## Chemo-Mechanical limitations of liquid alloy anodes for sodium solid-state batteries

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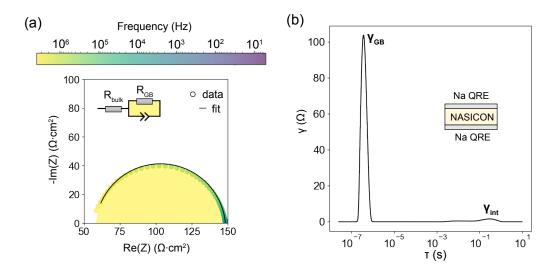
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Supplemental figures



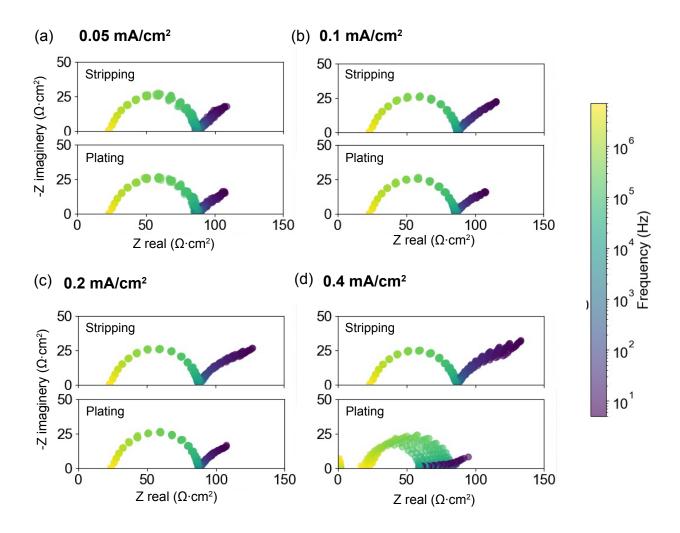
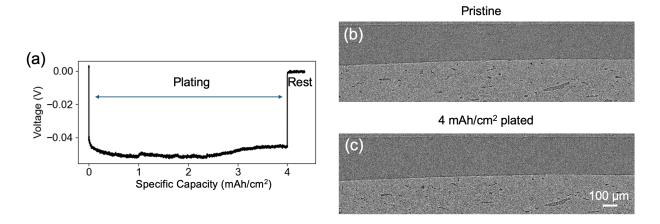
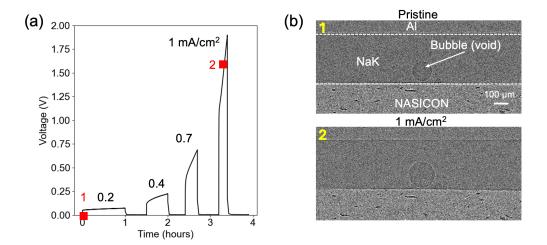


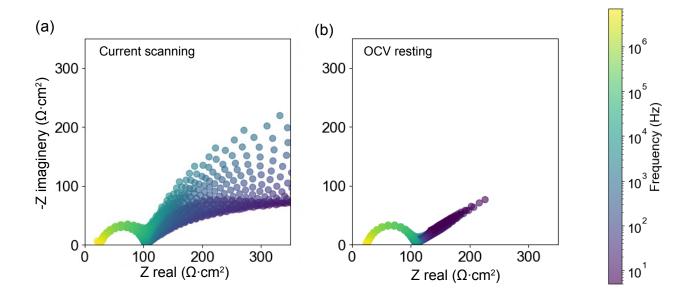
Figure S2 The *operando* GEIS spectra collected during the CCD test of NaK50 liquid electrode under different current densities.



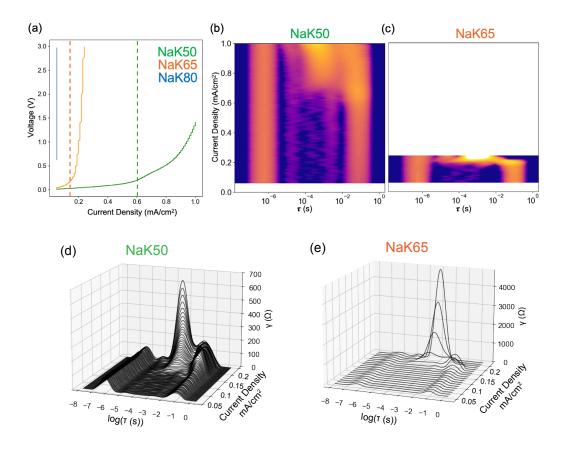
**Figure S3** in situ XCT collected over Na plating process of NaK liquid anode under 0.4 mA/cm<sup>2</sup> current density. (a) Voltage profile of the in situ XCT cell. (b-c) Reconstructed virtual cross-sections at the NaK/NASICON interface showing homogenous plating without crack formation.



**Figure S4** in situ XCT collected over staircase Na stripping process of NaK liquid electrode under 0.2, 0.4, 0.7 and 1.0 mA/cm<sup>2</sup> current densities. (a) Voltage profile of the in situ XCT cell. (b) Reconstructed virtual cross-sections at the NaK/NASICON interface.



**Figure S5** The *operando* GEIS spectra collected during Na stripping current scanning (a) and PEIS spectra collected during subsequent OCV resting (b) of NaK50 liquid electrode.



**Figure S6** (a) Voltage profiles of current scanning experiment performed in NaK liquid alloys at different Na concentrations. *Operando* DRT spectra as function of Na stripping current density collected on (b,d) NaK50 and (c,e) NaK65 working electrodes.

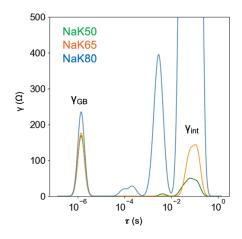
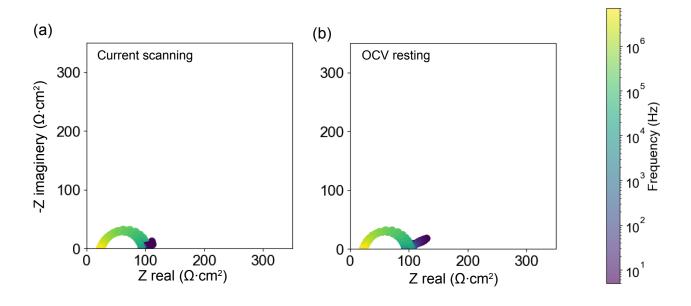
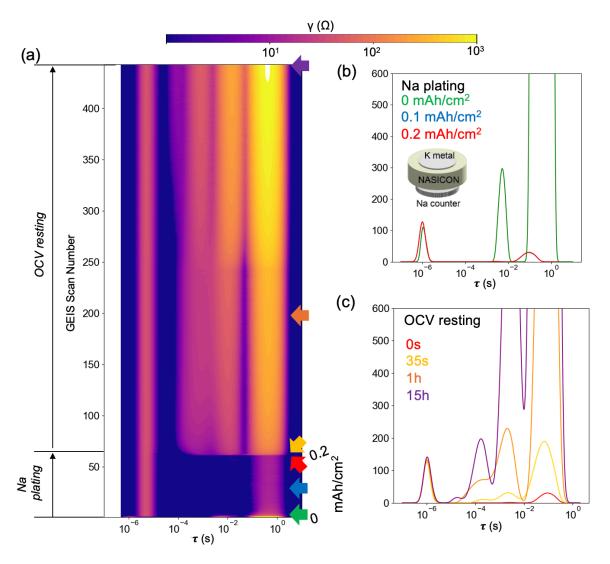


Figure S7 DRT spectra collected on pristine NaK/NASICON/Na cells with NaK50, NakK65 and NaK80 working electrodes.



**Figure S8** The *operando* GEIS spectra collected during Na plating current scanning (a) and PEIS spectra collected during subsequent OCV resting (b) of NaK50 liquid electrode.



**Figure S9** (a) *Operando* DRT spectra obtained during Na plating-OCV resting test on K metal working electrode. (b) DRT spectra overlay over the Na plating process at different plated capacities. (c) DRT spectra overlay over the OCV resting process.