

1 **Supplementary Material**

2 **for**

3 **Development and Evaluation of Operational Parameter Driven Mechanistic and**
4 **Empirical Kinetic Models for Photocatalytic Degradation of Emerging Contaminants**

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24 Appendix A: Data used for modeling

25 **Table S1. Dataset 1 extracted using Plot Digitizer [1]**

Material	Time (min)	Dose (g/L)	Initial Concentration (mg/L)	Light Intensity (W)	Removal (%)
P-1	0	0.2	5	50	0
P-1	30	0.2	5	50	12.25806452
P-1	60	0.2	5	50	19.35483871
P-1	90	0.2	5	50	27.09677419
P-1	120	0.2	5	50	30.32258065
P-1	0	0.4	5	50	0
P-1	30	0.4	5	50	14.38848921
P-1	60	0.4	5	50	24.46043165
P-1	90	0.4	5	50	38.84892086
P-1	120	0.4	5	50	46.04316547
P-1	0	0.6	5	50	0
P-1	30	0.6	5	50	36.43410853
P-1	60	0.6	5	50	59.68992248
P-1	90	0.6	5	50	70.54263566
P-1	120	0.6	5	50	78.29457364
P-1	0	0.8	5	50	0
P-1	30	0.8	5	50	52
P-1	60	0.8	5	50	74.4
P-1	90	0.8	5	50	84
P-1	120	0.8	5	50	88.8
P-1	0	1.2	5	50	0
P-1	30	1.2	5	50	33.96226415
P-1	60	1.2	5	50	47.16981132
P-1	90	1.2	5	50	63.20754717
P-1	120	1.2	5	50	67.9245283
P-1	0	0.8	1	50	0
P-1	30	0.8	1	50	22.83950617
P-1	60	0.8	1	50	45.0617284
P-1	90	0.8	1	50	57.40740741
P-1	120	0.8	1	50	63.58024691
P-1	0	0.8	2	50	0
P-1	30	0.8	2	50	31.12582781
P-1	60	0.8	2	50	54.96688742
P-1	90	0.8	2	50	69.53642384
P-1	120	0.8	2	50	74.17218543
P-1	0	0.8	5	50	0
P-1	30	0.8	5	50	52.41935484
P-1	60	0.8	5	50	74.19354839
P-1	90	0.8	5	50	83.87096774
P-1	120	0.8	5	50	88.70967742
P-1	0	0.8	8	50	0
P-1	30	0.8	8	50	40.625
P-1	60	0.8	8	50	60.15625

P-1	90	0.8	8	50	72.65625
P-1	120	0.8	8	50	78.125
P-1	0	0.8	10	50	0
P-1	30	0.8	10	50	34.32835821
P-1	60	0.8	10	50	50
P-1	90	0.8	10	50	61.19402985
P-1	120	0.8	10	50	66.41791045

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27 **Table S2. Dataset 2 extracted using Plot Digitizer [1]**

Material	Time (min)	Dose (g/L)	Initial		Removal (%)
			Concentration (mg/L)	Light Intensity (W)	
P-1	0	0.2	5	50	0
P-1	30	0.2	5	50	11.53846154
P-1	60	0.2	5	50	15.38461538
P-1	90	0.2	5	50	19.23076923
P-1	120	0.2	5	50	23.71794872
P-1	0	0.4	5	50	0
P-1	30	0.4	5	50	30
P-1	60	0.4	5	50	44.66666667
P-1	90	0.4	5	50	54
P-1	120	0.4	5	50	60.66666667
P-1	0	0.4	5	50	0
P-1	30	0.6	5	50	43.88489209
P-1	60	0.6	5	50	69.78417266
P-1	90	0.6	5	50	82.01438849
P-1	120	0.6	5	50	86.33093525
P-1	0	0.8	5	50	0
P-1	30	0.8	5	50	63.07692308
P-1	60	0.8	5	50	83.07692308
P-1	90	0.8	5	50	91.53846154
P-1	120	0.8	5	50	94.61538462
P-1	0	1.2	5	50	0
P-1	30	1.2	5	50	48.71794872
P-1	60	1.2	5	50	65.81196581
P-1	90	1.2	5	50	76.92307692
P-1	120	1.2	5	50	82.90598291
P-1	0	0.8	1	50	0
P-1	30	0.8	1	50	25.30120482
P-1	60	0.8	1	50	52.40963855
P-1	90	0.8	1	50	63.25301205
P-1	120	0.8	1	50	69.27710843
P-1	0	0.8	2	50	0
P-1	30	0.8	2	50	28.48101266
P-1	60	0.8	2	50	61.39240506
P-1	90	0.8	2	50	74.6835443
P-1	120	0.8	2	50	79.74683544
P-1	0	0.8	5	50	0

P-1	30	0.8	5	50	62.79069767
P-1	60	0.8	5	50	82.94573643
P-1	90	0.8	5	50	91.47286822
P-1	120	0.8	5	50	94.57364341
P-1	0	0.8	8	50	0
P-1	30	0.8	8	50	51.85185185
P-1	60	0.8	8	50	68.88888889
P-1	90	0.8	8	50	82.22222222
P-1	120	0.8	8	50	85.18518519
P-1	0	0.8	10	50	0
P-1	30	0.8	10	50	36.55172414
P-1	60	0.8	10	50	57.93103448
P-1	90	0.8	10	50	71.72413793
P-1	120	0.8	10	50	75.17241379

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29 **Table S3. Dataset 3 extracted using Plot Digitizer [2]**

Material	Time (min)	Dose (g/L)	Initial Concentration (mg/L)	Light Intensity (W)	Removal (%)
P-2	0	0.5	5	50	0
P-2	20	0.5	5	50	69.82758621
P-2	40	0.5	5	50	100
P-2	60	0.5	5	50	101.7241379
P-2	80	0.5	5	50	101.7241379
P-2	0	0.5	10	50	0
P-2	20	0.5	10	50	70.83333333
P-2	40	0.5	10	50	100
P-2	60	0.5	10	50	101.1904762
P-2	80	0.5	10	50	98.80952381
P-2	0	0.5	20	50	0
P-2	20	0.5	20	50	65.40540541
P-2	40	0.5	20	50	88.10810811
P-2	60	0.5	20	50	96.21621622
P-2	80	0.5	20	50	98.91891892
P-2	0	0.5	50	50	0
P-2	20	0.5	50	50	42.26804124
P-2	40	0.5	50	50	57.21649485
P-2	60	0.5	50	50	73.19587629
P-2	80	0.5	50	50	75.77319588
P-2	0	0.5	75	50	0
P-2	20	0.5	75	50	35.02538071
P-2	40	0.5	75	50	47.71573604
P-2	60	0.5	75	50	56.85279188
P-2	80	0.5	75	50	64.97461929
P-2	0	0.5	100	50	0
P-2	20	0.5	100	50	18.27411168
P-2	40	0.5	100	50	33.50253807
P-2	60	0.5	100	50	44.16243655

P-2	80	0.5	100	50	49.23857868
P-2	0	0.1	20	50	0
P-2	20	0.1	20	50	36.50793651
P-2	40	0.1	20	50	57.14285714
P-2	60	0.1	20	50	68.78306878
P-2	80	0.1	20	50	78.83597884
P-2	0	0.25	20	50	0
P-2	20	0.25	20	50	61.95652174
P-2	40	0.25	20	50	79.89130435
P-2	60	0.25	20	50	86.95652174
P-2	80	0.25	20	50	92.93478261
P-2	0	0.5	20	50	0
P-2	20	0.5	20	50	66.12903226
P-2	40	0.5	20	50	89.78494624
P-2	60	0.5	20	50	98.92473118
P-2	80	0.5	20	50	100
P-2	0	0.75	20	50	0
P-2	20	0.75	20	50	64.80446927
P-2	40	0.75	20	50	84.3575419
P-2	60	0.75	20	50	93.29608939
P-2	80	0.75	20	50	97.20670391
P-2	0	1	20	50	0
P-2	20	1	20	50	53.84615385
P-2	40	1	20	50	73.96449704
P-2	60	1	20	50	85.79881657
P-2	80	1	20	50	92.30769231
P-2	0	2	20	50	0
P-2	20	2	20	50	48.04469274
P-2	40	2	20	50	65.92178771
P-2	60	2	20	50	78.2122905
P-2	80	2	20	50	84.3575419

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31 **Table S4. Dataset 4 extracted using Plot Digitizer [3]**

Material	Time (min)	Dose (g/L)	Initial		Removal (%)
			Concentration (mg/L)	Light Intensity (W)	
P-3	0	0.1	10	50	0
P-3	30	0.1	10	50	14.74358974
P-3	60	0.1	10	50	26.28205128
P-3	90	0.1	10	50	34.61538462
P-3	120	0.1	10	50	37.17948718
P-3	0	0.25	10	50	0
P-3	30	0.25	10	50	30.40540541
P-3	60	0.25	10	50	47.97297297
P-3	90	0.25	10	50	56.75675676
P-3	120	0.25	10	50	61.48648649
P-3	0	0.5	10	50	0
P-3	30	0.5	10	50	41.72661871

P-3	60	0.5	10	50	64.74820144
P-3	90	0.5	10	50	73.38129496
P-3	120	0.5	10	50	82.01438849
P-3	0	0.75	10	50	0
P-3	30	0.75	10	50	47.79411765
P-3	60	0.75	10	50	72.79411765
P-3	90	0.75	10	50	84.55882353
P-3	120	0.75	10	50	93.38235294
P-3	0	0.75	10	50	0
P-3	30	1	10	50	40.76923077
P-3	60	1	10	50	66.15384615
P-3	90	1	10	50	81.53846154
P-3	120	1	10	50	87.69230769
P-3	0	0.75	1	50	0
P-3	30	0.75	1	50	30.26315789
P-3	60	0.75	1	50	53.28947368
P-3	90	0.75	1	50	66.44736842
P-3	120	0.75	1	50	75
P-3	0	0.75	5	50	0
P-3	30	0.75	5	50	38.29787234
P-3	60	0.75	5	50	63.82978723
P-3	90	0.75	5	50	75.17730496
P-3	120	0.75	5	50	80.85106383
P-3	0	0.75	10	50	0
P-3	30	0.75	10	50	47.05882353
P-3	60	0.75	10	50	72.05882353
P-3	90	0.75	10	50	84.55882353
P-3	120	0.75	10	50	92.64705882
P-3	0	0.75	15	50	0
P-3	30	0.75	15	50	29.57746479
P-3	60	0.75	15	50	54.22535211
P-3	90	0.75	15	50	69.71830986
P-3	120	0.75	15	50	77.46478873
P-3	0	0.75	20	50	0
P-3	30	0.75	20	50	28.18791946
P-3	60	0.75	20	50	48.99328859
P-3	90	0.75	20	50	63.75838926
P-3	120	0.75	20	50	70.46979866

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33 **Table S5. Dataset 5 extracted using Plot Digitizer [4]**

Material	Time (min)	Dose (g/L)	Initial		Removal (%)
			Concentration (mg/L)	Light Intensity (W)	
P-4	0	0.25	20	50	0
P-4	20	0.25	20	50	58.57142857
P-4	40	0.25	20	50	74.28571429
P-4	60	0.25	20	50	80
P-4	80	0.25	20	50	85.71428571

P-4	0	0.5	20	50	0
P-4	20	0.5	20	50	76.19047619
P-4	40	0.5	20	50	88.88888889
P-4	60	0.5	20	50	93.65079365
P-4	80	0.5	20	50	95.23809524
P-4	0	0.75	20	50	0
P-4	20	0.75	20	50	81.96721311
P-4	40	0.75	20	50	93.44262295
P-4	60	0.75	20	50	96.72131148
P-4	80	0.75	20	50	98.36065574
P-4	0	1	20	50	0
P-4	20	1	20	50	87.5
P-4	40	1	20	50	96.42857143
P-4	60	1	20	50	100
P-4	80	1	20	50	96.42857143
P-4	0	2	20	50	0
P-4	20	2	20	50	57.35294118
P-4	40	2	20	50	67.64705882
P-4	60	2	20	50	72.05882353
P-4	80	2	20	50	73.52941176
P-4	0	0.5	5	50	0
P-4	20	0.5	5	50	80.76923077
P-4	40	0.5	5	50	100
P-4	60	0.5	5	50	100
P-4	80	0.5	5	50	100
P-4	0	0.5	10	50	0
P-4	20	0.5	10	50	79.31034483
P-4	40	0.5	10	50	91.37931034
P-4	60	0.5	10	50	94.82758621
P-4	80	0.5	10	50	98.27586207
P-4	0	0.5	20	50	0
P-4	20	0.5	20	50	77.77777778
P-4	40	0.5	20	50	90.47619048
P-4	60	0.5	20	50	93.65079365
P-4	80	0.5	20	50	96.82539683
P-4	0	0.5	25	50	0
P-4	20	0.5	25	50	63.63636364
P-4	40	0.5	25	50	83.33333333
P-4	60	0.5	25	50	87.87878788
P-4	80	0.5	25	50	90.90909091
P-4	0	0.5	40	50	0
P-4	20	0.5	40	50	44.87179487
P-4	40	0.5	40	50	69.23076923
P-4	60	0.5	40	50	76.92307692
P-4	80	0.5	40	50	80.76923077

37 **Table S6. Dataset 6 extracted using Plot Digitizer [5]**

Material	Time (min)	Dose (g/L)	Initial Concentration (mg/L)	Light Intensity (W)	Removal (%)
P-5	0	0.4	100	16	0
P-5	40	0.4	100	16	64.61538462
P-5	50	0.4	100	16	74.87179487
P-5	60	0.4	100	16	80
P-5	75	0.4	100	16	86.66666667
P-5	90	0.4	100	16	88.71794872
P-5	105	0.4	100	16	89.74358974
P-5	120	0.4	100	16	90.25641026
P-5	135	0.4	100	16	91.79487179
P-5	150	0.4	100	16	93.84615385
P-5	0	0.4	150	16	0
P-5	40	0.4	150	16	58.97435897
P-5	50	0.4	150	16	68.71794872
P-5	60	0.4	150	16	74.35897436
P-5	75	0.4	150	16	82.56410256
P-5	90	0.4	150	16	83.58974359
P-5	105	0.4	150	16	84.61538462
P-5	120	0.4	150	16	85.64102564
P-5	135	0.4	150	16	86.15384615
P-5	150	0.4	150	16	88.20512821
P-5	0	0.4	200	16	0
P-5	40	0.4	200	16	47.17948718
P-5	50	0.4	200	16	57.43589744
P-5	60	0.4	200	16	63.07692308
P-5	75	0.4	200	16	70.25641026
P-5	90	0.4	200	16	73.84615385
P-5	105	0.4	200	16	74.35897436
P-5	120	0.4	200	16	74.35897436
P-5	135	0.4	200	16	74.87179487
P-5	150	0.4	200	16	75.38461538
P-5	0	0.4	250	16	0
P-5	40	0.4	250	16	43.58974359
P-5	50	0.4	250	16	52.82051282
P-5	60	0.4	250	16	56.92307692
P-5	75	0.4	250	16	61.02564103
P-5	90	0.4	250	16	63.58974359
P-5	105	0.4	250	16	63.07692308
P-5	120	0.4	250	16	62.56410256
P-5	135	0.4	250	16	62.56410256
P-5	150	0.4	250	16	62.05128205
P-5	0	0.2	150	16	0
P-5	30	0.2	150	16	37.03703704
P-5	40	0.2	150	16	56.61375661

P-5	50	0.2	150	16	67.72486772
P-5	60	0.2	150	16	71.42857143
P-5	75	0.2	150	16	74.6031746
P-5	90	0.2	150	16	74.6031746
P-5	105	0.2	150	16	75.13227513
P-5	120	0.2	150	16	77.77777778
P-5	135	0.2	150	16	79.36507937
P-5	150	0.2	150	16	78.30687831
P-5	0	0.4	150	16	-1.058201058
P-5	30	0.4	150	16	37.03703704
P-5	40	0.4	150	16	56.61375661
P-5	50	0.4	150	16	67.72486772
P-5	60	0.4	150	16	75.66137566
P-5	75	0.4	150	16	83.06878307
P-5	90	0.4	150	16	85.18518519
P-5	105	0.4	150	16	86.77248677
P-5	120	0.4	150	16	88.35978836
P-5	135	0.4	150	16	86.77248677
P-5	150	0.4	150	16	89.94708995
P-5	0	0.5	150	16	-1.058201058
P-5	30	0.5	150	16	44.97354497
P-5	40	0.5	150	16	59.78835979
P-5	50	0.5	150	16	75.13227513
P-5	60	0.5	150	16	82.01058201
P-5	75	0.5	150	16	88.35978836
P-5	90	0.5	150	16	90.47619048
P-5	105	0.5	150	16	91.53439153
P-5	120	0.5	150	16	92.06349206
P-5	135	0.5	150	16	93.12169312
P-5	150	0.5	150	16	94.17989418
P-5	0	0.6	150	16	-0.529100529
P-5	30	0.6	150	16	44.97354497
P-5	40	0.6	150	16	59.78835979
P-5	50	0.6	150	16	77.77777778
P-5	60	0.6	150	16	84.12698413
P-5	75	0.6	150	16	88.35978836
P-5	90	0.6	150	16	92.59259259
P-5	105	0.6	150	16	93.65079365
P-5	120	0.6	150	16	94.70899471
P-5	135	0.6	150	16	93.12169312
P-5	150	0.6	150	16	96.82539683
P-5	0	0.7	150	16	0
P-5	30	0.7	150	16	50.79365079
P-5	40	0.7	150	16	67.72486772
P-5	50	0.7	150	16	77.77777778
P-5	60	0.7	150	16	84.12698413
P-5	75	0.7	150	16	91.53439153
P-5	90	0.7	150	16	92.59259259

P-5	105	0.7	150	16	93.65079365
P-5	120	0.7	150	16	94.70899471
P-5	135	0.7	150	16	96.82539683
P-5	150	0.7	150	16	96.82539683
P-5	0	0.9	150	16	0
P-5	30	0.9	150	16	75.66137566
P-5	40	0.9	150	16	93.12169312
P-5	50	0.9	150	16	96.2962963
P-5	60	0.9	150	16	97.35449735
P-5	75	0.9	150	16	97.35449735
P-5	90	0.9	150	16	98.94179894
P-5	105	0.9	150	16	98.94179894
P-5	120	0.9	150	16	100
P-5	135	0.9	150	16	100.5291005
P-5	150	0.9	150	16	100.5291005
P-5	0	0.6	150	8	1.477832512
P-5	30	0.6	150	8	44.82758621
P-5	40	0.6	150	8	57.63546798
P-5	50	0.6	150	8	65.51724138
P-5	60	0.6	150	8	72.90640394
P-5	75	0.6	150	8	74.38423645
P-5	90	0.6	150	8	76.84729064
P-5	105	0.6	150	8	77.33990148
P-5	120	0.6	150	8	79.31034483
P-5	135	0.6	150	8	79.31034483
P-5	150	0.6	150	8	79.80295567
P-5	0	0.6	150	16	1.477832512
P-5	30	0.6	150	16	44.82758621
P-5	40	0.6	150	16	63.05418719
P-5	50	0.6	150	16	74.87684729
P-5	60	0.6	150	16	81.28078818
P-5	75	0.6	150	16	86.20689655
P-5	90	0.6	150	16	88.1773399
P-5	105	0.6	150	16	91.13300493
P-5	120	0.6	150	16	91.62561576
P-5	135	0.6	150	16	93.10344828
P-5	150	0.6	150	16	94.58128079

38

39 **Table S7. Dataset 7 extracted using Plot Digitizer [6]**

Material	Time (min)	Dose (g/L)	Initial Concentration (mg/L)	Light Intensity (mW/cm ²)	Removal (%)
P-6	0	0.05	10	60	0
P-6	5	0.05	10	60	9.683257919
P-6	10	0.05	10	60	15.38461538
P-6	15	0.05	10	60	18.37104072
P-6	30	0.05	10	60	27.87330317
P-6	45	0.05	10	60	28.95927602

P-6	60	0.05	10	60	30.58823529
P-6	75	0.05	10	60	30.58823529
P-6	90	0.05	10	60	30.58823529
P-6	0	0.15	10	60	0
P-6	5	0.15	10	60	20.54298643
P-6	10	0.15	10	60	27.87330317
P-6	15	0.15	10	60	34.9321267
P-6	30	0.15	10	60	49.86425339
P-6	45	0.15	10	60	53.12217195
P-6	60	0.15	10	60	53.93665158
P-6	75	0.15	10	60	55.56561086
P-6	90	0.15	10	60	55.83710407
P-6	0	0.3	10	60	0
P-6	5	0.3	10	60	29.23076923
P-6	10	0.3	10	60	47.69230769
P-6	15	0.3	10	60	59.36651584
P-6	30	0.3	10	60	71.58371041
P-6	45	0.3	10	60	77.28506787
P-6	60	0.3	10	60	82.44343891
P-6	75	0.3	10	60	88.41628959
P-6	90	0.3	10	60	89.77375566
P-6	0	0.4	10	60	0
P-6	5	0.4	10	60	34.38914027
P-6	10	0.4	10	60	49.59276018
P-6	15	0.4	10	60	61.26696833
P-6	30	0.4	10	60	87.87330317
P-6	45	0.4	10	60	91.13122172
P-6	60	0.4	10	60	92.760181
P-6	75	0.4	10	60	94.9321267
P-6	90	0.4	10	60	95.47511312
P-6	0	0.8	10	60	0
P-6	5	0.8	10	60	34.38914027
P-6	10	0.8	10	60	49.59276018
P-6	15	0.8	10	60	61.26696833
P-6	30	0.8	10	60	87.87330317
P-6	45	0.8	10	60	93.03167421
P-6	60	0.8	10	60	94.66063348
P-6	75	0.8	10	60	96.83257919
P-6	90	0.8	10	60	97.37556561
P-6	0	0.3	100	60	0
P-6	5	0.3	100	60	8.791208791
P-6	10	0.3	100	60	15.10989011
P-6	15	0.3	100	60	21.15384615
P-6	30	0.3	100	60	29.12087912
P-6	45	0.3	100	60	30.76923077
P-6	60	0.3	100	60	33.79120879
P-6	75	0.3	100	60	35.98901099
P-6	90	0.3	100	60	36.26373626

P-6	0	0.3	75	60	0
P-6	5	0.3	75	60	21.97802198
P-6	10	0.3	75	60	35.71428571
P-6	15	0.3	75	60	44.50549451
P-6	30	0.3	75	60	53.57142857
P-6	45	0.3	75	60	57.96703297
P-6	60	0.3	75	60	62.08791209
P-6	75	0.3	75	60	68.40659341
P-6	90	0.3	75	60	68.40659341
P-6	0	0.3	50	60	0
P-6	5	0.3	50	60	25.27472527
P-6	10	0.3	50	60	41.20879121
P-6	15	0.3	50	60	51.37362637
P-6	30	0.3	50	60	62.08791209
P-6	45	0.3	50	60	66.48351648
P-6	60	0.3	50	60	71.7032967
P-6	75	0.3	50	60	78.02197802
P-6	90	0.3	50	60	78.57142857
P-6	0	0.3	25	60	0
P-6	5	0.3	25	60	27.74725275
P-6	10	0.3	25	60	44.50549451
P-6	15	0.3	25	60	55.76923077
P-6	30	0.3	25	60	66.20879121
P-6	45	0.3	25	60	71.7032967
P-6	60	0.3	25	60	76.37362637
P-6	75	0.3	25	60	82.96703297
P-6	90	0.3	25	60	83.79120879
P-6	0	0.3	10	60	0.549450549
P-6	5	0.3	10	60	30.49450549
P-6	10	0.3	10	60	48.35164835
P-6	15	0.3	10	60	59.61538462
P-6	30	0.3	10	60	71.42857143
P-6	45	0.3	10	60	77.74725275
P-6	60	0.3	10	60	82.41758242
P-6	75	0.3	10	60	88.73626374
P-6	90	0.3	10	60	90
P-6	0	0.4	10	45	0
P-6	5	0.4	10	45	25.75757576
P-6	10	0.4	10	45	36.36363636
P-6	15	0.4	10	45	46.71717172
P-6	30	0.4	10	45	59.09090909
P-6	45	0.4	10	45	69.19191919
P-6	60	0.4	10	45	70.70707071
P-6	75	0.4	10	45	73.98989899
P-6	90	0.4	10	45	74.74747475
P-6	0	0.4	10	60	0.757575758
P-6	5	0.4	10	60	33.83838384
P-6	10	0.4	10	60	49.24242424

P-6	15	0.4	10	60	61.11111111
P-6	30	0.4	10	60	86.36363636
P-6	45	0.4	10	60	91.41414141
P-6	60	0.4	10	60	93.93939394
P-6	75	0.4	10	60	95.45454545
P-6	90	0.4	10	60	96.46464646
P-6	0	0.4	10	75	0
P-6	5	0.4	10	75	37.12121212
P-6	10	0.4	10	75	54.7979798
P-6	15	0.4	10	75	67.42424242
P-6	30	0.4	10	75	89.64646465
P-6	45	0.4	10	75	95.95959596
P-6	60	0.4	10	75	98.98989899
P-6	75	0.4	10	75	100.2525253
P-6	90	0.4	10	75	100.5050505

40

41 **Table S8. Validation Dataset extracted using Plot Digitizer [7]**

42

Time (min)	Dose (g/L)	Initial Concentration (mg/L)	Removal Efficiency (%)
0	0.01	10	0
12	0.01	10	18.13953488
24	0.01	10	26.04651163
36	0.01	10	34.41860465
48	0.01	10	41.39534884
60	0.01	10	51.62790698
72	0.01	10	65.58139535
0	0.02	10	0
12	0.02	10	29.76744186
24	0.02	10	40.93023256
36	0.02	10	61.86046512
48	0.02	10	73.02325581
60	0.02	10	83.72093023
72	0.02	10	93.02325581
0	0.04	10	0
12	0.04	10	40
24	0.04	10	53.02325581
36	0.04	10	75.81395349
48	0.04	10	86.04651163
60	0.04	10	94.88372093
72	0.04	10	99.53488372
0	0.02	5	0
12	0.02	5	0
24	0.02	5	1.449275362
36	0.02	5	7.246376812
48	0.02	5	8.695652174

60	0.02	5	14.00966184
72	0.02	5	16.42512077
0	0.02	10	0
12	0.02	10	26.57004831
24	0.02	10	38.16425121
36	0.02	10	57.00483092
48	0.02	10	65.2173913
60	0.02	10	83.57487923
72	0.02	10	92.2705314
0	0.02	20	0
12	0.02	20	31.40096618
24	0.02	20	46.37681159
36	0.02	20	67.63285024
48	0.02	20	76.32850242
60	0.02	20	90.33816425
72	0.02	20	95.65217391

43

44 **Table S9. Sensitivity Parameters for different Datasets across Different Models**

45

		Model 1	Model 2	Model 3	Model 4	Model 5	Model 6
Dataset 1	Time	0.7295	0.7339	0.7376	0.7050	0.6648	0.7249
	Dose	0.3419	0.4435	0.4914	0.6579	0.4520	0.4845
	IC	-0.0472	0.0000	0.0466	0.0412	0.0582	0.0363
Dataset 2	Time	0.5696	0.5827	0.6174	0.7603	0.6777	0.5994
	Dose	0.3563	0.3717	0.5235	0.7018	0.4997	0.3667
	IC	-0.0397	0.0840	0.0677	0.0580	0.0816	0.0628
Dataset 3	Time	0.4492	0.4701	0.4567	0.8274	0.2872	0.3510
	Dose	0.4354	0.0677	0.1730	-0.0205	0.0335	0.2776
	IC	-0.4511	-0.3710	-0.3574	-0.3190	-0.2197	-0.2679
Dataset 4	Time	0.7337	0.7355	0.7362	0.7807	0.7068	0.7248
	Dose	0.1302	0.2833	0.2832	0.5590	0.3061	0.3964
	IC	-0.1464	0.0000	-0.0475	-0.0440	0.0171	-0.0616
Dataset 5	Time	0.3295	0.3383	0.3454	10.0000	0.1807	0.3915
	Dose	0.2608	0.0000	0.1293	-20.8333	-0.0149	-0.1805
	IC	-0.2863	-0.2313	-0.2750	-21.9167	-0.1132	-1.4353
Dataset 6	Time	0.1921	0.2521	0.2600	0.3638	0.3315	0.2984
	Dose	0.1921	0.1705	0.2000	0.4026	0.2350	0.2249
	IC	-0.2224	-0.3412	-0.3799	-0.3224	0.0000	0.0000
	Light	0.1921	0.1752	0.2000	0.2649	0.1977	0.0847
Dataset 7	Time	0.0382	0.0286	0.0493	0.6361	0.2997	0.0843
	Dose	0.0379	0.0296	0.0513	0.2240	0.3311	0.0831
	IC	0.0352	-0.0183	-0.0148	-0.0257	-0.1507	0.0000
	Light	0.0379	0.0510	0.0513	0.1902	0.6385	0.0017

46

47 **Table S10. Experimental study used for model validation purpose**

48

Time (min)	Dose (g/L)	Initial Concentration (mg/L)	Light Intensity (W/m ²)	Removal (%)	Model Application
0	0.5	20	0	39	Training
30	0.5	20	31	39	Training
60	0.5	20	62	39	Training
90	0.5	20	77	39	Validation
120	0.5	20	81	39	Training
0	1	20	0	39	Training
30	1	20	43	39	Training
60	1	20	72	39	Validation
90	1	20	87	39	Training
120	1	20	91	39	Training
0	2	20	0	39	Validation
30	2	20	52	39	Training
60	2	20	71	39	Training
90	2	20	83	39	Training
120	2	20	89	39	Validation
0	1	10	0	39	Training
30	1	10	56	39	Training
60	1	10	85	39	Training
90	1	10	93	39	Training
120	1	10	97	39	Training
0	1	50	0	39	Training
30	1	50	36	39	Training
60	1	50	57	39	Training
90	1	50	73	39	Validation
120	1	50	79	39	Training
0	1	20	0	49	Training
30	1	20	56	49	Validation
60	1	20	78	49	Training
90	1	20	92	49	Training
120	1	20	98	49	Training
0	1	20	0	66	Training
30	1	20	57	66	Validation
60	1	20	81	66	Training
90	1	20	93	66	Training
120	1	20	97	66	Training

49

50

51 **Appendix B: Optimization Code**

52 % =====

53 % Decision variables:

```

54 % x(1) = time (t)
55 % x(2) = dose (D)
56 % x(3) = light intensity (I0)
57 % x(4) = initial concentration (C)
58 % =====
59
60 % ----- Bounds -----
61 lb = [0 0.5 39 10];
62 ub = [120 2.0 66 50];
63
64 x0 = [30 1.0 50 20];
65
66 opts = optimoptions('fmincon','Display','off');
67
68 % ----- Constants -----
69 k = 0.0009;
70 a = 0.3002;
71 b = 0.8276;
72 c = 0.4464;
73 d = 0.2354;
74
75 % ----- MODEL (anonymous function) -----
76 removal = @(x) (1 - exp( ...
77     -x(1) * (k * (x(2)^a * x(3)^b) / (x(4)^c * d)) ... )) * 100;
78
79 % =====
80 % CASE 1: Maximize removal at lowest time
81 wt = 0.05;
82 obj1 = @(x) -removal(x) + wt*x(1);
83
84 [x1,~] = fmincon(obj1,x0,[],[],[],[],lb,ub,[],opts);
85 R1 = removal(x1);
86
87 disp('--- Max Removal at Lowest Time ---')

```

```

88 disp('Time Dose Intensity Concentration Removal')
89 disp([x1 R1])
90
91 % =====
92 % CASE 2: Maximize removal at minimum dose
93 wd = 5;
94 obj2 = @(x) -removal(x) + wd*x(2);
95
96 [x2,~] = fmincon(obj2,x0,[],[],[],[],lb,ub,[],opts);
97 R2 = removal(x2);
98
99 disp('--- Max Removal at Minimum Dose ---')

```

```

100 disp('Time Dose Intensity Concentration Removal')
101 disp([x2 R2])

```

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103

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129