

# Rayleigh streaming phenomena at the physical origin of cellulose nanocrystals orientations during combined ultrasound and ultrafiltration processes.

Fanny Bosson<sup>1</sup>, Mathilde Challamel<sup>1</sup>, Mohamed Karrouch<sup>1</sup>, Nicolas Hengl<sup>1</sup>, Henda Djeridi<sup>2</sup>,

Frédéric Pignon<sup>1\*</sup>

## Supplementary data

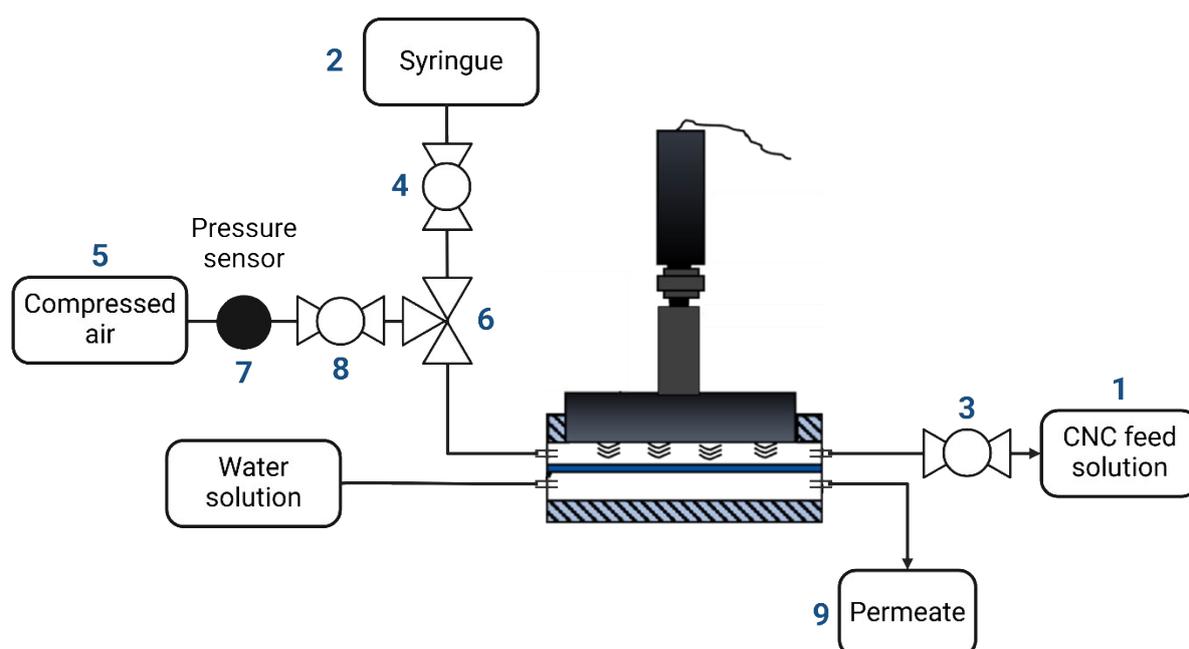


Figure S1. Schematic representation of the flow diagram of the FU-US system. (1) CNC feed solution, (2) syringe, (3) inlet valve, (4) outlet valve, (5) compressed air supply, (6) T-junction, (7) pressure sensor, (8) pressure vane and (9) small container for collecting the permeate.

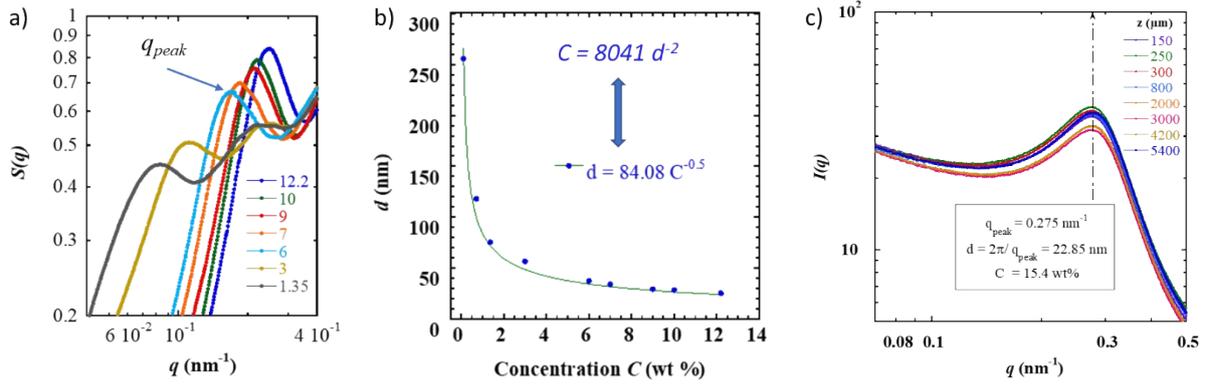


Figure S2. Determination of CNC concentration using SAXS. a) SAXS  $S(q)$  curves obtained for suspensions with known concentrations (1.35 wt % to 12.2 wt %), from which the  $q_{peak}$  values are measured. b) Relationship between the interparticle distance  $d$  (nm), calculating using  $d = \frac{2\pi}{q_{peak}}$ , and the CNC concentration (wt %). c) SAXS  $I(q)$  curves at different heights in the FU-US cell from the membrane surface to the vibrating blade after pressure release ( $t = 97$  min,  $\Delta P = 0$  Pa and  $P_a = 6 \text{ W.cm}^{-2}$ ) showing that the  $q_{peak}$  position is not changing (same concentration inside the channel). The concentration at each height is calculated using the relationship determined in b)  $C = 8041 d^{-2}$ .

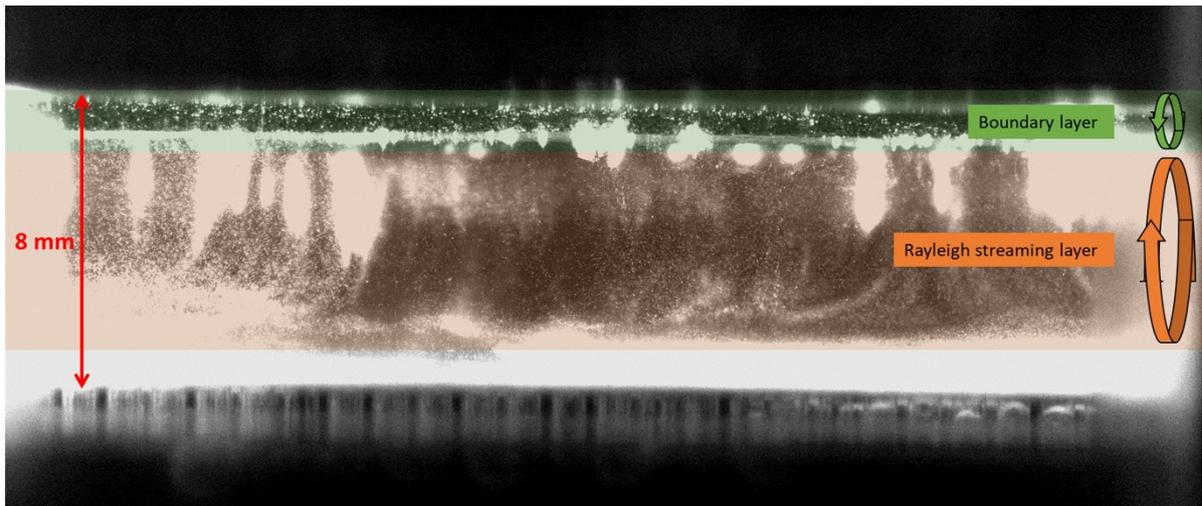


Figure S3. *In situ* micro-PIV image of the acoustic streaming phenomenon, obtained during Step 1 for  $t_{fl} = 88$  min,  $\Delta P = 1.2 \times 10^5$  Pa and  $P_a = 6 \text{ W.cm}^{-2}$ . In green the boundary layer and in orange the Rayleigh streaming layer.

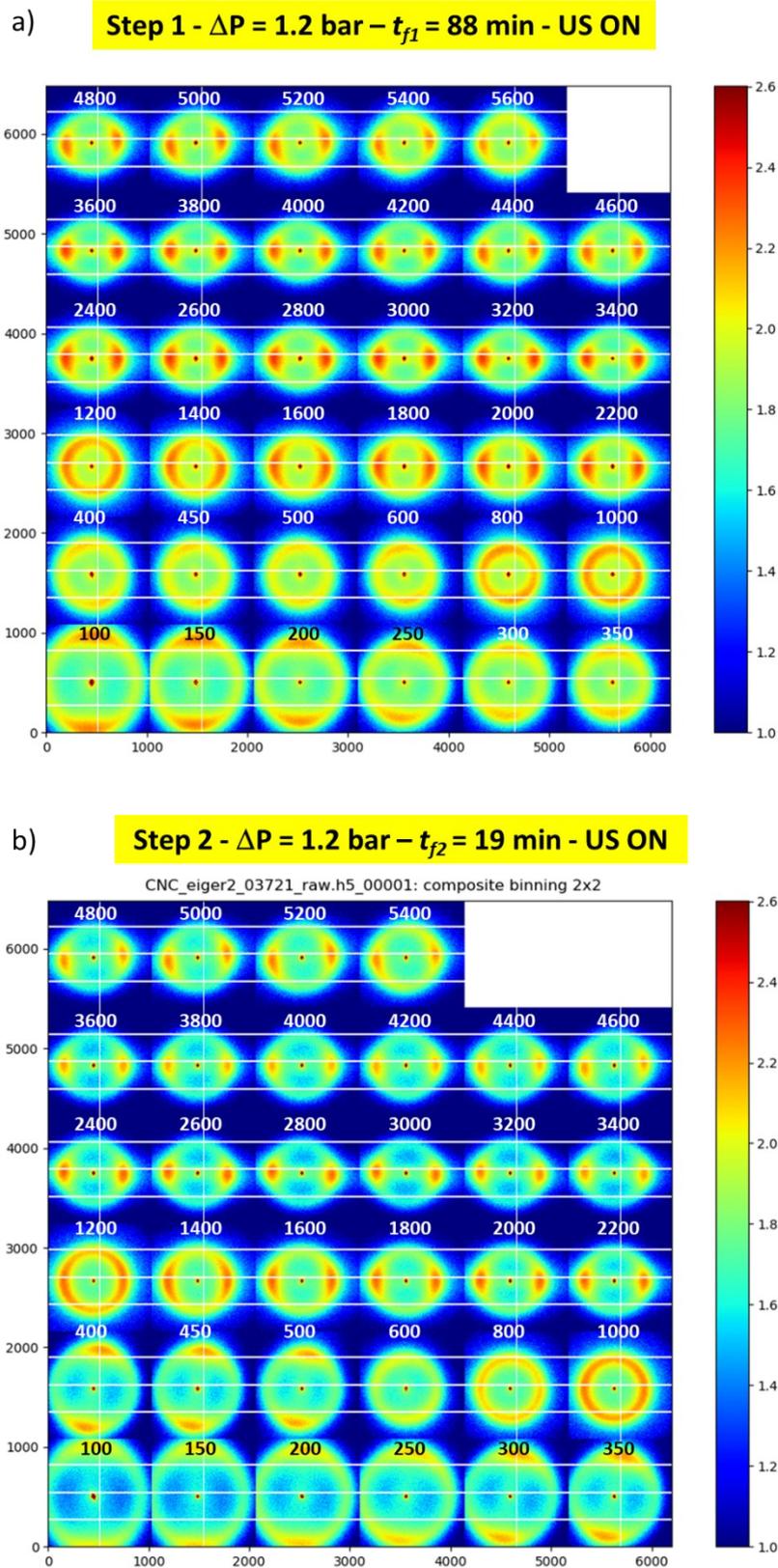


Figure S4. 2D-SAXS patterns for different  $z$  distance from the membrane surface for two conditions : a)  $t_{f1} = 88 \text{ min}$   $\Delta P = 1.2 \times 10^5 \text{ Pa}$  and b)  $t_{f2} = 19 \text{ min}$  and  $\Delta P = 1.2 \times 10^5 \text{ Pa}$ .

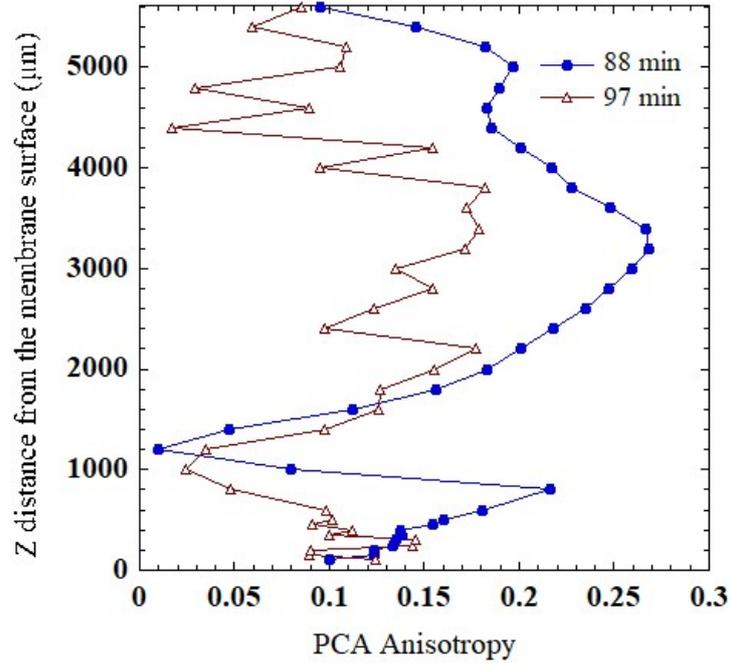


Figure S5. Comparison of *PCA Anisotropy* for two conditions : a)  $t_{f1} = 88$  min  $\Delta P = 1.2 \times 10^5$  Pa and b)  $t_{f1} = 97$  min and  $\Delta P = 0$  Pa.

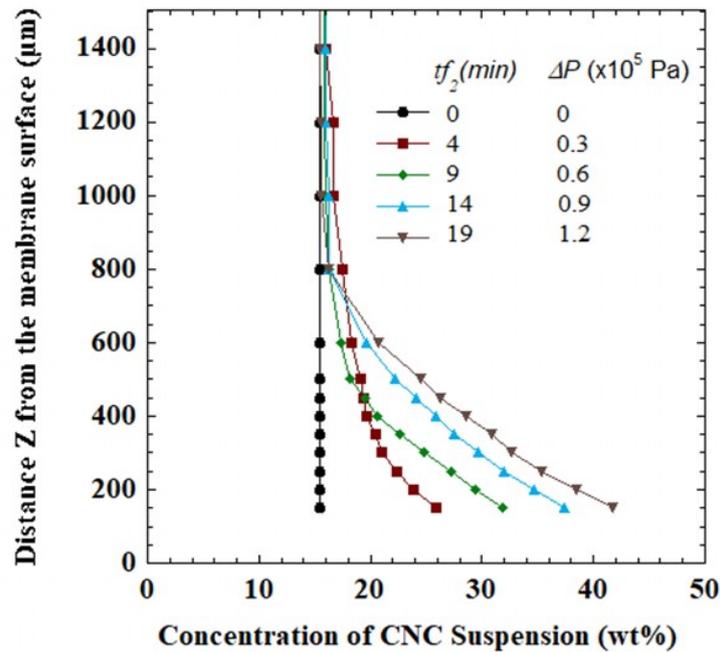


Figure S6: Concentration profile  $C(z,t)$  as a function of the distance  $z$  from the membrane surface and for various transmembrane pressures  $\Delta P$  applied during FU-US processing of a CNC suspension with initial concentration from beginning of Step 2 of about  $C = 15$  wt %.