## Supplementary Information for "First Principles Unveiling the Metallic $TaS_2/GeC$ Heterostructure as an Anode material in Sodium-Ion Batteries"

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TABLE S1: Several geometric parameters of the  $TaS_2/GeC$  structure during the Na ion adsorption and intercalation process. The symbols used in the table are explained in Figure S1.

Number of adsorbed Na layers	h (Å)	$d_{int}(\mathring{A})$	$d_1$ (Ta–S) (Å)	$d_2$ (Ta–S) (Å)	$\Delta_{\mathrm{Ge-C}}$ (Å)
0	6.02	2.87	2.46	2.46	0.10
1	6.11	2.97	2.48	2.45	0.10
2	7.17	3.99	2.47	2.47	0.49
3	7.68	4.01	2.47	2.47	0.49
4	7.69	3.94	2.47	2.47	0.60
5	7.70	3.94	2.47	2.47	0.59



FIG. 1: Projected band structures of TaS2/GeC heterostructure (a) without and (b) with presence of spin-orbit coupling. Blue and yellow lines represent the contributions of the TaS2 and GeC layer, respectively



FIG. S2: Several geometric parameters of the TaS<sub>2</sub>/GeC structure during the Na ion adsorption and intercalation process. Here, h denotes the thickness of the TaS<sub>2</sub>/GeC heterostructure,  $d_{int}$  is the interlayer distance, and  $d_1$ (Ta–S) and  $d_2$ (Ta–S) represent the Ta–S bond lengths in the outer and inner layers of the TaS<sub>2</sub> monolayer, respectively.  $\Delta_{Ge-C}$  indicates the buckling height of the GeC layer.

TABLE S2: Average charge transfer of Na layers in different Na–TaS<sub>2</sub>–GeC configurations.

Configuration	Na layers	Average charge transfer (e)	Notes	
$Na-TaS_2-GeC$	1	-0.50	1st Na layer on top of $TaS_2$	
Na-TaS <sub>2</sub> -Na-GeC	2	-0.47	1st Na layer on top of $TaS_2$	
		-0.80	2nd Na layer between $TaS_2$ and $GeC$	
Na <sub>2</sub> -TaS <sub>2</sub> -Na-GeC	3	-0.01	3rd Na layer on top of $TaS_2$	
		-0.43	1st Na layer on top of $TaS_2$	
		-0.80	2nd Na layer between $TaS_2$ and $GeC$	
Na <sub>2</sub> -TaS <sub>2</sub> -Na-GeC-Na	4	-0.02	3rd Na layer on top of $TaS_2$	
		-0.44	1st Na layer on top of $TaS_2$	
		-0.80	2th Na layer between TaS <sub>2</sub> and GeC	
		-0.46	4th Na layer on top of GeC	
Na <sub>2</sub> -TaS <sub>2</sub> -Na-GeC-Na <sub>2</sub>	5	-0.02	3rd Na layer on top of $TaS_2$	
		-0.45	1st Na layer on top of $TaS_2$	
		-0.80	2nd Na layer between $TaS_2$ and $GeC$	
		-0.48	$4\mathrm{th}$ Na layer on top of GeC	
		-0.01	5th Na layer on top of GeC	



FIG. S3: Side view of the geometric structures of the pristine  $TaS_2/GeC$  system and with Na atoms adsorbed/intercalated at various concentrations: (a) pristine structure; (b)–(f) structures with 1 to 5 Na layers adsorbed/intercalated, respectively.



FIG. S4: Partial density of states (PDOS) of the pristine  $TaS_2/GeC$  system and with Na atoms adsorbed/intercalated at different concentrations: (a) pristine structure; (b)–(f) structures with 1 to 5 layers of Na, respectively. The green and purple curves indicate the PDOS of  $TaS_2/GeC$  and the adsorbed/intercalated Na atoms, respectively.