

Supplementary Information

for paper

Novel bimetallic Ln^{III}/V^{IV} (Ln = Gd, Tb, Dy, Er, Yb, Lu) compounds based on cyclopropane-1,1-dicarboxylate anions and bulky tetrabutylammonium cations: synthesis, structure, magnetic properties, and thermal decomposition

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Description of the crystal structures

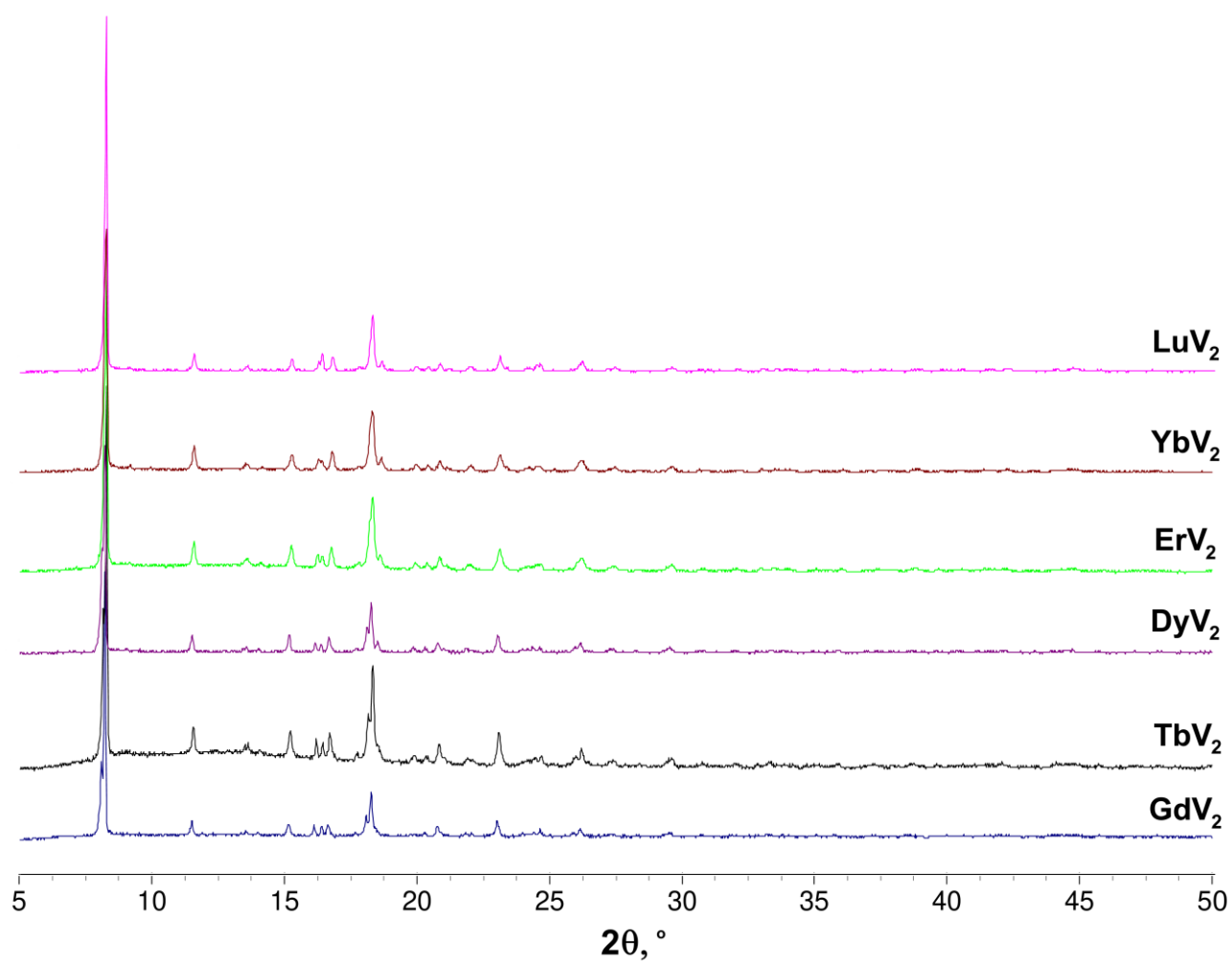


Figure S1. Experimental powder XRD patterns for compounds LnV_2 (2θ range of 5-50°).

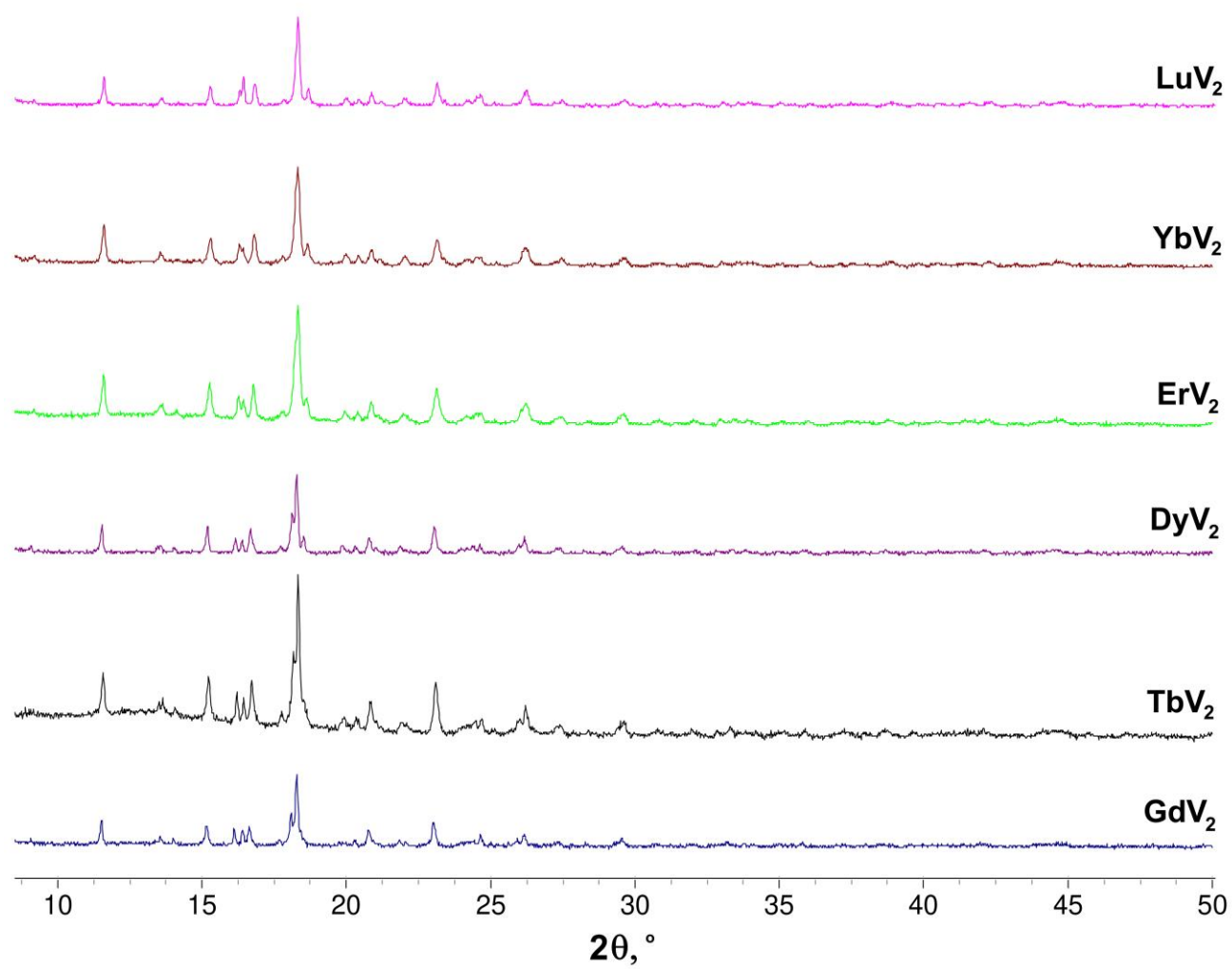


Figure S2. Experimental powder XRD patterns for compounds LnV_2 (2θ range of 10-50°).

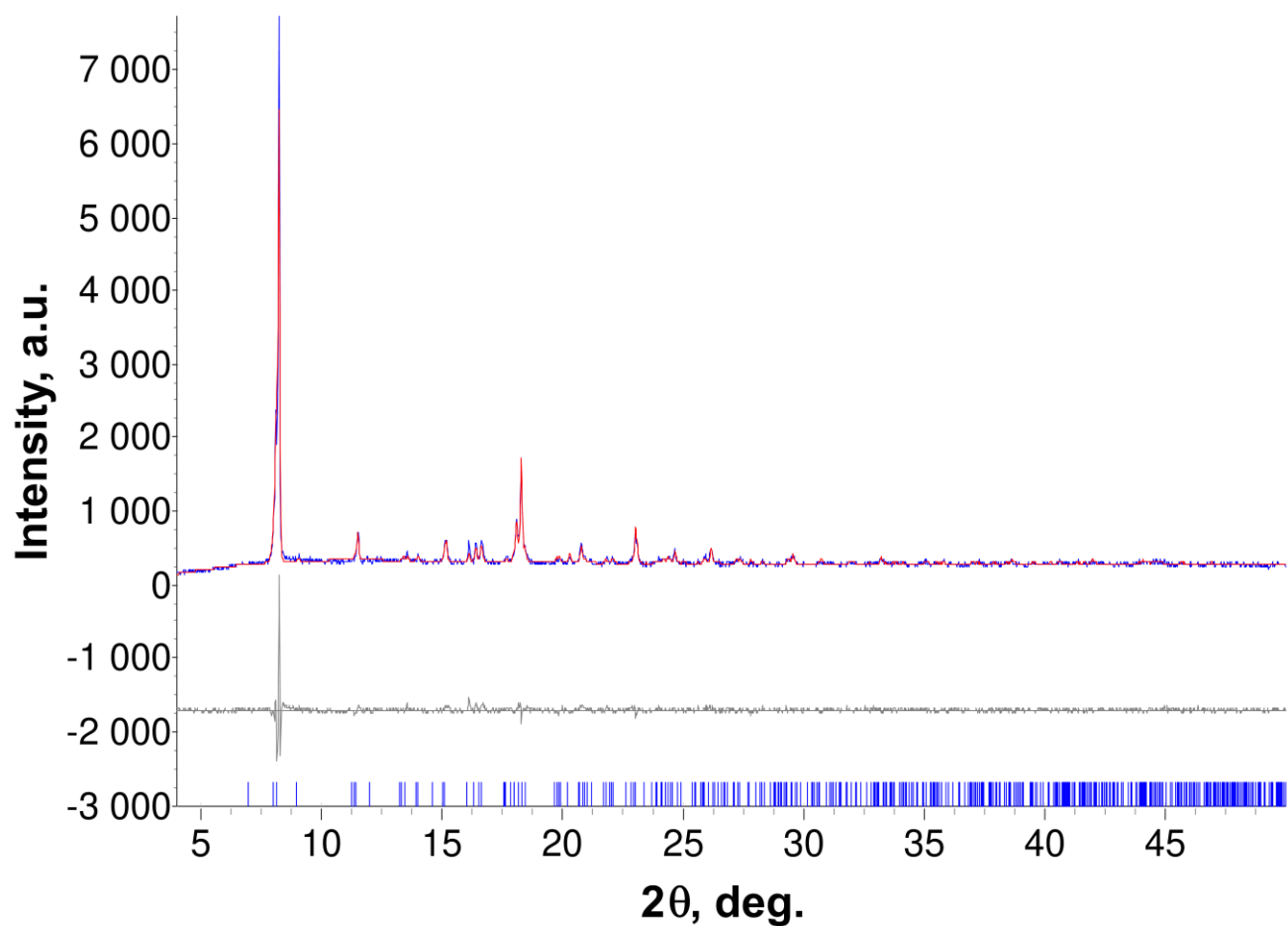


Figure S3. The experimental (blue line) and calculated (red line) powder XRD patterns for GdV_2 and their difference (grey line). The SCXRD data for GdV_2 was used to simulate the theoretical line. Blue ticks indicate calculated positions of the reflections.

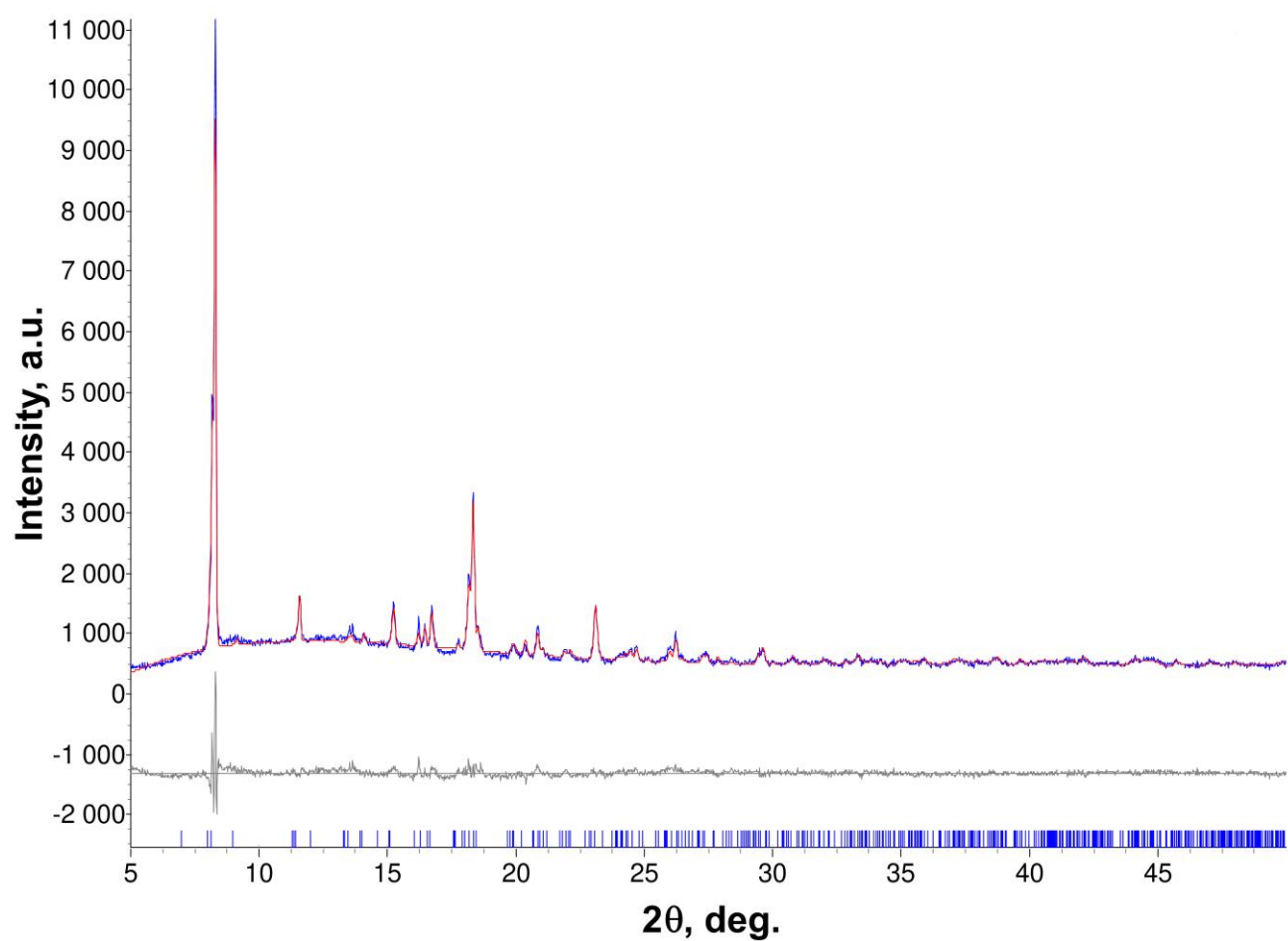


Figure S4. The experimental (blue line) and calculated (red line) powder XRD patterns for TbV_2 and their difference (grey line). The SCXRD data for TbV_2 was used to simulate the theoretical line. Blue ticks indicate calculated positions of the reflections.

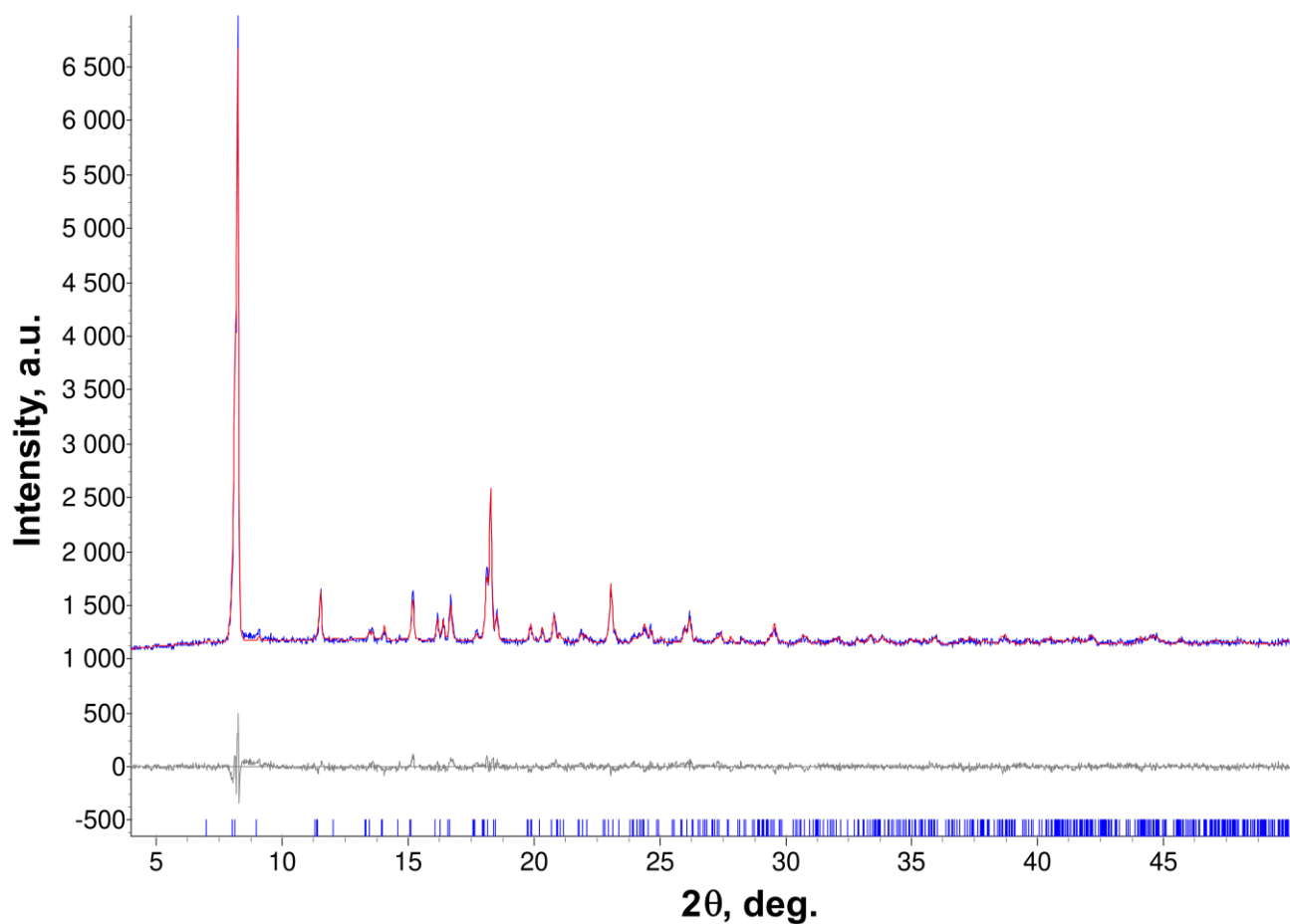


Figure S5. The experimental (blue line) and calculated (red line) powder XRD patterns for DyV_2 and their difference (grey line). The SCXRD data for DyV_2 was used to simulate the theoretical line. Blue ticks indicate calculated positions of the reflections.

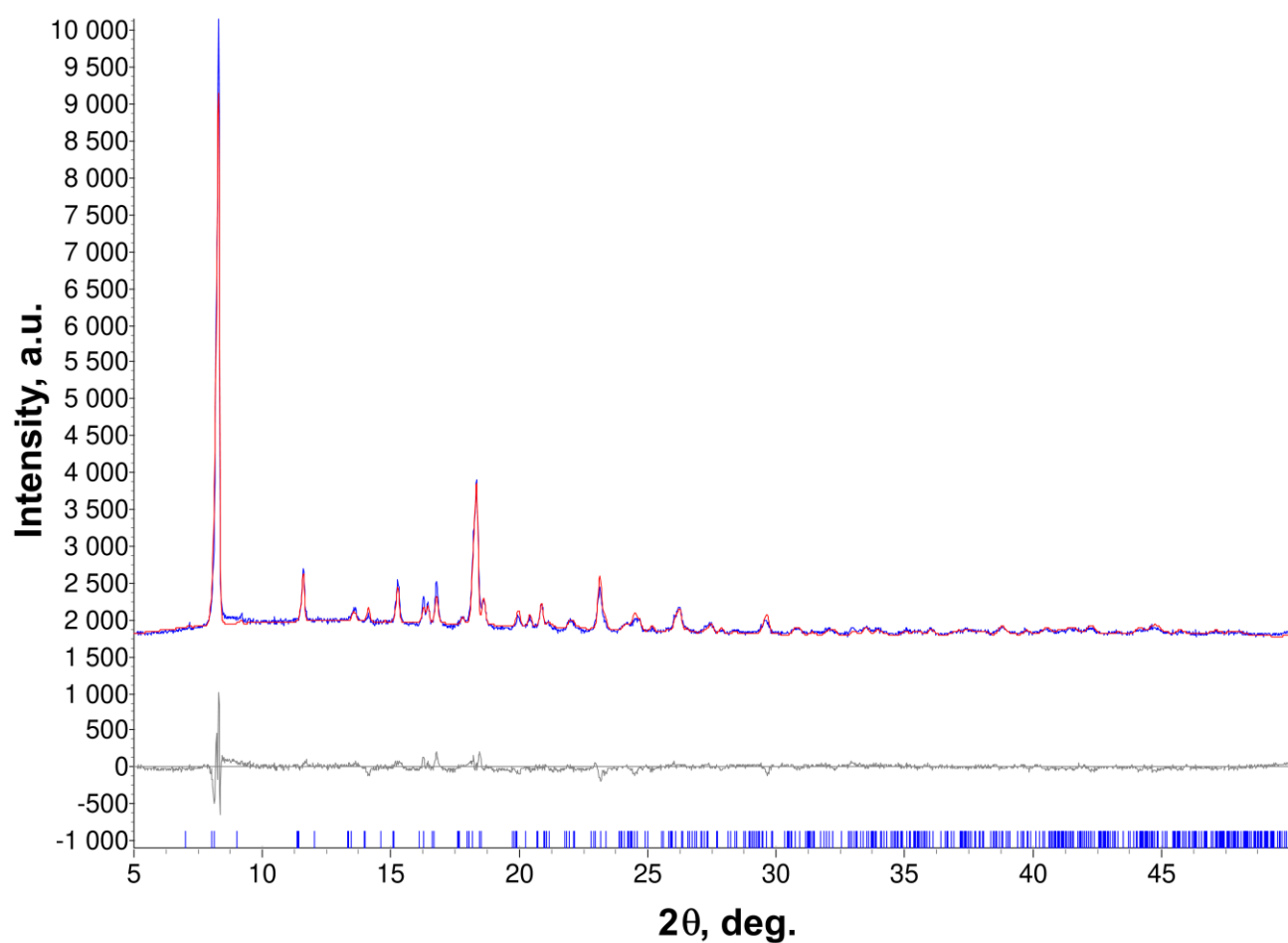


Figure S6. The experimental (blue line) and calculated (red line) powder XRD patterns for ErV_2 and their difference (grey line). The SCXRD data for DyV_2 was used to simulate the theoretical line. Blue ticks indicate calculated positions of the reflections.

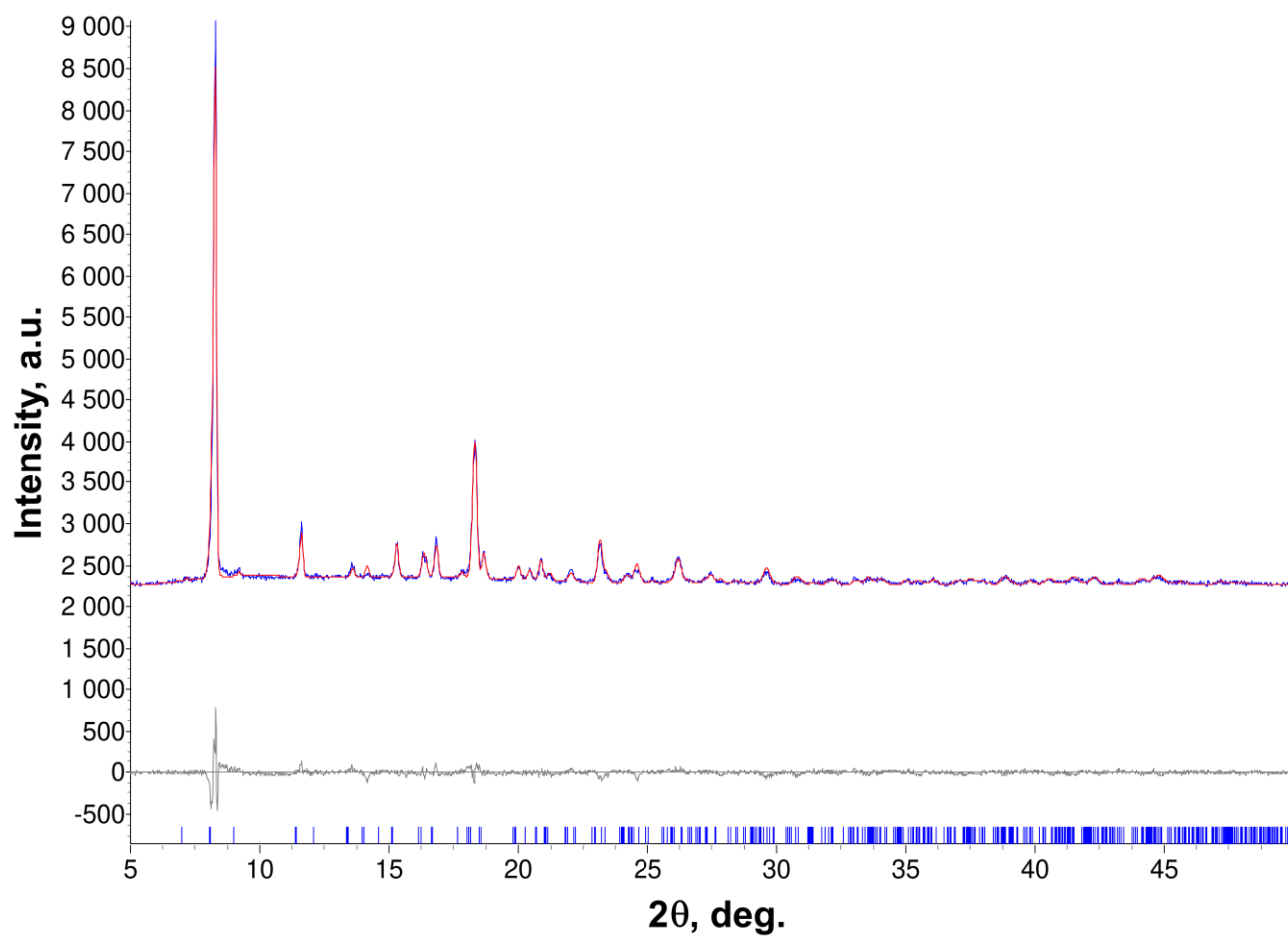


Figure S7. The experimental (blue line) and calculated (red line) powder XRD patterns for YbV_2 and their difference (grey line). The SCXRD data for DyV_2 was used to simulate the theoretical line. Blue ticks indicate calculated positions of the reflections.

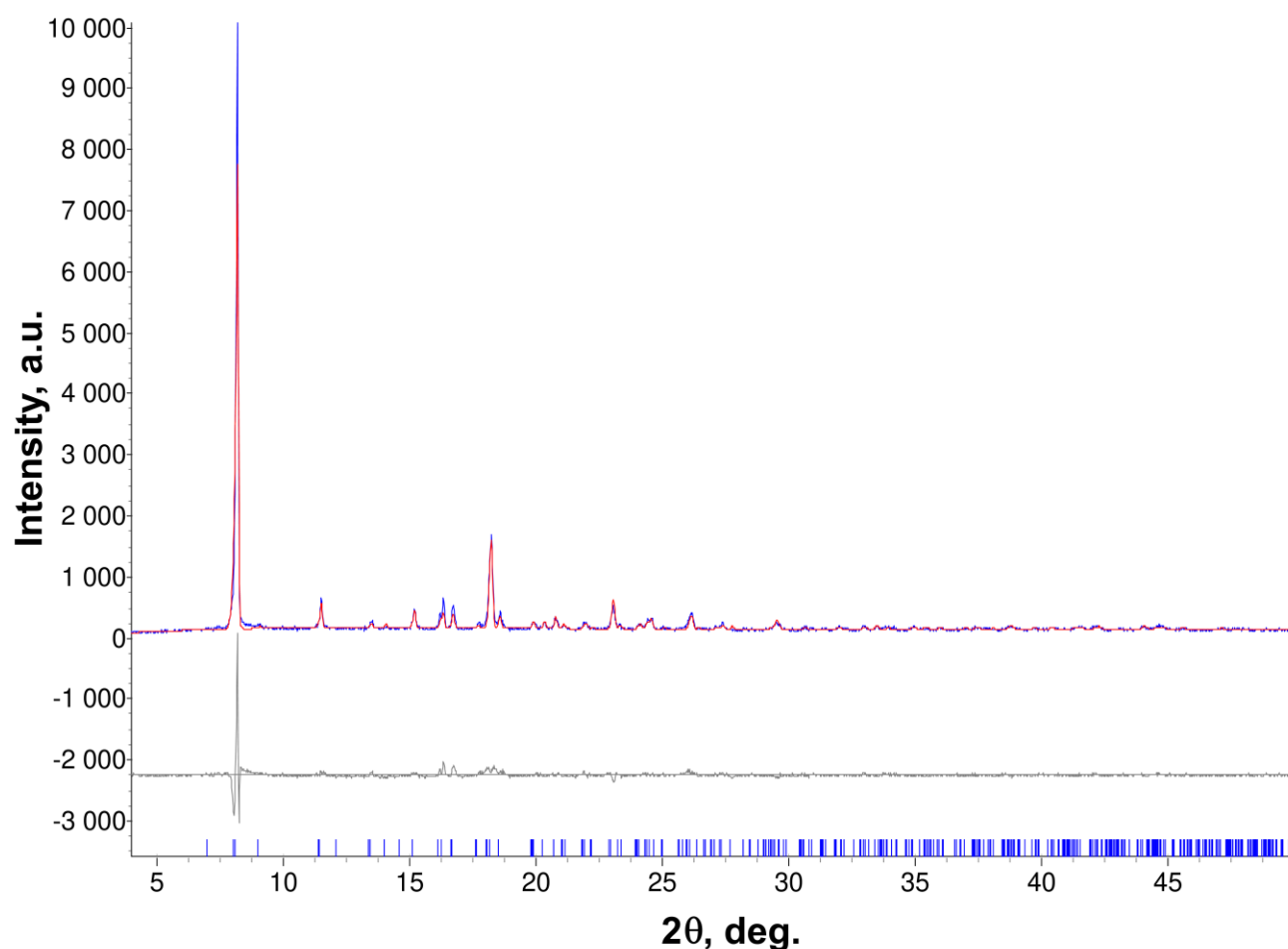


Figure S8. The experimental (blue line) and calculated (red line) powder XRD patterns for **LuV₂** and their difference (grey line). The SCXRD data for **DyV₂** was used to simulate the theoretical line. Blue ticks indicate calculated positions of the reflections.

Table S1. Continuous Shape Measures (CShM) for GdO₈, TbO₈ and DyO₈ coordination polyhedra in compounds **GdV₂**, **TbV₂**, and **DyV₂**. The lowest CShM values are highlighted, indicating the best fits.

Structure ML ₈	SAPR-8	TDD-8	JBTPR-8	BTPR-8	JSD-8
GdV₂	0.297	1.879	2.783	2.203	4.820
TbV₂	0.346	1.876	2.868	2.259	4.934
DyV₂	0.320	1.860	2.837	2.233	4.892

Codes: SAPR-8 (*D*_{4d}) Square antiprism; TDD-8 (*D*_{2d}) Triangular dodecahedron; JBTPR-8 (*C*_{2v}) Biaugmented trigonal prism J50; BTPR-8 (*C*_{2v}) Biaugmented trigonal prism; JSD-8 (*D*_{2d}) Snub disphenoid J84.

Table S2. Selected bond angles (ω , deg.) for **GdV₂**.

Angle	ω	Angle	ω
O11–Gd1–O11 ⁽ⁱ⁾	137.8(2)	O14 ⁽ⁱ⁾ –Gd1–O13	111.01(14)
O11 ⁽ⁱ⁾ –Gd1–O14 ⁽ⁱ⁾	76.50(14)	O14–Gd1–O13	141.41(14)
O11–Gd1–O14 ⁽ⁱ⁾	72.06(14)	O14–Gd1–O13 ⁽ⁱ⁾	111.00(14)
O11 ⁽ⁱ⁾ –Gd1–O14	72.06(14)	O14 ⁽ⁱ⁾ –Gd1–O13 ⁽ⁱ⁾	141.41(14)
O11–Gd1–O14	76.50(14)	O14 ⁽ⁱ⁾ –Gd1–O12 ⁽ⁱ⁾	144.11(14)
O11–Gd1–O13	74.17(14)	O14–Gd1–O12 ⁽ⁱ⁾	70.95(14)
O11 ⁽ⁱ⁾ –Gd1–O13	145.03(14)	O14–Gd1–O12	144.12(14)
O11–Gd1–O13 ⁽ⁱ⁾	145.03(14)	O14 ⁽ⁱ⁾ –Gd1–O12	70.95(14)
O11 ⁽ⁱ⁾ –Gd1–O13 ⁽ⁱ⁾	74.17(14)	O13–Gd1–O13 ⁽ⁱ⁾	81.3(2)
O11 ⁽ⁱ⁾ –Gd1–O12 ⁽ⁱ⁾	115.69(14)	O13–Gd1–O12 ⁽ⁱ⁾	78.98(14)
O11 ⁽ⁱ⁾ –Gd1–O12	78.37(14)	O13–Gd1–O12	72.70(14)
O11–Gd1–O12	115.69(14)	O13 ⁽ⁱ⁾ –Gd1–O12 ⁽ⁱ⁾	72.70(14)
O11–Gd1–O12 ⁽ⁱ⁾	78.37(14)	O13 ⁽ⁱ⁾ –Gd1–O12	78.98(14)
O14–Gd1–O14 ⁽ⁱ⁾	82.6(2)	O12 ⁽ⁱ⁾ –Gd1–O12	142.4(2)

Symmetry code: (i) $x, -y+3/2, -z+1/2$.**Table S3.** Selected bond angles (ω , deg.) for **TbV₂**.

Angle	ω	Angle	ω
O11–Tb1–O11 ⁽ⁱ⁾	137.85(19)	O12–Tb1–O14 ⁽ⁱ⁾	70.74(14)
O11 ⁽ⁱ⁾ –Tb1–O12	78.94(14)	O12 ⁽ⁱ⁾ –Tb1–O14	70.74(14)
O11–Tb1–O12	115.08(16)	O12–Tb1–O14	144.32(13)
O11 ⁽ⁱ⁾ –Tb1–O12 ⁽ⁱ⁾	115.08(16)	O12 ⁽ⁱ⁾ –Tb1–O14 ⁽ⁱ⁾	144.32(13)
O11–Tb1–O12 ⁽ⁱ⁾	78.94(14)	O13 ⁽ⁱ⁾ –Tb1–O12 ⁽ⁱ⁾	72.49(13)
O11–Tb1–O13 ⁽ⁱ⁾	145.26(13)	O13–Tb1–O12	72.49(13)
O11 ⁽ⁱ⁾ –Tb1–O13	145.26(13)	O13–Tb1–O12 ⁽ⁱ⁾	79.18(15)
O11 ⁽ⁱ⁾ –Tb1–O13 ⁽ⁱ⁾	73.91(14)	O13 ⁽ⁱ⁾ –Tb1–O12	79.17(15)
O11–Tb1–O13	73.91(14)	O13 ⁽ⁱ⁾ –Tb1–O13	81.6(2)
O11–Tb1–O14 ⁽ⁱ⁾	71.61(14)	O13–Tb1–O14	141.52(13)
O11–Tb1–O14	77.17(14)	O13–Tb1–O14 ⁽ⁱ⁾	110.44(14)
O11 ⁽ⁱ⁾ –Tb1–O14	71.61(14)	O13 ⁽ⁱ⁾ –Tb1–O14	110.44(14)
O11 ⁽ⁱ⁾ –Tb1–O14 ⁽ⁱ⁾	77.17(14)	O13 ⁽ⁱ⁾ –Tb1–O14 ⁽ⁱ⁾	141.52(13)
O12–Tb1–O12 ⁽ⁱ⁾	142.35(19)	O14 ⁽ⁱ⁾ –Tb1–O14	83.25(19)

Symmetry code: (i) $x, -y+3/2, -z+1/2$.

Table S4. Selected bond angles (ω , deg.) for **DyV₂**.

Angle	ω	Angle	ω
O12–Dy1–O12 ⁽ⁱ⁾	137.8(2)	O13–Dy1–O14	70.85(16)
O12–Dy1–O13 ⁽ⁱ⁾	76.68(17)	O13 ⁽ⁱ⁾ –Dy1–O14	144.65(16)
O12 ⁽ⁱ⁾ –Dy1–O13 ⁽ⁱ⁾	72.05(16)	O13–Dy1–O14 ⁽ⁱ⁾	144.65(16)
O12 ⁽ⁱ⁾ –Dy1–O13	76.68(17)	O13 ⁽ⁱ⁾ –Dy1–O14 ⁽ⁱ⁾	70.85(16)
O12–Dy1–O13	72.05(16)	O14–Dy1–O14 ⁽ⁱ⁾	141.9(2)
O12 ⁽ⁱ⁾ –Dy1–O14	78.76(16)	O11–Dy1–O13	141.28(15)
O12–Dy1–O14 ⁽ⁱ⁾	78.76(16)	O11 ⁽ⁱ⁾ –Dy1–O13	110.82(16)
O12 ⁽ⁱ⁾ –Dy1–O14 ⁽ⁱ⁾	115.45(17)	O11–Dy1–O13 ⁽ⁱ⁾	110.83(16)
O12–Dy1–O14	115.45(17)	O11 ⁽ⁱ⁾ –Dy1–O13 ⁽ⁱ⁾	141.28(15)
O12 ⁽ⁱ⁾ –Dy1–O11 ⁽ⁱ⁾	145.07(16)	O11–Dy1–O14	78.88(17)
O12–Dy1–O11	145.07(16)	O11–Dy1–O14 ⁽ⁱ⁾	72.41(16)
O12–Dy1–O11 ⁽ⁱ⁾	74.16(16)	O11 ⁽ⁱ⁾ –Dy1–O14	72.41(16)
O12 ⁽ⁱ⁾ –Dy1–O11	74.17(16)	O11 ⁽ⁱ⁾ –Dy1–O14 ⁽ⁱ⁾	78.88(17)
O13–Dy1–O13 ⁽ⁱ⁾	83.2(2)	O11–Dy1–O11 ⁽ⁱ⁾	81.2(2)

Symmetry code: (i) $x, -y+1/2, -z+3/2$.**Table S5.** Hydrogen bonding parameters of structure **GdV₂**.

Fragment D–H $\cdots$ A	Distance/ Å			D–H $\cdots$ A /°
	D–H	H $\cdots$ A	D $\cdots$ A	
O11–H $\cdots$ O6 ⁽ⁱ⁾	0.85	1.83	2.684(7)	180
O11–H $a\cdots$ O3	0.85	2.03	2.821(7)	156
O1–H1 $a\cdots$ O1S ⁽ⁱⁱ⁾	0.98	1.62	2.602(12)	174
O1–H1 $b\cdots$ O4A ⁽ⁱⁱ⁾	0.98	2.28	2.98(2)	127
O14–H $b\cdots$ O4A ⁽ⁱⁱ⁾	0.85	1.90	2.69(3)	155
O14–H $c\cdots$ O7	0.85	1.97	2.726(6)	147
O13–H $d\cdots$ O10 ⁽ⁱⁱⁱ⁾	0.85	1.89	2.739(7)	180
O13–H $e\cdots$ O5 ⁽ⁱ⁾	0.85	2.02	2.768(7)	147
O12–H $f\cdots$ O9 ⁽ⁱⁱⁱ⁾	0.85	1.87	2.720(7)	179
O12–H $g\cdots$ O8 ⁽ⁱⁱ⁾	0.85	1.99	2.785(7)	155

Symmetry codes: ⁱ $-1/2+x, y, 1-z$; ⁱⁱ $x, 3/2-y, 1/2-z$; ⁱⁱⁱ $-1/2+x, 3/2-y, -1/2+z$.

Table S6. Hydrogen bonding parameters of structure **TbV₂**.

Fragment D–H⋯A	Distance/ Å			D–H⋯A /°
	D–H	H⋯A	D⋯A	
O1–H1 <i>a</i> ⋯O1S ⁽ⁱ⁾	0.85	1.79	2.581(14)	154
O1–H1 <i>b</i> ⋯O4A ⁽ⁱⁱ⁾	0.85	2.12	2.920(10)	156
O11–H11 <i>e</i> ⋯O6 ⁽ⁱⁱⁱ⁾	0.85	1.84	2.686(6)	176
O11–H11 <i>f</i> ⋯O3	0.85	2.02	2.812(6)	155
O12–H12 <i>e</i> ⋯O9 ^(iv)	0.85	1.88	2.716(6)	168
O12–H12 <i>f</i> ⋯O8A ⁽ⁱⁱ⁾	0.85	1.97	2.808(8)	170
O13–H13 <i>e</i> ⋯O8 ^(iv)	0.85	1.89	2.742(6)	178
O13–H13 <i>f</i> ⋯O5 ⁽ⁱⁱⁱ⁾	0.85	1.94	2.765(4)	164
O14–H14 <i>g</i> ⋯O4A ⁽ⁱⁱ⁾	0.86	1.96	2.685(10)	141
O14–H14 <i>h</i> ⋯O7	0.86	1.89	2.731(6)	165

Symmetry codes: ⁱ 1/2+x, y, 1–z; ⁱⁱ x, 3/2–y, 1/2–z; ⁱⁱⁱ –1/2+x, y, 1–z; ^{iv} –1/2+x, 3/2–y, –1/2+z.

Table S7. Hydrogen bonding parameters of structure **DyV₂**.

Fragment D–H⋯A	Distance/ Å			D–H⋯A /°
	D–H	H⋯A	D⋯A	
O1–H1 <i>a</i> ⋯O1S ⁽ⁱ⁾	0.86	1.80	2.593(16)	154
O1–H1 <i>b</i> ⋯O6A ⁽ⁱⁱ⁾	0.86	2.13	2.96(3)	162
O11–H11 <i>e</i> ⋯O8 ⁽ⁱⁱⁱ⁾	0.85	1.89	2.738(8)	180
O11–H11 <i>f</i> ⋯O3 ^(iv)	0.85	2.02	2.768(7)	147
O12–H12 <i>e</i> ⋯O4 ⁽ⁱⁱⁱ⁾	0.85	1.83	2.679(8)	180
O12–H12 <i>f</i> ⋯O5	0.85	2.03	2.824(7)	156
O13–H13 <i>e</i> ⋯O6A	0.85	2.02	2.71(3)	137
O13–H13 <i>f</i> ⋯O5 ⁽ⁱⁱ⁾	0.85	2.54	3.346(7)	158
O14–H14 <i>g</i> ⋯O7 ^(iv)	0.85	1.86	2.713(7)	180
O14–H14 <i>h</i> ⋯O10 ⁽ⁱⁱ⁾	0.85	1.99	2.782(8)	155

Symmetry codes: ⁱ 1/2+x, 1/2–y, –1/2+z; ⁱⁱ x, 1/2–y, 3/2–z; ⁱⁱⁱ –1/2+x, y, 1–z; ^{iv} –1/2+x, 1/2–y, 1/2+z.

Magnetic properties

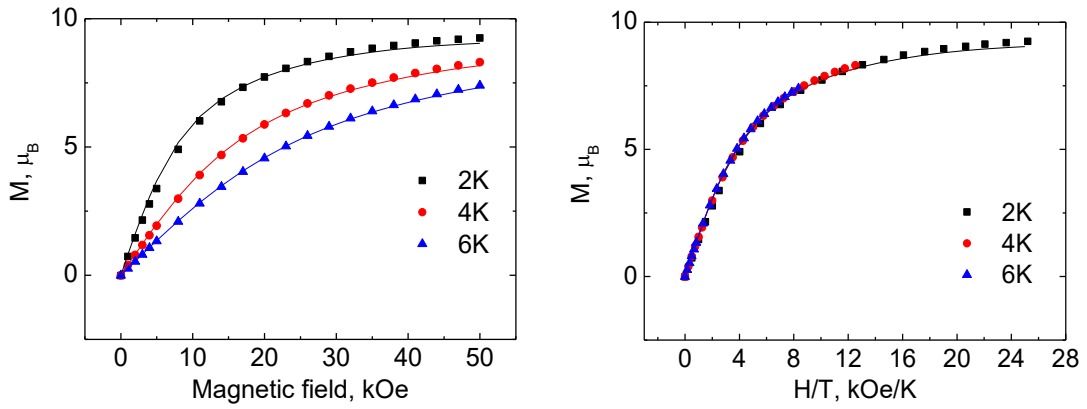


Figure S9. Dependencies of the magnetization [μ_B] vs dc -magnetic field H (left) and H/T (right) for GdV_2 at 2, 4 and 6 K. Calculated values are represented by black lines.

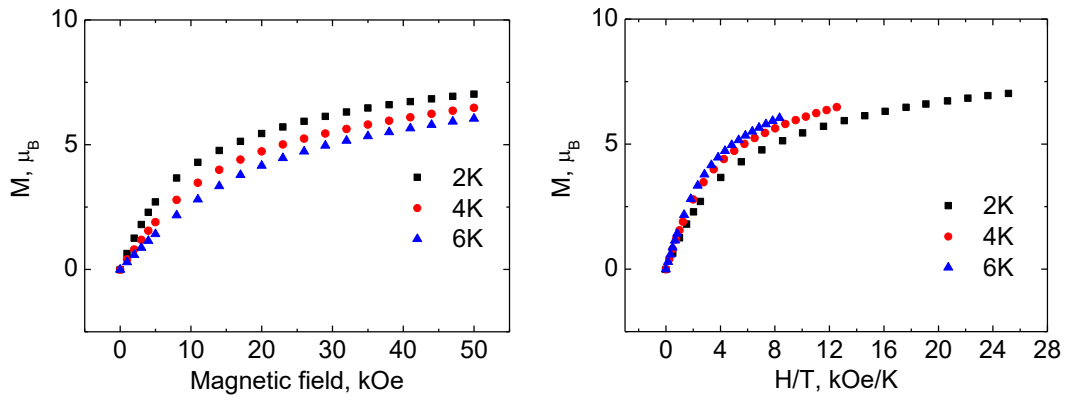


Figure S10. Dependencies of the magnetization [μ_B] vs dc -magnetic field H (left) and H/T (right) for TbV_2 at 2, 4 and 6 K.

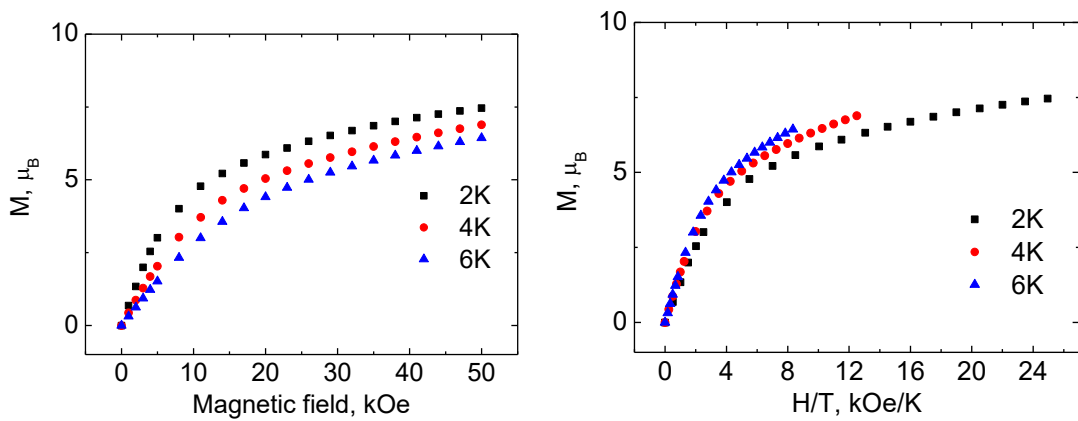


Figure S11. Dependencies of the magnetization [μ_B] vs dc -magnetic field H (left) and H/T (right) for DyV_2 at 2, 4 and 6 K.

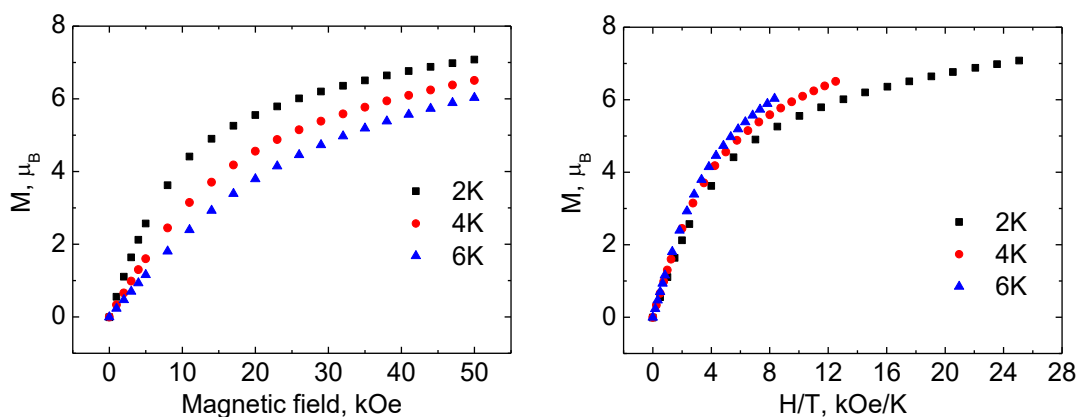


Figure S12. Dependencies of the magnetization [μ_B] vs dc -magnetic field H (left) and H/T (right) for ErV_2 at 2, 4 and 6 K.

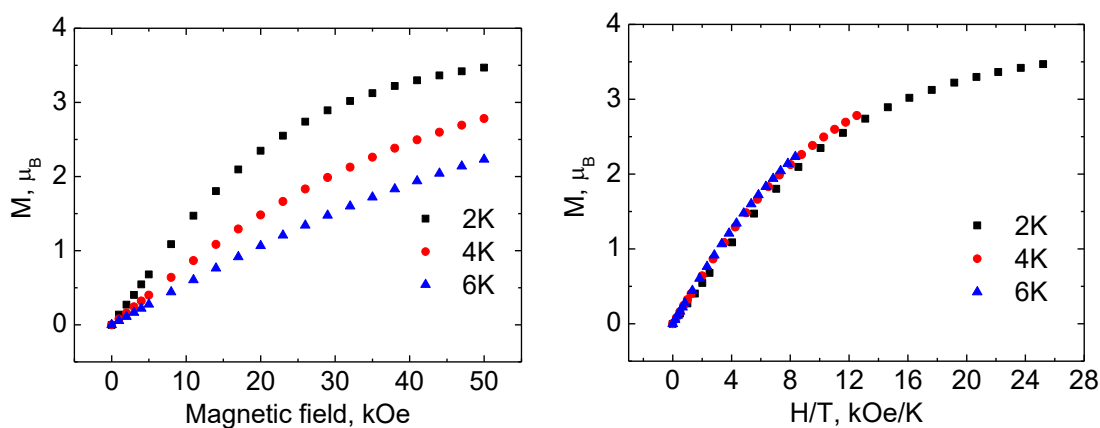


Figure S13. Dependencies of the magnetization [μ_B] vs dc -magnetic field H (left) and H/T (right) for YbV_2 at 2, 4 and 6 K.

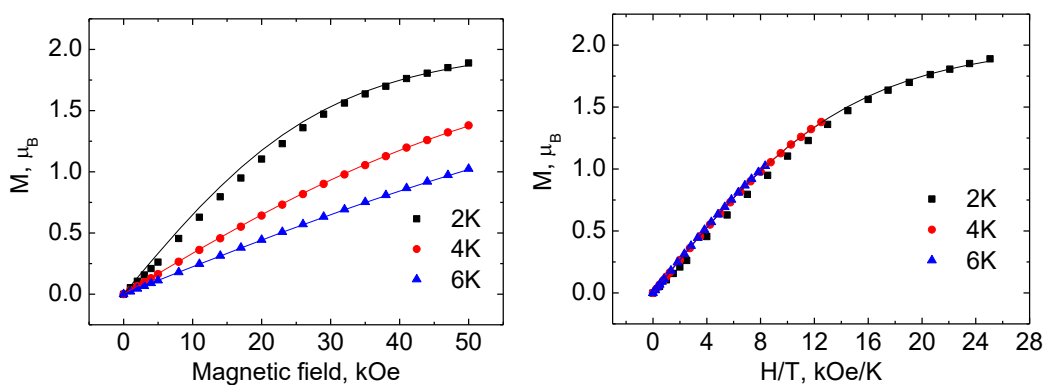


Figure S14. Dependencies of the magnetization [μ_B] vs dc -magnetic field H (left) and H/T (right) for LuV_2 at 2, 4 and 6 K. Calculated values are represented by black lines.

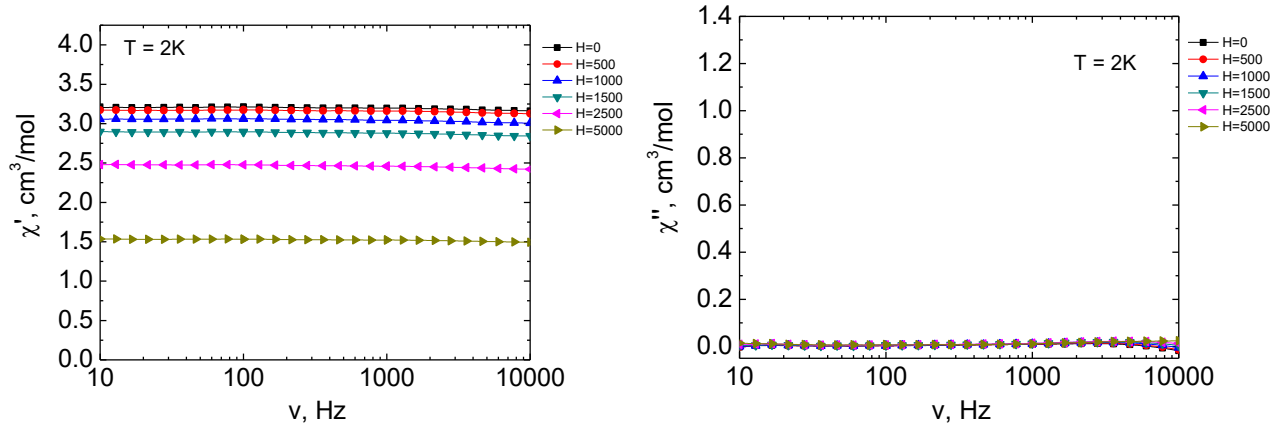


Figure S15. Frequency dependencies of the in-phase (χ' , left) and out-of-phase (χ'' , right) components of the ac susceptibility for **TbV₂** up to a 5000 Oe dc magnetic field at 2 K.

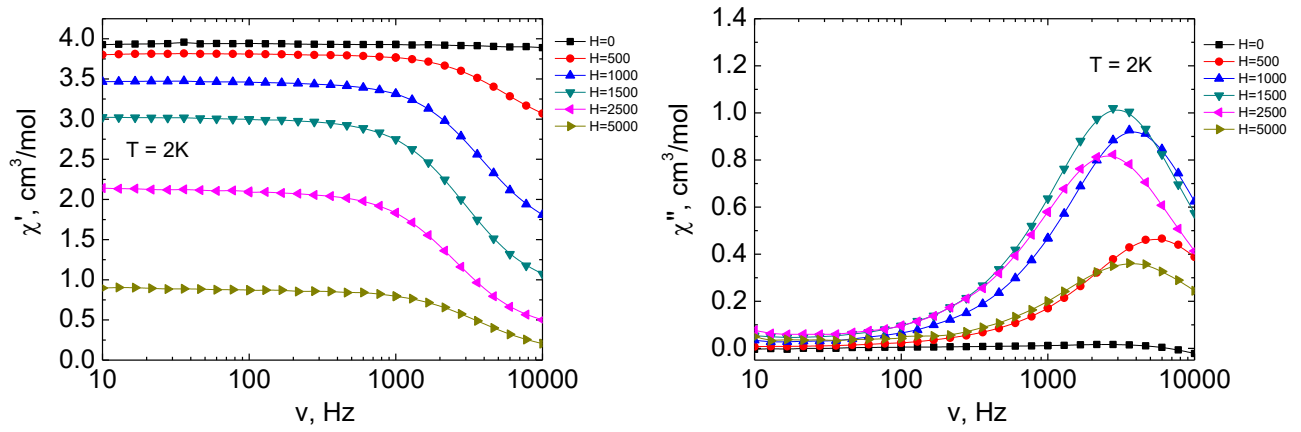


Figure S16. Frequency dependencies of the in-phase (χ' , left) and out-of-phase (χ'' , right) components of the ac susceptibility for **GdV₂** up to a 5000 Oe dc magnetic field at 2 K.

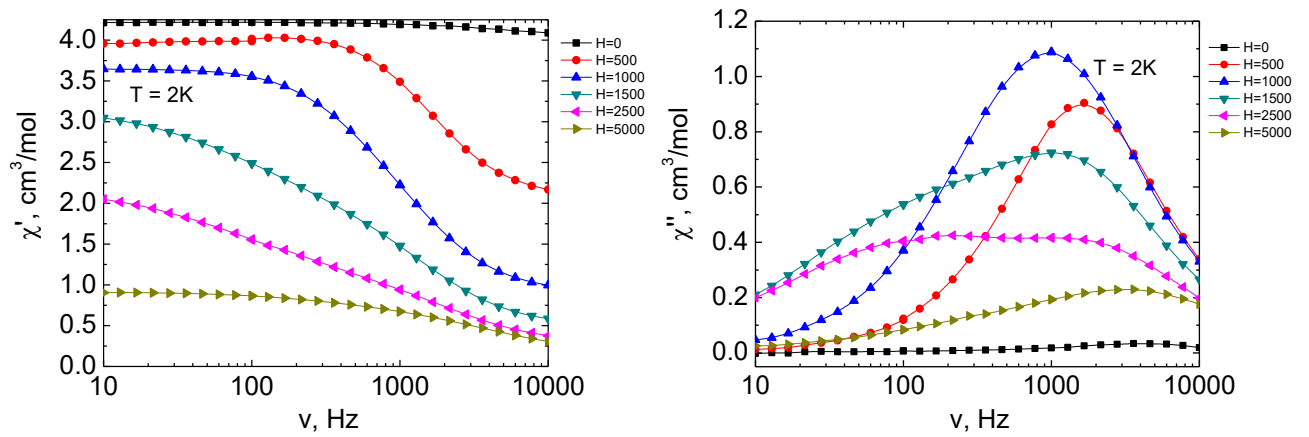


Figure S17. Frequency dependencies of the in-phase (χ' , left) and out-of-phase (χ'' , right) components of the ac susceptibility for **DyV₂** up to a 5000 Oe dc magnetic field at 2 K.

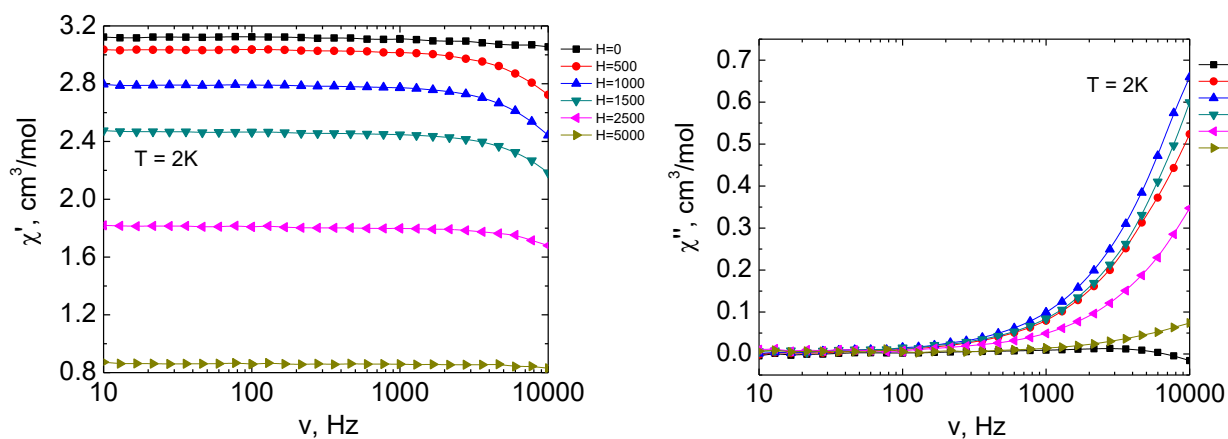


Figure S18. Frequency dependencies of the in-phase (χ' , left) and out-of-phase (χ'' , right) components of the ac susceptibility for ErV_2 up to a 5000 Oe dc magnetic field at 2 K.

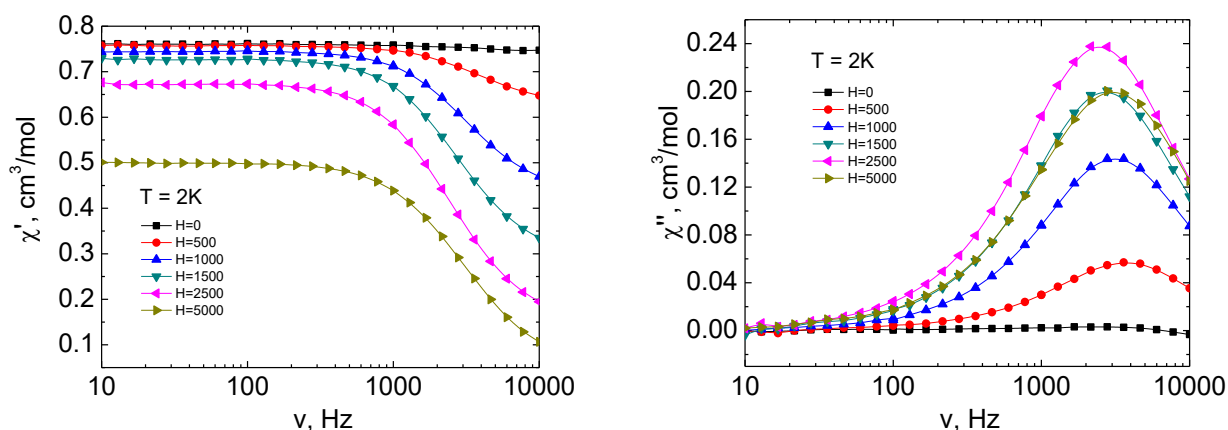


Figure S19. Frequency dependencies of the in-phase (χ' , left) and out-of-phase (χ'' , right) components of the ac susceptibility for YbV_2 up to a 5000 Oe dc magnetic field at 2 K.

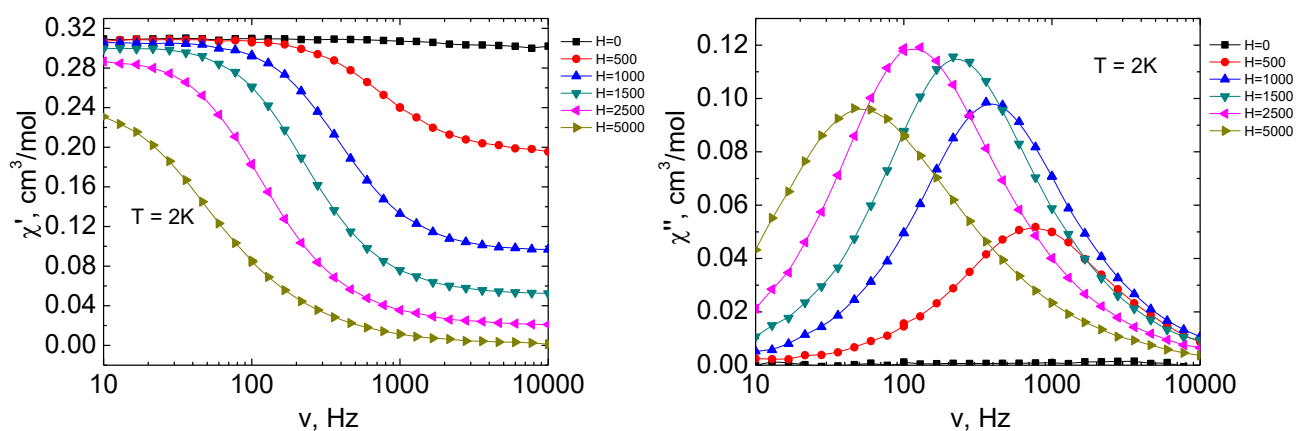


Figure S20. Frequency dependencies of the in-phase (χ' , left) and out-of-phase (χ'' , right) components of the ac susceptibility for LuV_2 up to a 5000 Oe dc magnetic field at 2 K.

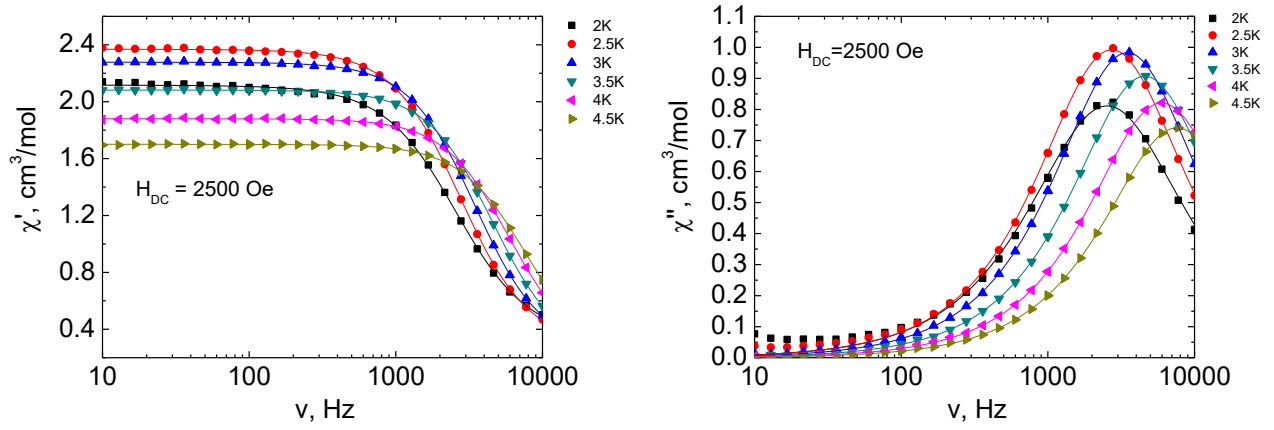


Figure S21. Frequency dependences of the in-phase (χ' , left) and out-of-phase (χ'' , right) components of ac magnetic susceptibility for **GdV₂** in the temperature range of 2-4.5 K under a 2500 Oe dc magnetic field. Solid lines represent fitting by the generalized Debye model.

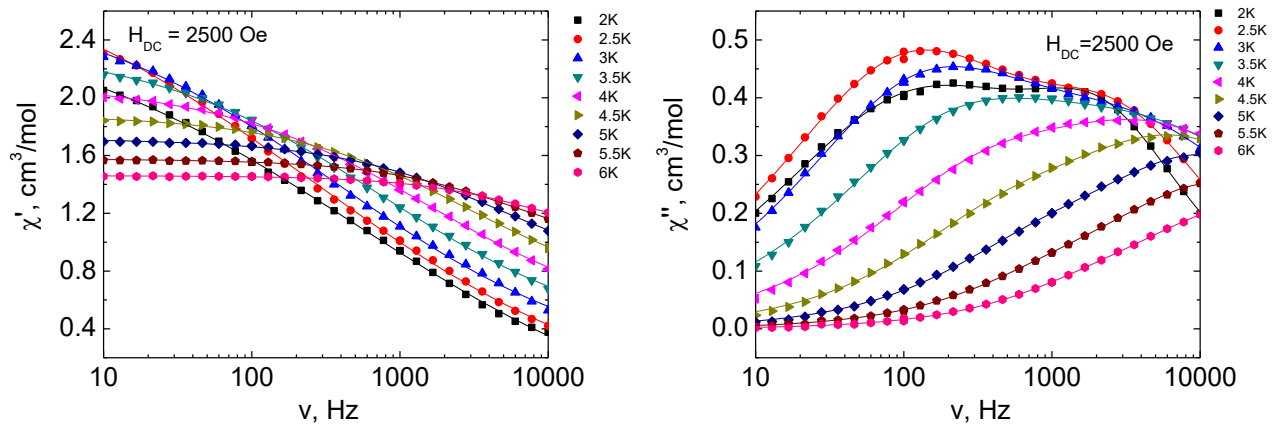


Figure S22. Frequency dependences of the in-phase (χ' , left) and out-of-phase (χ'' , right) components of ac magnetic susceptibility for **DyV₂** in the temperature range of 2-6 K under a 2500 Oe dc magnetic field. Solid lines represent fitting by the generalized Debye model.

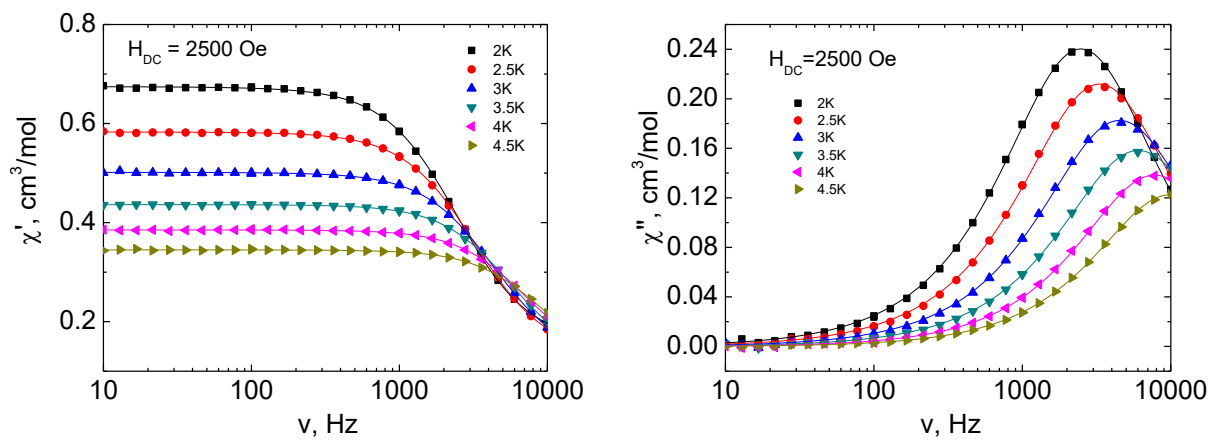


Figure S23. Frequency dependences of the in-phase (χ' , left) and out-of-phase (χ'' , right) components of ac magnetic susceptibility for **YbV₂** in the temperature range of 2-4.5 K under a 2500 Oe dc magnetic field. Solid lines represent fitting by the generalized Debye model.

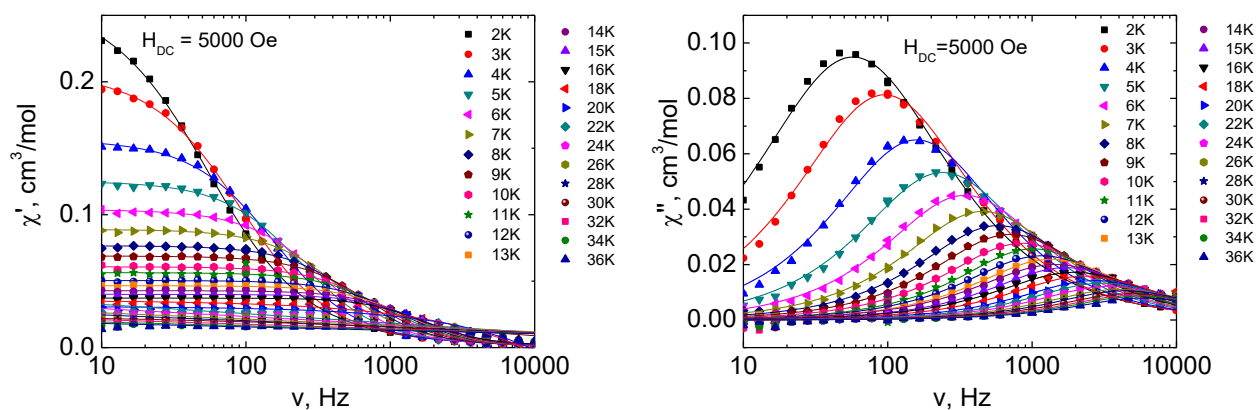


Figure S24. Frequency dependences of the in-phase (χ' , left) and out-of-phase (χ'') components of ac magnetic susceptibility for **LuV₂** in the temperature range of 2-36 K under a 5000 Oe dc magnetic field. Solid lines represent fitting by the generalized Debye model.

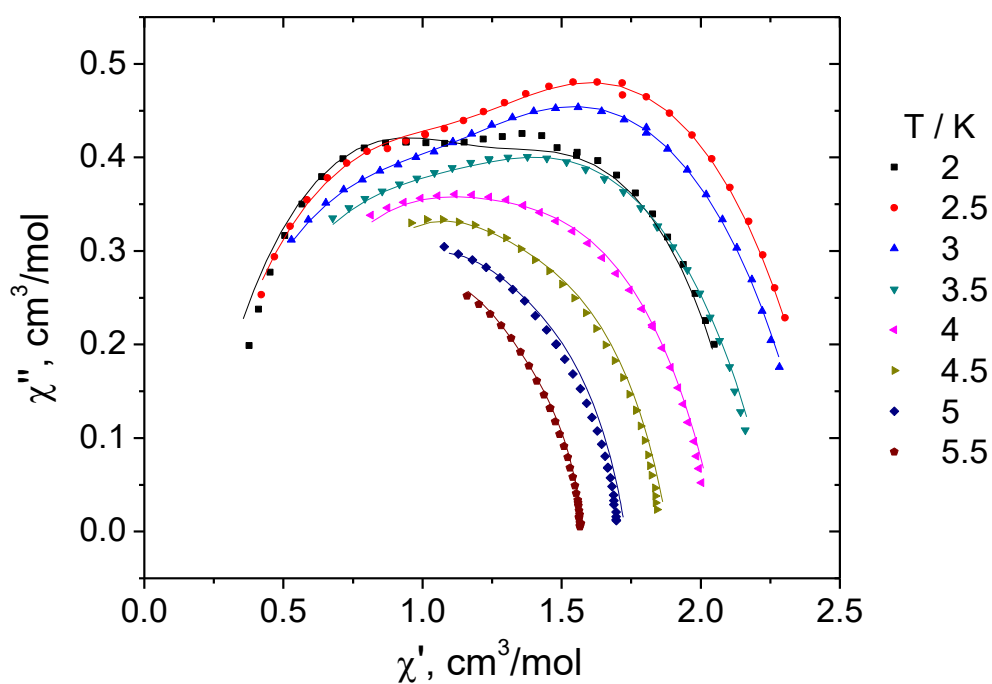


Figure S25. Cole-Cole plots for **DyV₂**. Solid lines were fitted by generalized Debye model for two modes of relaxation.

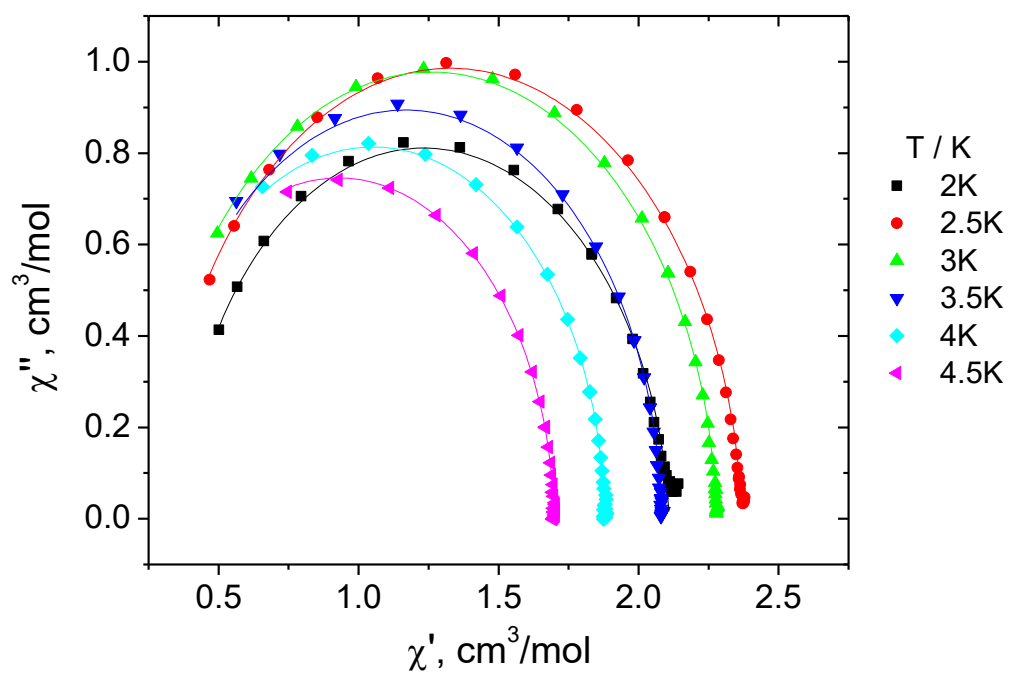


Figure S26. Cole-Cole plots for GdV_2 . Solid lines were fitted by generalized Debye model.

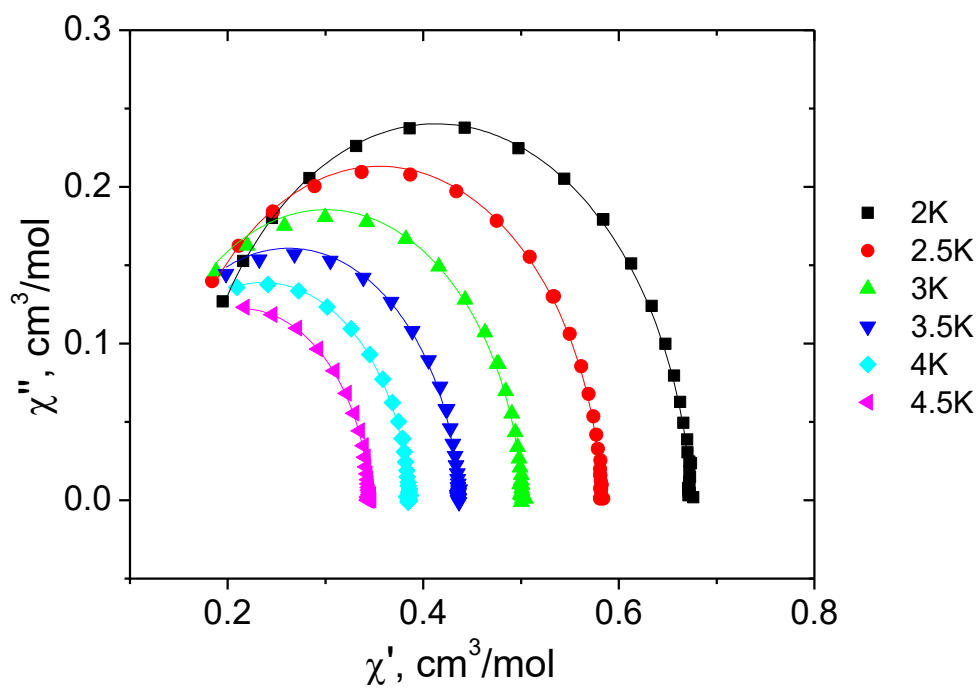


Figure S27. Cole-Cole plots for YbV_2 . Solid lines were fitted by generalized Debye model.

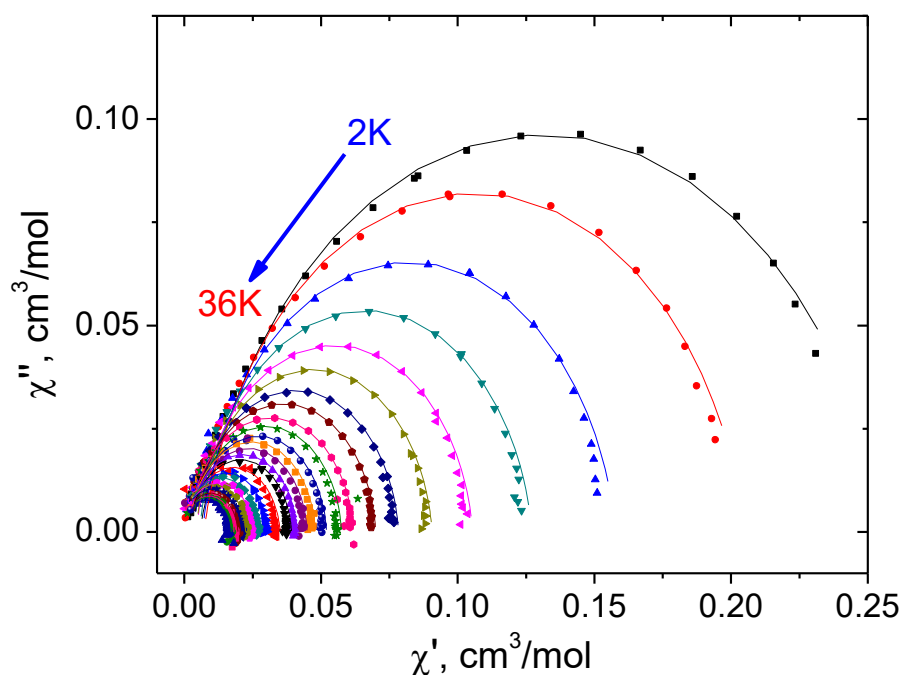
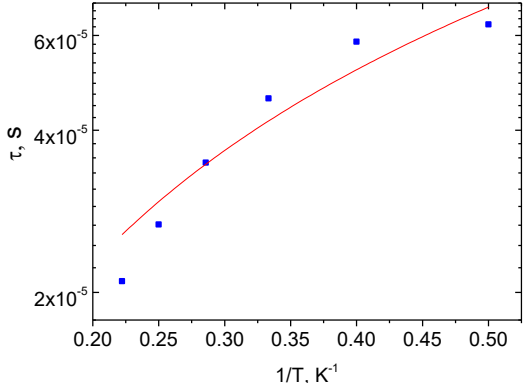
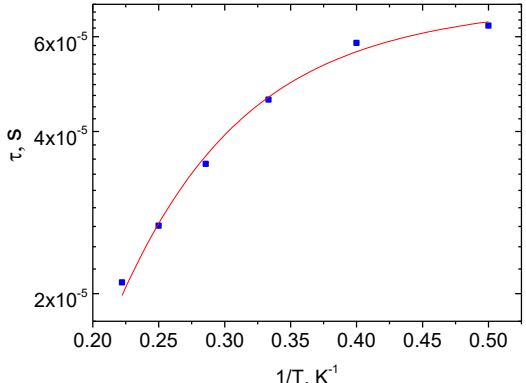
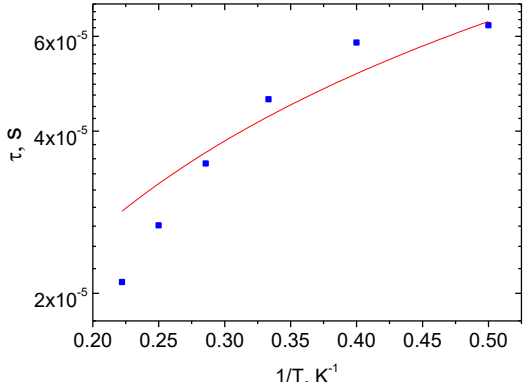
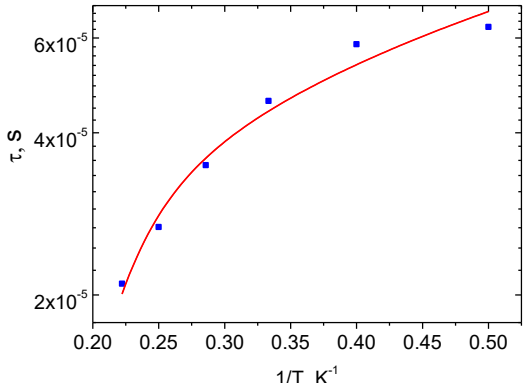
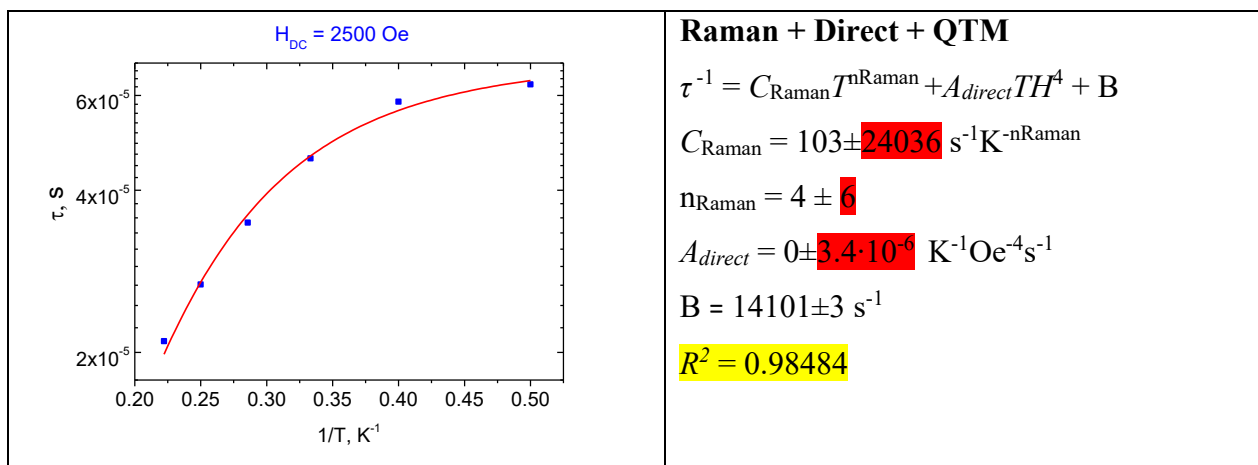


Figure S28. Cole-Cole plots for **LuV₂**. Solid lines were fitted by generalized Debye.

Table S8. Fitting of the τ vs. T dependences for **GdV₂** under an optimal dc field ($H_{DC} = 2500$ Oe, $T = 4.5$ K). Meaningless parameters are specified in **red color** while **yellow color** emphasizes insufficient R^2 values. Reliable fits are specified in **green color**.

Fitting	Fit function, temperature range, best-fit parameters with uncertainties.
	Direct $\tau^{-1} = A_{direct} T H^4$ $A_{direct} = 2.0 \cdot 10^{-10} \pm 1 \cdot 10^{-11} \text{ K}^{-1} \text{Oe}^{-4} \text{s}^{-1}$ $R^2 = 0.89654$

$H_{DC} = 2500 \text{ Oe}$ 	Raman $\tau^{-1} = C_{\text{Raman}} T^{n_{\text{Raman}}}$ $C_{\text{Raman}} = 6435 \pm 1199 \text{ s}^{-1} \text{K}^{-n_{\text{Raman}}}$ $n_{\text{Raman}} = 1.2 \pm 0.2$ $R^2 = 0.90196$
$H_{DC} = 2500 \text{ Oe}$ 	Raman + QTM $\tau^{-1} = C_{\text{Raman}} T^{n_{\text{Raman}}} + B$ $C_{\text{Raman}} = 104 \pm 76 \text{ s}^{-1} \text{K}^{-n_{\text{Raman}}}$ $n_{\text{Raman}} = 3.9 \pm 0.5$ $B = 14099 \pm 859 \text{ s}^{-1}$ $R^2 = 0.99394$
$H_{DC} = 2500 \text{ Oe}$ 	Direct + QTM $\tau^{-1} = A_{\text{direct}} T H^4 + B$ $B = 0 \pm 4505 \text{ s}^{-1}$ $A_{\text{direct}} = 2.0 \cdot 10^{-10} \pm 5 \cdot 10^{-11} \text{ K}^{-1} \text{Oe}^{-4} \text{s}^{-1}$ $R^2 = 0.87069$
$H_{DC} = 2500 \text{ Oe}$ 	Raman + Direct $\tau^{-1} = C_{\text{Raman}} T^{n_{\text{Raman}}} + A_{\text{direct}} T H^4$ $C_{\text{Raman}} = 0.0374 \pm 0.3866 \text{ s}^{-1} \text{K}^{-n_{\text{Raman}}}$ $n_{\text{Raman}} = 9 \pm 7$ $A_{\text{direct}} = 1.9 \cdot 10^{-10} \pm 1 \cdot 10^{-11} \text{ K}^{-1} \text{Oe}^{-4} \text{s}^{-1}$ $R^2 = 0.94244$



Quantum chemical calculations

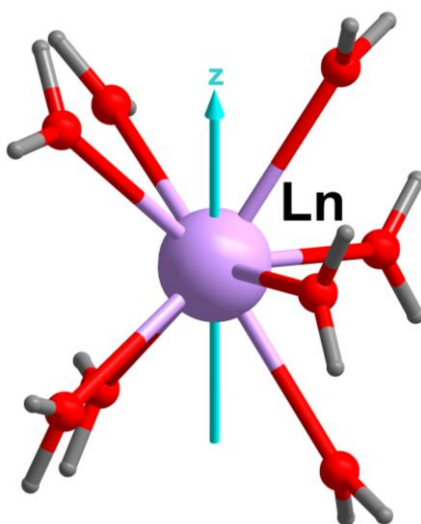


Fig. S29. CASSCF computed main magnetic g_{zz} -axis of the $[\text{Ln}(\text{H}_2\text{O})_8]^{3+}$ unit.

Table S9. Calculated energy (cm^{-1}) and wavefunction decomposition of Ising pseudo-doublets analysis for Tb^{3+} ion in **TbV2** (values above 10% are given, the major dominating values are kept in bold).

Energy	Wavefunction decomposition
0.000	99.2% $ \pm 6\rangle$
0.003	99.2% $ \pm 6\rangle$
140.265	24.8% $ \pm 2\rangle$ + 24.4% $ \pm 3\rangle$ + 20.2% $ \pm 5\rangle$ + 16.0% $ \pm 1\rangle$ + 13.2% $ \pm 4\rangle$
140.641	27.8% $ \pm 2\rangle$ + 25.0% $ \pm 3\rangle$ + 21.2% $ \pm 5\rangle$ + 13.4% $ \pm 4\rangle$ + 10.4% $ \pm 1\rangle$
165.817	30.4% $ \pm 5\rangle$ + 29.4% $ \pm 1\rangle$ + 24.9% $ 0\rangle$
168.916	38.8% $ \pm 5\rangle$ + 34.0% $ \pm 1\rangle$ + 15.6% $ \pm 2\rangle$

182.405	45.9% 0⟩+26.6% ±5⟩+14.0% ±2⟩
190.398	30.0% ±1⟩+27.4% ±5⟩+22.8% ±3⟩
202.445	19.8% ±3⟩+14.8% 0⟩+12.4% ±5⟩+10.8% ±4⟩
228.104	34.0% ±4⟩+33.2% ±2⟩+14.6% ±1⟩
231.669	39.8% ±2⟩+30.2% ±4⟩+16.8% ±1⟩
307.092	40.8% ±3⟩+37.6% ±4⟩+13.6% ±2⟩
307.355	41.2% ±3⟩+36.3% ±4⟩+14.6% ±2⟩

Table S10. Calculated energy (cm⁻¹) and g-tensors for each Kramers doublets for Ln³⁺ ions in compounds **LnV₂**.

$ \pm M_J\rangle$ states	Energy	g_{xx}	g_{yy}	g_{zz}
Dy³⁺				
KD ⁰	0	0.007	0.014	19.435
KD ¹	105.750	0.061	0.067	15.456
KD ²	148.741	2.311	2.717	11.722
KD ³	195.362	7.078	6.248	2.415
KD ⁴	245.444	2.431	3.522	9.573
KD ⁵	286.940	1.200	2.359	13.685
KD ⁶	326.751	0.550	0.787	18.207
KD ⁷	364.813	0.289	0.436	19.245
Er³⁺				
KD ⁰	0	0.742	2.677	14.920
KD ¹	45.371	8.633	5.993	2.363
KD ²	80.548	1.864	2.272	8.841
KD ³	113.082	0.288	0.525	16.203
KD ⁴	156.289	2.739	2.510	0.427
KD ⁵	164.351	6.639	3.914	0.775
KD ⁶	203.100	0.080	0.836	9.742
KD ⁷	255.670	0.015	0.148	15.846
Yb³⁺				
KD ⁰	0	0.144	0.455	7.618
KD ¹	109.280	1.283	1.974	6.213
KD ²	220.175	1.693	2.507	4.777
KD ³	282.596	0.233	0.296	7.909

Table S11. Calculated energy (cm^{-1}) and wavefunction decomposition analysis of doublets for Dy^{3+} , Er^{3+} , and Yb^{3+} ions in compounds LnV_2 (values above 10% are given, the major dominating values are kept in bold).

$ \pm M_J\rangle$ states	Energy	Wavefunction decomposition
Dy^{3+}		
1	0	93.8% $ \pm 15/2\rangle$
2	105.750	74.0% $ \pm 13/2\rangle$ +10.8% $ \pm 7/2\rangle$
3	148.741	41.5% $ \pm 11/2\rangle$ +18.5% $ \pm 5/2\rangle$ +16.0% $ \pm 3/2\rangle$ +10.5% $ \pm 9/2\rangle$
4	195.362	34.6% $ \pm 9/2\rangle$ +25.0% $ \pm 11/2\rangle$ +17.1% $ \pm 1/2\rangle$ +15.2% $ \pm 3/2\rangle$
5	245.444	30.7% $ \pm 7/2\rangle$ + 30.1% $ \pm 9/2\rangle$ + 21.7% $ \pm 1/2\rangle$ + 13.3% $ \pm 5/2\rangle$
6	286.940	31.7% $ \pm 7/2\rangle$ + 30.5% $ \pm 5/2\rangle$ + 26.9% $ \pm 3/2\rangle$
7	326.751	26.9% $ \pm 11/2\rangle$ + 19.1% $ \pm 9/2\rangle$ + 18.4% $ \pm 5/2\rangle$ + 17.3% $ \pm 13/2\rangle$
8	364.813	45.4% $ \pm 1/2\rangle$ + 33.4% $ \pm 3/2\rangle$ + 12.6% $ \pm 5/2\rangle$
Er^{3+}		
1	0	66.2% $ \pm 15/2\rangle$ + 18.1% $ \pm 11/2\rangle$
2	45.371	32.4% $ \pm 13/2\rangle$ + 28.4% $ \pm 5/2\rangle$ + 13.3% $ \pm 1/2\rangle$ + 10.0% $ \pm 3/2\rangle$
3	80.548	24.8% $ \pm 3/2\rangle$ + 23.4% $ \pm 13/2\rangle$ + 14.4% $ \pm 9/2\rangle$ + 10.7% $ \pm 5/2\rangle$
4	113.082	37.0% $ \pm 1/2\rangle$ + 16.6% $ \pm 9/2\rangle$ + 16.5% $ \pm 3/2\rangle$ + 11.9% $ \pm 5/2\rangle$ + 11.2% $ \pm 7/2\rangle$
5	156.289	23.2% $ \pm 1/2\rangle$ + 22.7% $ \pm 9/2\rangle$ + 15.4% $ \pm 11/2\rangle$ + 10.7% $ \pm 15/2\rangle$ + 10.6% $ \pm 13/2\rangle$
6	164.351	48.3% $ \pm 7/2\rangle$ + 16.3% $ \pm 11/2\rangle$ + 13.7% $ \pm 3/2\rangle$
7	203.100	30.2% $ \pm 11/2\rangle$ + 20.8% $ \pm 13/2\rangle$ + 18.8% $ \pm 5/2\rangle$ + 12.4% $ \pm 9/2\rangle$
8	255.670	19.4% $ \pm 5/2\rangle$ + 19.2% $ \pm 3/2\rangle$ + 15.1% $ \pm 1/2\rangle$ + 12.0% $ \pm 7/2\rangle$ + 11.0% $ \pm 9/2\rangle$
Yb^{3+}		
1	0	49.2% $ \pm 7/2\rangle$ + 27.1% $ \pm 3/2\rangle$ + 22.4% $ \pm 5/2\rangle$
2	109.280	44.4% $ \pm 5/2\rangle$ + 37.8% $ \pm 1/2\rangle$ + 13.6% $ \pm 3/2\rangle$
3	220.175	38.2% $ \pm 3/2\rangle$ + 23.0% $ \pm 7/2\rangle$ + 22.9% $ \pm 1/2\rangle$ + 15.9% $ \pm 5/2\rangle$
4	282.596	37.9% $ \pm 1/2\rangle$ + 23.6% $ \pm 7/2\rangle$ + 21.1% $ \pm 3/2\rangle$ + 17.3% $ \pm 5/2\rangle$

Table S12. Calculated crystal-field parameters B_k^q (cm^{-1}) for nonequivalent Ln^{3+} ions in compounds LnV_2 . The major components in the table are in bold.

k	q	B			
		Tb^{3+}	Dy^{3+}	Er^{3+}	Yb^{3+}
2	-2	-0.638	$-0.846 \cdot 10^{-3}$	0.725	$-0.457 \cdot 10^{-3}$
	-1	$0.322 \cdot 10^1$	$-0.107 \cdot 10^{-2}$	$-0.852 \cdot 10^{-4}$	$-0.490 \cdot 10^{-3}$
	0	$-0.147 \cdot 10^1$	-0.139	-0.391	$-0.192 \cdot 10$
	1	-0.989	-0.750	$-0.126 \cdot 10^{-3}$	$0.615 \cdot 10$
	2	0.306	-0.566	$-0.783 \cdot 10^{-1}$	$0.923 \cdot 10$
4	-4	$-0.166 \cdot 10^{-3}$	$0.489 \cdot 10^{-4}$	$-0.176 \cdot 10^{-2}$	$-0.164 \cdot 10^{-4}$
	-3	$0.998 \cdot 10^{-2}$	$-0.213 \cdot 10^{-3}$	$-0.264 \cdot 10^{-6}$	$-0.479 \cdot 10^{-4}$
	-2	$-0.116 \cdot 10^{-1}$	$0.454 \cdot 10^{-4}$	$-0.122 \cdot 10^{-2}$	$-0.507 \cdot 10^{-4}$
	-1	$-0.325 \cdot 10^{-1}$	$-0.162 \cdot 10^{-4}$	$-0.314 \cdot 10^{-6}$	$-0.333 \cdot 10^{-4}$
	0	$-0.123 \cdot 10^{-1}$	$-0.222 \cdot 10^{-2}$	$-0.196 \cdot 10^{-2}$	$0.242 \cdot 10^{-1}$
	1	$0.894 \cdot 10^{-2}$	$-0.161 \cdot 10^{-1}$	$0.104 \cdot 10^{-5}$	0.585
	2	$0.317 \cdot 10^{-2}$	$0.206 \cdot 10^{-1}$	$0.120 \cdot 10^{-1}$	0.349
	3	$0.330 \cdot 10^{-2}$	$-0.584 \cdot 10^{-1}$	$0.287 \cdot 10^{-5}$	0.454
	4	$0.987 \cdot 10^{-3}$	$0.979 \cdot 10^{-2}$	$-0.175 \cdot 10^{-1}$	$0.145 \cdot 10^{-1}$
6	-6	$-0.133 \cdot 10^{-4}$	$-0.751 \cdot 10^{-6}$	$-0.253 \cdot 10^{-4}$	$0.529 \cdot 10^{-6}$
	-5	$-0.272 \cdot 10^{-4}$	$-0.196 \cdot 10^{-5}$	$-0.306 \cdot 10^{-6}$	$0.386 \cdot 10^{-5}$
	-4	$0.128 \cdot 10^{-4}$	$0.901 \cdot 10^{-6}$	$0.115 \cdot 10^{-3}$	$-0.265 \cdot 10^{-6}$
	-3	$-0.104 \cdot 10^{-3}$	$-0.107 \cdot 10^{-5}$	$-0.902 \cdot 10^{-7}$	$-0.465 \cdot 10^{-5}$
	-2	$0.394 \cdot 10^{-4}$	$0.110 \cdot 10^{-6}$	$0.663 \cdot 10^{-4}$	$-0.151 \cdot 10^{-5}$
	-1	$-0.170 \cdot 10^{-3}$	$0.105 \cdot 10^{-6}$	$0.739 \cdot 10^{-7}$	$-0.914 \cdot 10^{-6}$
	0	$-0.180 \cdot 10^{-4}$	$-0.111 \cdot 10^{-4}$	$-0.436 \cdot 10^{-5}$	$-0.654 \cdot 10^{-3}$
	1	$0.241 \cdot 10^{-4}$	$0.138 \cdot 10^{-3}$	$-0.264 \cdot 10^{-7}$	$0.175 \cdot 10^{-1}$
	2	$0.378 \cdot 10^{-4}$	$0.722 \cdot 10^{-5}$	$0.163 \cdot 10^{-3}$	$0.939 \cdot 10^{-2}$
	3	$0.556 \cdot 10^{-4}$	$-0.186 \cdot 10^{-3}$	$-0.162 \cdot 10^{-6}$	$0.328 \cdot 10^{-1}$
	4	$-0.117 \cdot 10^{-3}$	$0.191 \cdot 10^{-3}$	$-0.334 \cdot 10^{-3}$	$-0.163 \cdot 10^{-2}$
	5	$0.160 \cdot 10^{-3}$	$-0.457 \cdot 10^{-3}$	$-0.753 \cdot 10^{-7}$	$-0.120 \cdot 10^{-1}$
	6	$-0.305 \cdot 10^{-5}$	$-0.109 \cdot 10^{-3}$	$0.280 \cdot 10^{-3}$	$0.240 \cdot 10^{-3}$