |                    | -13.4            | 18.4                    |             |                    |
| 84  |             |                    | -2.6             | 10.8                    |             |                    |

TABLE III. Radiative lifetimes of the vibrational states ( $j=0$ ) of  $X^2\Pi$  of LiS molecule.

| $v$ | $\tau_v$ (s) ( $X^2\Pi$ ) | $\tau_v$ (ms) ( $A^2\Sigma$ ) | $\tau_v$ (ns) ( $2^2\Pi$ ) |
|-----|---------------------------|-------------------------------|----------------------------|
| 0   | 14.537                    | 0.4817                        | 74.552                     |
| 1   | 0.7209                    | 0.3336                        | 70.314                     |
| 2   | 0.3960                    | 0.2560                        | 65.933                     |
| 3   | 0.2887                    | 0.2043                        | 62.059                     |
| 4   | 0.2314                    | 0.1688                        | 58.662                     |
| 5   | 0.1944                    | 0.1434                        | 56.136                     |
| 6   | 0.1694                    | 0.1245                        | 54.510                     |
| 7   | 0.1508                    | 0.1101                        | 53.362                     |
| 8   | 0.1365                    | 0.0987                        | 52.658                     |
| 9   | 0.1253                    | 0.0895                        | 52.149                     |
| 10  | 0.1164                    | 0.0820                        | 51.779                     |
| 11  | 0.1090                    | 0.0757                        | 51.524                     |
| 12  | 0.1028                    | 0.0703                        | 51.343                     |
| 13  | 0.0973                    | 0.0657                        | 51.230                     |
| 14  | 0.0924                    | 0.0617                        | 51.159                     |
| 15  | 0.0880                    | 0.0582                        | 51.121                     |
| 16  | 0.0839                    | 0.0552                        | 51.134                     |
| 17  | 0.0799                    | 0.0524                        | 51.251                     |
| 18  | 0.0762                    | 0.0500                        | 51.551                     |
| 19  | 0.0726                    | 0.0478                        | 52.094                     |
| 20  | 0.0690                    | 0.0458                        | 52.799                     |
| 21  | 0.0655                    | 0.0440                        | 53.357                     |
| 22  | 0.0620                    | 0.0422                        | 53.452                     |
| 23  | 0.0587                    | 0.0406                        | 53.210                     |
| 24  | 0.0555                    | 0.0389                        | 53.065                     |
| 25  | 0.0524                    | 0.0374                        | 53.266                     |
| 26  | 0.0495                    | 0.0361                        | 53.683                     |
| 27  | 0.0466                    | 0.0349                        | 54.204                     |
| 28  | 0.0439                    | 0.0338                        | 55.016                     |
| 29  | 0.0415                    | 0.0326                        | 55.746                     |
| 30  | 0.0392                    | 0.0315                        | 56.719                     |
| 31  | 0.0371                    | 0.0304                        | 58.334                     |
| 32  | 0.0351                    | 0.0293                        | 60.171                     |
| 33  | 0.0333                    | 0.0282                        | 61.872                     |
| 34  | 0.0316                    | 0.0272                        | 64.772                     |
| 35  | 0.0301                    | 0.0260                        | 67.565                     |
| 36  | 0.0287                    | 0.0249                        | 70.652                     |
| 37  | 0.0275                    | 0.0237                        | 74.705                     |
| 38  | 0.0263                    | 0.0226                        | 80.605                     |
| 39  | 0.0253                    | 0.0216                        | 93.482                     |
| 40  | 0.0243                    | 0.0207                        | 139.47                     |
| 41  | 0.0234                    | 0.0198                        | 191.70                     |
| 42  | 0.0226                    | 0.0189                        | 321.93                     |
| 43  | 0.0218                    | 0.0181                        | 576.85                     |
| 44  | 0.0211                    | 0.0172                        | 816.92                     |
| 45  | 0.0205                    | 0.0164                        | 1191.2                     |
| 46  | 0.0199                    | 0.0156                        |                            |
| 47  | 0.0193                    | 0.0148                        |                            |
| 48  | 0.0188                    | 0.0141                        |                            |
| 49  | 0.0184                    | 0.0133                        |                            |

TABLE IV. Continued

| $v$ | $\tau_v(\text{s}) (X^2\Pi)$ | $\tau_v(\text{ms}) (A^2\Sigma)$ | $\tau_v(\text{s}) (2^2\Pi)$ |
|-----|-----------------------------|---------------------------------|-----------------------------|
| 50  | 0.0179                      | 0.0126                          |                             |
| 51  | 0.0176                      | 0.0119                          |                             |
| 52  | 0.0173                      | 0.0112                          |                             |
| 53  | 0.0170                      | 0.0106                          |                             |
| 54  | 0.0168                      | 0.0099                          |                             |
| 55  | 0.0167                      | 0.0093                          |                             |
| 56  | 0.0166                      | 0.0087                          |                             |
| 57  | 0.0167                      | 0.0082                          |                             |
| 58  | 0.0168                      | 0.0077                          |                             |
| 59  | 0.0171                      | 0.0072                          |                             |
| 60  | 0.0177                      | 0.0067                          |                             |
| 61  | 0.0185                      | 0.0063                          |                             |
| 62  | 0.0193                      | 0.0059                          |                             |
| 63  | 0.0197                      | 0.0056                          |                             |
| 64  | 0.0203                      | 0.0052                          |                             |
| 65  | 0.0209                      | 0.0049                          |                             |
| 66  | 0.0217                      | 0.0047                          |                             |
| 67  | 0.0229                      | 0.0042                          |                             |
| 68  | 0.0248                      | 0.0039                          |                             |
| 69  | 0.0285                      | 0.0042                          |                             |
| 70  | 0.0398                      | 0.0045                          |                             |
| 71  | 0.0534                      | 0.0047                          |                             |
| 72  | 0.0739                      | 0.0059                          |                             |
| 73  | 0.1309                      | 0.0069                          |                             |
| 74  | 0.1875                      | 0.0079                          |                             |
| 75  | 0.3884                      | 0.0099                          |                             |
|     |                             | 0.0121                          |                             |
|     |                             | 0.0163                          |                             |
|     |                             | 0.0223                          |                             |
|     |                             | 0.0339                          |                             |
|     |                             | 0.0734                          |                             |
|     |                             | 0.1312                          |                             |
|     |                             | 0.2419                          |                             |
|     |                             | 0.8401                          |                             |
|     |                             | 2.0052                          |                             |

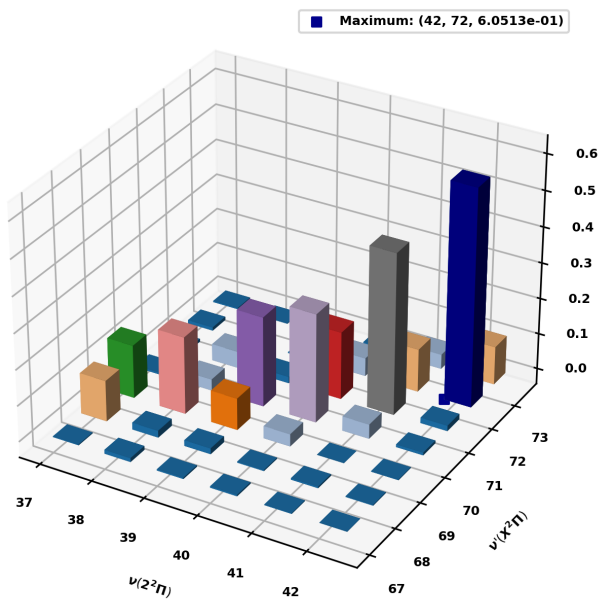


FIG. 2. Franck-Condon Factor diagram of the  $\text{LiS } 2^2\Pi \rightarrow X^2\Pi$  Vibrational Levels.

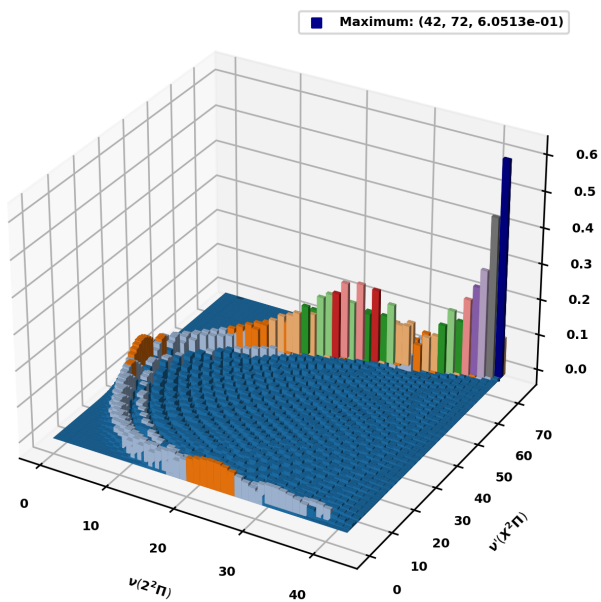


FIG. 3. 3D Visualization of Franck-Condon Factors for  $\text{LiS } 2^2\Pi \rightarrow X^2\Pi$  Vibrational Transitions

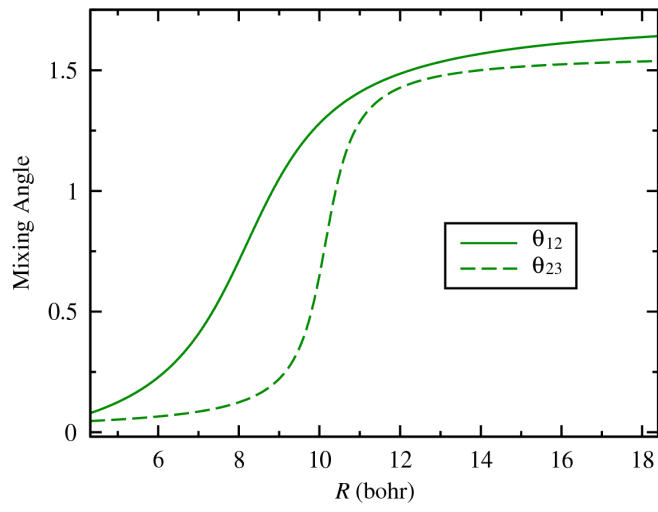


FIG. 4. Mixing Angle of LiS