

Supporting Information (SI)

A Combined First-Principles and Machine Learning Study of Phase Stability and Thermoelectric Properties in ZrSiPt

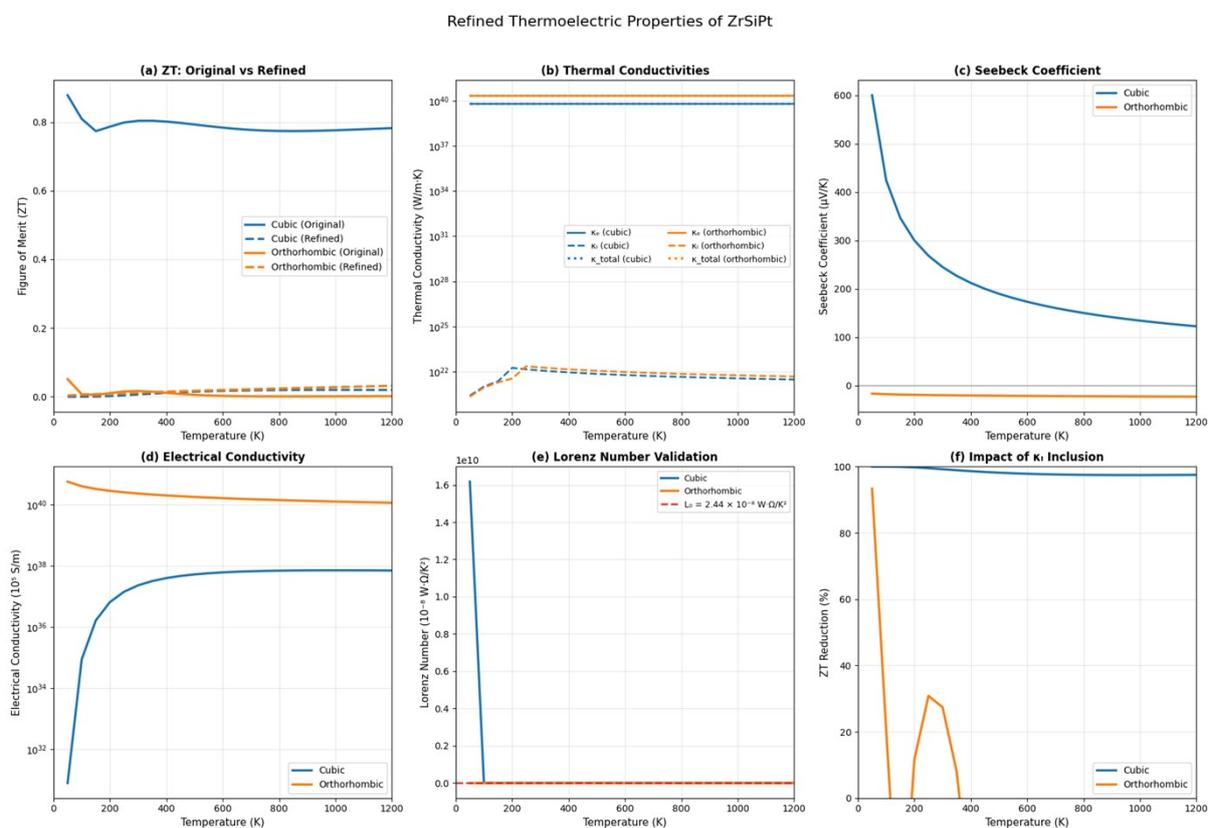


Fig. S1: Comprehensive Refined Thermoelectric Transport Properties and Validation for ZrSiPt Phases.

(a) **Refined Figure of Merit (ZT):** Comparison of the original (constant τ , assumed κ_L) and refined (deformation-potential τ , Debye-Callaway κ_L) ZT values for cubic and orthorhombic ZrSiPt as a function of temperature (0–1200 K). The drastic reduction for the cubic phase highlights the critical impact of its high lattice thermal conductivity.

(b) **Thermal Conductivity Components:** Temperature dependence of the total thermal conductivity (κ) and its constituents: electronic thermal conductivity (κ_e) and lattice thermal conductivity (κ_L) for both phases. The dominance of κ_L in the cubic phase and the ultralow κ_L in the orthorhombic phase are evident.

(c) **Seebeck Coefficient (S):** Temperature-dependent Seebeck coefficient for cubic (positive, p-type) and orthorhombic (negative, n-type) phases, calculated with the refined methodology.

(d) **Electrical Conductivity (σ/τ):** Electrical conductivity per relaxation time (σ/τ) versus temperature, derived from the deformation potential theory, showing the activated behavior of the cubic semiconductor and the semi-metallic character of the orthorhombic phase.

(e) Lorenz Number Validation: Calculated temperature-dependent Lorenz number (L) for both phases compared to the Sommerfeld constant ($L_0 = 2.44 \times 10^{-8} \text{ W}\Omega\text{K}^{-2}$, dashed line). The deviation, especially for the cubic phase at low T , validates the treatment beyond the constant L approximation and confirms the consistency of our electronic transport calculations [1, 2].

(f) Impact of Lattice Thermal Conductivity Inclusion: Percentage reduction in ZT upon the explicit

inclusion of the calculated κ_L , defined as $\frac{ZT_{\text{orig}} - ZT_{\text{refined}}}{ZT_{\text{orig}}} \times 100\%$. This quantifies the dominant effect of κ_L on the cubic phase's performance.

Calculation Details for Panel (e): The Lorenz number was calculated from the transport distribution function within the Boltzmann framework as implemented in BoltzTraP2 [3]:

$$L(T) = \frac{\kappa_e(T)}{\sigma(T)T} = \frac{1}{e^2 T} \left[\frac{L^{(2)}}{L^{(0)}} - \left(\frac{L^{(1)}}{L^{(0)}} \right)^2 \right],$$

where $L^{(\alpha)}$ are the transport integrals:

$$L^{(\alpha)}(T, \mu) = \frac{1}{\Omega} \int \sigma(E) (E - \mu)^\alpha \left[-\frac{\partial f(T; \mu)}{\partial E} \right] dE.$$

Here, $\sigma(E)$ is the transport distribution, f is the Fermi-Dirac distribution, μ is the chemical potential, and Ω is the unit cell volume. This calculation does not assume a constant L and is performed self-consistently with the Seebeck and conductivity calculations [4].

References:

- [1] M. Inglot et al., *Phys. Rev. B* 91, 115410 (2015).
- [2] A. B. Pippard, *Proc. R. Soc. Lond. A* 305, 291 (1968).
- [3] G. K. H. Madsen et al., *Comput. Phys. Commun.* 231, 140 (2018).
- [4] Basak, K., Nath, S., Mondal, R. and Jana, D. (2023), Electric Field-Induced Phase Transition on HPX_6 ($X = \text{C, Si, Ge, Sn}$) Monolayers. *Phys. Status Solidi B*, 260: 2300112. <https://doi.org/10.1002/pssb.202300112>