

Enhancing Electrocatalytic Activities of High-Entropy Borides (HEBs) for C–N Coupling in Induced Cation and pH-Dependent Microenvironments via Multiscale Modeling Strategy

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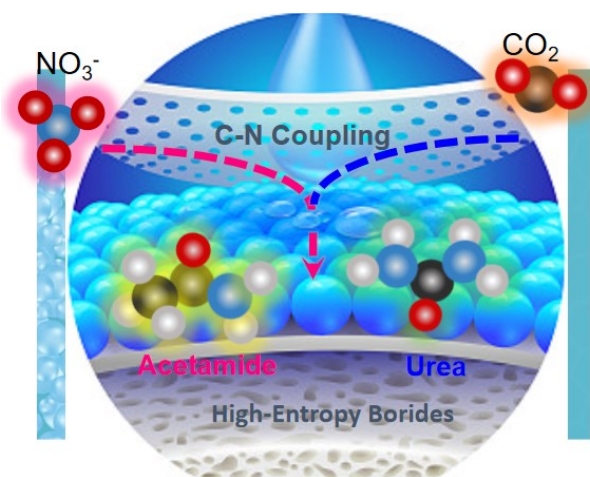
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Graphical abstract



Mechanism pathway analysis

In this work, we proposed a new mechanism of the acetamide synthesis based on electrochemical Co-reduction of CO₂ and N₂ via C-N Coupling on high entropy alloy borides (HEA-MBene) materials.

(Acid environment)

1. CO₂ Reduction Reaction Pathway

1. $* + \text{CO}_2 \rightarrow * \text{CO}_2$
2. $* + \text{CO}_2 + (\text{H}^+ + \text{e}^-) \rightarrow * \text{COOH}$
3. $* + \text{CO}_2 + 2(\text{H}^+ + \text{e}^-) \rightarrow * \text{CO} + \text{H}_2\text{O}$
4. $* + 2\text{CO}_2 + 2(\text{H}^+ + \text{e}^-) \rightarrow * \text{CO} + * \text{CO}_2 + \text{H}_2\text{O}$
5. $* + 2\text{CO}_2 + 3(\text{H}^+ + \text{e}^-) \rightarrow * \text{CO} + * \text{COOH} + \text{H}_2\text{O}$
6. $* + 2\text{CO}_2 + 4(\text{H}^+ + \text{e}^-) \rightarrow * \text{CO} * \text{CO} + 2\text{H}_2\text{O}$
7. $* + 2\text{CO}_2 + 5(\text{H}^+ + \text{e}^-) \rightarrow * \text{COCO} + 2\text{H}_2\text{O}$
8. $* + 2\text{CO}_2 + 6(\text{H}^+ + \text{e}^-) \rightarrow * \text{COHCOH} + 2\text{H}_2\text{O}$
9. $* + 2\text{CO}_2 + 6(\text{H}^+ + \text{e}^-) \rightarrow * \text{CCO} + 3\text{H}_2\text{O}$

2. Amination Reaction Pathway

1. $* + 2\text{CO}_2 + \text{NH}_3 + 6(\text{H}^+ + \text{e}^-) \rightarrow * \text{CCOH}(\text{NH}_2) + 3\text{H}_2\text{O}$

2. $*+2\text{CO}_2+\text{NH}_3+6(\text{H}^++\text{e}^-)\rightarrow*\text{CHCO}(\text{NH}_2)+3\text{H}_2\text{O}$
3. $*+2\text{CO}_2+\text{NH}_3+7(\text{H}^++\text{e}^-)\rightarrow*\text{CH}_2\text{CO}(\text{NH}_2)+3\text{H}_2\text{O}$
4. $*+2\text{CO}_2+\text{NH}_3+8(\text{H}^++\text{e}^-)\rightarrow*\text{CH}_3\text{CO}(\text{NH}_2)+3\text{H}_2\text{O}$
5. $*+2\text{CO}_2+\text{NH}_3+12(\text{H}^++\text{e}^-)\rightarrow*\text{CH}_3\text{CH}_2\text{NH}_2+4\text{H}_2\text{O}$

3. Secondary Reaction

(COCO Path)

1. $*+\text{CO}_2+2(\text{H}^++\text{e}^-)\rightarrow*\text{CO}+\text{H}_2\text{O}$
2. $*+2\text{CO}_2+3(\text{H}^++\text{e}^-)\rightarrow*\text{COCOOH}+\text{H}_2\text{O}$
3. $*+2\text{CO}_2+4(\text{H}^++\text{e}^-)\rightarrow*\text{CO}*\text{CO}+2\text{H}_2\text{O}$

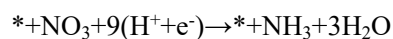
(COCOH Path)

1. $*+\text{CO}_2+3(\text{H}^++\text{e}^-)\rightarrow*\text{COH}+\text{H}_2\text{O}$
2. $*+2\text{CO}_2+4(\text{H}^++\text{e}^-)\rightarrow*\text{COHCOOH}+\text{H}_2\text{O}$
3. $*+2\text{CO}_2+5(\text{H}^++\text{e}^-)\rightarrow*\text{COHCO}+2\text{H}_2\text{O}$

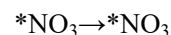
(CHOCO Path)

1. $*+\text{CO}_2+3(\text{H}^++\text{e}^-)\rightarrow*\text{CHO}+\text{H}_2\text{O}$
2. $*+2\text{CO}_2+4(\text{H}^++\text{e}^-)\rightarrow*\text{CHOCOOH}+\text{H}_2\text{O}$
3. $*+2\text{CO}_2+5(\text{H}^++\text{e}^-)\rightarrow*\text{CHOCO}+2\text{H}_2\text{O}$
4. $*+2\text{CO}_2+6(\text{H}^++\text{e}^-)\rightarrow*\text{CH}(\text{OH})\text{CO}+2\text{H}_2\text{O}$

5. NO₃ Reduction Reaction Pathway



- 1.
2. $*\text{NO}_3+(\text{H}^++\text{e}^-)\rightarrow*\text{NOOOH}$
3. $*\text{NO}_3+2(\text{H}^++\text{e}^-)\rightarrow*\text{NO}_2+\text{H}_2\text{O}$
3. $*\text{NO}_3+3(\text{H}^++\text{e}^-)\rightarrow*\text{NOOH}+\text{H}_2\text{O}$
4. $*\text{NO}_3+4(\text{H}^++\text{e}^-)\rightarrow*\text{NO}+2\text{H}_2\text{O}$
5. $*\text{NO}_3+5(\text{H}^++\text{e}^-)\rightarrow*\text{NOH}+2\text{H}_2\text{O}$
6. $*\text{NO}_3+6(\text{H}^++\text{e}^-)\rightarrow*\text{N}+3\text{H}_2\text{O}$
7. $*\text{NO}_3+7(\text{H}^++\text{e}^-)\rightarrow*\text{NH}+3\text{H}_2\text{O}$
8. $*\text{NO}_3+8(\text{H}^++\text{e}^-)\rightarrow*\text{NH}_2+3\text{H}_2\text{O}$
9. $*\text{NO}_3+9(\text{H}^++\text{e}^-)\rightarrow*\text{NH}_3+3\text{H}_2\text{O}$
10. $*\text{NO}_3+9(\text{H}^++\text{e}^-)\rightarrow*\text{NH}_3+3\text{H}_2\text{O}$
11. $*\text{NO}_3+9(\text{H}^++\text{e}^-)\rightarrow*+\text{NH}_3+3\text{H}_2\text{O}$
12. $*\text{NO}_3+5(\text{H}^++\text{e}^-)\rightarrow*\text{HNO}+2\text{H}_2\text{O}$
13. $*\text{NO}_3+6(\text{H}^++\text{e}^-)\rightarrow*\text{HNOH}+2\text{H}_2\text{O}$
14. $*\text{NO}_3+7(\text{H}^++\text{e}^-)\rightarrow*\text{H}_2\text{NOH}+2\text{H}_2\text{O}$



Urea synthesis

1. $*+\text{CO}_2\rightarrow*\text{CO}_2$
2. $*+\text{CO}_2+(\text{H}^++\text{e}^-)\rightarrow*\text{COOH}$
3. $*+\text{CO}_2+2(\text{H}^++\text{e}^-)\rightarrow*\text{CO}+\text{H}_2\text{O}$
4. $*+\text{CO}_2+\text{H}_2\text{NOH}+3(\text{H}^++\text{e}^-)\rightarrow*\text{H}_2\text{NCO}+2\text{H}_2\text{O}$
5. $*+\text{CO}_2+2\text{H}_2\text{NOH}+4(\text{H}^++\text{e}^-)\rightarrow*\text{H}_2\text{NCONH}_2+3\text{H}_2\text{O}$

(Alkaline environment)

Path CO₂RR (Alkaline)

1. $*+CO_2 \rightarrow *CO_2$
2. $*+CO_2+H_2O+2e^- \rightarrow *COOH+OH^-$
3. $*+CO_2+H_2O+2e^- \rightarrow *CO+2OH^-$
4. $*+2CO_2+2H_2O+4e^- \rightarrow *COCO OH+3OH^-$
5. $*+2CO_2+2H_2O+4e^- \rightarrow *COCO+4OH^-$
6. $*+2CO_2+3H_2O+6e^- \rightarrow *COCO H+5OH^-$
7. $*+2CO_2+4H_2O+8e^- \rightarrow *COHCO H+6OH^-$
8. $*+2CO_2+4H_2O+8e^- \rightarrow *CCO+6OH^-+H_2O$
9. $*+2CO_2+NH_3+4H_2O+8e^- \rightarrow *CC(OH)NH_2+6OH^-+H_2O$
10. $*+2CO_2+NH_3+4H_2O+8e^- \rightarrow *HCCONH_2+6OH^-+H_2O$
11. $*+2CO_2+NH_3+5H_2O+10e^- \rightarrow *H_2CCONH_2+7OH^-+H_2O$
12. $*+2CO_2+NH_3+6H_2O+12e^- \rightarrow *H_3CCONH_2+8OH^-+H_2O$

Path CHOCO (Alkaline)

4. $*+CO_2+2H_2O+4e^- \rightarrow *CHO+3OH^-$
5. $*+2CO_2+3H_2O+6e^- \rightarrow *CHOCOOH+4OH^-$
6. $*+2CO_2+3H_2O+6e^- \rightarrow *CHOCO+5OH^-$
7. $*+2CO_2+4H_2O+8e^- \rightarrow *HCOHCO+6OH^-$

Path COHCO (Alkaline)

4. $*+CO_2+2H_2O+4e^- \rightarrow *COH+3OH^-$
5. $*+2CO_2+3H_2O+6e^- \rightarrow *COHCOOH+4OH^-$

NO₃RR

Path A (Alkaline)

1. $*+NO_3 \rightarrow *NO_3$
2. $*+NO_3+H_2O+2e^- \rightarrow *NO_2+2OH^-$
3. $*+NO_3+2H_2O+4e^- \rightarrow *NO+4OH^-$
4. $*+NO_3+3H_2O+6e^- \rightarrow *N+6OH^-$
5. $*+NO_3+4H_2O+8e^- \rightarrow *NH+7OH^-$
6. $*+NO_3+5H_2O+10e^- \rightarrow *NH_2+8OH^-$
7. $*+NO_3+6H_2O+12e^- \rightarrow *NH_3+9OH^-$
8. $*+NO_3+6H_2O+12e^- \rightarrow *+NH_3+9OH^-$

Path B (Alkaline)

5. $*+NO_3+3H_2O+6e^- \rightarrow *NOH+5OH^-$
5. $*+NO_3+3H_2O+6e^- \rightarrow *HNO+5OH^-$
6. $*+NO_3+4H_2O+8e^- \rightarrow *HNOH+6OH^-$
7. $*+NO_3+5H_2O+10e^- \rightarrow *H_2NOH+7OH^-$

Urea synthesis

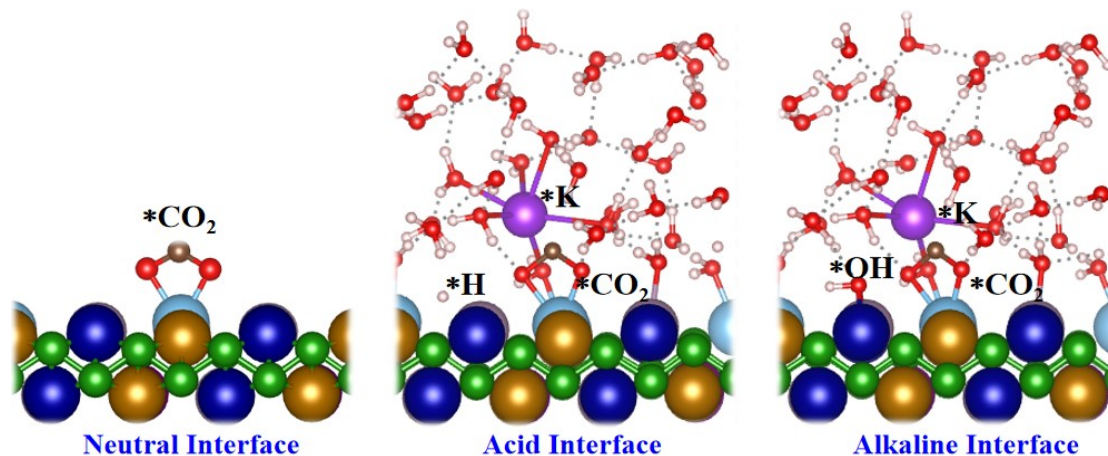
1. $*+CO_2+H_2NOH+H_2O+2e^- \rightarrow *H_2NCO+3OH^-$
2. $*+CO_2+2H_2NOH+H_2O+2e^- \rightarrow *H_2NCONH_2+4OH^-$

Computational hydrogen electrode model.

The energy of electron and proton pair is calculated as $1/2H_2$ according to calculated hydrogen

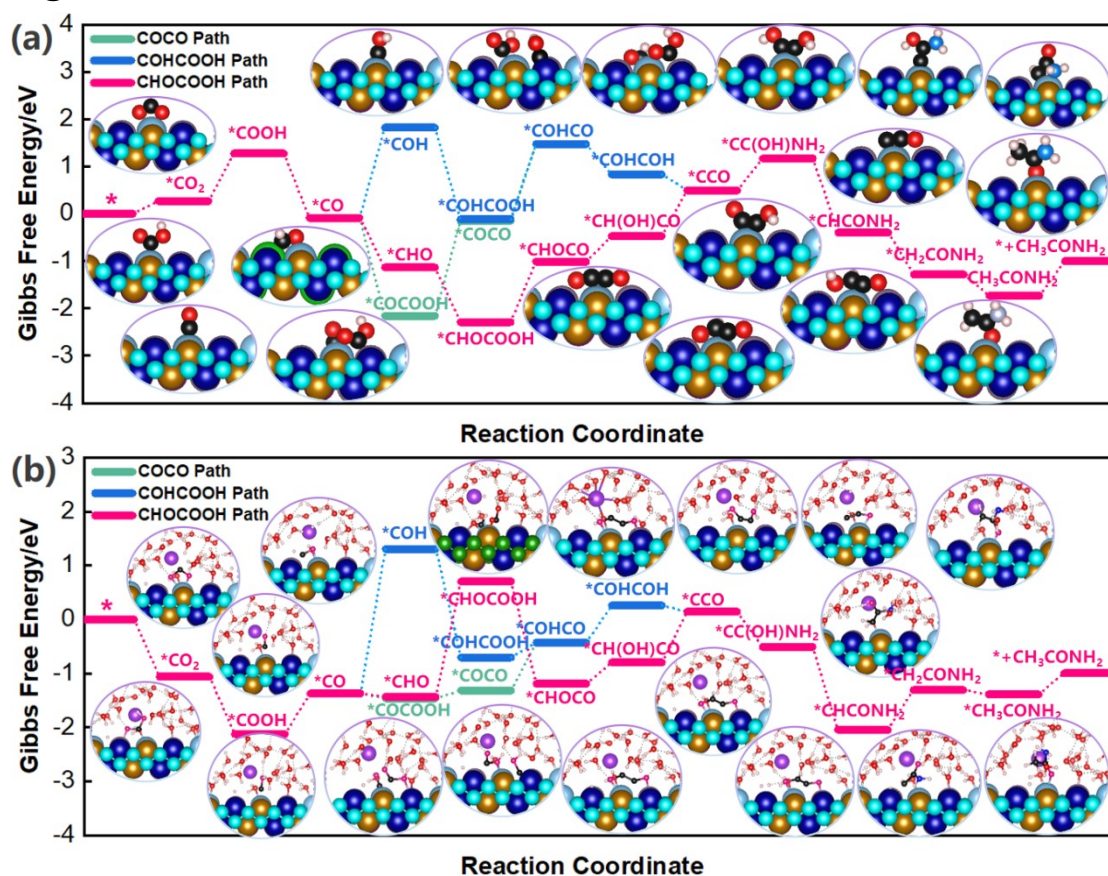
electrode (CHE) by Nørskov, which corresponds to reverse hydrogen electrode (RHE). Therefore, in the RHE, the chemical potential of a proton–electron pair was defined as $1/2H_2$. Therefore, in the RHE, the chemical potential of a proton–electron pair was defined as:

$$\Delta G(H^+ + e^-) = \frac{1}{2} \Delta G(H_2)$$



Computational model for neutral, acid and alkaline microenvironment interface.

Figures:



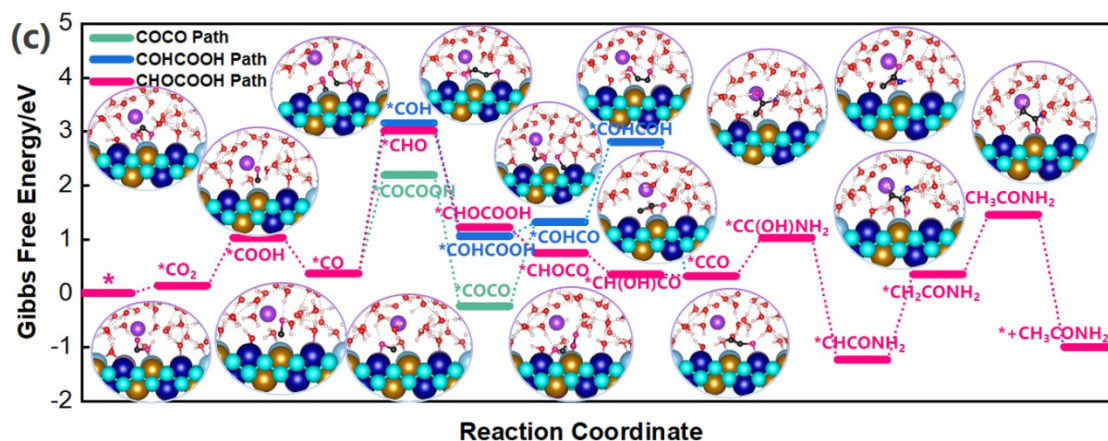
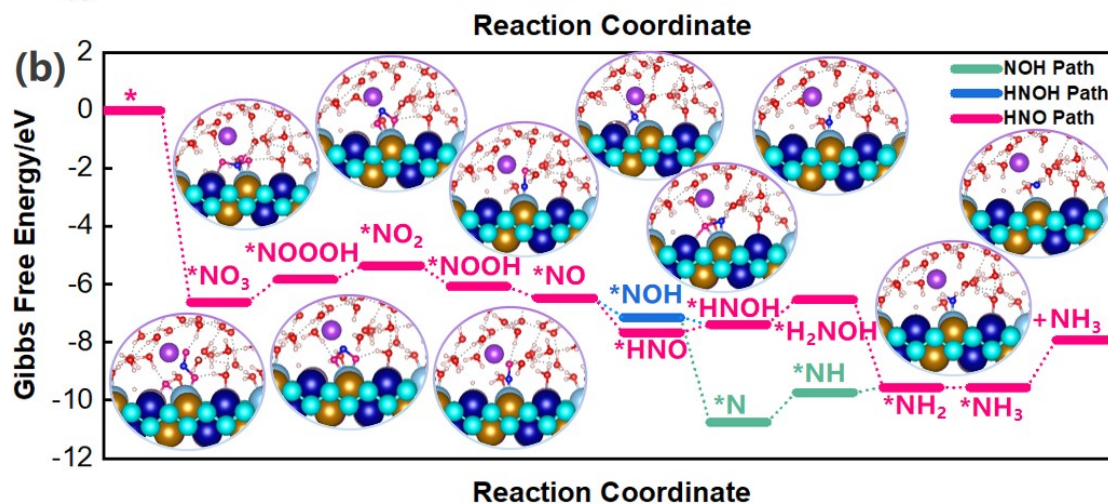
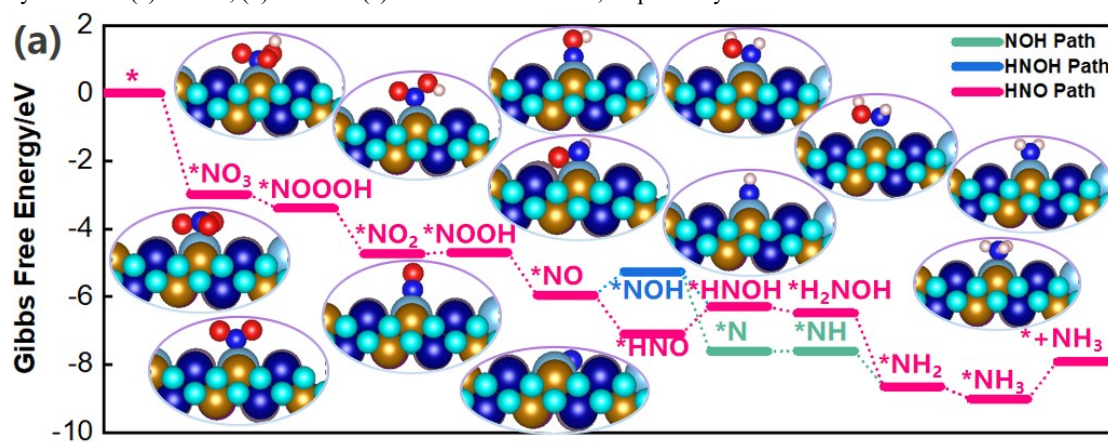


Figure S1. Calculated Gibbs free energy diagram via all potential energy profile path and corresponding their binding configurations of various intermediates generated over TiCrMnFeMoB (HEBs) catalysts during acetamide synthesis in (a) neutral, (b) acid and (c) alkaline environment, respectively.



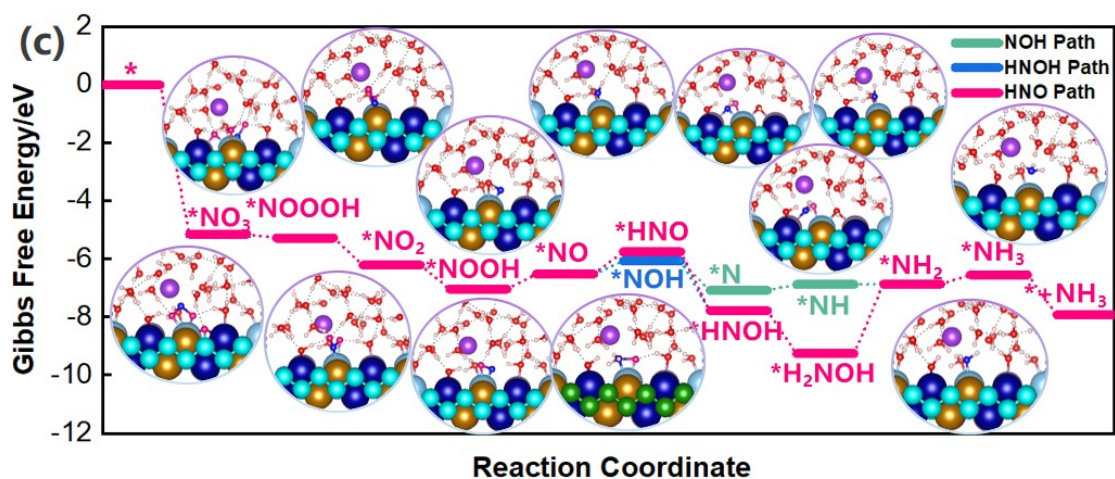
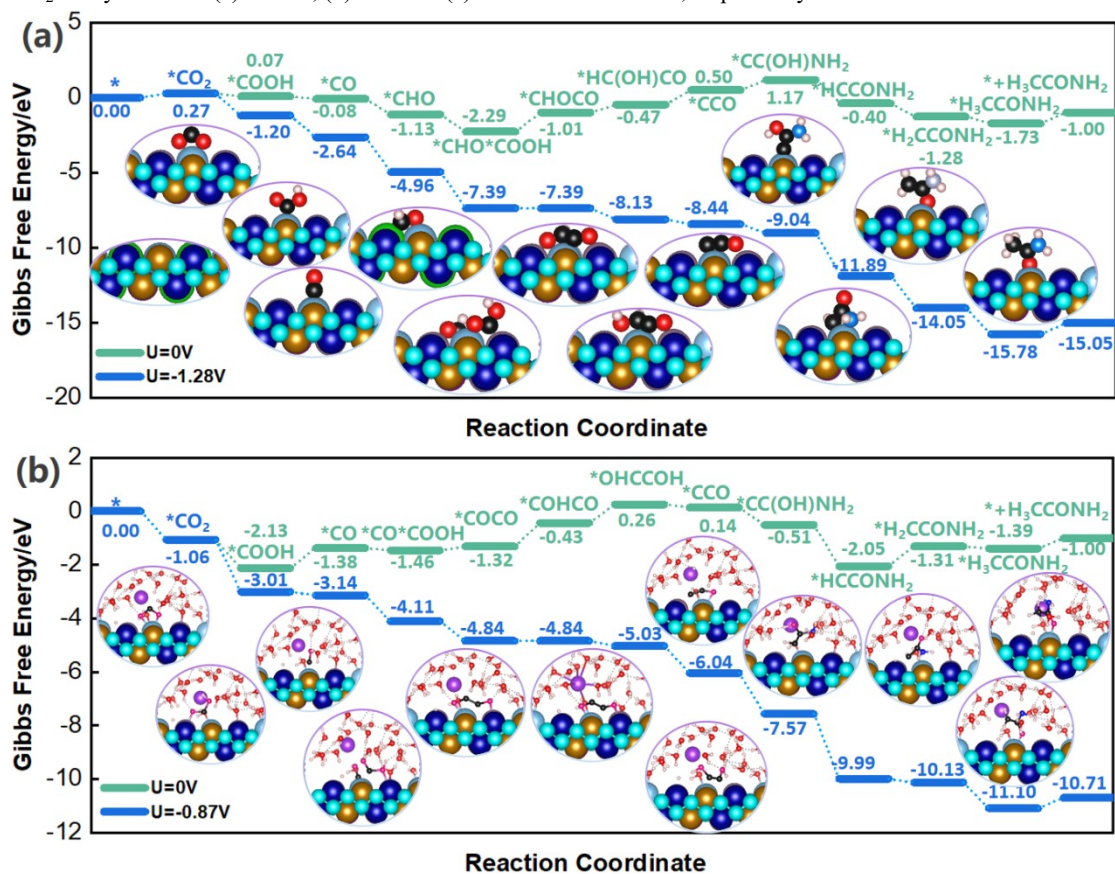


Figure S2. Calculated Gibbs free energy diagram via all potential energy profile path and corresponding their binding configurations of various intermediates generated over TiCrMnFeMoB (HEBs) catalysts during NH_3 and NH_2OH synthesis in (a) neutral, (b) acid and (c) alkaline environment, respectively.



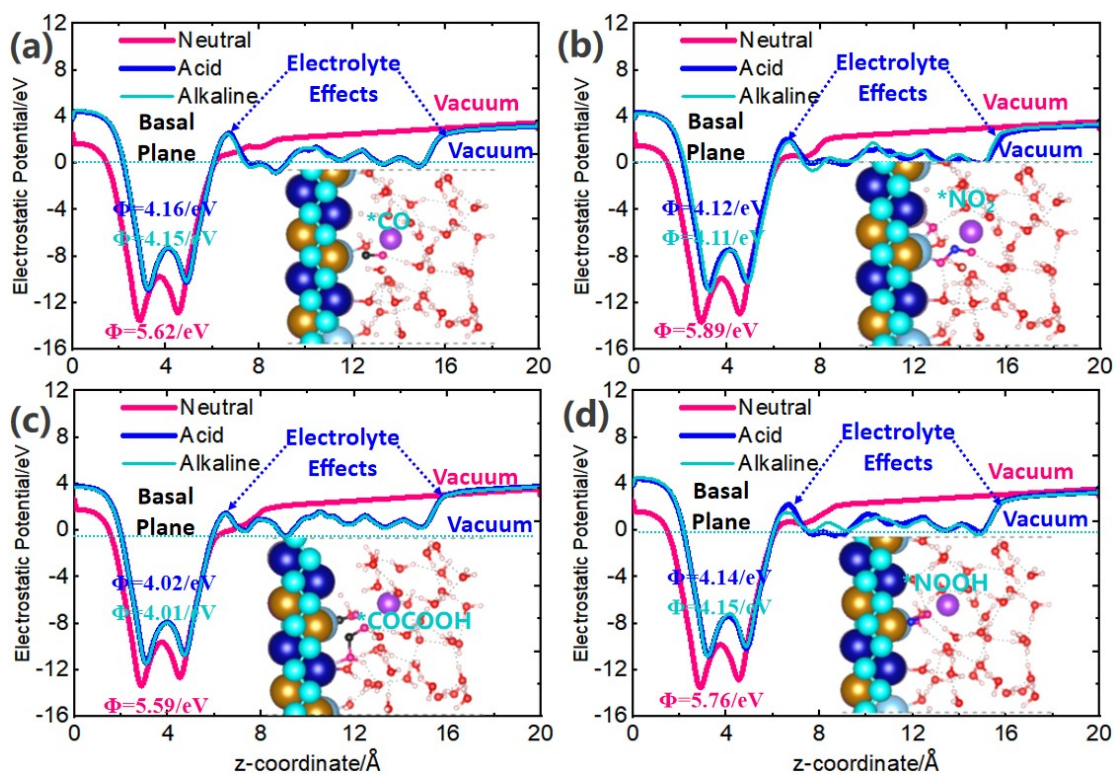


Figure S5. The electrostatic potential along z-direction slab model in neutral, acid and alkaline environments, a,c (Left) for CO₂RR and b,d for NitrRR (Right) intermediates, respectively.

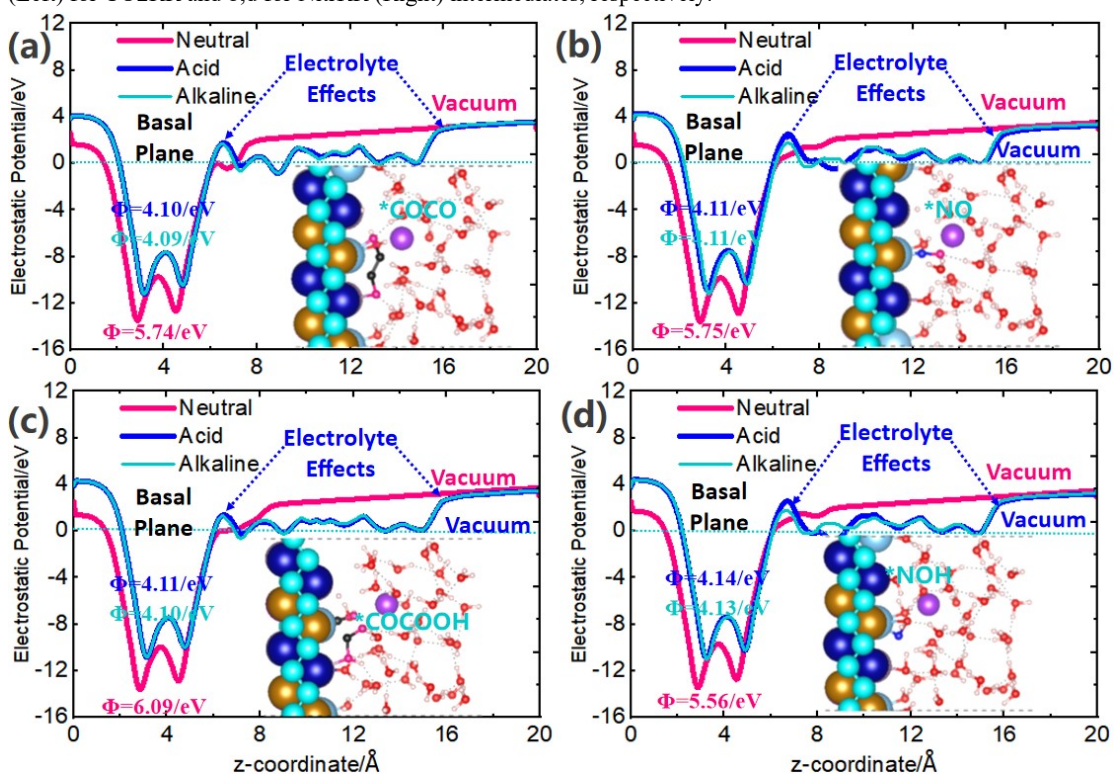


Figure S6. The electrostatic potential along z-direction slab model in neutral, acid and alkaline environments, a,c (Left) for CO₂RR and b,d for NitrRR (Right) intermediates, respectively.

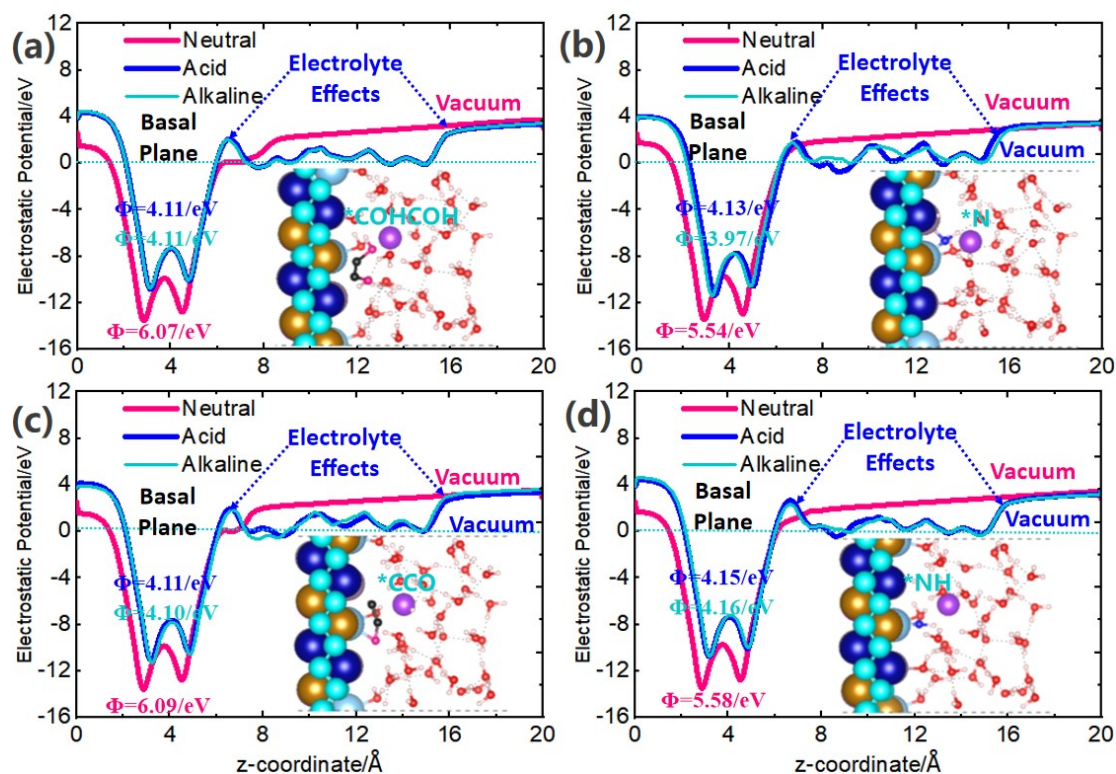


Figure S7. The electrostatic potential along z-direction slab model in neutral, acid and alkaline environments, a,c (Left) for CO₂RR and b,d for NitrRR (Right) intermediates, respectively.

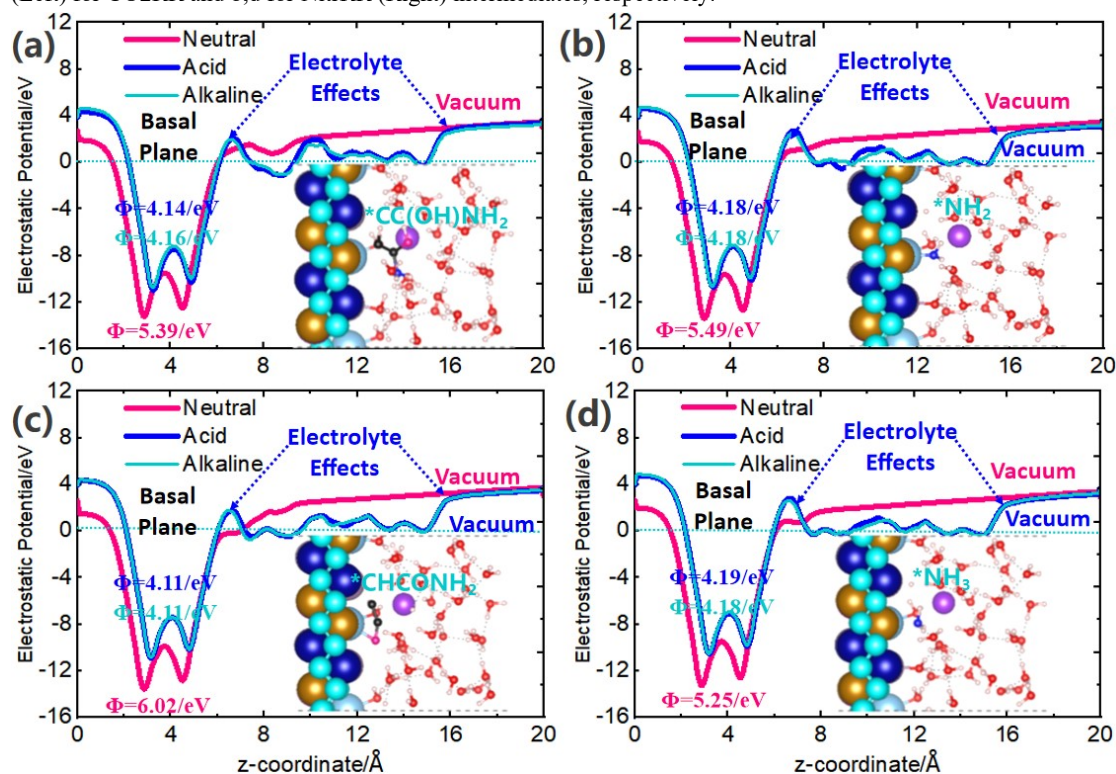


Figure S8. The electrostatic potential along z-direction slab model in neutral, acid and alkaline environments, a,c (Left) for CO₂RR and b,d for NitrRR (Right) intermediates, respectively.

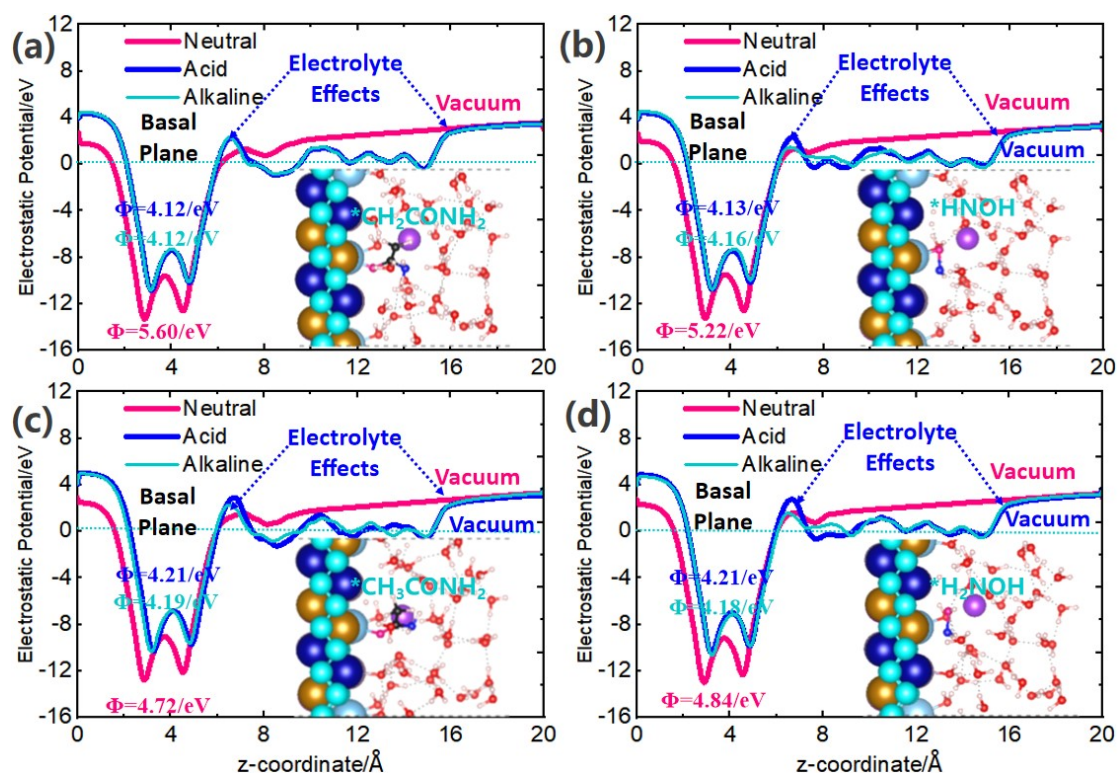


Figure S9. The electrostatic potential along z -direction slab model in neutral, acid and alkaline environments, a,c (Left) for CO₂RR and b,d for NitrRR (Right) intermediates, respectively.

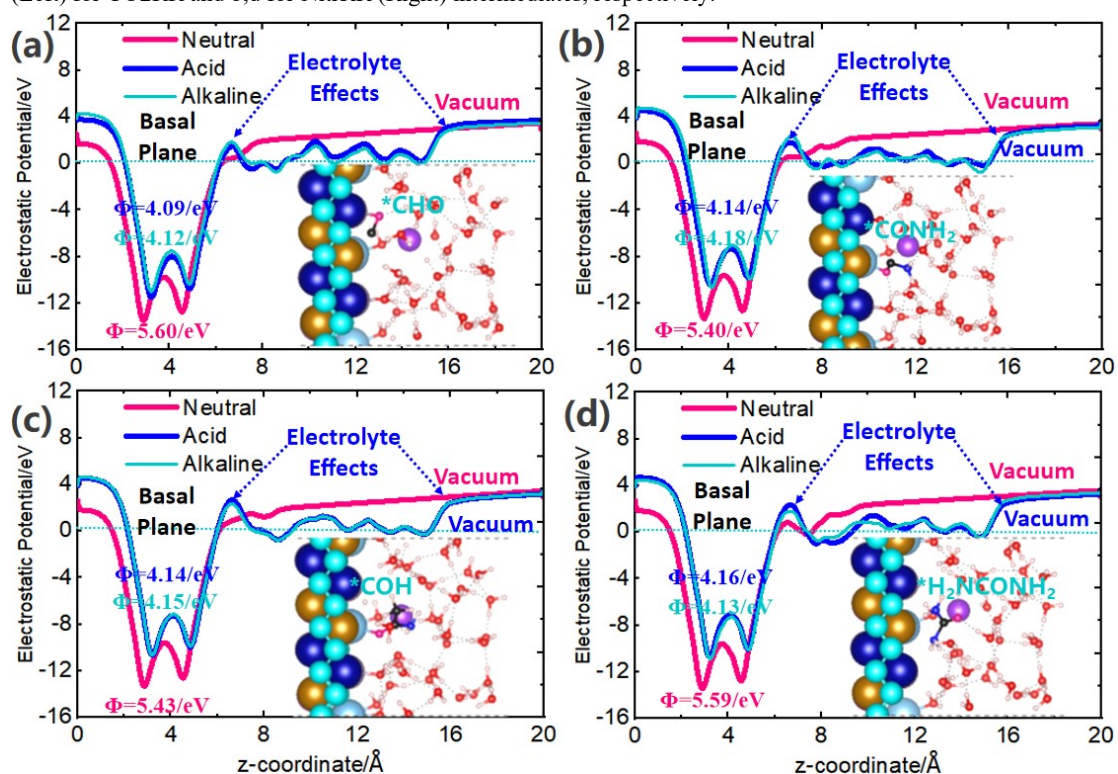


Figure S10. The electrostatic potential along z -direction slab model in neutral, acid and alkaline environments, a,c (Left) for CO₂RR and b,d for NitrRR (Right) intermediates, respectively.

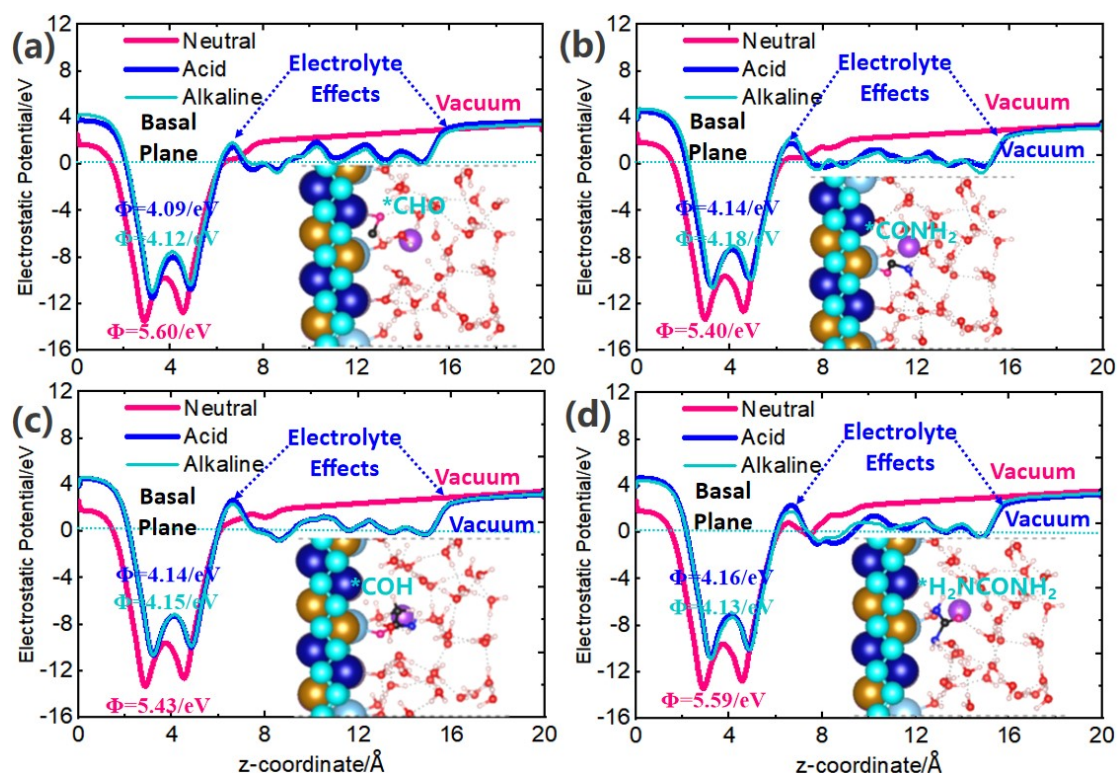


Figure S11. The electrostatic potential along z-direction slab model in neutral, acid and alkaline environments, a,c (Left) for CO₂RR and b,d for NitrRR (Right) intermediates, respectively.

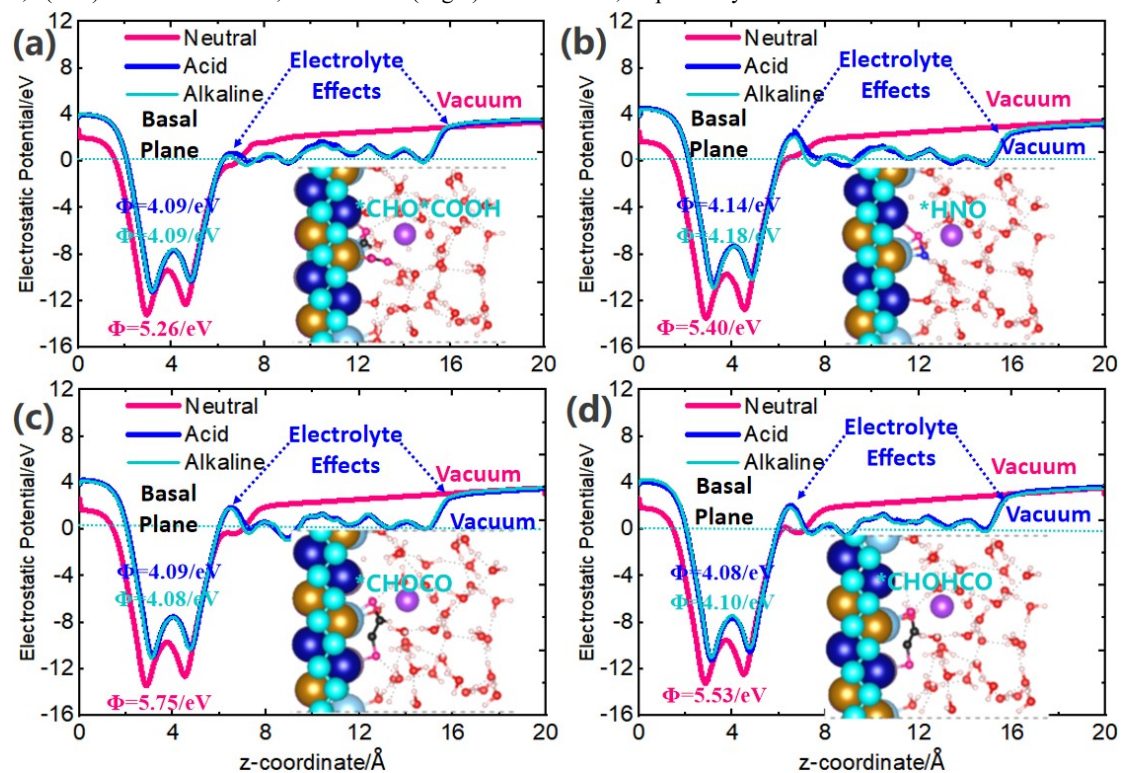
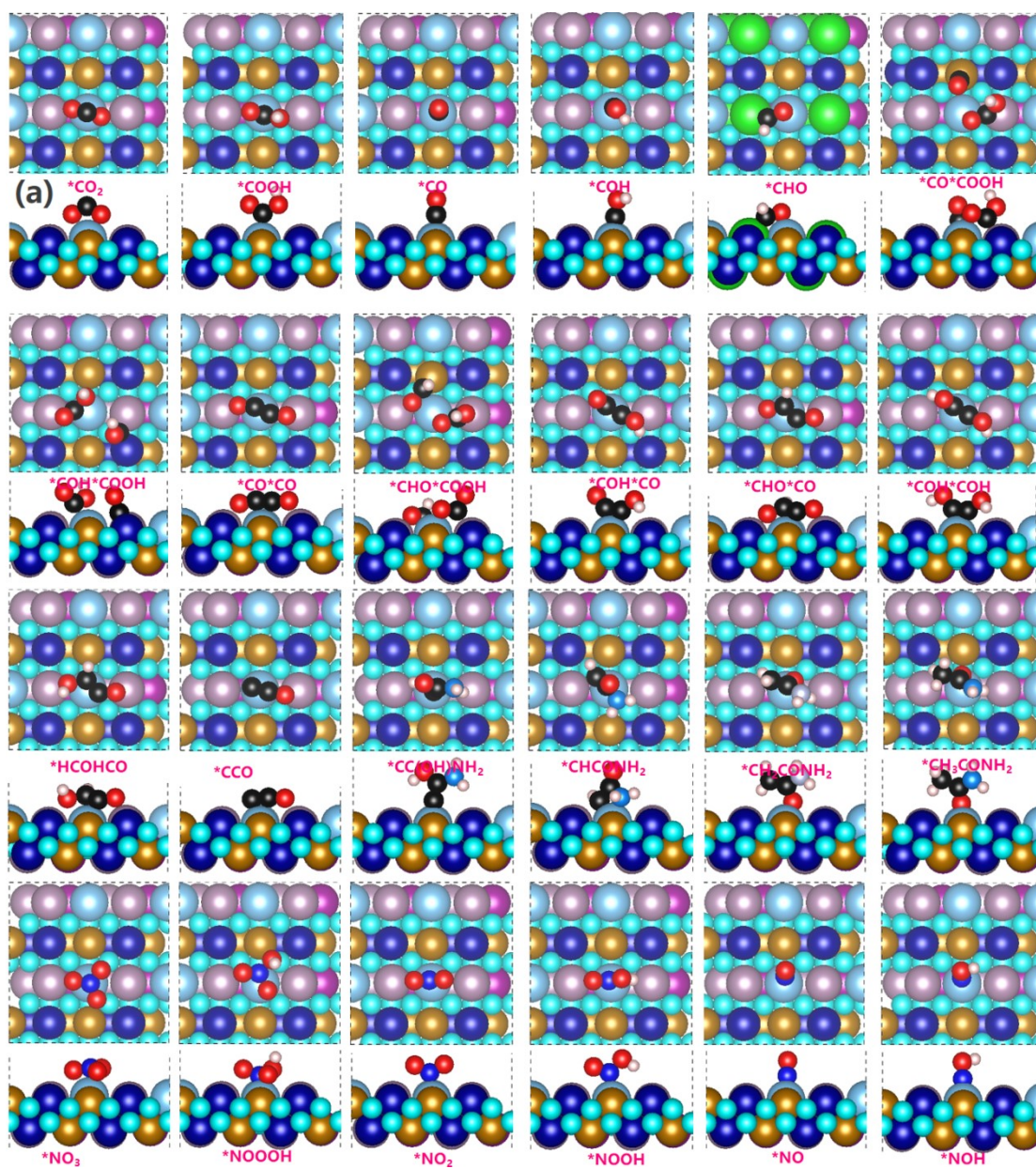


Figure S12. The electrostatic potential along z-direction slab model in neutral, acid and alkaline environments, a,c (Left) for CO₂RR and b,d for NitrRR (Right) intermediates, respectively.



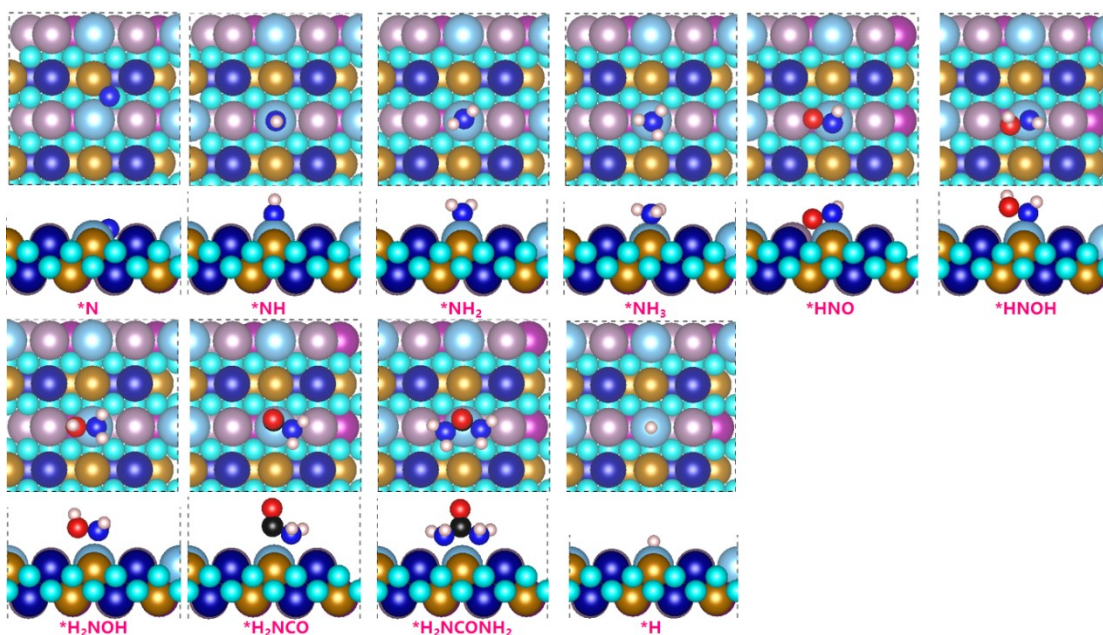


Figure S13. The corresponding binding configurations of various CO₂RR and NtrRR intermediates generated over TiCrMnFeMoB (HEBs) catalysts during acetamide synthesis in neutral environment.

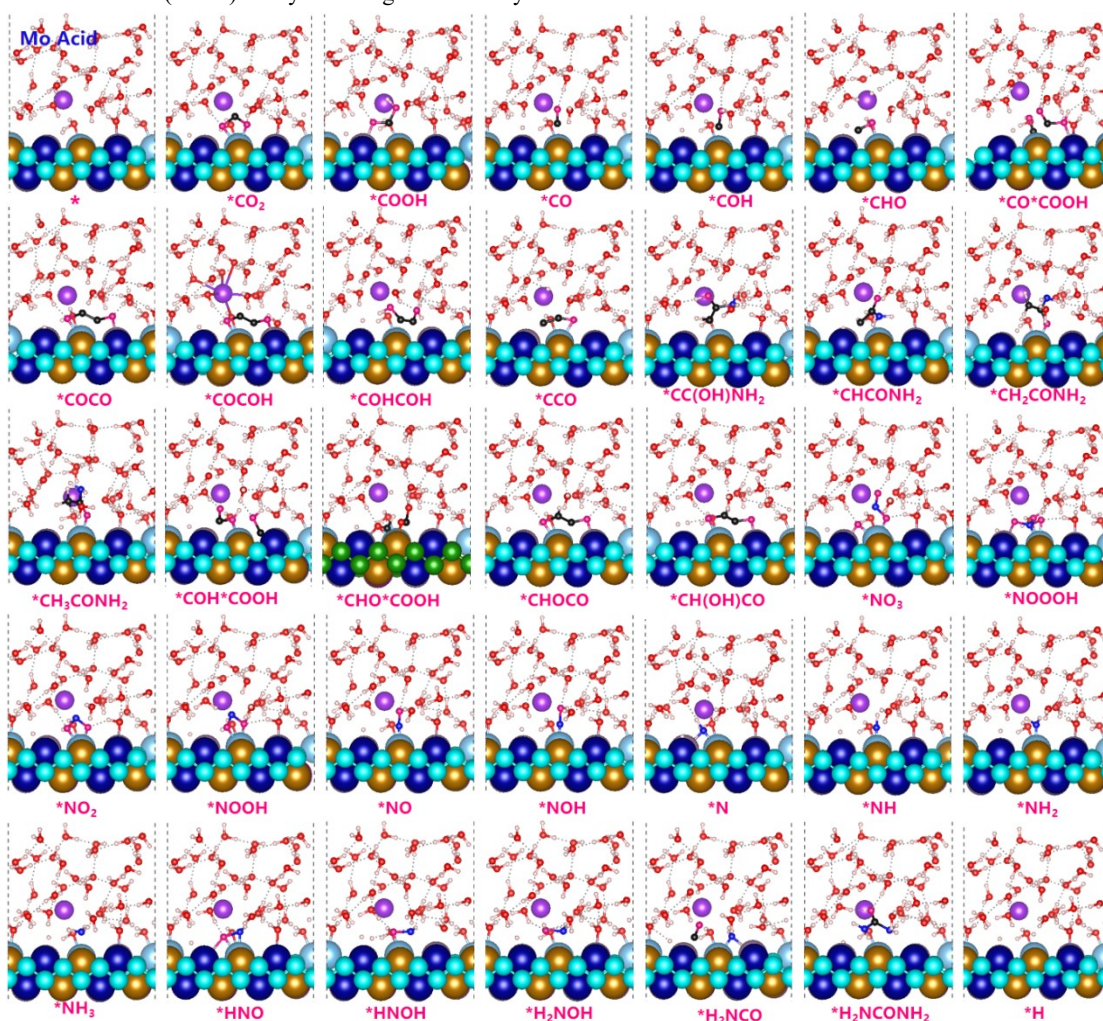


Figure S14. The corresponding binding configurations of various CO₂RR and NtrRR intermediates generated over TiCrMnFeMoB (HEBs) catalysts during acetamide synthesis in acid environment.

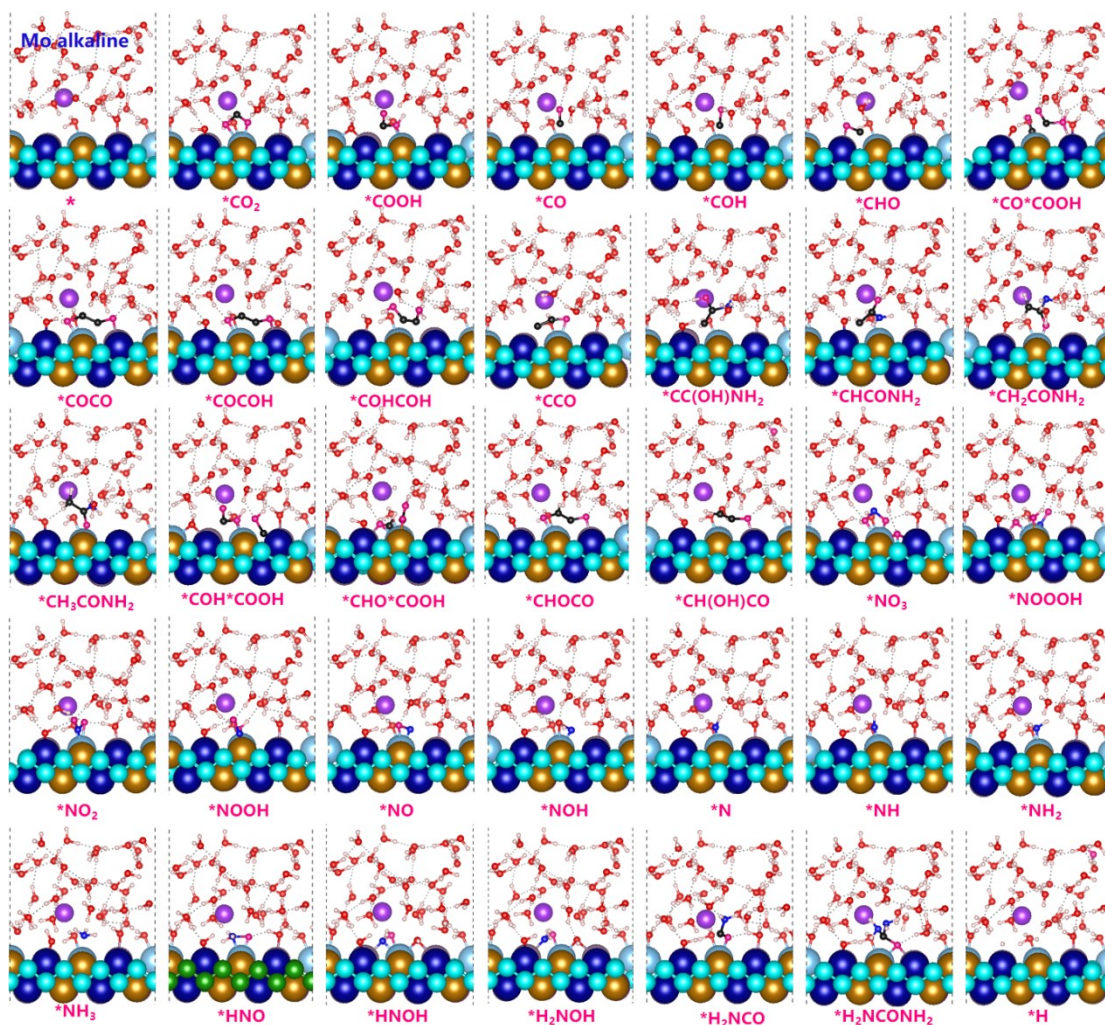


Figure S15. The corresponding binding configurations of various CO₂RR and NtrRR intermediates generated over TiCrMnFeMoB (HEBs) catalysts during acetamide synthesis in alkaline environment.

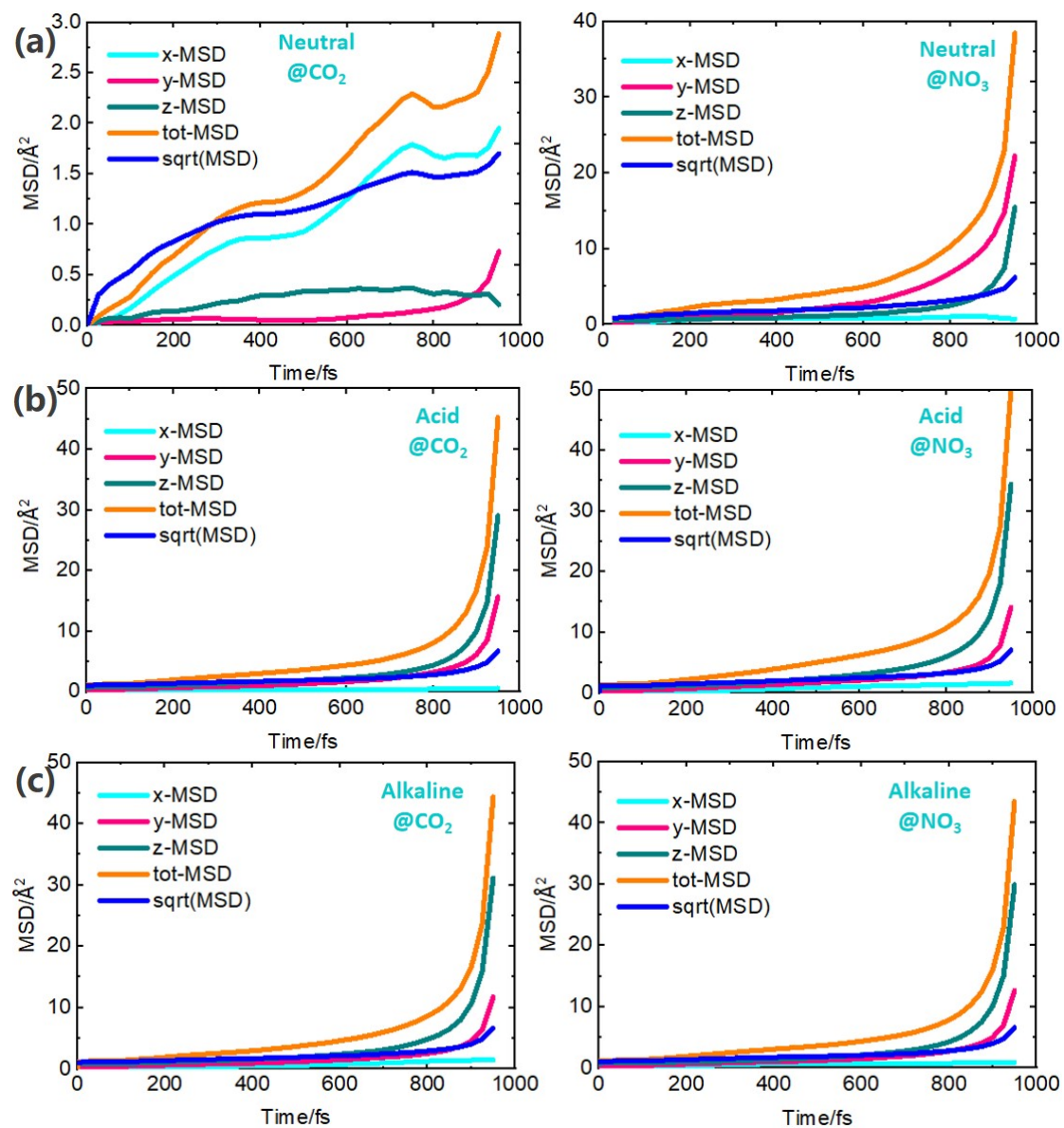


Figure S16. Time dependence of the mean square displacement (MSD) of the CO_2 (Left) and NO_3 (Right) adsorbed at neutral, acid and alkaline obtained by AIMD simulations, respectively.

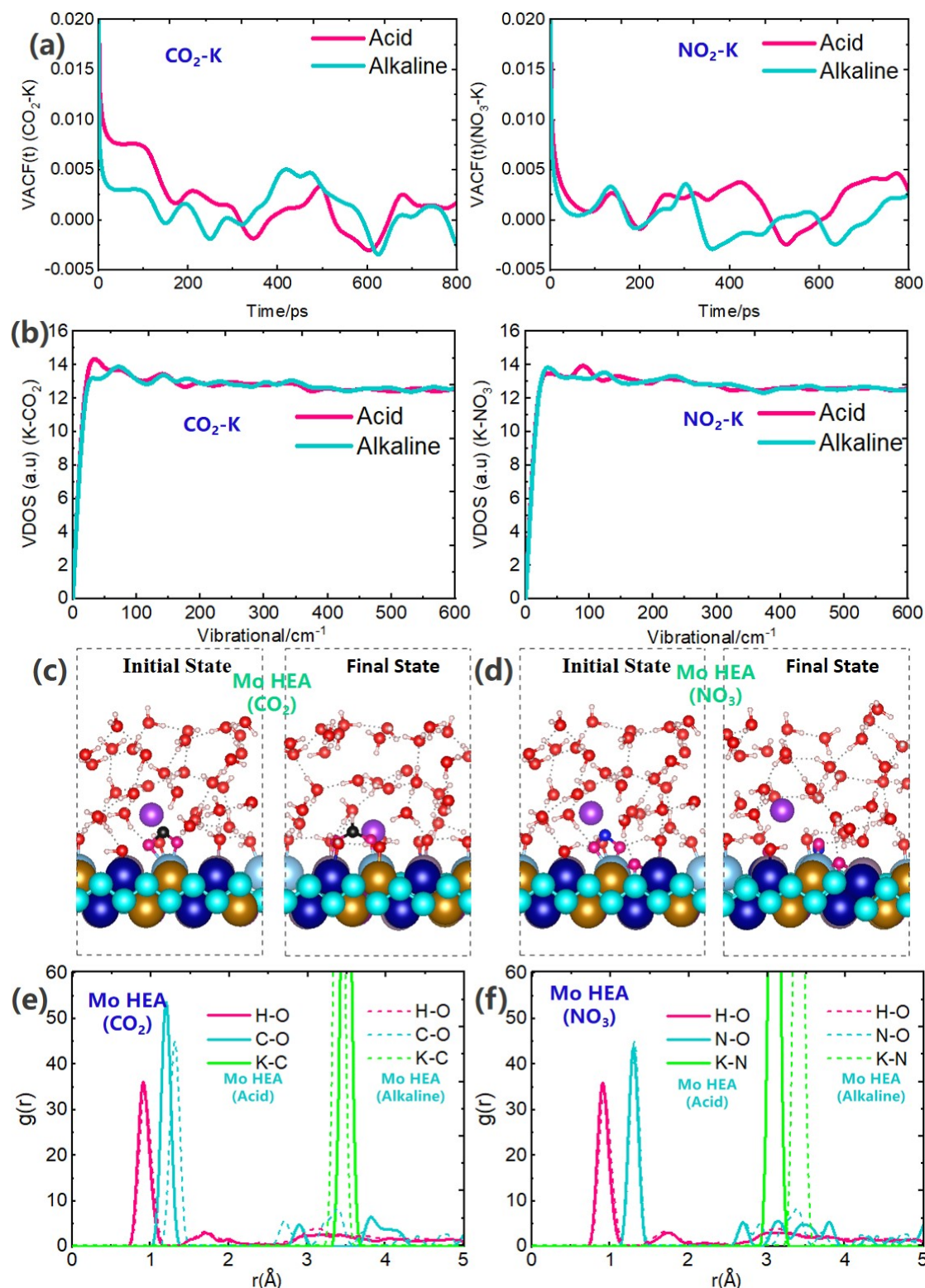


Figure S17. (a) The velocity autocorrelation function (VACF) of K⁺ cation in an aqueous acid solution over TiCrMnFeMoB (HEBs) catalysts for CO₂ (Left) and NO₃ (Right) adsorbed. (b) Vibrational density of states (VDOS) of K⁺ cation in an aqueous acid solution over TiCrMnFeMoB (HEBs) catalysts for CO₂ (Left) and NO₃ (Right) adsorbed. (c-d) AIMD snapshot of initial state and final state after 20ps simulation CO₂ (c) and NO₃ (d) adsorbed over TiCrMnFeMoB (HEBs) catalysts. (e-f) AIMD snapshot of radial distribution function (RDF) for O-H, C-O and K-C or K-N distance after 20ps simulation in CO₂ (e) and NO₃ (f) adsorbed over TiCrMnFeMoB (HEBs) catalysts, respectively.

Actually, in order to investigate the structural details involving in liquid–solid interface of the

CO₂RR to acetamide and urea, MD simulations were performed using a NVT ensemble at 300K. Fig 6c-d show the RDF between O atoms H atoms of cations HEB interface. The highest peak of RDF is relevant to O··H, and there is very low peak of RDF is relevant to O··H, which further confirms our previous conclusion that the CO₂ molecules prefer to attract with the K⁺. In addition, the highest peak of RDF occurs at 1.0 Å, indicating the hydrogen bonds form between O atoms and H atoms with 1.7~1.3 Å distance. The peak is high involving in the strong interaction in H₃O⁺ or OH⁻, it also indicates that the role of water is the solvation when K⁺ is added into the CO₂RR.

Fig 6e-f showed the RDF distribution of CO₂ molecules with K⁺ cations in the near the HEB surface and number of the H-bond around one CO₂ molecule. Within the 5 Å distance from the center of a CO₂ molecule. Moreover, it can be seen from the structures that most of CO₂ molecules easily attach around the K⁺ towards the C atom in CO₂ which is are consistent with our DFT results. Such structural distribution indicates the cation forms multi-ions synergistic catalytic mechanism by a mesoscale micro-environment, which will be elucidated in future work.

Table S1 The total Gibbs free energy of all CO₂RR and NtrRR intermediate species for acetamide and NH₃ or NH₂OH synthesis on TiCrMnFeMoB (HEBs) catalysts. * symbol represents the active states of intermediates.

System	Neutral	Acid	Alkaline	System	Neutral	Acid	Alkaline
Sur	-502.85	-1027.85	-1037.56	Sur	-502.85	-1027.85	-1037.56
*CO ₂	-525.95	-1052.28	-1060.79	*NO ₃	-529.14	-1057.78	-1066.03
*COOH	-528.38	-1056.78	-1063.34	*NOOOH	-532.99	-1060.44	-1069.60
*CO	-518.96	-1044.95	-1053.23	*NO ₂	-523.56	-1049.18	-1059.75
*CO+*COOH	-547.83	-1072.14	-1078.20	*NOOH	-526.96	-1053.33	-1064.01
*COCO	-535.05	-1061.41	-1069.85	*NO	-517.44	-1042.95	-1052.72
*COCOHO	-536.86	-1063.47	-1071.73	*NOH	-520.18	-1047.07	-1055.71
*COHCOH	-540.94	-1066.11	-1073.68	*N	-511.76	-1039.90	-1045.93
*CCO	-527.06	-1052.42	-1061.95	*NH	-515.18	-1042.31	-1049.18
*CC(OH)NH ₂	-545.91	-1072.60	-1080.77	*NH ₂	-519.67	-1045.57	-1052.59
*CHCONH ₂	-547.48	-1074.43	-1083.04	*NH ₃	-523.47	-1049.01	-1055.72
*CH ₂ CONH ₂	-551.80	-1076.63	-1084.89	*HNO	-522.02	-1047.59	-1055.38
*CH ₃ CONH ₂	-555.69	-1080.35	-1087.22	*HNOH	-524.65	-1050.74	-1060.85
*H	-506.03	-1031.69	-1041.69	*H ₂ NOH	-528.28	-1053.32	-1065.77
*COH	-520.49	-1046.01	-1053.87	*H ₂ NCO	-536.27	-1061.62	-1069.81
*CHO	-523.44	-1048.75	-1054.01	*H ₂ NCONH	-550.22	-1077.57	-1084.64
				2			
*COHCOOH	-549.23	-1074.82	-1082.77				
*CHOCOOH	-551.40	-1073.41	-1082.61				
*CHOCO	-539.35	-1064.53	-1072.30				
*CH(OH)CO	-542.24	-1067.57	-1076.14				

Table S2 The electrostatic potential, Fermi energy and work function of the charged system.

System	Vacu um	Work Function	E- fermi	System	Vacu um	Work Function	E- fermi	U _q (V/SHE) CO ₂ RR	U _q (V/SH E)NO ₃ RR
HEA	3.35	5.43	-2.09	HEA	3.35	5.43	-2.09	0.99	0.99
*CO ₂	3.57	5.88	-2.30	*NO ₃	3.56	5.76	-2.21	1.44	1.32
*COOH	3.53	5.68	-2.15	*NOOOH	3.54	5.71	-2.17	1.24	1.27

*CO	3.47	5.62	-2.15	*NO ₂	3.56	5.89	-2.33	1.18	1.45
*CO*COOH	3.54	5.59	-2.05	*NOOH	3.53	5.76	-2.22	1.15	1.32
*COCO	3.56	5.74	-2.19	*NO	3.50	5.75	-2.25	1.30	1.31
*COCOH	3.69	6.09	-2.40	*NOH	3.45	5.56	-2.11	1.65	1.12
*COHCOH	3.74	6.07	-2.33	*N	3.41	5.54	-2.14	1.63	1.10
*CCO	3.55	5.83	-2.28	*NH	3.43	5.58	-2.16	1.39	1.14
*CCOHNH ₂	3.46	5.39	-1.92	*NH ₂	3.44	5.49	-2.05	0.95	1.05
*CHCONH ₂	3.71	6.02	-2.32	*NH ₃	3.37	5.25	-1.88	1.58	0.81
*CH ₂ CONH ₂	3.58	5.60	-2.03	*HNO	3.48	5.65	-2.17	1.16	1.21
*CH ₃ CONH ₂	3.29	4.72	-1.44	*HNOH	3.33	5.22	-1.89	0.28	0.78
CH ₃ CONH ₂			0.00	*H ₂ NOH	3.23	4.84	-1.61		0.40
*H	3.40	5.63	-2.23					1.19	
*COH	3.42	5.43	-2.01	*H ₂ NCO	3.40	5.40	-2.01	0.99	0.96
*CHO	3.45	5.60	-2.15	*H ₂ NCO NH ₂	3.55	5.59	-2.04	1.16	1.15
*COHCOOH	3.47	5.45	-1.98	H ₂ NCON H ₂				1.01	
*CHOCOOH	3.36	5.26	-1.90					0.82	
*CHOCO	3.57	5.75	-2.19					1.31	
*CH(OH)CO	3.54	5.53	-1.99					1.09	
HEA acid	4.60	4.17	0.44	HEA acid	4.60	4.17	0.44	-0.28	-0.28
*CO ₂	4.25	4.12	0.13	*NO ₃	4.11	4.10	0.02	-0.32	-0.34
*COOH	4.65	4.16	0.49	*NOOOH	4.56	4.14	0.41	-0.28	-0.30
*CO	4.45	4.14	0.31	*NO ₂	4.36	4.12	0.24	-0.30	-0.32
*CO+*COO H	3.79	4.02	-0.23	*NOOH	4.42	4.14	0.28	-0.42	-0.30
*COCO	4.09	4.10	0.00	*NO	4.30	4.11	0.18	-0.35	-0.33
*COCOH	4.32	4.11	0.21	*NOH	4.42	4.14	0.28	-0.33	-0.30
*COHCOH	4.38	4.11	0.28	*N	4.01	4.13	-0.12	-0.33	-0.31
*CCO	4.14	4.11	0.03	*NH	4.45	4.15	0.30	-0.33	-0.29
*CCOHNH ₂	4.35	4.14	0.21	*NH ₂	4.62	4.18	0.44	-0.30	-0.27
*CHCONH ₂	4.35	4.11	0.24	*NH ₃	4.78	4.19	0.60	-0.33	-0.26
*CH ₂ CONH ₂	4.39	4.12	0.28	*HNO	4.55	4.15	0.39	-0.33	-0.29
*CH ₃ CONH ₂	5.02	4.21	0.81	*HNOH	4.42	4.13	0.29	-0.23	-0.31
CH ₃ CONH ₂			0.00	*H ₂ NOH	4.88	4.21	0.67		-0.23
*H	4.48	4.17	0.31					-0.27	
*COH	4.56	4.14	0.42	*H ₂ NCO	4.55	4.14	0.41	-0.30	-0.30
*CHO	3.77	4.09	-0.32	*H ₂ NCO NH ₂	4.70	4.16	0.54	-0.35	-0.28
*COHCOOH	4.66	4.14	0.52	H ₂ NCON H ₂				-0.30	
*CHOCOOH	4.00	4.09	-0.09					-0.35	
*CHOCO	4.22	4.09	0.13					-0.35	
*CH(OH)CO	4.09	4.08	0.00					-0.36	

HEA alkaline	4.25	4.14	0.11	HEA alkaline	4.25	4.14	0.11	-0.30	-0.30
*CO ₂	4.26	4.13	0.14	*NO ₃	4.43	4.12	0.32	-0.31	-0.32
*COOH	4.59	4.14	0.45	*NOOOH	4.13	4.11	0.02	-0.30	-0.33
*CO	4.54	4.15	0.39	*NO ₂	4.27	4.11	0.16	-0.29	-0.33
*CO*COOH	3.54	5.59	-2.05	*NOOH	4.54	4.15	0.40	1.15	-0.30
*COCO	4.10	4.09	0.01	*NO	4.18	4.11	0.07	-0.35	-0.33
*COCO ₂ H	4.32	4.10	0.23	*NOH	4.40	4.13	0.27	-0.34	-0.31
*COHCOH	4.48	4.11	0.36	*N	4.10	3.97	0.13	-0.33	-0.47
*CCO	3.91	4.09	-0.17	*NH	4.61	4.16	0.45	-0.36	-0.28
*CCOHNH ₂	4.63	4.16	0.48	*NH ₂	4.74	4.18	0.56	-0.28	-0.26
*CHCONH ₂	4.40	4.11	0.30	*NH ₃	4.88	4.18	0.70	-0.33	-0.26
*CH ₂ CONH ₂	4.49	4.12	0.36	*HNO	4.47	4.14	0.33	-0.32	-0.30
*CH ₃ CONH ₂	4.98	4.19	0.80	*HNOH	4.55	4.16	0.39	-0.26	-0.29
CH ₃ CONH ₂			0.00	*H ₂ NOH	4.72	4.18	0.53		-0.26
*H	4.48	4.17	0.31					-0.27	
*COH	4.64	4.15	0.49	*H ₂ NCO	4.78	4.18	0.60	-0.30	-0.26
*CHO	4.26	4.12	0.15	*H ₂ NCO NH ₂	4.46	4.13	0.33	-0.32	-0.31
*COHCOOH	4.60	4.12	0.49	H ₂ NCON H ₂				-0.32	
*CHOCOOH	4.05	4.09	-0.04					-0.36	
*CHOCO	4.16	4.08	0.08					-0.36	
*CH(OH)CO	4.30	4.10	0.20					-0.34	

Table S3 the Gibbs free energy of the gas molecular from the DFT calculation at 298.15 K (T).

CO ₂	-23.36583388	H ₂	-6.87426486	CH ₃ CONH ₂	-52.10930419	NO ₃	-23.31657567
NH ₃	-19.52793996	H ₂ O	-14.21570483	NH ₂ CONH 2	-46.49885425	*H ₂ NO H	-24.47159266

Table S4. Comparison of the CO₂RR performance of high-entropy alloy catalytic systems.

Reaction	Potential barrier	High-entropy alloy	Reaction	Potential barrier	High-entropy alloy
CO ₂ RR	1.996	AgScTiWZn	NRR	0.634	HfLaPbVZn
	2.041	AlInScTiY		0.639	CdLaPbTaV
	2.057	CrNbPbZnZr		0.672	NbPbRhTiY
	2.062	AuScTiVY		0.677	AuGaHfSnY
	2.076	CoHfHgScTi		0.678	CrReSnWZr
	2.084	AgAuFeHfLa		0.678	AlCrPbTiW
	2.094	HfPbScTiTi		0.687	AgHfPbScTi
	2.1	IrScTaTeTi		0.689	IrLaTaWY
	2.105	CdHfMoNbZn		0.692	BiPbScTiZr
	2.11	AlCdHfTaW		0.702	BiMnNiSnTi

Table S5. Summary of synthesis methods for HEAs electrocatalysts.

Catalyst	Structure	Synthetic method	Catalytic reaction	Ref.
PtPdRhNi and PtPdFeCoNi	FCC	Carbothermal shock	ORR	[1]
RuIrCeNi and RuIrCeNiWCuCrCo	FCC	Carbothermal shock	ORR and OER	[2]
PtNiFeCoCu	FCC	Colloidal synthesis	HER and MOR	[3]
PdFeCoNiCu	BCC	Colloidal synthesis	HER	[4]
RuFeCoNiCu	HCP	Colloidal synthesis	NRR	[5]
PdCuPtNiCo	FCC	Colloidal synthesis	ORR	[6]
MnFeCoNiCu	FCC	Solvothermal	OER	[7]
IrPdPtRhRu	FCC	Polyol method	HER	[8]
IrOsPdPtRhRu	FCC	Polyol method	EOR	[9]
IrOsReRhRu	HCP	Thermal decomposition	MOR	[0]
CoFeLaNiPt	Amorphous	Electrodeposition	OER and HER	[11]
FeCoPdIrPt	FCC	Fast moving bed pyrolysis	HER	[12]
AlNiCoIrMo	FCC	Dealloying	OER	[13]
AlNiCoFeX (X = Mo, Nb, and Cr)	FCC	Dealloying	OER	[14]
AlNiCoFeX (X = Mo, Nb, and Cr)	FCC	Dealloying	ORR and OER	[15]

The activity of a catalyst generally depends on its specific surface area, because larger surface areas expose more reactive sites. However, the current HEA fabrication methods (e.g., mechanical alloying, arc melting, magnetron sputtering, laser deposition, etc.) tend to produce bulk materials. Therefore, to reduce the sizes of HEAs and increase their specific surface areas, it is imperative to develop new synthetic methods for HEA preparation (Table).

Table S6 the adsorption energy and Bader charge transfer of the CO₂ and NO₃⁻ molecular from the DFT calculation.

Systems	Neutral		Acid		Alkaline	
	E _{ads}	Bader Charge	E _{ads}	Bader Charge	E _{ads}	Bader Charge
CO ₂	0.26958	0.738875	-1.06318	1.043732	0.14239	0.959345
NO ₃ ⁻	-2.97533	1.06417	-6.61591	0.090739	-5.14707	2.20659

Table S7 Total energies (E_{tot}) of *CO₂ and *NO₃ on HEB surfaces at different potentials (vs reversible hydrogen electrode).

U _{SHE}	-2	-1.5	-1	-0.5	0	0.5	1	1.5	2
Neutral	-507.03	-505.98	-504.94	-503.89	-502.85	-501.81	-500.76	-499.72	-498.67
*CO ₂	-530.55	-529.4	-528.25	-527.1	-525.95	-524.79	-523.64	-522.49	-521.34
Acid	-1026.98	-1027.2	-1027.41	-1027.63	-1027.85	-1028.07	-1028.29	-1028.51	-1028.72
*CO ₂	-1052.02	-1052.08	-1052.15	-1052.21	-1052.28	-1052.35	-1052.41	-1052.48	-1052.54
Alkaline	-1036.69	-1036.91	-1037.13	-1037.35	-1037.56	-1037.78	-1038	-1038.22	-1038.44
*CO ₂	-1060.53	-1060.59	-1060.66	-1060.72	-1060.79	-1060.85	-1060.92	-1060.98	-1061.05
Neutral	-507.03	-505.98	-504.94	-503.89	-502.85	-501.81	-500.76	-499.72	-498.67
*NO ₃	-533.55	-532.45	-531.35	-530.24	-529.14	-528.04	-526.94	-525.83	-524.73

Acid	-1026.98	-1027.2	-1027.41	-1027.63	-1027.85	-1028.07	-1028.29	-1028.51	-1028.72
*NO ₃	-1057.75	-1057.76	-1057.77	-1057.78	-1057.78	-1057.79	-1057.8	-1057.81	-1057.82
Mo alkaline	-1037.35	-1037.4	-1037.46	-1037.51	-1037.56	-1037.62	-1037.67	-1037.72	-1037.78
*NO ₃	-1065.4	-1065.55	-1065.71	-1065.87	-1066.03	-1066.18	-1066.34	-1066.5	-1066.66

Table S8 Binding energies of *CO₂ and *NO₃ on HEB surfaces at different potentials (vs reversible hydrogen electrode).

Applied Potential	-2.00	-1.50	-1.00	-0.50	0.00	0.50	1.00	1.50	2.00
U _{SHE}	-0.16	-0.05	0.05	0.16	0.27	0.38	0.48	0.59	0.7
Acid *CO ₂	-1.68	-1.52	-1.37	-1.22	-1.06	-0.91	-0.76	-0.6	-0.45
Akaline *CO ₂	-0.47	-0.32	-0.16	-0.01	0.14	0.3	0.45	0.6	0.75
Neutral *NO ₃	-3.21	-3.15	-3.09	-3.03	-2.98	-2.92	-2.86	-2.8	-2.74
Acid *NO ₃	-7.46	-7.25	-7.04	-6.83	-6.62	-6.41	-6.19	-5.98	-5.77
Akaline *NO ₃	-4.73	-4.84	-4.94	-5.04	-5.15	-5.25	-5.36	-5.46	-5.56

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