

1 Supplemental Information for
2 Viscosity Reduction in HPAM Solutions Induced by Silica
3 Nanoparticle Additives

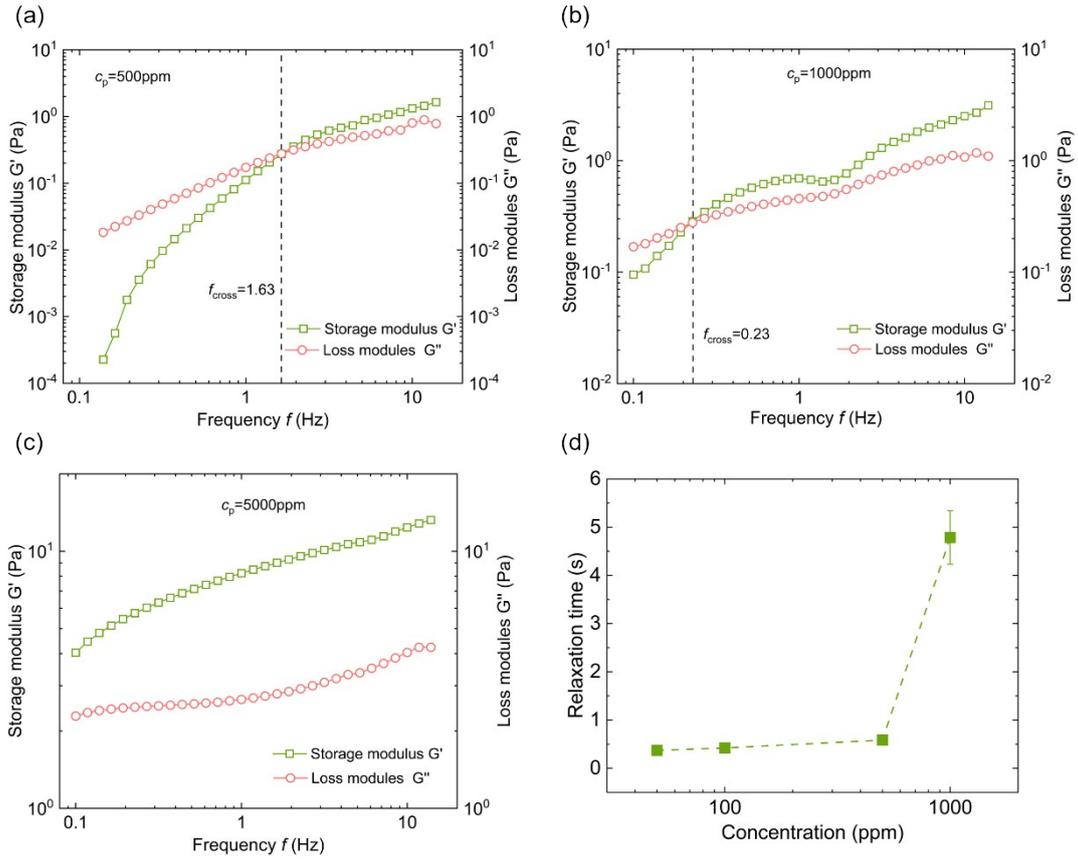
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8 **I. Supplementary Frequency-Sweep Measurements of G' and G''**

9 Dynamic oscillatory rheology was performed to further characterize the
10 viscoelastic response of HPAM solutions across polymer concentrations. Frequency-
11 sweep measurements were carried out to obtain the storage and loss moduli, G' and G'' ,
12 over the accessible frequency window. As shown in Fig. S1a and Fig. S1b, clear
13 $G' - G''$ crossovers are observed for the 500 ppm and 1000 ppm solutions, respectively,
14 indicating the emergence of an elastic contribution with increasing frequency. Notably,
15 the crossover shifts to higher frequencies at 500 ppm and moves toward lower
16 frequencies at 1000 ppm, suggesting a pronounced increase in the characteristic
17 relaxation time as the polymer concentration increases. For the 5000 ppm solution (Fig.
18 S1c), G' remains higher than G'' throughout the entire measurable frequency range,
19 implying that the terminal regime is shifted below the instrument's low-frequency limit
20 and that the viscoelastic response is dominated by elastic storage within the
21 experimental window.

22 To quantify the concentration-dependent transition, the crossover frequency
23 f_{cross} was extracted when applicable, and the corresponding relaxation time was
24 estimated as $\tau = \frac{1}{f_{cross}}$. The resulting $\tau(c_p)$ trend is summarized in Fig. S1d, where a
25 pronounced increase in relaxation time is observed around 1000 ppm, consistent with
26 an apparent crossover toward entanglement-dominated viscoelasticity for the present
27 HPAM system¹ under the investigated conditions.

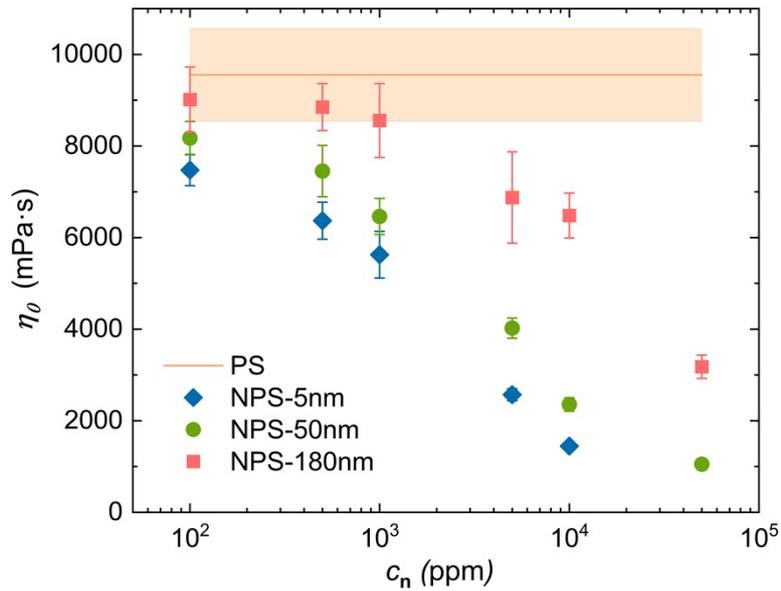
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28
 29 **Fig. S1.** Frequency-sweep measurements of the storage and loss moduli, G' and G'' , for
 30 HPAM solutions at (a) 500 ppm, (b) 1000 ppm, and (c) 5000 ppm. (d) Relaxation time
 31 τ as a function of polymer concentration.
 32

33 II. Additional Rheological Data with Different Silica Nanoparticle Sizes

34 The Supplementary rheological measurements were performed for silica
 35 nanoparticles with different particle sizes (5 nm, 50 nm, and 180 nm), and the resulting
 36 zero-shear viscosity η_0 is summarized in Fig. S2. The orange line and shaded band
 37 represent the mean η_0 of the nanoparticle-free HPAM solution (PS) and the associated
 38 experimental uncertainty (mean \pm error), respectively. For all tested particle sizes, η_0
 39 decreases with increasing nanoparticle concentration c_n , and the measured values fall
 40 below the PS baseline at sufficiently high c_n . These results indicate that the viscosity-
 41 reduction trend is reproducible and remains robust within the investigated HPAM-
 42 silica system.



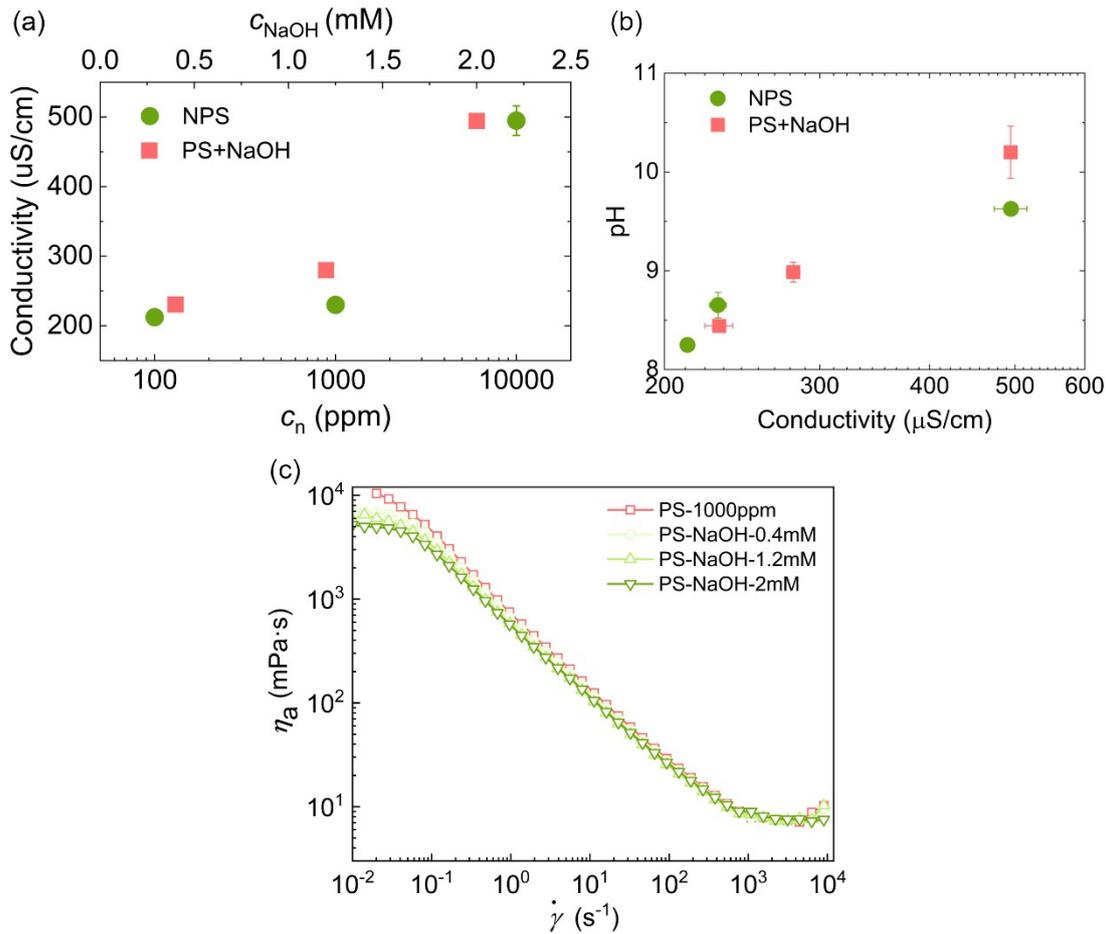
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44 Fig. S2. Dependence of zero-shear viscosity η_0 on nanoparticle concentration c_n for
 45 HPAM solutions containing silica nanoparticles of different particle sizes (5, 50, and
 46 180 nm). Error bars indicate measurement variability, and the orange line/shaded band
 47 shows the nanoparticle-free HPAM baseline (PS; mean \pm error).

48

49 III. Effect of Ionic Conductivity and pH on the Rheology of HPAM Solutions

50 To evaluate whether the viscosity reduction observed upon the addition of silica
 51 nanoparticles can be fully attributed to changes in ionic conditions, the ionic
 52 conductivity and pH of HPAM solutions containing different concentrations of silica
 53 nanoparticles were systematically examined. As shown in Fig. S3a, the ionic
 54 conductivity increases monotonically with increasing nanoparticle concentration,
 55 indicating an increase in the concentration of mobile ions in the system.



56

57 Fig. S3. (a) Ionic conductivity of HPAM solutions as a function of silica nanoparticle
 58 concentration. (b) pH and ionic conductivity of nanoparticle-free HPAM solutions
 59 adjusted by NaOH to match the values measured in silica-containing samples. (c)
 60 Apparent viscosity of the conductivity- and pH-matched control solutions compared
 61 with HPAM solutions measured under identical rheological conditions.

62

63 The origin of this conductivity increase can be traced to the stabilization
 64 mechanism of colloidal silica dispersions. The silica nanoparticles used in this work are
 65 stabilized under mildly alkaline conditions, a common practice achieved by adjusting
 66 the dispersion using bases such as NaOH or ammonia/amine species. Under these
 67 conditions, surface silanol groups undergo deprotonation ($\equiv \text{Si} - \text{OH} \rightarrow \equiv \text{Si} - \text{O}^-$),
 68 leading to enhanced surface charge and electrostatic stabilization. This process is
 69 accompanied by counterions and may introduce a small amount of residual electrolyte
 70 (primarily Na^+), which contributes to the measured ionic conductivity. Consistent with
 71 this interpretation, a slight increase in solution pH is also observed after nanoparticle
 72 addition.

73 To evaluate whether the observed changes in pH and ionic conductivity alone are
74 sufficient to explain the viscosity reduction, a matched-control experiment was
75 performed. Specifically, NaOH was added to nanoparticle-free HPAM solutions to
76 adjust both the pH and ionic conductivity to match those measured in the corresponding
77 silica-containing samples. The resulting pH and conductivity values are summarized in
78 Fig. S3b. Rheological measurements were then conducted on these conductivity- and
79 pH-matched control solutions under identical conditions, with the apparent viscosity
80 results shown in Fig. S3c.

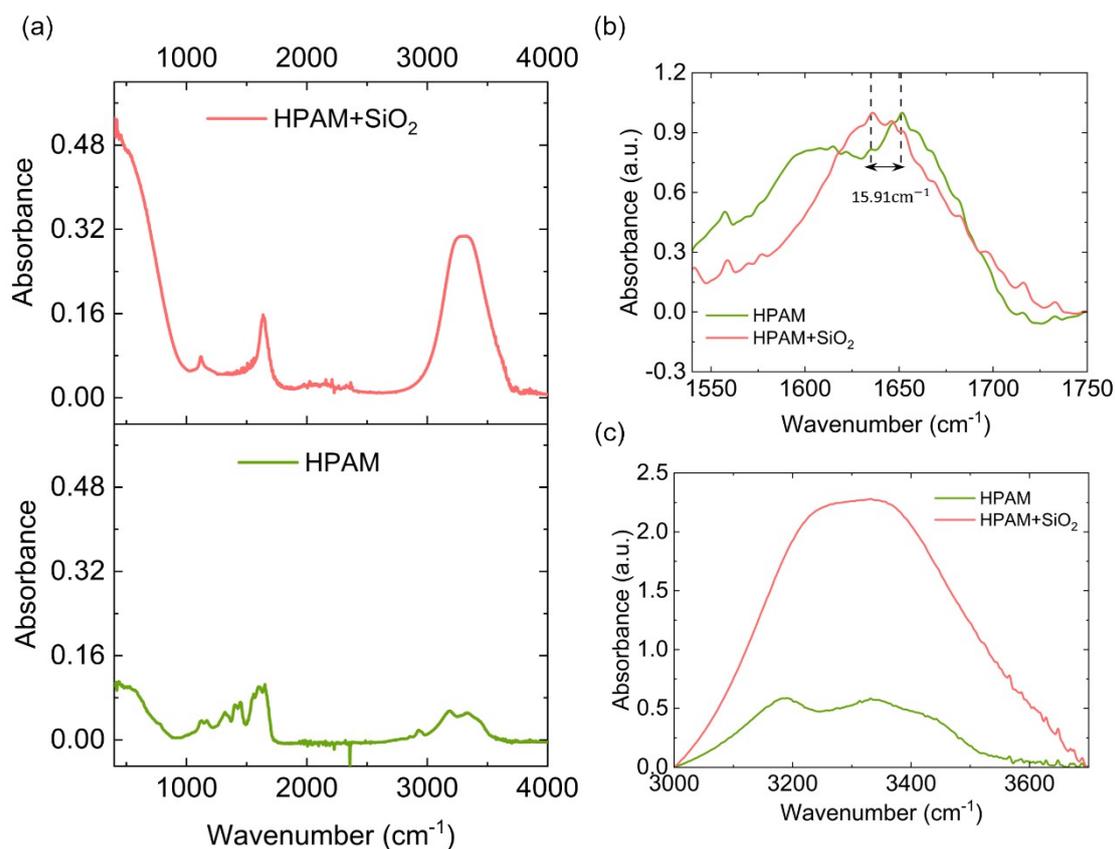
81 The control experiments demonstrate that ion- and pH-related effects can indeed
82 induce a measurable decrease in viscosity, indicating that ionic conditions contribute to
83 the baseline rheological response of HPAM solutions. However, even under matched
84 pH and conductivity conditions, the magnitude of viscosity reduction remains
85 substantially smaller than that observed in the presence of silica nanoparticles. This
86 comparison indicates that the conductivity increase associated with nanoparticle
87 addition is not sufficient to account for the full extent of the viscosity reduction,
88 supporting the presence of an additional nanoparticle-mediated contribution beyond
89 simple ionic screening effects.

90

91 **IV. FT-IR Spectral Comparison of HPAM and HPAM–SiO₂ Mixtures and** 92 **Evidence for Enhanced Hydrogen Bonding**

93 Fig. S4 compares the FT-IR spectra of the pure HPAM solution and the HPAM–
94 SiO₂ mixture. Fig. S4(a) shows the raw spectra, highlighting the overall absorption
95 features as well as baseline differences arising from the solution background, bound
96 water and nanoparticle-related scattering. Fig. S4(b) presents a magnified view of the
97 1550–1750 cm⁻¹ region (amide bands), which mainly contains the HPAM Amide I band
98 (*C=O* stretching, ~1650 cm⁻¹) and Amide II band (*N–H* bending/*C–N* stretching,
99 ~1550 cm⁻¹). To enable a robust comparison of peak positions and shapes, a local linear
100 baseline correction was applied within the selected window by subtracting the straight

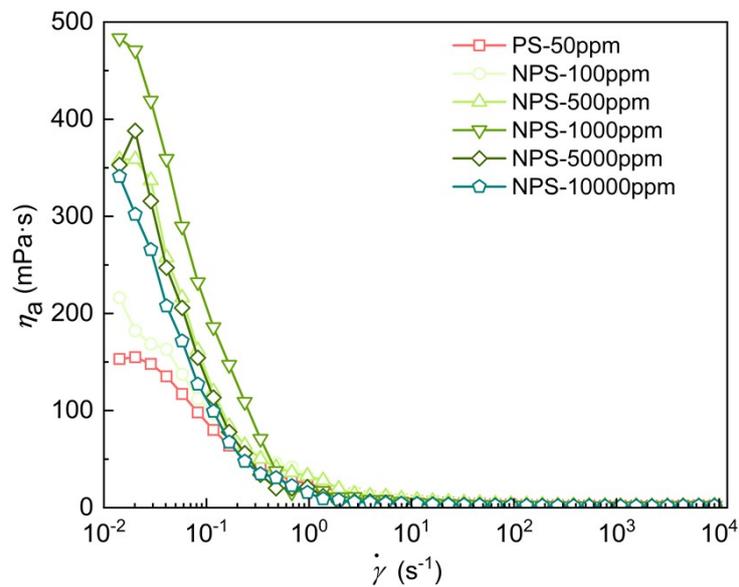
101 line connecting the two endpoints, followed by optional peak-height normalization
 102 within the Amide I window. A pronounced red shift of the Amide I band ($\sim 16 \text{ cm}^{-1}$) is
 103 observed upon adding SiO_2 , indicating a strengthened hydrogen-bonding environment
 104 around the carbonyl groups ($\text{C}=\text{O}$ acting as a hydrogen-bond acceptor interacting with
 105 silanol groups and/or bound water on silica surfaces). Fig. S4(c) shows the magnified
 106 $3000\text{--}3700 \text{ cm}^{-1}$ region corresponding to O-H/N-H stretching vibrations, processed
 107 using the same local baseline correction and scaled with the normalization factor used
 108 in Fig. S4(b). Compared with pure HPAM, the HPAM– SiO_2 mixture exhibits a stronger
 109 and broader O-H/N-H band, consistent with an enhanced hydrogen-bonding network.
 110 Taken together, the Amide I red shift in (b) and the broadened O-H/N-H band in (c)
 111 support the conclusion that introducing SiO_2 enhances hydrogen bonding in the system.



112
 113 Fig. S4. FT-IR spectra of pure HPAM and the HPAM– SiO_2 mixture. (a) Raw spectra;
 114 (b) $1550\text{--}1750 \text{ cm}^{-1}$ zoom-in after local linear baseline correction and Amide I peak-
 115 height normalization, showing an $\sim 16 \text{ cm}^{-1}$ red shift of Amide I; (c) $3000\text{--}3700 \text{ cm}^{-1}$
 116 zoom-in processed with the same local baseline correction and scaled using the
 117 normalization factor in (b), showing an enhanced O-H/N-H band.
 118

119 **V. Supplementary rheology of 50 ppm HPAM–nanoparticle mixtures**

120 To supplement the dilute-polymer regime, the complete apparent-viscosity–shear-
121 rate curves are provided for 50 ppm polyacrylamide solutions containing nanoparticles
122 at different concentrations (Fig. S5). The measurements were conducted using the same
123 rheological protocol as described in the main text. The results indicate that, in dilute
124 polymer solutions, an apparent viscosity increase is induced by nanoparticle addition,
125 together with a thickening plateau at higher nanoparticle concentrations and an eventual
126 reversal. These data allow readers to examine in detail the evolution of the viscosity
127 increase.



128
129 **Fig. S5.** Apparent viscosity as a function of shear rate for 50 ppm polyacrylamide
130 solution (PS-50 ppm) with nanoparticles added at different concentrations (100–10,000
131 ppm).
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