

## Supporting Information

### **Trans-interfacial distribution of Se vacancies in Bi<sub>2</sub>Se<sub>3</sub> core and carbon nanofiber matrix enables long-lifespan and ultra-stable sodium storage**

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## Methods

### 1. Material characterizations

X-ray diffraction (XRD, SmartLab-SE, 40 kV, Cu-K $\alpha$  Radiation,  $\lambda = 0.154$  nm) and X-ray photoelectron spectroscopy (XPS, Thermo Scientific K-Alpha) were employed for the phase characterization of the samples. Morphology and structural characterization were performed using field-emission scanning electron microscopy (FESEM, Hitachi S-4800) and transmission electron microscopy (TEM, JEOL JEM-2100F). Raman spectroscopy testing was conducted using a Xplora Plus. Electron paramagnetic resonance (EPR) spectra obtained using a Bruker W500 spectrometer. Nitrogen adsorption-desorption isotherm and Brunauer-Emmett-Teller (BET) surface area measurements were conducted at 77 K using a Micromeritics ASAP 2460 instrument. The carbon content of Bi<sub>2</sub>Se<sub>3-x</sub>@CNFs composite material was analyzed using thermogravimetric analysis (TGA, Hitachi STA7300) from 30 to 800 °C in air with a heating rate of 10 °C min<sup>-1</sup>.

### 2. Electrochemical measurements

The electrochemical properties of the as-obtained samples were assessed using CR2032 half-cells, which were assembled in an Ar-filled glove box. The working electrode was prepared by mixing the active material, Super P, and polyvinylidene fluoride (PVDF) in a mass ratio of 7:2:1 in N-methyl-2-pyrrolidone (NMP). Then, the slurry was uniformly coated onto a copper foil and vacuum-dried at 70 °C for 12 hours. The electrode was punched into disks with a diameter of 12 mm. The half-cell assembly included sodium metal as the counter electrode, a Whatman GF/D glass fiber as the separator, and 1 M NaPF<sub>6</sub> in DME as the electrolyte. The assembly of full cells involved using Bi<sub>2</sub>Se<sub>3-x</sub>@CNFs as the anode material and Na<sub>3</sub>V<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub> mixed with Super P and polyvinylidene fluoride (PVDF) in an 8:1:1 ratio, coated on aluminum foil as the cathode material and assessed within a voltage range of 0.8-3.8 V. Galvanostatic charge-discharge (GCD) tests and galvanostatic intermittent titration technique (GITT) measurements were performed on a LAND CT-2001A battery

testing system within a voltage window of 0.01-3.0 V(vs. Na<sup>+</sup>/Na). Cyclic voltammetry (CV) and electrochemical impedance spectroscopy (EIS) tests were conducted on the CHI 660E electrochemical workstation (Chenhua Instrument Company, Shanghai, China). The CV tests were performed at scan rates ranging from 0.1 to 1 mV s<sup>-1</sup>, while the EIS measurements were taken over a frequency range of 10<sup>5</sup> Hz to 10<sup>-2</sup> Hz.

### 3. Calculation process for Bi<sub>2</sub>Se<sub>3</sub> content in Bi<sub>2</sub>Se<sub>3-x</sub>@CNFs from TGA analysis

The content of Bi<sub>2</sub>Se<sub>3</sub> in Bi<sub>2</sub>Se<sub>3-x</sub>@CNFs was determined by thermogravimetric analysis (TGA). The weight increment of Bi<sub>2</sub>O<sub>3</sub>, generated by the oxidation of Bi<sub>2</sub>Se<sub>3</sub> (2Bi<sub>2</sub>Se<sub>3</sub> + 10O<sub>2</sub> + C → 2Bi<sub>2</sub>O<sub>3</sub> + CO<sub>2</sub>↑ + 6SeO<sub>2</sub>↑), was analyzed based on the weight loss due to carbon combustion (Figure S3b). According to the reaction equation, the weight loss of pure Bi<sub>2</sub>Se<sub>3</sub> to form Bi<sub>2</sub>O<sub>3</sub> is 28.9%. Therefore, the content of Bi<sub>2</sub>Se<sub>3</sub> in Bi<sub>2</sub>Se<sub>3-x</sub>@CNFs can be calculated by the following formula:

$$X * 28.9\% + (100 - X) = 86.4\% \quad (S1)$$

where  $X$  represents the loading content of Bi<sub>2</sub>Se<sub>3</sub>, and the loading content of carbon is (100%- $X$ ). From this, it can be calculated that the content of Bi<sub>2</sub>Se<sub>3</sub> in Bi<sub>2</sub>Se<sub>3-x</sub>@CNFs-600 is 18.8%.

### 4. The calculation process for the pseudocapacitive contribution:

The measured current of the CV curves can be attributed to two types of charge storage mechanisms for electrode materials. Typically, the kinetics of charge storage can be explored through the power-law relationship between the measured current density ( $i$ ) and the sweep rate ( $v$ ), which is described by the following equations:

$$i = av^b \quad (S2)$$

$$\log(i) = b\log(v) + \log(a) \quad (S3)$$

in these equations,  $a$  and  $b$  are variables. Specifically, the  $b$ -value of 0.5 indicates a purely faradaic intercalation process, while the  $b$ -value of 1 signifies an ideally capacitive contribution process. Quantitatively, the mixed behaviors can be further distinguished by separating the current response ( $i$ ) at a specific potential ( $V$ ), as

described by the following equations:

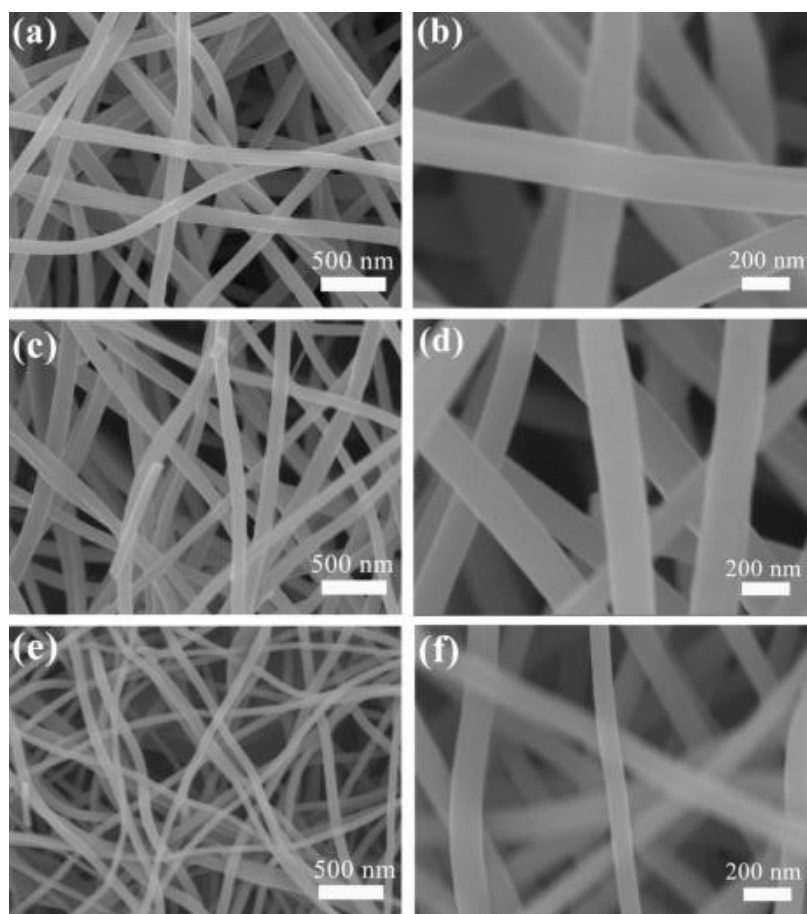
$$i(\nu) = k_1\nu + k_2\nu^{1/2} \quad (\text{S4})$$

where  $k_1\nu$  and  $k_2\nu^{1/2}$  represent the contributions of the capacitive and diffusion behaviors, respectively.

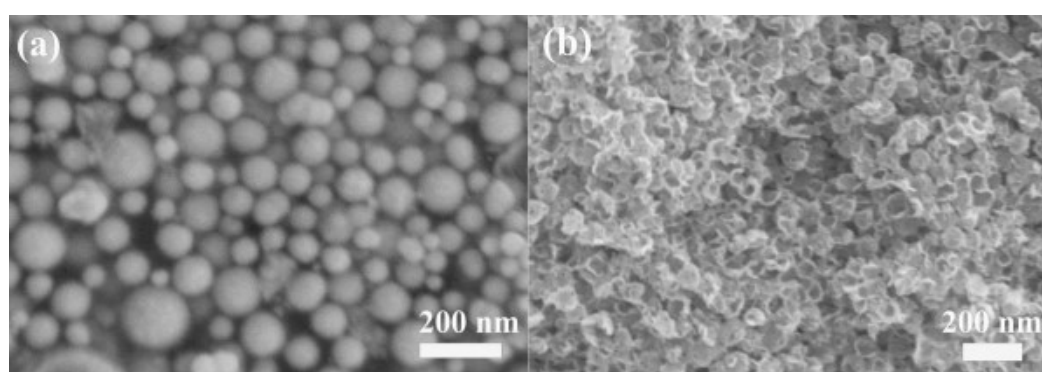
## 5. DFT method

All the computations were carried out by spin-polarized DFT method, as implemented in Vienna ab initio Simulation Package (VASP 5.4.4). The exchange correlation energy was modeled by the Perdew–Burke–Ernzerhof (PBE) functional within the generalized gradient approximation (GGA). An energy cutoff of 450 eV was adopted for the plane-wave basis. In structural optimizations, the energy and force convergence thresholds were set to  $10^{-5}$  eV and 0.05 eV/Å, respectively. The Brillouin zone was sampled by  $2 \times 2 \times 1$  k-points using the Monkhorst–Pack scheme. we constructed  $3 \times 3 \times 1$  supercells from the unit cells of  $\text{Bi}_2\text{Se}_3$  and  $5 \times 5 \times 1$  supercells from graphene to build heterostructures. A vacuum of 30 Å along the z-direction was fixed to avoid interaction between adjacent layers. Visualization was performed using VESTA, and postprocessing of the VASP data was conducted with VASPKIT.

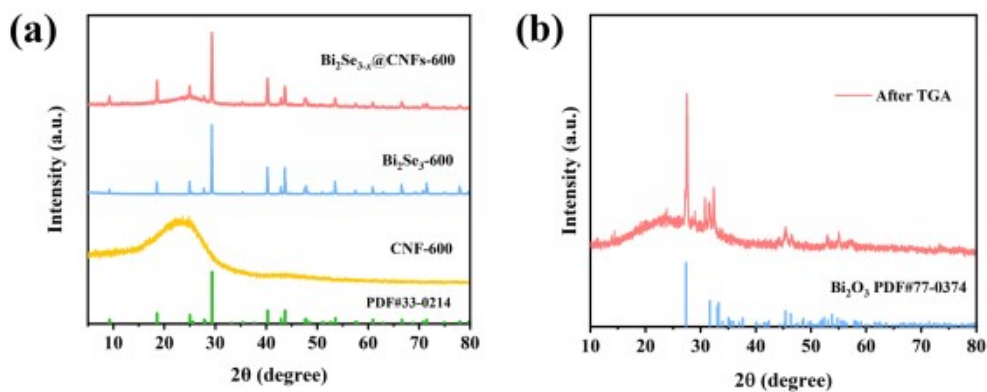
## Supplementary Figures and Tables



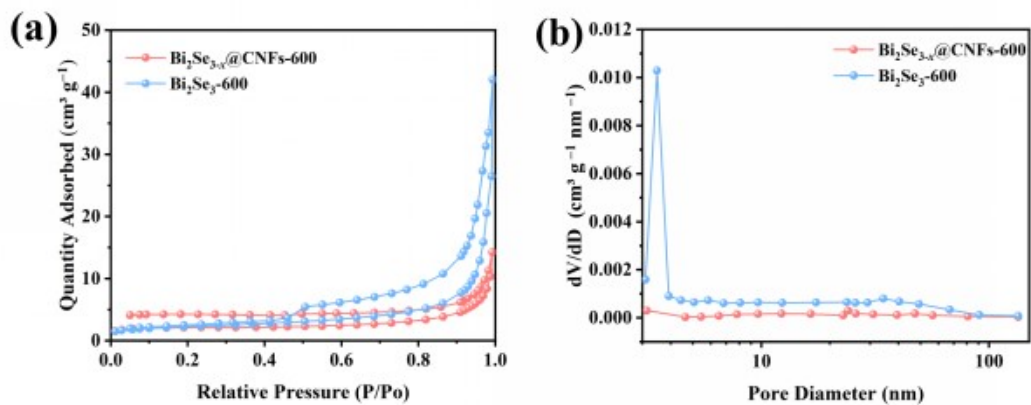
**Fig. S1.** SEM images of (a, b)  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-500}$ , (c, d)  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-700}$  and (e, f) CNFs.



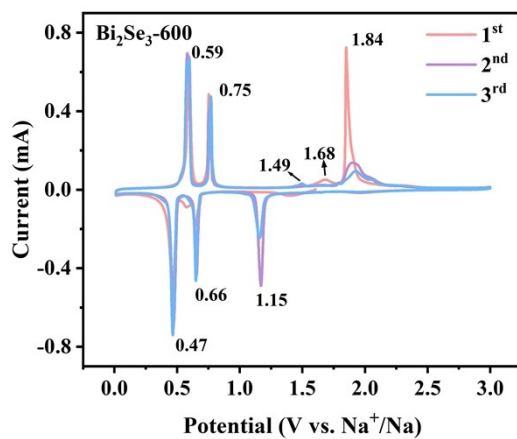
**Fig. S2.** SEM images of (a) Bi PNS and (b)  $\text{Bi}_2\text{Se}_3$ .



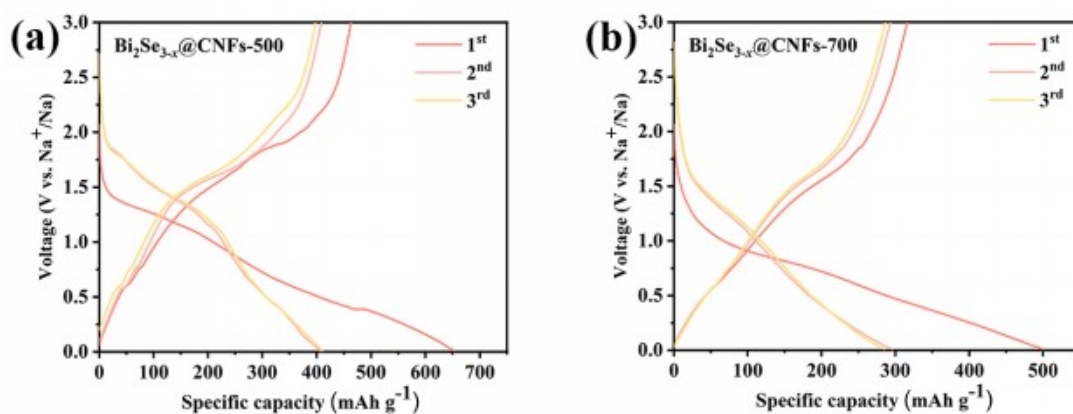
**Fig. S3.** (a) XRD patterns of  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-600}$ ,  $\text{Bi}_2\text{Se}_3\text{-600}$  and pure CNF, (b) XRD pattern of  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-600}$  residue after the TGA test.



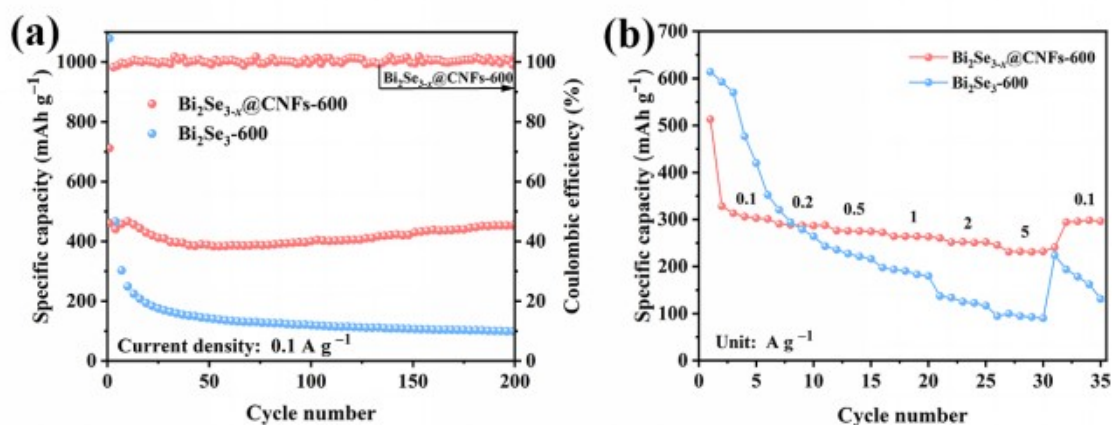
**Fig. S4.** (a)  $\text{N}_2$  adsorption-desorption isotherms and (b) Pore size distribution profiles of  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-600}$  and  $\text{Bi}_2\text{Se}_3\text{-600}$ .



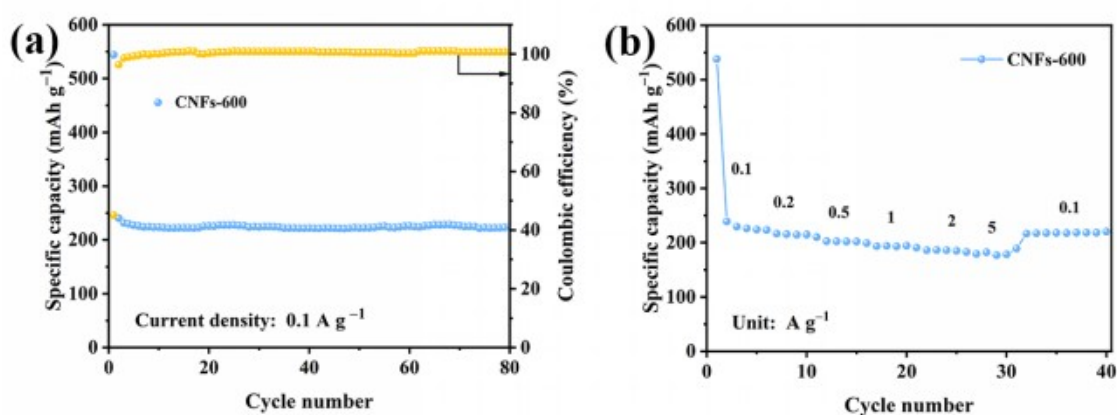
**Fig. S5.** CV curves of  $\text{Bi}_2\text{Se}_3\text{-600}$  at  $0.1 \text{ mV s}^{-1}$ .



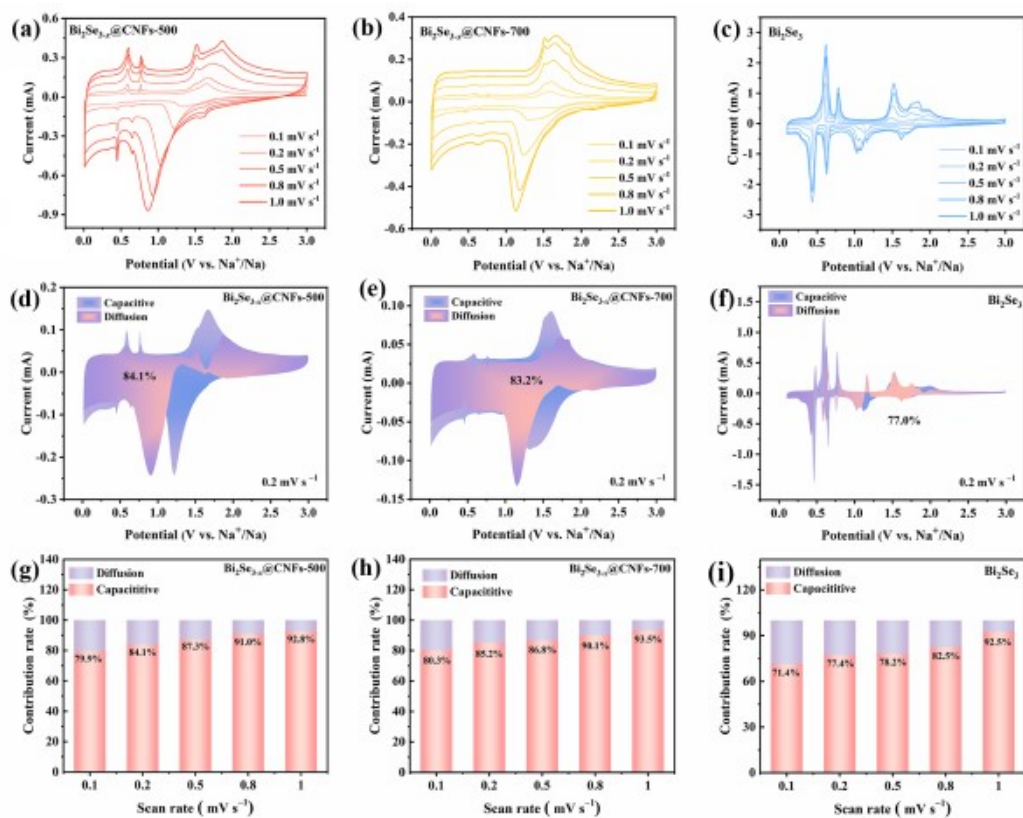
**Fig. S6.** GCD profiles at  $0.1 \text{ A g}^{-1}$  of (a)  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-500}$  and (b)  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-700}$ .



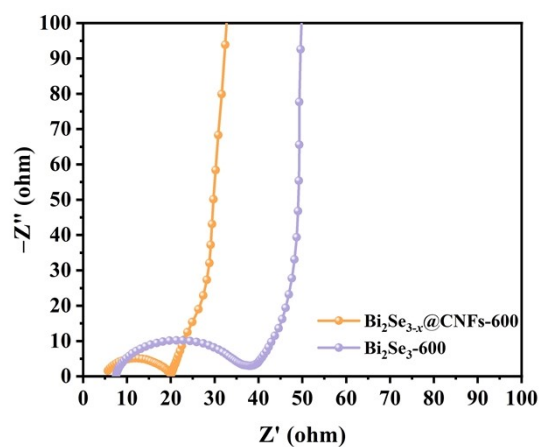
**Fig. S7.** (a) Cycling performance at  $0.1 \text{ A g}^{-1}$ , (b) rate performance of  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-600}$  and  $\text{Bi}_2\text{Se}_3\text{-600}$ .



**Fig. S8.** (a) Cycling performance at  $0.1 \text{ A g}^{-1}$ , (b) rate performance of CNFs-600.



**Fig. S9.** (a-c) CV curves at various scan rates. (d-f) Capacitive contribution at 0.2  $\text{mV s}^{-1}$ . (g-i) Capacitive contribution ratios of  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-500}$ ,  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-700}$  and  $\text{Bi}_2\text{Se}_3$  at various scan rates.



**Fig. S10.** Nyquist plots of  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-600}$  and  $\text{Bi}_2\text{Se}_3\text{-600}$ .



**Table S1.** The electrochemical performance comparison of  $\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-600}$  with other reported  $\text{Bi}_2\text{Se}_3$ -based anode materials.

Sample	Current density ( $\text{A g}^{-1}$ )	Cycles	Capacity after cycling ( $\text{mAh g}^{-1}$ )	Ref.
$\text{Bi}_2\text{Se}_3/\text{NG-7}$	1	129 <sup>th</sup>	254.5	[1]
G- $\text{Bi}_2\text{Se}_3/\text{C}$	0.1	100 <sup>th</sup>	375.3	[2]
$\text{Bi}_2\text{Se}_3\text{-C/G-1}$	2	1000 <sup>th</sup>	241	[3]
$\text{Bi}_2\text{Se}_3/\text{Bi}_2\text{O}_3$	0.1	100 <sup>th</sup>	310	[4]
$\text{Bi}_2\text{Se}_3$ nanocrystal	1	200 <sup>th</sup>	210.2	[5]
$\text{Bi}_2\text{Se}_{3-x}\text{@DNC}$	5	1500 <sup>th</sup>	253.4	[6]
$\text{Bi}_2\text{Se}_3\text{@NC}(\text{Co})$	5	500 <sup>th</sup>	238	[7]
$\text{Bi}_2\text{Se}_{3-x}\text{@CNFs-600}$	5	3000 <sup>th</sup>	284	This work

## References

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