

Supporting Information

Design Principles of Biphenylene-Supported Dual-Atom Catalysts for Efficient and Selective Nitrate Reduction to Ammonia

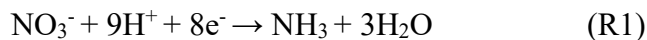
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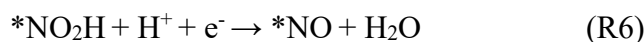
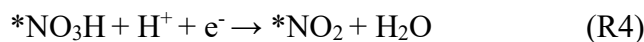
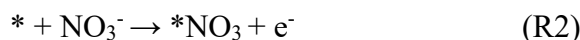
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Note S1. Elementary and kinetic steps of NO₃RR

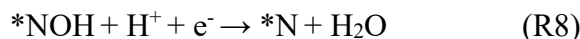
Electrochemical reduction of NO₃⁻ results in the formation of NH₃ with nine protons and eight electrons transferred. The whole reaction can be summarized as



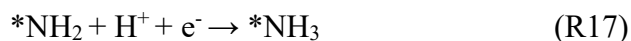
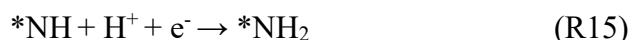
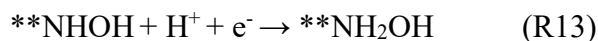
Involving the intermediates *NO₃, *NO₃H, *NO₂, *NO₂H, *NO, *NOH, *N, *NH, *NH₂ and *NH₃, N-end and NO-side pathways are considered as the most favorable pathway on TM₂@BPN and the elementary steps of these pathways are described as follows:



N-end pathway



NO-side pathway





The ΔG between two states involve in the NO_3RR reduction process can be expressed as to:

$$\Delta G = G(\text{NO}_{3-m}\text{H}_n) + m G(\text{H}_2\text{O}) - G(\text{NO}_3^-) - n/2 G(\text{H}_2) - G(*)$$

where $*$ denotes the surface of $\text{TM}_2@\text{BPN}$, n is the number of H^+/e^- pairs transferred, and

m ($m=0, 1, 2, 3$) is the number of H_2O molecules released. Thus,

$$\Delta G(*\text{NO}_3\text{H}) = G(*\text{NO}_3\text{H}) - G(*) - G(\text{NO}_3^-) - 1/2 G(\text{H}_2)$$

$$\Delta G(*\text{NO}_2) = G(*\text{NO}_2) - G(*) - G(\text{NO}_3^-) - G(\text{H}_2) + G(\text{H}_2\text{O})$$

$$\Delta G(*\text{NO}_2\text{H}) = G(*\text{NO}_2\text{H}) - G(*) - G(\text{NO}_3^-) - 3/2 G(\text{H}_2) + G(\text{H}_2\text{O})$$

$$\Delta G(*\text{NO}) = G(*\text{NO}) - G(*) - G(\text{NO}_3^-) - 2G(\text{H}_2) + 2G(\text{H}_2\text{O})$$

$$\Delta G(*\text{NOH}) = G(*\text{NOH}) - G(*) - G(\text{NO}_3^-) - 5/2 G(\text{H}_2) + 2G(\text{H}_2\text{O})$$

$$\Delta G(*\text{N}) = G(*\text{N}) - G(*) - G(\text{NO}_3^-) - 3G(\text{H}_2) + 3G(\text{H}_2\text{O})$$

$$\Delta G(**\text{NHOH}) = G(**\text{NHOH}) - G(*) - G(\text{NO}_3^-) - 3G(\text{H}_2) + 2G(\text{H}_2\text{O})$$

$$\Delta G(**\text{NH}_2\text{O}) = G(**\text{NH}_2\text{O}) - G(*) - G(\text{NO}_3^-) - 3G(\text{H}_2) + 2G(\text{H}_2\text{O})$$

$$\Delta G(**\text{NH}_2\text{OH}) = G(**\text{NH}_2\text{OH}) - G(*) - G(\text{NO}_3^-) - 7/2 G(\text{H}_2) + 2G(\text{H}_2\text{O})$$

$$\Delta G(*\text{NH}) = G(*\text{NH}) - G(*) - G(\text{NO}_3^-) - 7/2 G(\text{H}_2) + 3G(\text{H}_2\text{O})$$

$$\Delta G(*\text{NH}_2) = G(*\text{NH}_2) - G(*) - G(\text{NO}_3^-) - 4G(\text{H}_2) + 3G(\text{H}_2\text{O})$$

$$\Delta G(*\text{NH}_3) = G(*\text{NH}_3) - G(*) - G(\text{NO}_3^-) - 9/2 G(\text{H}_2) + 3G(\text{H}_2\text{O})$$

For example, if we consider the rate-determining step of $\text{Rh}_2@\text{BPN}$

$$1. \Delta G(*\text{NO}) = G(*\text{NO}) - G(\text{Rh}_2@\text{BPN}) - G(\text{NO}_3^-) - 2G(\text{H}_2) + 2G(\text{H}_2\text{O})$$

$$G(*\text{NO}) = -499.8132972, G(\text{Rh}_2@\text{BPN}) = -484.3864813, G(\text{NO}_3^-) = -24.91378556, G(\text{H}_2) = -6.9$$

$$G(\text{H}_2\text{O}) = -14.32$$

$$\Delta G(*\text{NO}) = -499.8132972 - (-484.3864813) - (-24.91378556) - 2(-6.9) + 2(-14.32)$$

$$\Delta G(*NO) = -5.353 \text{ eV}$$

$$2. \Delta G(*NOH) = G(*NOH) - G(Rh_2@BPN) - G(NO_3^-) - 5/2G(H_2) + 2G(H_2O)$$

$$G(*NOH) = -503.0984867$$

$$\Delta G(*NOH) = -503.0984867 - (-484.3864813) - (-24.91378556) - 5/2(-6.9) + 2(-14.32)$$

$$\Delta G(*NOH) = -5.188 \text{ eV}$$

$$\text{The relative energy is } \Delta G(*NOH) - \Delta G(*NO) = -5.188 - (-5.353) = \mathbf{0.16 \text{ eV}}$$

Consider the rate-determining step of $Os_2@BPN$

$$1. \Delta G(*NO) = G(*NO) - G(Os_2@BPN) - G(NO_3^-) - 2G(H_2) + 2G(H_2O)$$

$$G(*NO) = -504.004074, G(Os_2@BPN) = -489.0776676, G(NO_3^-) = -24.91378556, G(H_2) = -6.9$$

$$G(H_2O) = -14.32$$

$$\Delta G(*NO) = -504.004074 - (-489.0776676) - (-24.91378556) - 2(-6.9) + 2(-14.32)$$

$$\Delta G(*NO) = -4.852 \text{ eV}$$

$$2. \Delta G(*NOH) = G(*NOH) - G(Os_2@BPN) - G(NO_3^-) - 5/2G(H_2) + 2G(H_2O)$$

$$G(*NOH) = -507.1287723$$

$$\Delta G(*NOH) = -507.1287723 - (-489.0776676) - (-24.91378556) - 5/2(-6.9) + 2(-14.32)$$

$$\Delta G(*NOH) = -4.527 \text{ eV}$$

$$\text{The relative energy is } \Delta G(*NOH) - \Delta G(*NO) = -4.527 - (-4.852) = \mathbf{0.32 \text{ eV}}$$

The kinetic steps of NO₃RR on Rh₂@BPN and Os₂@BPN

However, in Figures S11 and S12, we performed nudged elastic band calculations for *NO + (H₃O⁺ + e⁻) → *NOH + H₂O on Rh₂@BPN and *NO + (H₃O⁺ + e⁻) → *NOH + H₂O on Os₂@BPN.

So, the energy difference is calculated by

$$\Delta E = E(*\text{HNO} + \text{H}_2\text{O}) - E(*\text{NO} + (\text{H}_3\text{O}^+ + \text{e}^-)) \text{ for Rh}_2\text{@BPN}$$

$$= -515.6195836 - (-512.90064229)$$

$$= \mathbf{-2.72 \text{ eV}}$$

$$\Delta E = E(*\text{NOH} + \text{H}_2\text{O}) - E(*\text{NO} + (\text{H}_3\text{O}^+ + \text{e}^-)) \text{ for Os}_2\text{@BPN}$$

$$= -519.3878837 - (-516.9307566)$$

$$= \mathbf{-2.46 \text{ eV}}$$

Note S2. Solvent effect

Specifically, we employed the implicit solvation model VASPsol, (1) to simulate aqueous conditions. Due to the computational cost we have chosen best catalyst ($\text{Rh}_2@\text{BPN}$, $\text{Os}_2@\text{BPN}$) from our study. The results obtained from calculations, are as summarized in Table S17 and S18. The results show that solvation alters the limiting potential by 0.08 and 0.03 V. However, previous studies report that solvent effects on NO_3RR are minor and have often been neglected. Accordingly, solvation effects are omitted in this work. (2-4).

Reference

1. K. Mathew, R. Sundararaman, K. Letchworth-Weaver, T. A. Arias and R. G. Hennig, J. Chem. Phys., 2014, 140.
2. H. Niu, Z. Zhang, X. Wang, X. Wan, C. Shao and Y. Guo, Adv. Funct. Mater., 2021, 31, 2008533.
3. T. Zhao, K. Chen, X. Xu, X. Li, X. Zhao, Q. Cai, K. Chu and J. Zhao, Appl. Catal. B: Environ., 2023, 339, 123156.
4. X. Guo, J. Gu, S. Lin, S. Zhang, Z. Chen and S. Huang, J. Am. Chem. Soc., 2020, 142, 5709-5721.

Note S3. Faradaic efficiency

The following equation estimates the theoretical Faradaic efficiencies (FE) and quantitatively represents the NO₃RR selectivity on TM₂@BPN.

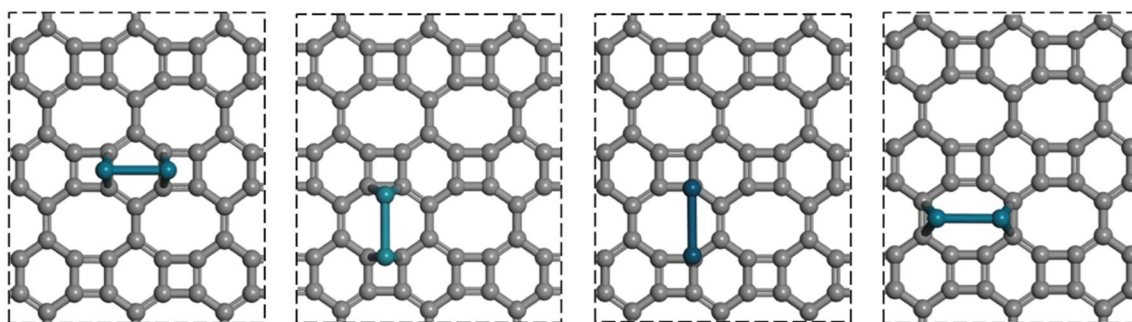
$$FE = \left[\frac{1}{(1 + e^{-\Delta G/k_B T})} \right]$$

Where ΔG represents the difference in free energy of the potential determining step between the HER and NO₃RR, k_B represents the Boltzmann constant ($8.617 \times 10^{-5} \text{ eV K}^{-1}$), and T represents the room temperature (298.15 K). The theoretical formula for Faradaic efficiency employed in this study was adapted from recently published works.⁽¹⁻⁵⁾ These studies established the theoretical framework in which the hydrogen evolution reaction (HER) is treated as the primary competing process against NO₃RR and the corresponding statistical model is derived based on the following assumptions: (1) the mass and electron transfer are not the rate determining factors for both HER and NO₃RR (2) only HER and NO₃RR are competing reactions, and (3) the selectivity of NO₃RR in comparison to HER could be estimated by Boltzmann distribution. Under these assumptions, the adopted formula offers a feasible theoretical approach for evaluating FE in NO₃RR. The total FE values approaching 100% should be regarded as theoretical probabilities before normalization, reflecting the potential tendency of each reaction under the given conditions. As experimental calibration data are not yet available, the FE values presented in Table S16 serve as theoretical references for future experimental validation.

Reference

1. W. Zhao, L. Zhang, Q. Luo, Z. Hu, W. Zhang, S. Smith and J. Yang, ACS Catal., 2019, 9, 3419-3425.
2. X. Liu, Y. Jiao, Y. Zheng, M. Jaroniec and S.-Z. Qiao, J. Am. Chem. Soc., 2019, 141, 9664-9672.

3. N. Sathishkumar and H.-T. Chen, J. Phys. Chem. C., 2023, 127, 994-1005.
4. D. Jiao, Y. Liu, Q. Cai and J. Zhao, J. Mater. Chem. A., 2021, 9, 1240-1251.
5. X. Lv, W. Wei, B. Huang, Y. Dai and T. Frauenheim, Nano Letters, 2021, 21, 1871-1878.



Configuration -I

Configuration -II

Configuration -III

Configuration -IV

Figure S1. Four possible binding configurations of TM dimer on BPN.

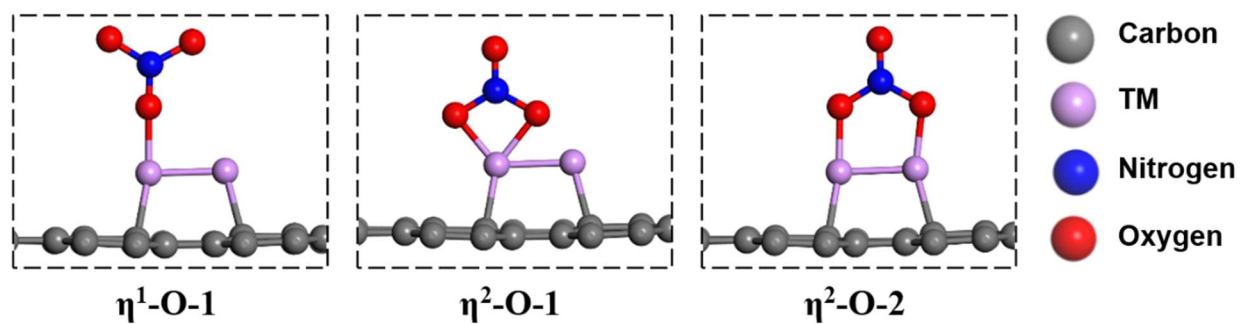
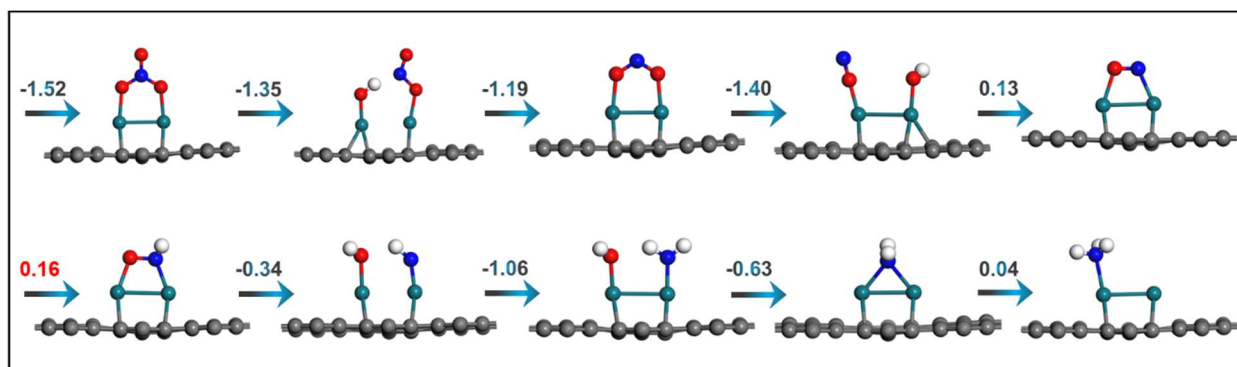
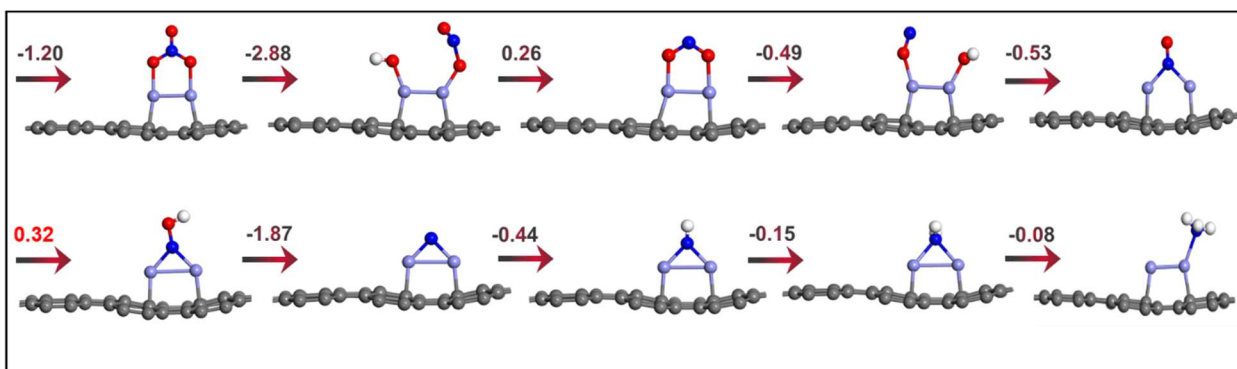


Figure S2. Three possible adsorption configurations of NO_3^- on $\text{TM}_2\text{@BPN}$.

(a)



(b)



(c)

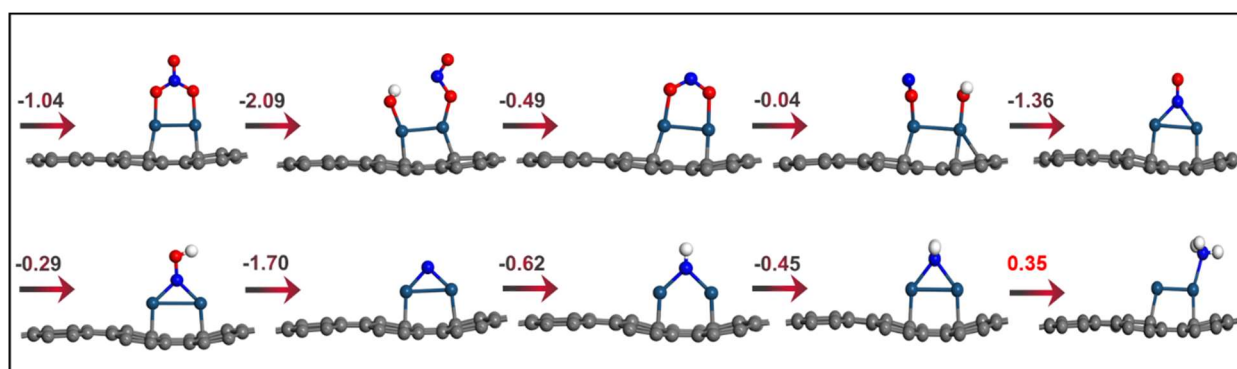


Figure S3 (a-c). DFT-optimized configurations of intermediates associated with free energy diagram of $\text{Rh}_2@BPN$, $\text{Os}_2@BPN$ and $\text{Ir}_2@BPN$ respectively.

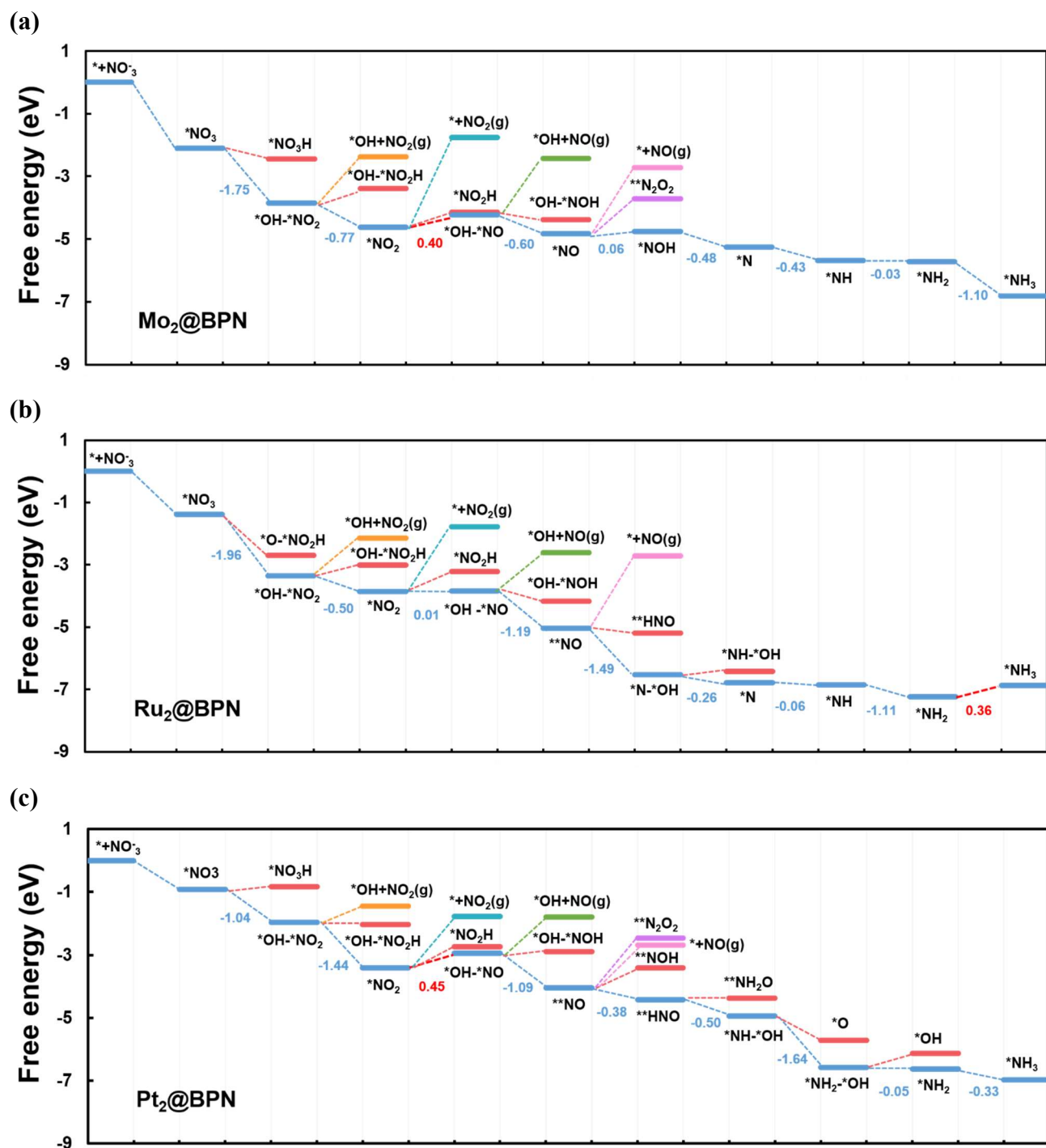
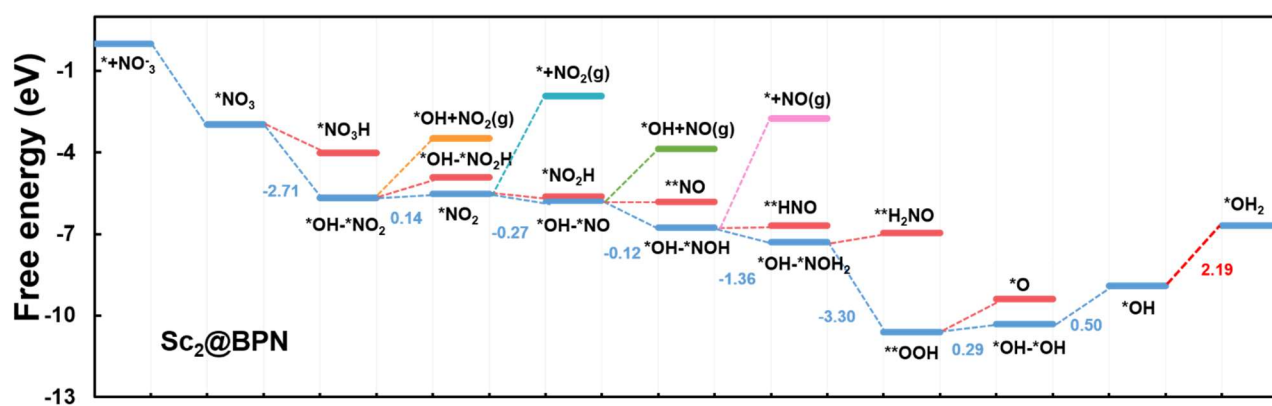
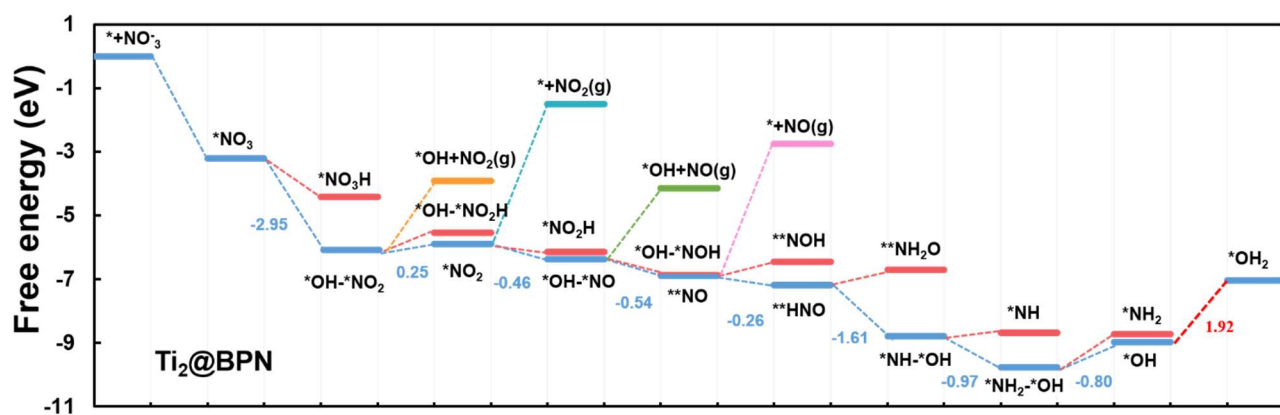


Figure S4 (a-c). Free energy diagram for NO₃RR on Mo₂@BPN, Ru₂@BPN and Pt₂@BPN catalysts respectively. ($U_L > -0.5V$)

(a)



(b)



(c)

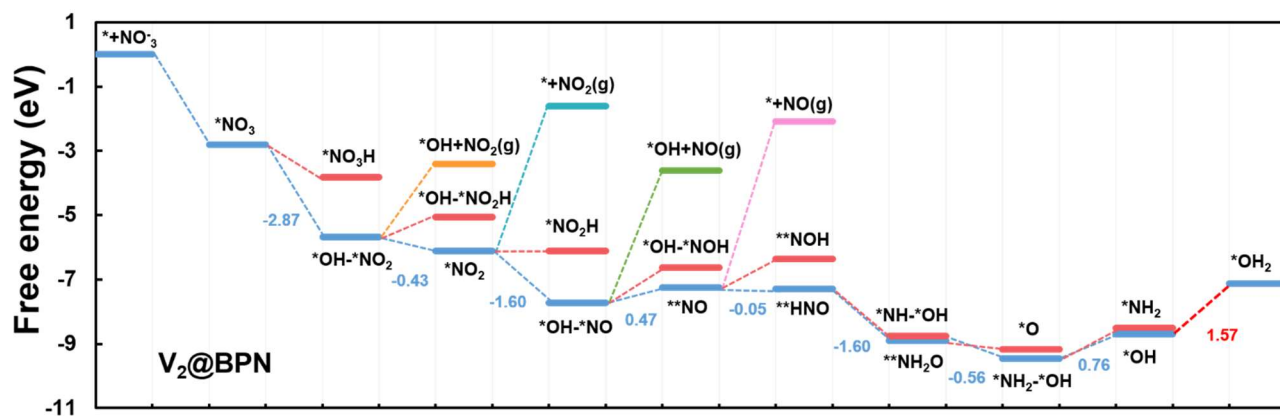


Figure S5 (a-c). Free energy diagram for NO_3RR on $\text{Sc}_2\text{@BPN}$, $\text{Ti}_2\text{@BPN}$ and $\text{V}_2\text{@BPN}$ catalysts respectively.

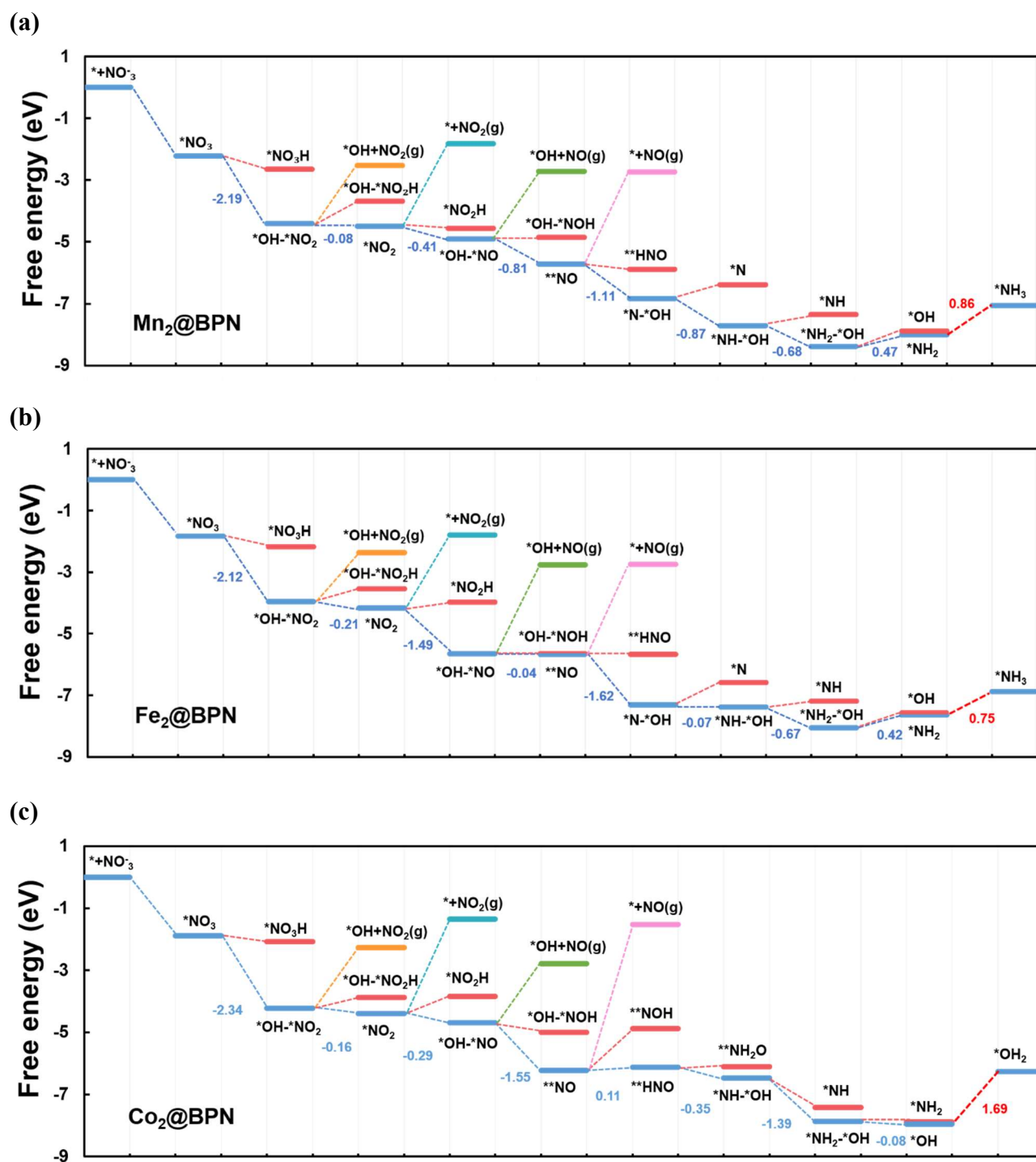


Figure S6 (a-c). Free energy diagram for NO₃RR on Mn₂@BPN, Fe₂@BPN and Co₂@BPN catalysts respectively.

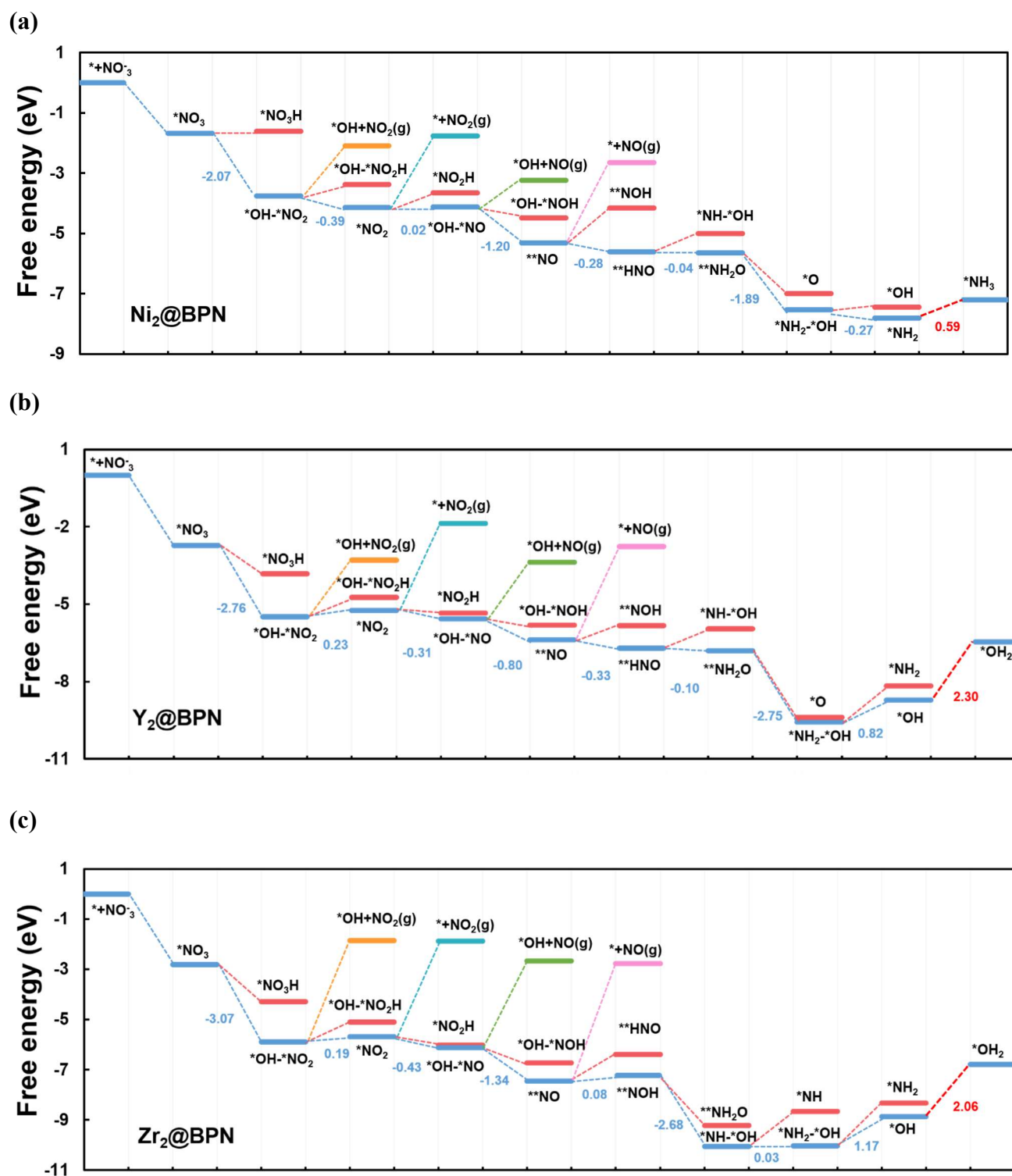


Figure S7 (a-c). Free energy diagram for NO₃RR on Ni₂@BPN, Y₂@BPN and Zr₂@BPN catalysts respectively.

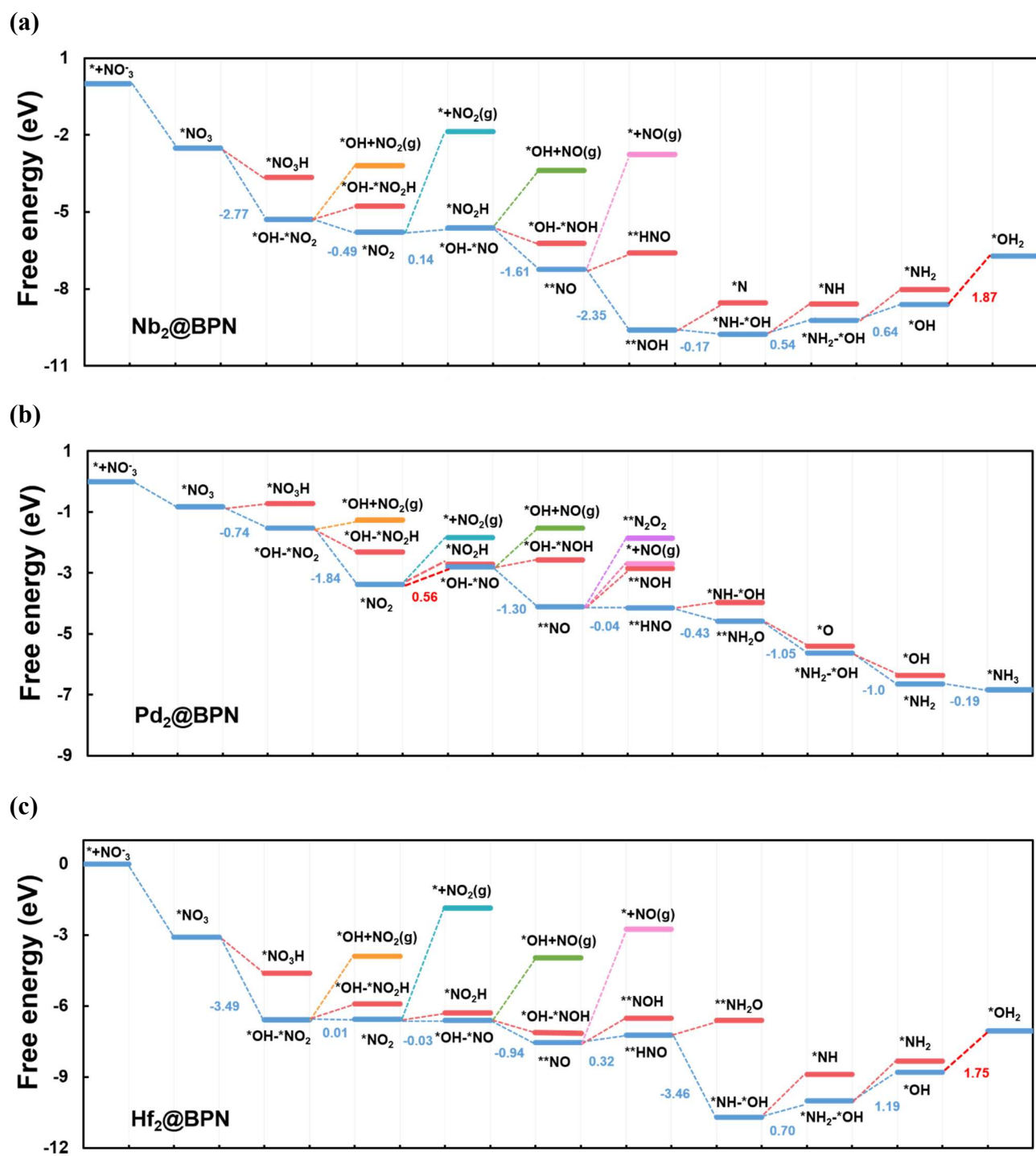


Figure S8 (a-c). Free energy diagram for NO_3RR on $\text{Nb}_2\text{@BPN}$, $\text{Pd}_2\text{@BPN}$ and $\text{Hf}_2\text{@BPN}$ catalysts respectively.

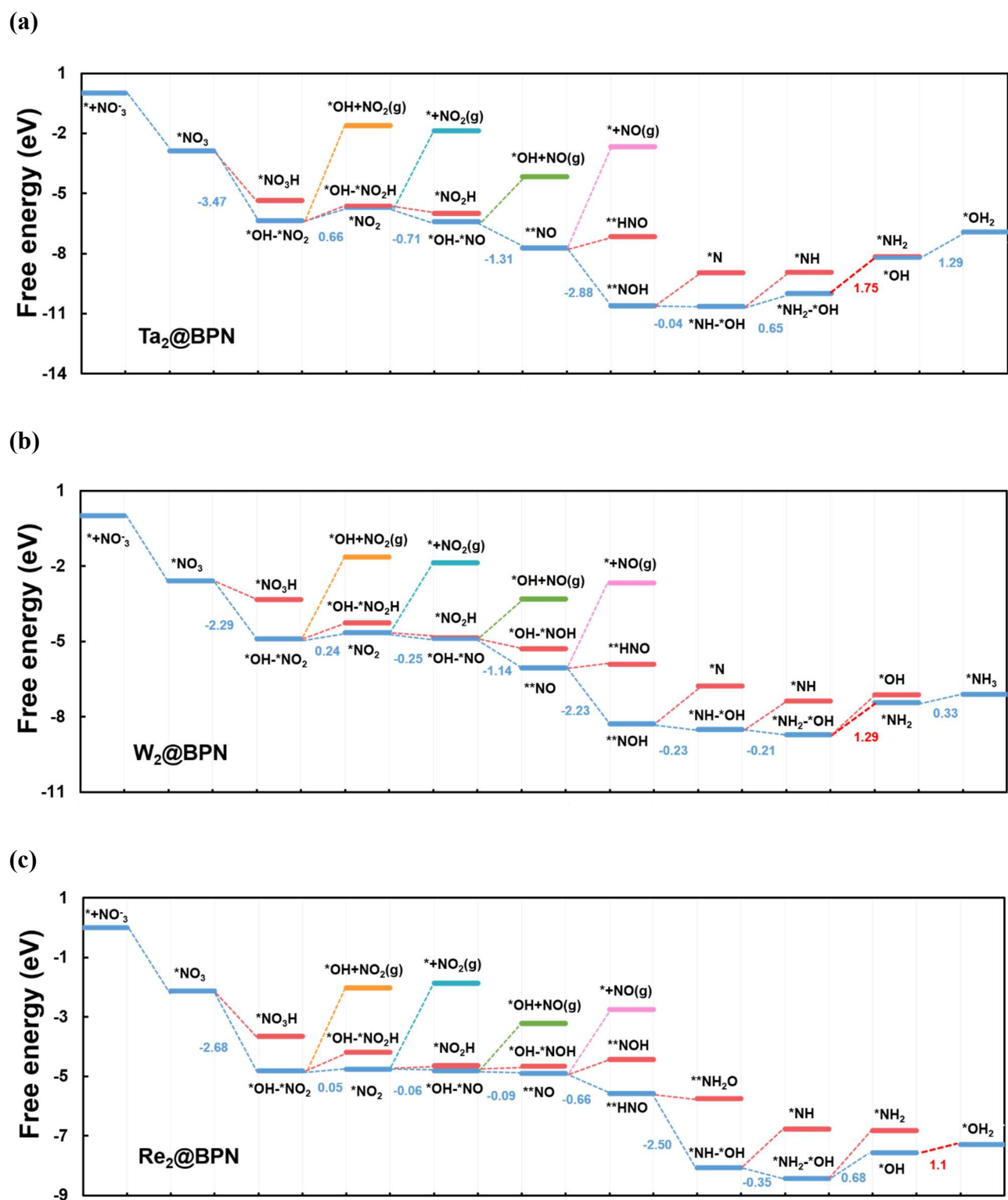


Figure S9 (a-c). Free energy diagram for NO_3RR on $\text{Ta}_2\text{@BPN}$, $\text{W}_2\text{@BPN}$ and $\text{Re}_2\text{@BPN}$ catalysts respectively.

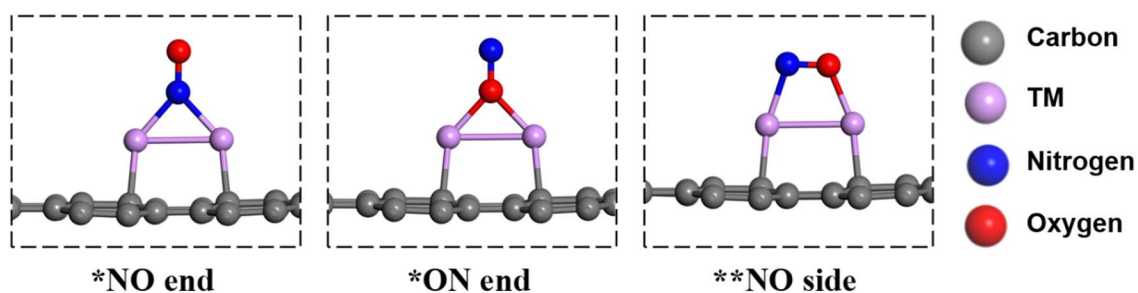


Figure S10. Three possible adsorption configurations of NO on $\text{TM}_2\text{@BPN}$.

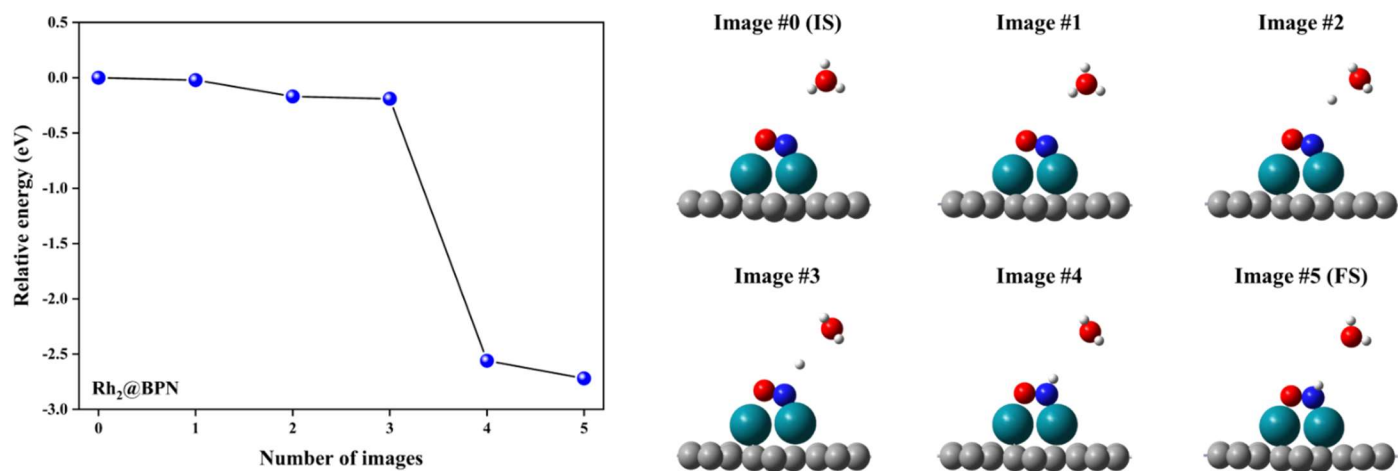


Figure S11. Nudged elastic band calculation results for $*\text{NO} + (\text{H}_3\text{O}^+ + \text{e}^-) \rightarrow *\text{NOH} + \text{H}_2\text{O}$ on $\text{Rh}_2\text{@BPN}$.

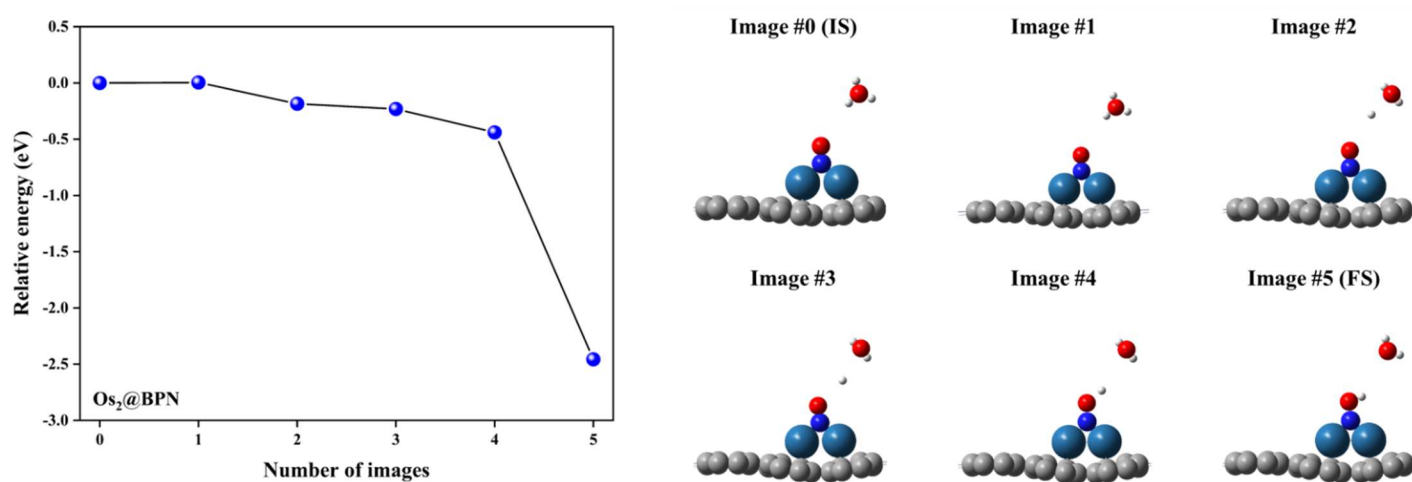


Figure S12. Nudged elastic band calculation results for $*\text{NO} + (\text{H}_3\text{O}^+ + \text{e}^-) \rightarrow *\text{NOH} + \text{H}_2\text{O}$ on $\text{Os}_2\text{@BPN}$.

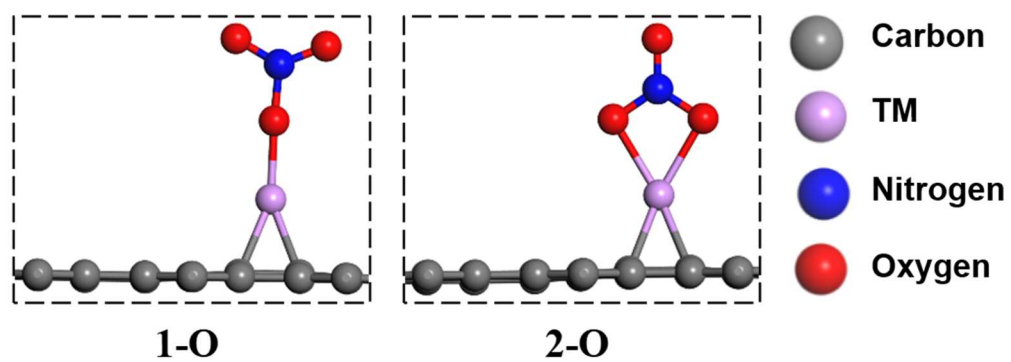


Figure S13. Two possible adsorption configurations of NO_3^- on TM@BPN.

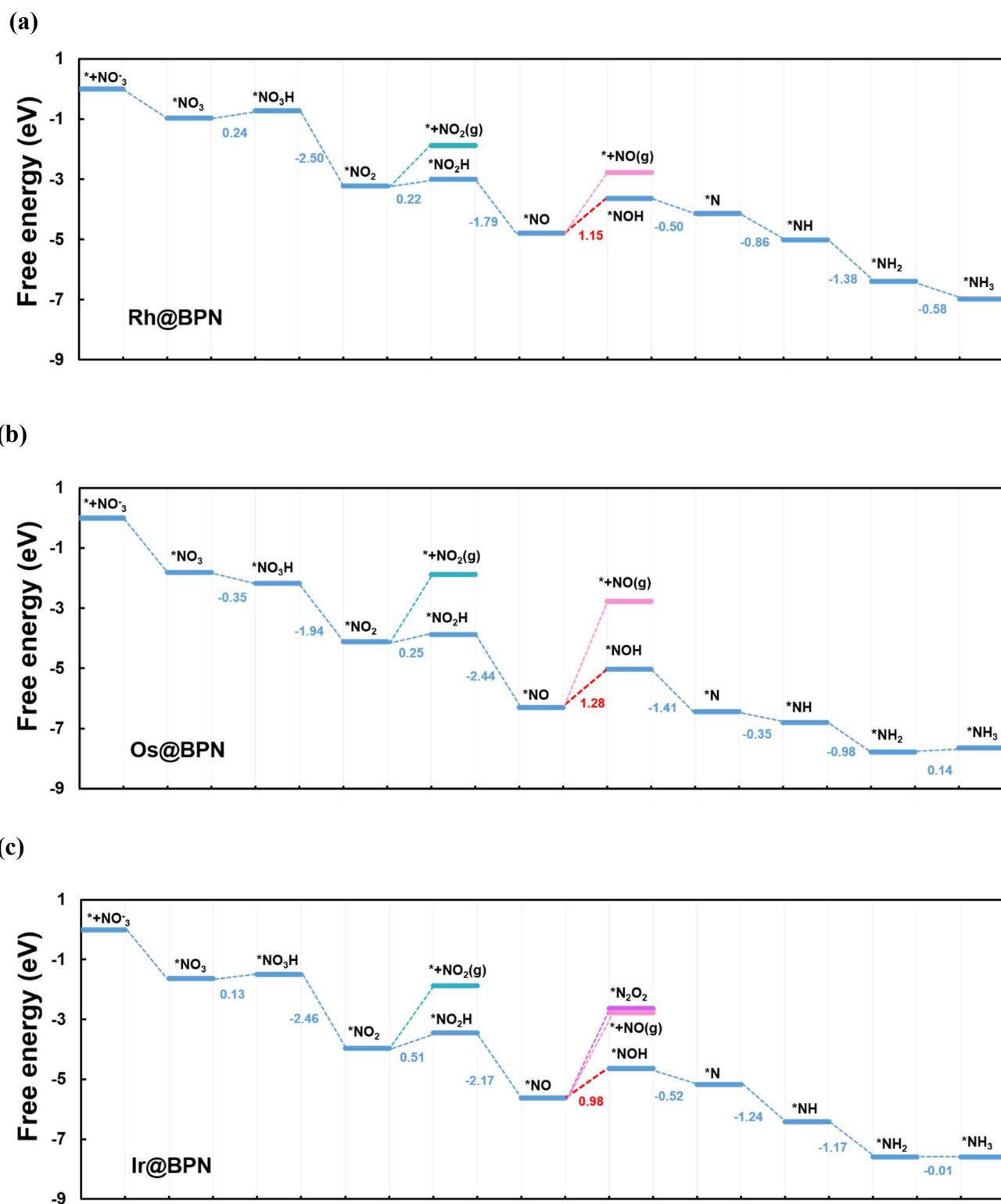


Figure S14 (a-c). Free energy diagram for NO₃RR on Rh@BPN, Os@BPN and Ir@BPN SACs catalysts respectively.

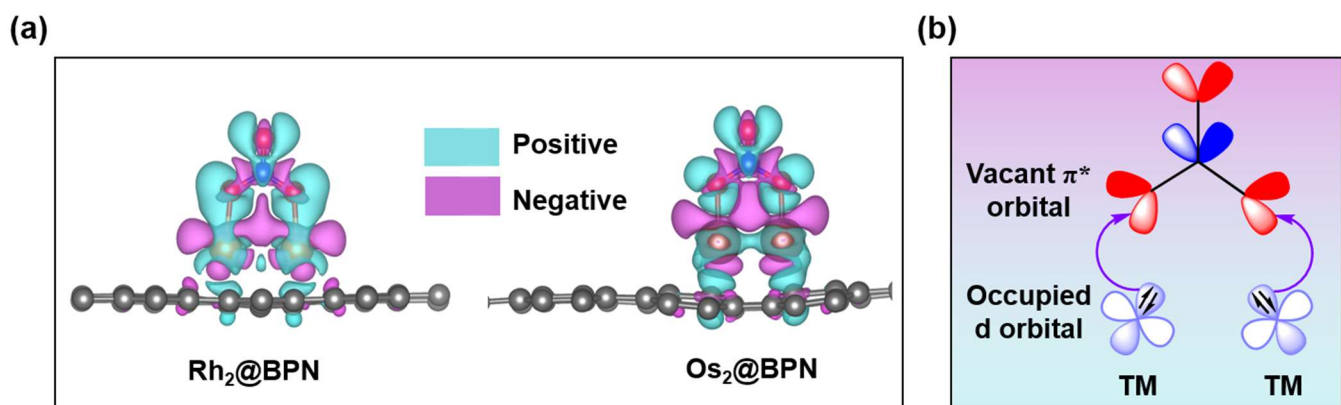


Figure S15 (a) Charge density differences of nitrate adsorbed on $\text{Rh}_2\text{@BPN}$, and $\text{Os}_2\text{@BPN}$ the isosurface value is $0.001 \text{ e} / \text{\AA}^3$. **(b)** Schematic representation of the nitrate adsorption mechanism on the TM dimer.

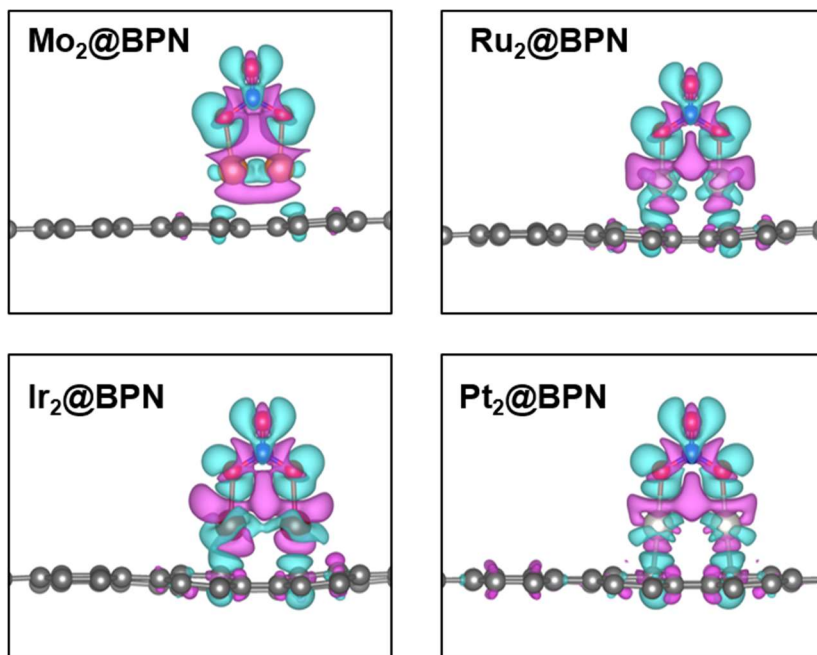


Figure S16. Charge density differences of nitrate adsorbed on $\text{Mo}_2\text{@BPN}$, $\text{Ru}_2\text{@BPN}$, $\text{Ir}_2\text{@BPN}$ and $\text{Pt}_2\text{@BPN}$, the isosurface value is $0.001 \text{ e} / \text{\AA}^3$. The charge depletion and accumulation were depicted by cyan and violet respectively.

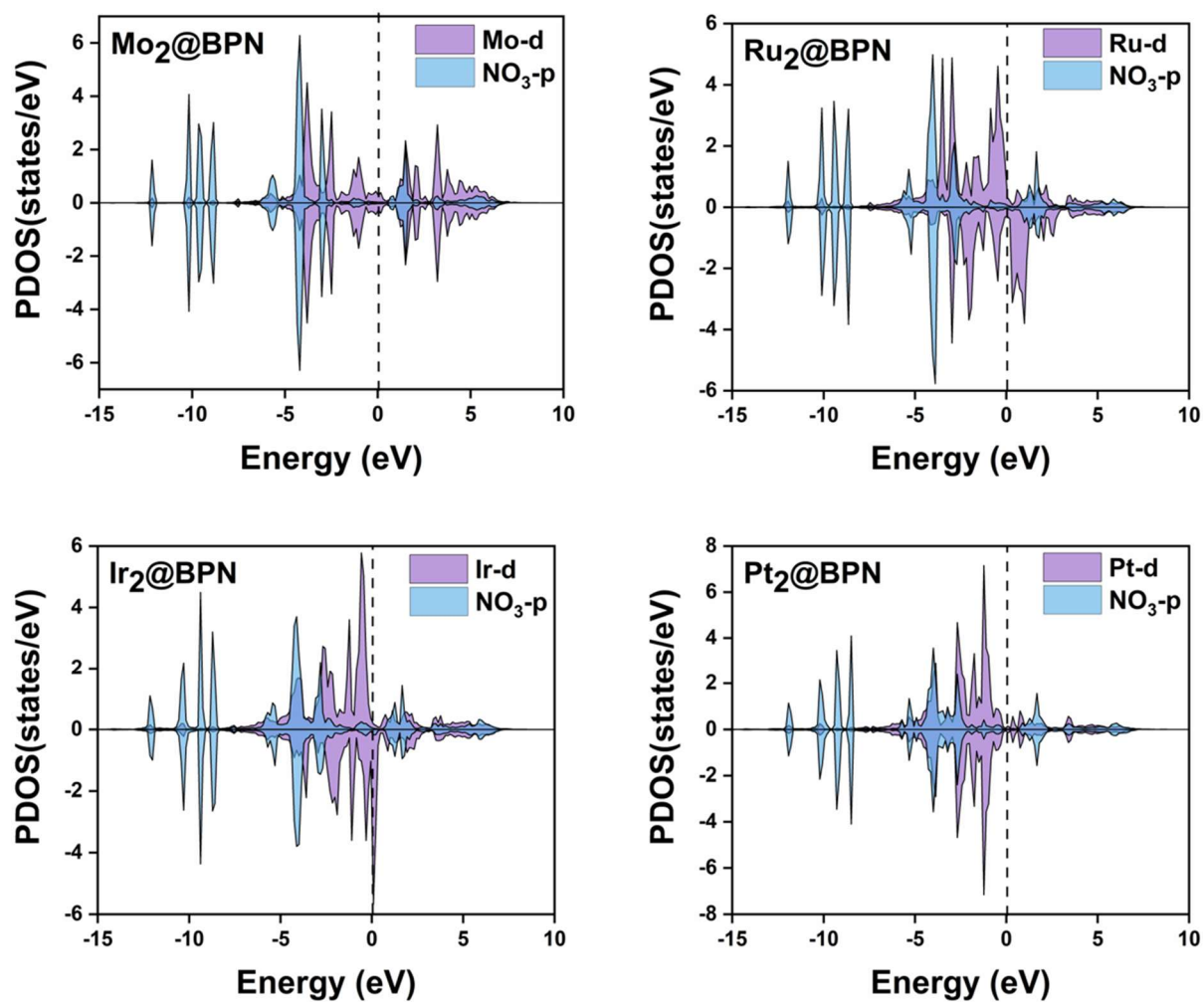
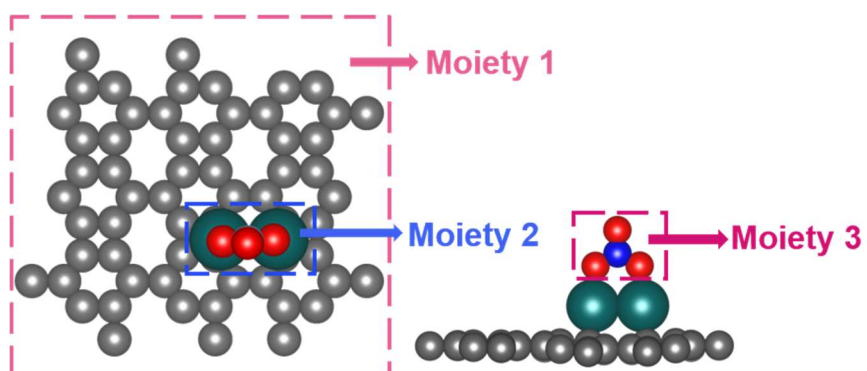


Figure S17. Partial density of states (PDOS) on the molecular orbital of NO₃ and the d orbital of metal atoms on Mo₂@BPN, Ru₂@BPN, Ir₂@BPN and Pt₂@BPN catalysts after NO₃ adsorption.

(a)



(b)

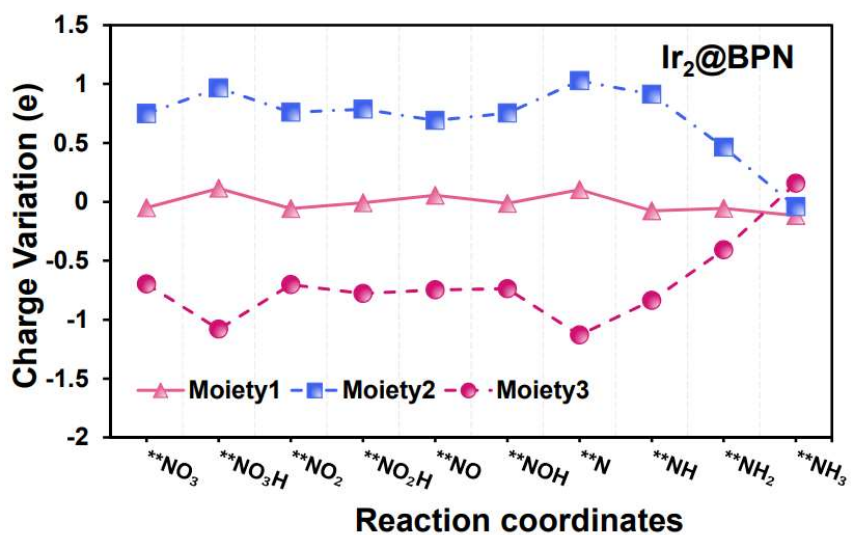
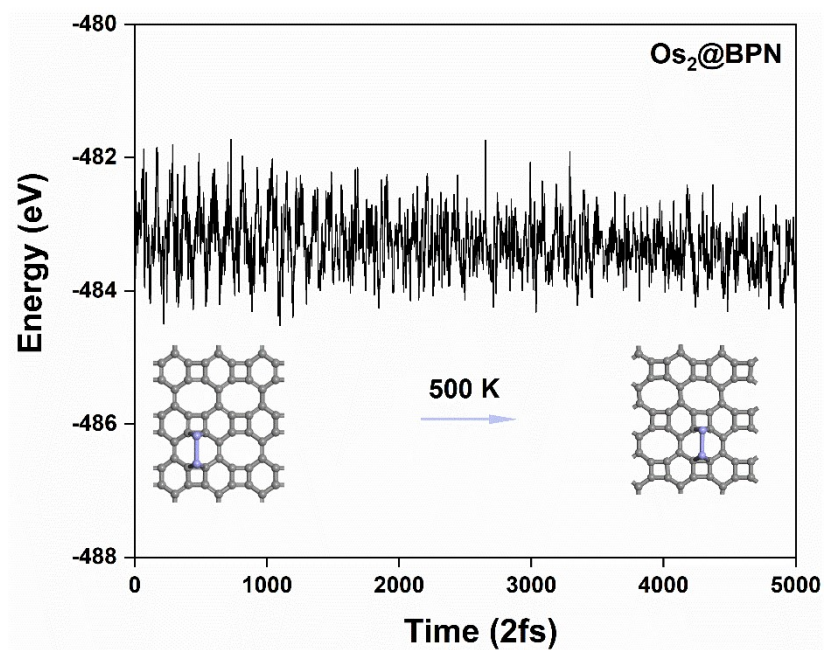


Figure S18. (a) Three moieties of $\text{TM}_2@\text{BPN}$. (b) Charge variation during the process of NO_3RR on $\text{Ir}_2@\text{BPN}$.

(a)



(b)

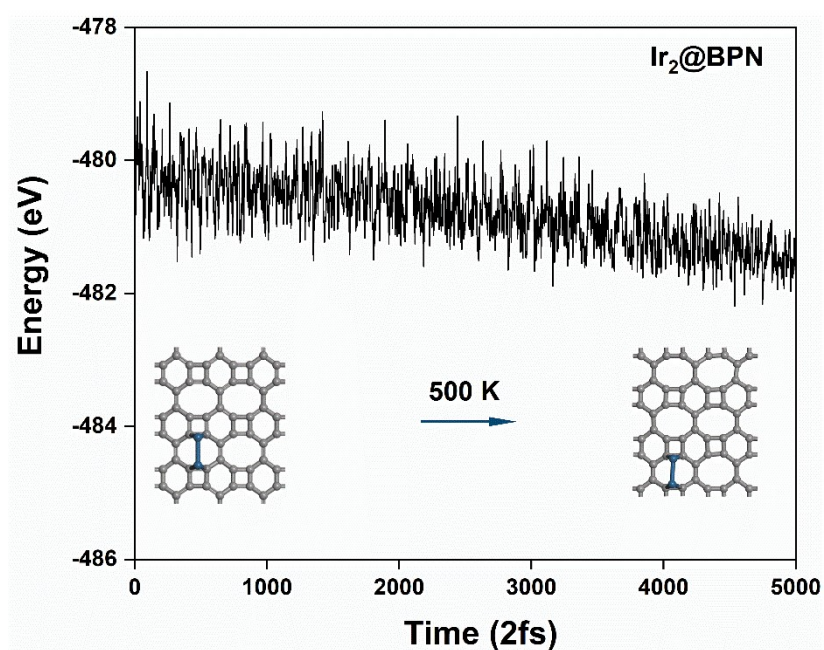


Figure S19. Ab initio molecular dynamics simulation of (a) $\text{Os}_2@\text{BPN}$, and (b) $\text{Ir}_2@\text{BPN}$ was carried out at 500 K for a total duration of 10 ps with a time step of 2 fs.

Table S1. Zero-point energy (ΔE_{ZPE}) and entropy ($T\Delta S$) at room temperature of gaseous molecules from the NIST database.

Species	E_{ZPE}	$T\Delta S$
HNO₃	0.69	0.83
H₂	0.27	0.41
NH₃	0.91	0.59
H₂O	0.58	0.67
NO₂	0.23	0.74
NO	0.12	0.64

Table S2. The computed binding energy (E_b), cohesive energy (E_{coh}) and the difference between binding and cohesive (E_b-E_{coh}) of TM dimers in TM₂@BPN.

Metal	E_b (eV)	E_{coh} (eV)	E_b-E_{coh} (eV)
Sc₂	-7.85	-5.27	-2.58
Ti₂	-7.22	-6.21	-1.01
V₂	-5.33	-5.60	0.02
Cr₂	-2.90	-4.19	1.03
Mn₂	-4.48	-4.62	0.14
Fe₂	-8.56	-7.43	-1.13
Co₂	-4.88	-5.14	0.12
Ni₂	-5.89	-4.96	-0.93
Cu₂	-2.91	-3.73	0.53
Zn₂	-0.07	-1.00	0.93
Y₂	-7.81	-4.75	-3.05
Zr₂	-9.28	-7.03	-2.25
Nb₂	-8.10	-6.94	-1.15
Mo₂	-7.28	-6.42	-0.86
Ru₂	-8.85	-8.16	-0.69
Rh₂	-6.85	-5.80	-1.05
Pd₂	-4.46	-3.74	-0.72
Ag₂	-1.77	-2.82	0.72
Cd₂	-0.08	-0.62	0.54
Hf₂	-9.31	-7.31	-1.99
Ta₂	-9.87	-8.56	-1.31
W₂	-9.62	-8.88	-0.74
Re₂	-7.60	-7.85	0.25
Os₂	-8.74	-8.71	-0.03
Ir₂	-8.07	-7.18	-0.88
Pt₂	-7.02	-5.43	-1.58
Au₂	-2.58	-3.09	0.51
Hg₂	-0.06	-0.20	0.14

Table S3. Electronic and structural properties of TM₂@BPN, including TM dimer bond length (**d_{M-M}**), charge transfer (**CT**) from TM dimer to substrate, and d band center (**ε_d**).

Metal	d_{M-M} (Å)	CT (e)	ε_d (eV)
Sc₂	4.07	3.27	2.24
Ti₂	3.77	2.95	0.57
V₂	2.43	1.98	0.51
Mn₂	2.56	1.28	-0.96
Fe₂	2.18	0.94	-1.89
Co₂	2.17	0.69	-2.32
Ni₂	2.35	0.61	-2.29
Y₂	4.09	2.57	3.42
Zr₂	3.55	2.34	2.02
Nb₂	2.60	1.72	0.76
Mo₂	1.72	0.95	-1.73
Ru₂	2.25	0.65	-2.61
Rh₂	2.62	0.52	-2.37
Pd₂	2.65	0.29	-3.95
Hf₂	3.28	4.41	1.90
Ta₂	2.48	2.89	0.69
W₂	2.10	1.39	-0.03
Re₂	2.13	0.99	-1.77
Os₂	2.27	0.69	-2.64
Ir₂	2.40	0.35	-3.39
Pt₂	2.55	0.16	-4.58

Table S4. Calculated adsorption free energy $\Delta G^*_{\text{NO}_3}$ (eV) on $\text{TM}_2\text{@BPN}$, via ($\eta^1\text{-O-1}$), ($\eta^2\text{-O-1}$) and ($\eta^2\text{-O-2}$) configuration.

Metal	($\eta^1\text{-O-1}$)	($\eta^2\text{-O-1}$)	($\eta^2\text{-O-2}$)
Sc₂	-1.43	-2.39	-2.96
Ti₂	-1.67	---	-3.20
V₂	-1.62	Relax to $\eta^2\text{-O-2}$	-2.80
Mn₂	-0.57	Relax to $\eta^2\text{-O-2}$	-2.12
Fe₂	Relax to $\eta^2\text{-O-2}$	Relax to $\eta^2\text{-O-2}$	-1.83
Co₂	Relax to $\eta^2\text{-O-2}$	Relax to $\eta^2\text{-O-2}$	-1.88
Ni₂	Relax to $\eta^2\text{-O-2}$	Relax to $\eta^2\text{-O-2}$	-1.68
Y₂	-1.45	-2.15	-2.87
Zr₂	-1.52	-2.20	-2.81
Nb₂	-1.14	Relax to $\eta^2\text{-O-2}$	-2.51
Mo₂	-0.87	Relax to $\eta^2\text{-O-2}$	-2.11
Ru₂	Relax to $\eta^2\text{-O-1}$	-0.89	-1.39
Rh₂	Relax to $\eta^2\text{-O-2}$	Relax to $\eta^2\text{-O-2}$	-1.52
Pd₂	-0.38	-0.69	-0.77
Hf₂	-1.64	---	-3.08
Ta₂	-1.53	---	-2.88
W₂	Relax to $\eta^1\text{-O-2}$	---	-2.60
Re₂	-1.22	Relax to $\eta^2\text{-O-2}$	-2.13
Os₂	-6.78	-0.82	-1.21
Ir₂	-0.10	-0.37	-1.04
Pt₂	Relax to $\eta^2\text{-O-2}$	Relax to $\eta^2\text{-O-2}$	-0.91

Table S5. Transition Metal to Oxygen bond distance for the stable NO₃⁻ adsorbed configuration (η^2 -O-2) on TM₂@BPN.

Metal	dM ₁ -O ₁ (Å)	dM ₂ -O ₂ (Å)
Sc₂	2.10	2.08
Ti₂	1.97	1.97
V₂	1.96	1.96
Mn₂	1.95	1.94
Fe₂	1.92	1.92
Co₂	1.89	1.89
Ni₂	1.88	1.89
Y₂	2.25	2.22
Zr₂	2.14	2.15
Nb₂	2.13	2.11
Mo₂	2.12	2.13
Ru₂	2.07	2.07
Rh₂	2.06	2.03
Pd₂	2.12	2.11
Hf₂	2.08	2.07
Ta₂	2.04	2.05
W₂	2.03	2.03
Re₂	2.04	2.04
Os₂	2.07	2.06
Ir₂	2.05	2.09
Pt₂	2.09	2.09

Table S6. Calculated Gibbs free energy of *H (ΔG^*_{H}) adsorption on $TM_2@BPN$.

Metal	ΔG^*_{H} (eV)
Sc₂	0.43
Ti₂	-1.06
V₂	-1.52
Mn₂	-1.002
Fe₂	-0.69
Co₂	-0.89
Ni₂	-0.85
Y₂	-0.88
Zr₂	-0.53
Nb₂	-1.17
Mo₂	-0.50
Ru₂	-0.39
Rh₂	-1.02
Pd₂	-0.44
Hf₂	-0.86
Ta₂	-1.17
W₂	-0.39
Re₂	-0.75
Os₂	-0.66
Ir₂	-0.58
Pt₂	-0.27

Table S7. Calculated charge transfer (CT) from TM dimer to NO₃, on TM₂@BPN.

Metal	CT (e)
Sc₂	-1.03
Ti₂	-1.13
V₂	-0.97
Mn₂	-0.87
Fe₂	-0.88
Co₂	-0.73
Y₂	-0.97
Zr₂	-0.99
Nb₂	-0.89
Mo₂	-0.90
Ru₂	-0.76
Rh₂	-0.74
Pd₂	-0.73
Hf₂	-1.09
W₂	-1.09
Re₂	-0.93
Os₂	-0.80
Ir₂	-0.69
Pt₂	-0.68

Table S8. The Computed limiting potential (U_L) and potential determining step (PDS) of $TM_2@BPN$ for NO_3RR .

Metal	U_L (V)	PDS
Sc₂	-2.19	$*OH \rightarrow *OH_2$
Ti₂	-1.92	$*OH \rightarrow *OH_2$
V₂	-1.57	$*OH \rightarrow *OH_2$
Mn₂	-0.86	$*NH_2 \rightarrow *NH_3$
Fe₂	-0.75	$*NH_2 \rightarrow *NH_3$
Co₂	-1.69	$*OH \rightarrow *OH_2$
Ni₂	-0.59	$*NH_2 \rightarrow *NH_3$
Y₂	-2.3	$*OH \rightarrow *OH_2$
Zr₂	-2.06	$*OH \rightarrow *OH_2$
Nb₂	-1.87	$*OH \rightarrow *OH_2$
Mo₂	-0.40	$*NO_2 \rightarrow *OH-*NO$
Ru₂	-0.36	$*NH_2 \rightarrow *NH_3$
Rh₂	-0.16	$**NO \rightarrow **NOH$
Pd₂	-0.56	$*NO_2 \rightarrow *OH-*NO$
Hf₂	-1.75	$*OH \rightarrow *OH_2$
Ta₂	-1.79	$*NH_2OH \rightarrow *OH$
W₂	-1.29	$*NH_2OH \rightarrow *OH$
Re₂	-1.10	$*OH \rightarrow *OH_2$
Os₂	-0.32	$*NO \rightarrow *NOH$
Ir₂	-0.35	$*NH_2 \rightarrow *NH_3$
Pt₂	-0.45	$*NO_2 \rightarrow *OH-*NO$

Table S9. The calculated Zero-point energy (ΔE_{ZPE}) and entropic contributions ($T\Delta S$) at room temperature (298.15 K) to the Gibbs free energies of each elementary step for Rh₂@BPN. The unit is eV.

Reaction Intermediate	ZPE	$T\Delta S$
*NO ₃	0.411886356	0.237674
*NO ₃ H	0.594182189	0.36836
*NO ₂	0.246676255	0.192045
*NO ₂ H	0.528059538	0.285605
*NO	0.174623183	0.180012
*NOH	0.478887257	0.120561
*NHOH	0.687736906	0.194516
*NH ₂ OH	0.989150923	0.279013
*NH ₂	0.688463775	0.120496
*NH ₃	0.972807823	0.201186

Table S10. The calculated Zero-point energy (ΔE_{ZPE}) and entropic contributions ($T\Delta S$) at room temperature (298.15 K) to the Gibbs free energies of each elementary step for Os₂@BPN. The unit is eV.

Reaction Intermediate	ZPE	$T\Delta S$
*NO ₃	0.407854772	0.23698396
*NO ₃ H	0.598977333	0.33509831
*NO ₂	0.269120928	0.17842331
*NO ₂ H	0.47364532	0.32699135
*NO	0.183149329	0.15536326
*NOH	0.47166756	0.15971709

*N	0.092907907	0.04237797
*NH	0.360087728	0.07510918
*NH₂	0.710595576	0.08048906
*NH₃	1.029020916	0.17182477

Table S11. The calculated Zero-point energy (ΔE_{ZPE}) and entropic contributions ($T\Delta S$) at room temperature (298.15 K) to the Gibbs free energies of each elementary step for Ir₂@BPN. The unit is eV.

Reaction Intermediate	ZPE	$T\Delta S$
*NO₃	0.4105032	0.2444296
*NO₃H	0.57244292	0.4347727
*NO₂	0.27766138	0.1789226
*NO₂H	0.5118728	0.2985911
*NO	0.16876833	0.1847541
*NOH	0.46187944	0.1865558
*N	0.08414371	0.0785057
*NH	0.34859161	0.1056357
*NH₂	0.70977985	0.0869787
*NH₃	1.02871144	0.1976006

Table S12. Calculated adsorption free energy ΔG^*_{NO} (eV) on $\text{TM}_2\text{@BPN}$, via *NO end, *ON end, and **NO side configurations.

Metal	*NO-end	*ON-end	**NO-side
Sc₂	Relax to NO-side	Relax to NO-side	-5.82
Ti₂	Relax to NO-side	Relax to NO-side	-6.90
V₂	Relax to NO-side	-4.41	-7.24
Mn₂	-5.27	-3.69	-5.71
Fe₂	Relax to NO-side	-3.74	-5.69
Co₂	Relax to NO-side	-3.62	-6.23
Ni₂	-4.51	Relax to NO-side	-5.32
Y₂	-5.77	Relax to NO-side	-6.51
Zr₂	-5.23	Relax to NO-side	-7.46
Nb₂	Relax to NO-side	-4.13	-7.25
Mo₂	-4.83	-3.29	-4.33
Ru₂	Relax to NO-side	-3.07	-5.03
Rh₂	Relax to NO-side	-3.41	-5.35
Pd₂	-3.94	Relax to NO-end	-4.10
Hf₂	Relax to NO-side	Relax to NO-side	-7.56
Ta₂	Relax to NO-side	Relax to NO-side	-7.72
W₂	-5.38	-3.56	-6.05
Re₂	-4.73	-2.91	-4.90
Os₂	-4.85	-2.34	-4.54
Ir₂	-4.96	-2.61	-4.83
Pt₂	-3.86	-2.88	-4.04

Table S13. Calculated adsorption free energy $\Delta G^*_{\text{NO}_3}$ (eV) on TM@BPN, via 1-O, and 2-O configuration.

Metal (SACs)	1-O	2-O
Rh	-0.17	-0.96
Os	-1.12	-1.81
Ir	-0.89	-1.63

Table S14. The comparison of catalytic performance (reflected by limiting potential, U_L) for Nitrate reduction reaction on various electrocatalysts.

Electrocatalysts	U_L (V)	References
Fe-V₂O₅	-0.37	1
BiPd	-0.40	2
FeB₂	-0.31	3
RuO_x	-0.33	4
Ni-Cu-SSA	-0.33	5
10Cu/TiO_{2-x}	-1.18	6
Cu-<i>cis</i>-N₂O₂	-0.39	7
WSe_{2-x}	-0.86	8
Fe-SnS₂-Vs	-3.04	9
FeS₂	-0.71	10
Rh₂@BPN	-0.16	This work
Os₂@BPN	-0.32	This work
Ir₂@BPN	-0.35	This work

Table S15. Calculated d-band center (ϵ_d) of TM@BPN.

Metal (SACs)	ϵ_d (eV)
Rh	-3.26
Os	-2.50
Ir	-3.05

Table S16. Calculated limiting potential of HER and NO₃RR and faradic efficiency (FE) values for TM₂@BPN.

Metals	U _L (NO ₃ RR)	U _L (HER)	FE%
Mo₂	-0.40	-0.50	98.0
Ru₂	-0.36	-0.39	78.8
Rh₂	-0.16	-0.69	100.0
Os₂	-0.32	-0.41	99.9
Ir₂	-0.35	-0.39	99.9
Pt₂	-0.45	-0.27	0.09

Table S17. Comparison of nitrate reduction reaction pathways on the Rh₂@BPN by using DFT-D3 and DFT-Sol method.

Rh	NO ₃	1	2	3	4	5	6	7	8	9	U _L
DFT-D3	-1.525	-2.877	-4.069	-5.479	-5.353	-5.188	-5.535	-6.598	-7.234	-7.188	0.16
DFT-D3-Sol	-1.371	-2.861	-3.916	-5.329	-5.088	-5.011	-5.383	-6.450	-7.103	-7.410	0.24

Table S18. Comparison of nitrate reduction reaction pathways on the Os₂@BPN by using DFT-D3 and DFT-Sol method.

Os	NO ₃	1	2	3	4	5	6	7	8	9	U _L
DFT-D3	-1.208	-4.093	-3.827	-4.318	-4.852	-4.527	-6.398	-6.840	-6.991	-7.079	0.32
DFT-D3-Sol	-1.209	-4.184	-3.851	-4.402	-4.915	-4.629	-6.434	-6.834	-7.133	-7.487	0.29

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