Supplementary Materials for Sliding ferroelectricity in bilayer phosphorus-analogue compounds: mechanisms and applications

Dong-Dong Wang,^a Xin-Yi Gao,^a Yan-Dong Guo,^{*a} Yu-Ting Guo,^a Zhi-Peng Huan,^a Li-Yan Lin,^a Yue Jiang,^{*b} Zeng-Yun Gu,^a Hong-Li Zeng,^{*c} Xiao-Hong Yan^c

^aCollege of Electronic and Optical Engineering, Nanjing University of Posts and Telecommunications, Nanjing 210046, China. E-mail: yandongguo@njupt.edu.cn

^bCollege of Science, Jinling Institute of Technology, Nanjing 211169, China. E-mail: jiangyue@jit.edu.cn ^cCollege of Natural Science, Nanjing University of Posts and Telecommunications, Nanjing 210046, China. E-mail: hlzeng@njupt.edu.cn



Fig. S1 (a)-(i) The energy profiles of the sliding bilayer α -phase MX materials (M = Si, Ge, and Sn; X = S, Se, and Te). Among these materials, only the bilayer α -SiS exhibits a clear double well sliding path.

Table S1 Lattice constant, ferroelectric switching barrier (E_b) and out-of-plane polarization (P_{out}) of MX materials (M = Si, Ge, Sn, and Pb; X = S, Se, and Te).

Configuration	Lattice constant (Å)	$E_{\rm b}~({\rm meV/u.c.})$	$P_{\rm out}~({\rm pC/m})$
bilayer α -SiS	4.32/4.10	7.8	5.6
bilayer β -SiS	3.30	3.89	0.28
bilayer β -SiSe	3.50	5.50	0.38
bilayer β -SiTe	3.82	7.50	0.55
bilayer β -GeS	3.48	4.70	0.28
bilayer β -GeSe	3.65	6.55	0.33
bilayer β -GeTe	3.94	8.85	0.55
bilayer β -SnS	3.73	6.17	0.1
bilayer β -SnSe	3.91	8.84	0.2
bilayer β -SnTe	4.16	11.14	0.5
bilayer β -PbS	3.94	9.56	0.08
bilayer β -PbSe	4.06	12.10	0.13
bilayer $\beta\text{-PbTe}$	4.30	14.20	0.53



Fig. S2 (a)-(l) The energy profiles of the sliding bilayer β -phase MX materials (M = Si, Ge, Sn and Pb; X = S, Se, and Te). All materials exhibit distinct double potential energy well.



Fig. S3 (a)-(l) The differential charge density distributions of the maximum polarization in the MX materials (M = Si, Ge, Sn, and Pb; X = S, Se, and Te), where yellow indicates charge accumulation and blue indicates hole accumulation. When the M atom is fixed, with the increasing atomic number of X atom, the number of charges involved in interlayer transfer also increases significantly.



Fig. S4 (a)-(l) The planar differential charge density distributions of the maximum polarization in the MX materials (M = Si, Ge, Sn, and Pb; X = S, Se, and Te). By using contrast to highlight, as the atomic number of X atom increases, the overall amount of charge involved in charge transfer also increases.



Fig. S5 (a)-(c) The band structure diagrams of β -GeTe, β -PbTe, and β -SnTe, which are used as channel materials.



Fig. S6 (a)-(b) The doping concentration testing of bilayer α -SiS. (c)-(d) The doping concentration testing of bilayer β -SiTe. (e)-(f) The doping concentration testing of bilayer β -SnTe. (g)-(h) The doping concentration testing of bilayer β -PbTe. The black dashed lines represent the ITRS off-state current standards for high performance (HP) and low power (LP) devices, respectively.

Table S2 The device performance of the sub-5-nm-gate bilayer α -SiS FETs against the ITRS 2013 requirements for HP and LP application, including on-state current ($I_{\rm on}$), off-state current ($I_{\rm off}$) and on-off-ratio ($I_{\rm on}/I_{\rm off}$). The data in bold black indicates compliance with the ITRS standards, while the data represented by hyphens indicates that the curve struggles to reach the cutoff current.

Type	Expansion direction	$L_{\rm g}({\rm nm}) + {\rm UL}({\rm nm})$	HP			LP		
			$\mathit{I}_{\mathrm{on}}~(\mu\mathrm{A}/\mu\mathrm{m})$	$I_{\rm off}~(\mu {\rm A}/\mu {\rm m})$	$I_{\rm on}/I_{\rm off}$	$\mathit{I}_{\mathrm{on}}~(\mu\mathrm{A}/\mu\mathrm{m})$	$\mathit{I}_{\rm off}~(\mu A/\mu m)$	$I_{\rm on}/I_{\rm off}$
ITRS 2	013		900.00	0.10		295.00	5E-5	
n-type	along a direction	5 + 0	1892.00	0.10	1.89E + 04	-	-	-
n-type	along a direction	5+1	3189.46	0.10	3.19E + 04	567.04	5E-5	1.13E + 07
n-type	along a direction	5+2	2761.85	0.10	2.76E + 04	888.98	5E-5	1.77E+07
n-type	along a direction	5+3	1878.52	0.10	1.88E + 04	638.77	5E-5	$1.27\mathrm{E}{+07}$
n-type	along a direction	3+0	-	-	-	-	-	-
n-type	along a direction	3+1	-	-	-	-	-	-
n-type	along a direction	3+2	1963.41	0.10	$1.96E{+}04$	-	-	-
n-type	along a direction	3+3	1293.07	0.10	$1.29E{+}04$	-	-	-
n-type	along a direction	1 + 0	-	-	-	-	-	-
p-type	along a direction	5 + 0	1187.24	0.10	1.18E + 04	-	-	-
p-type	along a direction	5+1	2454.24	0.10	2.45E + 04	0.01	5E-5	$1.30E{+}02$
p-type	along a direction	5+2	2321.13	0.10	$2.32E{+}04$	340.32	5E-5	6.80E + 06
p-type	along a direction	5 + 3	738.98	0.10	7.38E + 03	334.19	5E-5	6.60E + 06
p-type	along a direction	3+0	-	-	-	-	-	-
p-type	along a direction	3+1	534.95	0.10	$5.34\mathrm{E}{+03}$	-	-	-
p-type	along a direction	3+2	1180.43	0.10	1.18E + 04	-	-	-
p-type	along a direction	3+3	878.07	0.10	8.78E + 03	4.24	5E-5	8.48E + 04
p-type	along a direction	1 + 0	-	-	-	-	-	-

Table S3 The device performance of the sub-5-nm-gate bilayer β -SiTe FETs against the ITRS 2013 requirements for HP and LP application, including on-state current (I_{on}), off-state current (I_{off}) and on-off-ratio (I_{on}/I_{off}). The data in bold black indicates compliance with the ITRS standards, while the data represented by hyphens indicates that the curve struggles to reach the cutoff current.

Type	Expansion direction	$L_{\rm g}({\rm nm}) + {\rm UL}({\rm nm})$		HP			LP	
			$I_{\rm on}~(\mu A/\mu m)$	$I_{\rm off}~(\mu A/\mu m)$	$I_{\rm on}/I_{\rm off}$	$I_{\rm on}~(\mu A/\mu m)$	$I_{\rm off}~(\mu A/\mu m)$	$I_{\rm on}/I_{\rm off}$
ITRS 2	013		900.00	0.10		295.00	5E-5	
n-type	along a direction	5+0	3417.69	0.10	3.42E+04	-	-	-
n-type	along a direction	5+1	5026.35	0.10	5.63E + 04	-	-	-
n-type	along a direction	5+3	2329.51	0.10	2.23E + 04	719.13	5E-5	1.44E + 07
n-type	along a direction	5 + 5	916.99	0.10	9.17E+03	291.92	5E-5	5.84E + 06
n-type	along a direction	3+0	-	-	-	-	-	-
n-type	along a direction	3+1	166.08	0.10	$1.66E{+}03$	-	-	-
n-type	along a direction	3+3	1967.96	0.10	1.97E + 04	-	-	-
n-type	along a direction	3+5	739.04	0.10	$7.39E{+}03$	87.48	5E-5	$1.75E{+}06$
n-type	along a direction	1 + 0	-	-	-	-	-	-
n-type	along b direction	5+0	2380.46	0.10	2.38E + 04	-	-	-
n-type	along b direction	5+1	5311.86	0.10	5.31E + 04	-	-	-
n-type	along b direction	5+3	2189.99	0.10	2.19E + 04	226.58	5E-5	$4.53E{+}06$
n-type	along b direction	5 + 5	848.95	0.10	$8.49E{+}03$	243.52	5E-5	4.87E + 06
n-type	along b direction	3+0	-	-	-	-	-	-
n-type	along b direction	3+1	-	-	-	-	-	-
n-type	along b direction	3+3	3430.98	0.10	3.43E + 04	-	-	-
n-type	along b direction	3+5	1512.03	0.10	1.51E + 04	0.76	5E-5	$1.52E{+}04$
n-type	along b direction	1 + 0	-	-	-	-	-	-
p-type	along a direction	5 + 0	1647.56	0.10	$1.65E{+}04$	879.85	5E-5	$1.76E{+}07$
p-type	along a direction	5+1	1597.34	0.10	1.60E + 04	750.03	5E-5	$1.50\mathrm{E}{+07}$
p-type	along a direction	5+3	672.14	0.10	$6.72\mathrm{E}{+}03$	291.08	5E-5	$5.82\mathrm{E}{+06}$
p-type	along a direction	5 + 5	329.01	0.10	$3.29E{+}03$	-	-	-
p-type	along a direction	3+0	1498.10	0.10	$1.50E{+}04$	-	-	-
p-type	along a direction	3+1	1462.40	0.10	1.46E + 04	348.04	5E-5	6.96E + 06
p-type	along a direction	3+3	614.98	0.10	$6.15E{+}03$	255.69	5E-5	$5.11\mathrm{E}{+06}$
p-type	along a direction	3+5	305.89	0.10	3.06E+03	138.20	5E-5	$2.76\mathrm{E}{+}06$
p-type	along a direction	1 + 0	-	-	-	-	-	-
p-type	along b direction	5 + 0	1484.71	0.10	1.48E + 04	889.62	5E-5	1.78E + 07
p-type	along b direction	5+1	1462.13	0.10	1.46E + 04	769.30	5E-5	1.54E+07
p-type	along b direction	5 + 3	634.35	0.10	$6.34\mathrm{E}{+03}$	289.93	5E-5	$5.80\mathrm{E}{+}06$
p-type	along b direction	5 + 5	310.64	0.10	$3.11E{+}03$	128.02	5E-5	$2.56\mathrm{E}{+06}$
p-type	along b direction	3+0	2360.72	0.10	2.36E + 04	-	-	-
p-type	along b direction	3+1	2625.63	0.10	2.62E + 04	518.76	5E-5	1.04E + 07
p-type	along b direction	3+3	941.67	0.10	9.42E + 03	408.90	5E-5	8.18E + 06
p-type	along b direction	3+5	474.78	0.10	$4.75\mathrm{E}{+03}$	236.50	5E-5	$4.73\mathrm{E}{+06}$
p-type	along b direction	1 + 0	-	-	-	-	-	-

Table S4 The device performance of the sub-5-nm-gate bilayer β -SnTe FETs against the ITRS 2013 requirements for HP and LP application, including on-state current (I_{on}), off-state current (I_{off}) and on-off-ratio (I_{on}/I_{off}). The data in bold black indicates compliance with the ITRS standards, while the data represented by hyphens indicates that the curve struggles to reach the cutoff current.

Type	Expansion direction	$L_{\rm g}({\rm nm}) + {\rm UL}({\rm nm})$		HP			LP	
			$I_{\rm on}~(\mu A/\mu m)$	$I_{\rm off}~(\mu {\rm A}/\mu {\rm m})$	$I_{\rm on}/I_{\rm off}$	$\mathit{I}_{\mathrm{on}}~(\mu\mathrm{A}/\mu\mathrm{m})$	$I_{\rm off}~(\mu A/\mu m)$	$I_{\rm on}/I_{\rm off}$
ITRS 2	013		900.00	0.10		295.00	5E-5	
n-type	along a direction	5 + 0	4227.00	0.10	4.23E + 04	-	-	-
n-type	along a direction	5+1	4787.28	0.10	4.79E + 04	36.02	5E-5	7.20E + 05
n-type	along a direction	5+3	2136.27	0.10	2.14E + 04	1187.34	5E-5	2.37E + 07
n-type	along a direction	5 + 5	770.38	0.10	7.70E + 03	518.20	5E-5	1.04E+07
n-type	along a direction	3+0	10.91	0.10	$1.09E{+}02$	-	-	-
n-type	along a direction	3+1	1086.89	0.10	1.09E + 04	-	-	-
n-type	along a direction	3+3	1737.27	0.10	1.74E + 04	4.37	5E-5	$8.73E{+}04$
n-type	along a direction	3+5	1259.89	0.10	1.26E + 04	659.25	5E-5	$1.32E{+}07$
n-type	along a direction	1 + 0	-	-	-	-	-	-
n-type	along b direction	5 + 0	5123.68	0.10	5.12E+04	-	-	-
n-type	along b direction	5+1	6031.19	0.10	6.03E + 04	0.39	5E-5	$7.73E{+}03$
n-type	along b direction	5+3	2524.02	0.10	$2.52E{+}04$	1082.62	5E-5	2.17E+07
n-type	along b direction	5 + 5	1040.30	0.10	1.04E + 04	520.60	5E-5	1.04E + 07
n-type	along b direction	3+0	-	-	-	-	-	-
n-type	along b direction	3+1	881.90	0.10	8.82E + 03	-	-	-
n-type	along b direction	3+3	2297.39	0.10	2.30E + 04	-	-	-
n-type	along b direction	3+5	2485.34	0.10	2.49E + 04	1326.67	5E-5	2.65E+07
n-type	along b direction	1 + 0	-	-	-	-	-	-
p-type	along a direction	5 + 0	1544.27	0.10	$1.54E{+}04$	1207.42	5E-5	2.41E + 07
p-type	along a direction	5+1	1559.89	0.10	$1.56\mathrm{E}{+04}$	1077.46	5E-5	$2.15\mathrm{E}{+07}$
p-type	along a direction	5+3	834.68	0.10	8.35E+03	371.08	5E-5	7.42E + 06
p-type	along a direction	5 + 5	491.51	0.10	$4.92E{+}03$	-	-	-
p-type	along a direction	3+0	1422.49	0.10	1.42E + 04	-	-	-
p-type	along a direction	3+1	1485.04	0.10	1.49E + 04	-	-	-
p-type	along a direction	3+3	826.31	0.10	8.26E + 03	305.26	5E-5	6.11E + 06
p-type	along a direction	3+5	379.82	0.10	$3.80E{+}03$	176.76	5E-5	$3.54\mathrm{E}{+06}$
p-type	along a direction	1 + 0	-	-	-	-	-	-
p-type	along b direction	5+0	1487.32	0.10	1.49E + 04	1049.17	5E-5	2.10E + 07
p-type	along b direction	5+1	1461.78	0.10	1.46E + 04	1067.34	5E-5	$2.13E{+}07$
p-type	along b direction	5+3	775.61	0.10	7.76E + 03	356.25	5E-5	7.12E+06
p-type	along b direction	5 + 5	363.22	0.10	3.63E + 03	-	-	-
p-type	along b direction	3+0	1440.30	0.10	1.44E + 04	-	-	-
p-type	along b direction	3+1	1444.49	0.10	1.45E+04	-	-	-
p-type	along b direction	3+3	767.39	0.10	$7.67\mathrm{E}{+03}$	308.60	5E-5	6.17E + 06
p-type	along b direction	3+5	361.19	0.10	$3.61E{+}03$	-	-	-
p-type	along b direction	1 + 0	-	-	-	-	-	-

Table S5 The device performance of the sub-5-nm-gate bilayer β -PbTe FETs against the ITRS 2013 requirements for HP and LP application, including on-state current (I_{on}), off-state current (I_{off}) and on-off-ratio (I_{on}/I_{off}). The data in bold black indicates compliance with the ITRS standards, while the data represented by hyphens indicates that the curve struggles to reach the cutoff current.

Type	Expansion direction	$L_{\rm g}({\rm nm}) + {\rm UL}({\rm nm})$		HP			LP	
			$I_{\rm on}~(\mu A/\mu m)$	$I_{\rm off}~(\mu A/\mu m)$	$I_{\rm on}/I_{\rm off}$	$I_{\rm on}~(\mu A/\mu m)$	$I_{\rm off}~(\mu A/\mu m)$	$I_{\rm on}/I_{\rm off}$
ITRS 2	013		900.00	0.10		295.00	5E-5	
n-type	along a direction	5+0	3388.01	0.10	3.39E + 04	-	-	-
n-type	along a direction	5+1	3434.10	0.10	3.43E + 04	-	-	-
n-type	along a direction	5+3	1529.83	0.10	$1.53E{+}04$	887.78	5E-5	1.78E + 07
n-type	along a direction	5 + 5	540.81	0.10	5.41E + 03	320.73	5E-5	6.41E + 06
n-type	along a direction	3+0	22.70	0.10	$2.27\mathrm{E}{+}02$	-	-	-
n-type	along a direction	3+1	823.13	0.10	8.23E + 03	-	-	-
n-type	along a direction	3+3	1395.73	0.10	1.40E + 04	-	-	-
n-type	along a direction	3+5	456.40	0.10	$4.56\mathrm{E}{+03}$	195.98	5E-5	3.92E + 06
n-type	along a direction	1 + 0	-	-	-	-	-	-
n-type	along b direction	5 + 0	4240.21	0.10	4.24E + 04	-	-	-
n-type	along b direction	5+1	4834.59	0.10	4.83E + 04	-	-	-
n-type	along b direction	5+3	2573.55	0.10	$2.57\mathrm{E}{+04}$	1251.89	5E-5	$2.50\mathrm{E}{+07}$
n-type	along b direction	5 + 5	999.78	0.10	1.00E + 04	508.67	5E-5	1.02E + 07
n-type	along b direction	3+0	1.94	0.10	$1.94E{+}01$	-	-	-
n-type	along b direction	3+1	706.57	0.10	7.07E + 03	-	-	-
n-type	along b direction	3+3	1201.14	0.10	$1.20E{+}04$	-	-	-
n-type	along b direction	3+5	2397.92	0.10	2.40E + 04	1286.66	5E-5	2.57E+07
n-type	along b direction	1 + 0	-	-	-	-	-	-
p-type	along a direction	5+0	2167.58	0.10	$2.17E{+}04$	1092.60	5E-5	2.19E + 07
p-type	along a direction	5+1	2242.60	0.10	2.24E + 04	1251.06	5E-5	$2.50\mathrm{E}{+07}$
p-type	along a direction	5+3	1082.05	0.10	1.08E + 04	423.18	5E-5	8.46E + 06
p-type	along a direction	5 + 5	488.88	0.10	$4.89E{+}03$	146.00	5E-5	2.92E + 06
p-type	along a direction	3+0	1462.20	0.10	1.46E + 04	-	-	-
p-type	along a direction	3+1	2017.09	0.10	2.02E + 04	-	-	-
p-type	along a direction	3+3	885.29	0.10	8.85E + 03	297.16	5E-5	5.94E + 06
p-type	along a direction	3+5	446.41	0.10	4.46E + 03	147.76	5E-5	2.96E + 06
p-type	along a direction	1 + 0	-	-	-	-	-	-
p-type	along b direction	5+0	2174.14	0.10	2.17E + 04	1059.83	5E-5	2.12E + 07
p-type	along b direction	5+1	2150.27	0.10	$2.15E{+}04$	1122.54	5E-5	2.25E + 07
p-type	along b direction	5+3	1123.35	0.10	1.12E + 04	508.01	5E-5	1.02E + 07
p-type	along b direction	5 + 5	490.41	0.10	4.90E + 03	242.35	5E-5	4.85E + 06
p-type	along b direction	3+0	705.04	0.10	7.05E + 03	-	-	-
p-type	along b direction	3+1	2082.52	0.10	2.08E + 04	-	-	-
p-type	along b direction	3+3	942.49	0.10	9.42E+03	330.24	5E-5	6.60E + 06
p-type	along b direction	3+5	476.58	0.10	4.77E + 03	-	-	-
p-type	along b direction	1 + 0	-	-	-	-	-	-