

Supporting Information

Design of moderate-pressure superconductivity in the ternary hydride system

Contents

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Contents

1. **Figure S1.** The convex hulls for LiTiH₆, LiZrH₆, and LiHfH₆ at 50 GPa.
2. **Figure S2.** Calculated phonon spectrum of newly predicted ABH₃ under different pressure.
3. **Figure S3.** Calculated phonon spectrum of newly predicted ABH₆ under different pressure.
4. **Figure S4.** Calculated phonon spectrum of newly predicted AB₂H₆ under different pressure.
5. **Figure S5.** The superconducting energy gaps Δ_{nk} at different temperatures for LiTiH₆, LiZrH₆, and LiHfH₆ at 50 GPa.
6. **Table S1.** Key superconducting parameters for dynamically stable ABH₃, ABH₆ and AB₂H₆ at different pressures.
7. **Table S2.** Possible reaction routes and formation enthalpies for LiTiH₆, LiZrH₆ and LiHfH₆ at 50 GPa.
8. **Table S3.** Computed superconducting parameters for BeZrH₃ and MgHCu₃.

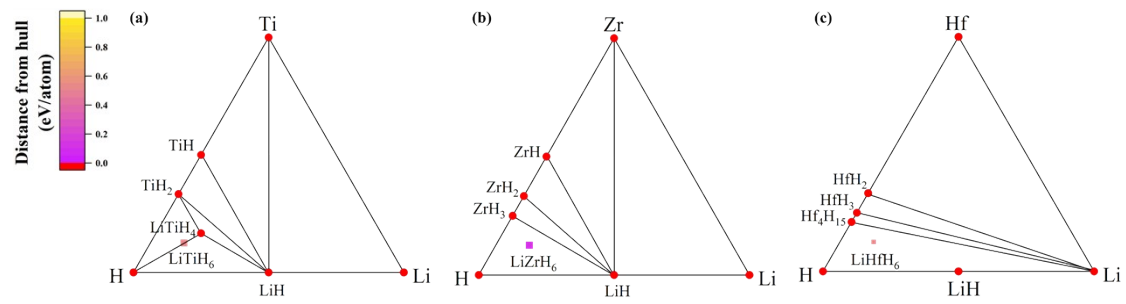


Figure S1. The convex hulls for LiTiH_6 , LiZrH_6 , and LiHfH_6 at 50 GPa.

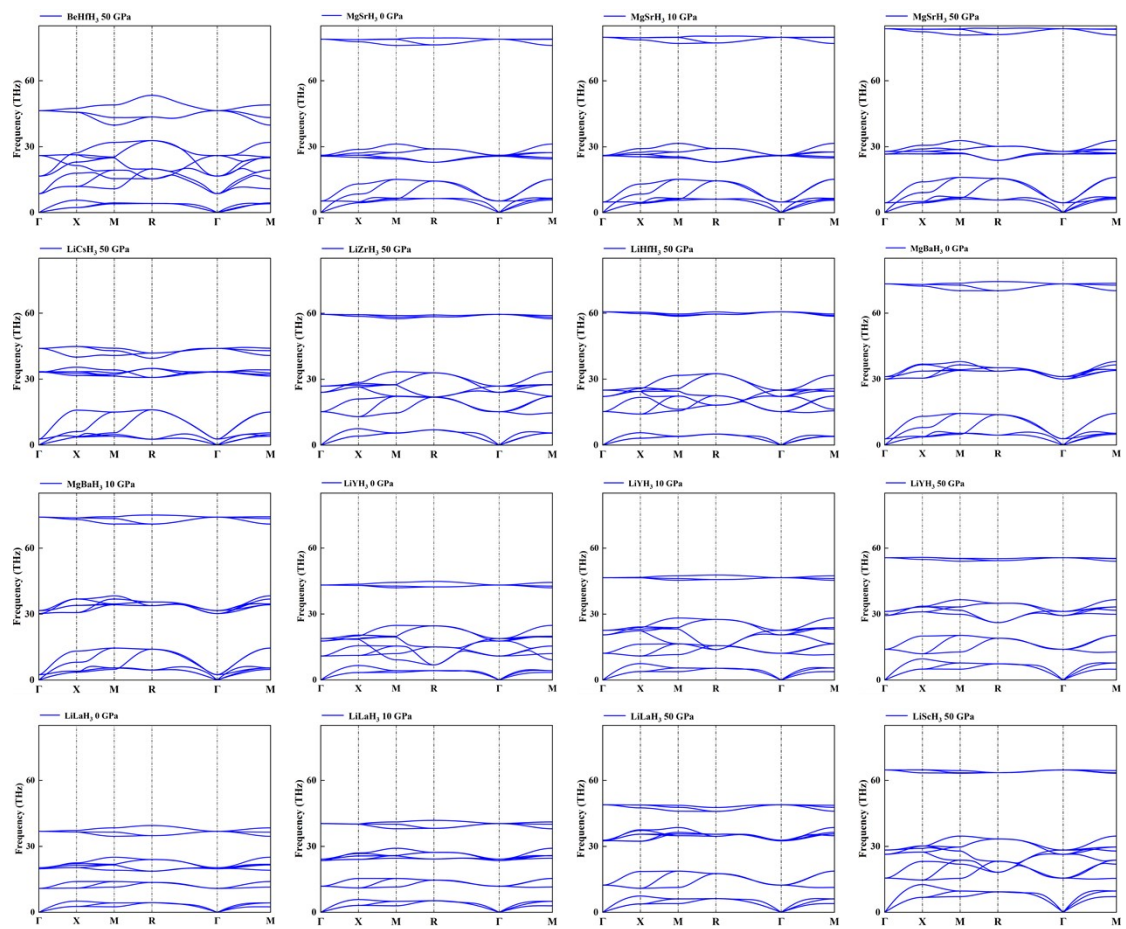


Figure S2. Calculated phonon spectrum of newly predicted ABH_3 under different pressure.

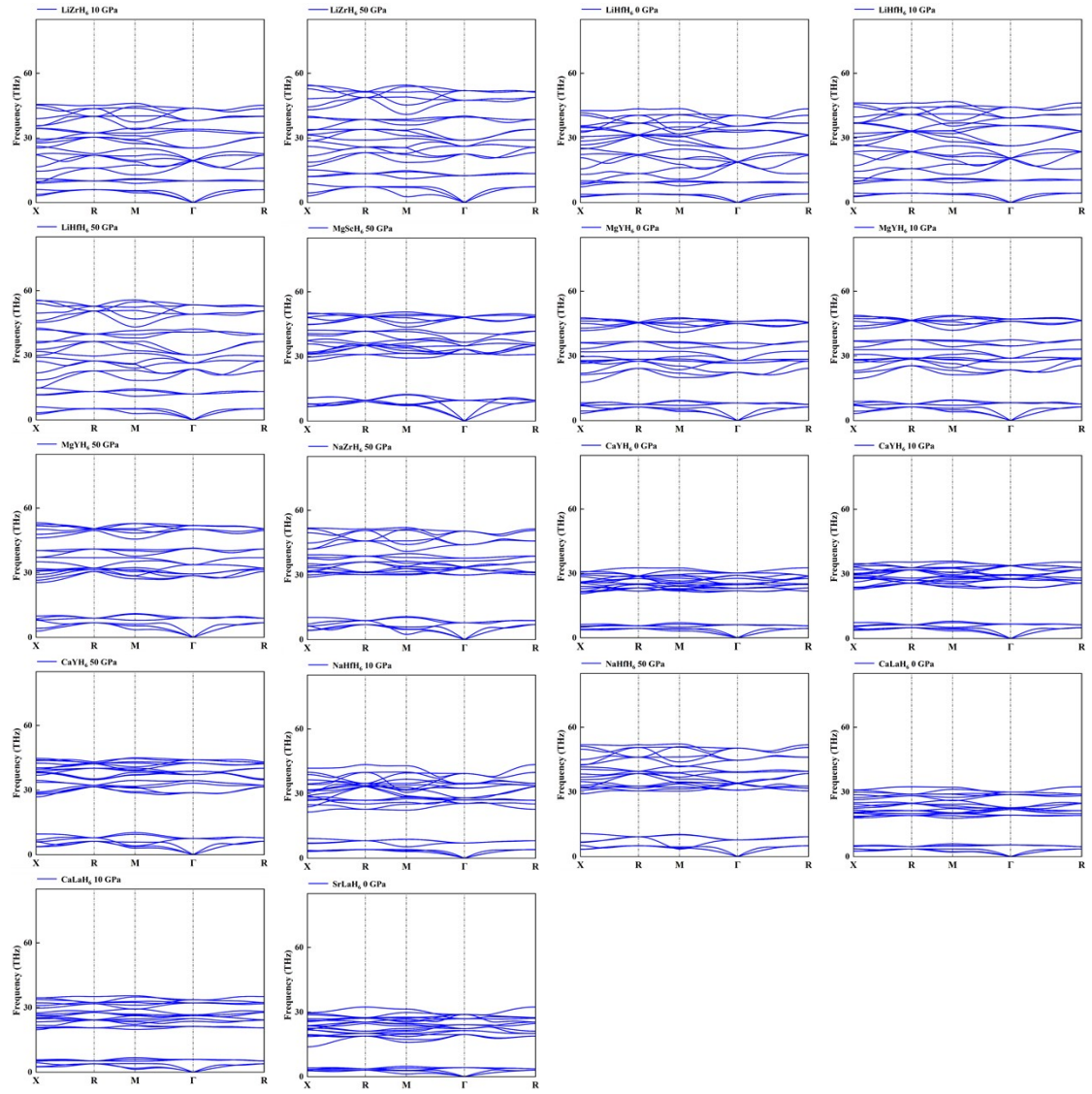


Figure S3. Calculated phonon spectrum of newly predicted ABH₆ under different pressure.

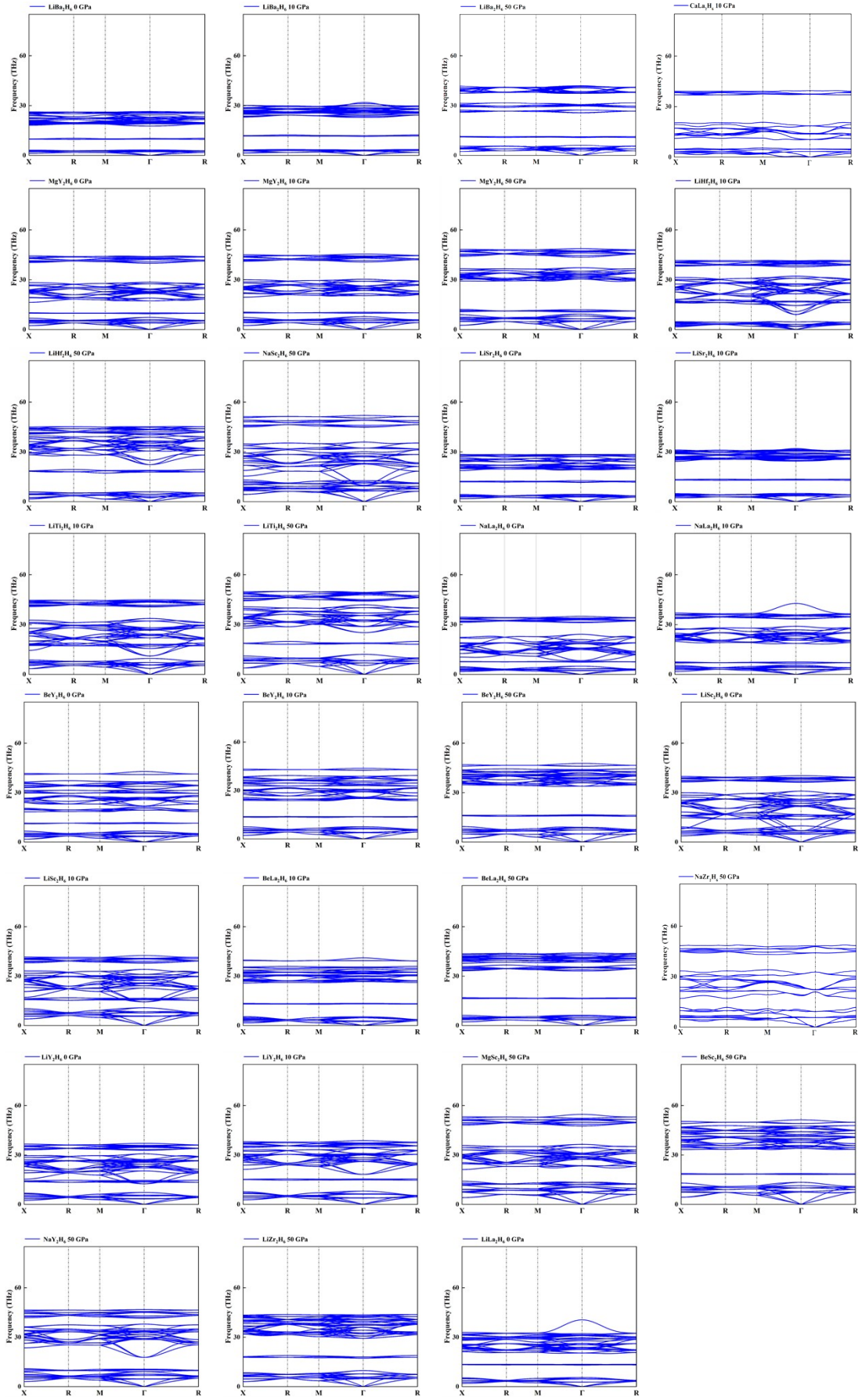


Figure S4. Calculated phonon spectrum of newly predicted AB₂H₆ under different pressure.

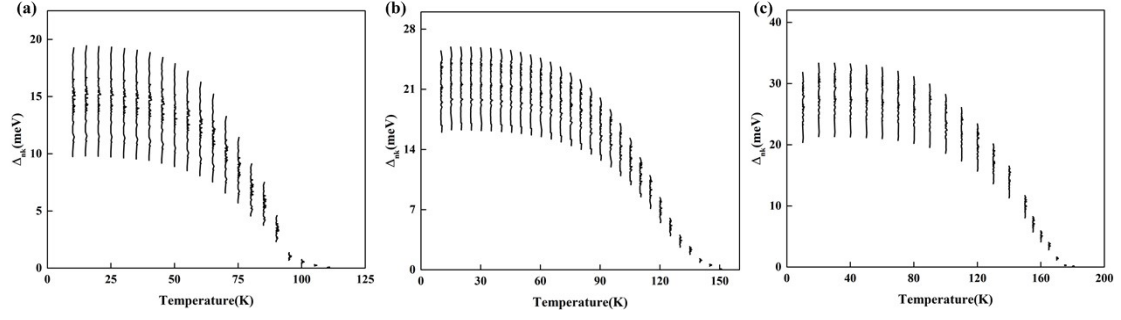


Figure S5. The superconducting energy gaps Δ_{nk} at different temperatures for LiTiH_6 , LiZrH_6 , and LiHfH_6 at 50 GPa. We have used the Wannier interpolation technique to calculate electron-phonon coupling superconductivity. The electronic and phononic states are interpolated onto fine k - and q -grids of $24 \times 24 \times 24$, and the double Dirac δ functions for electrons and phonons are smeared out by Gaussian functions with widths of 50 and 0.5 meV, respectively. The Matsubara frequency is truncated at $\omega_c = 3.0$ eV, which is about twelve times the highest phonon excitation energy. The screening Coulomb potential μ^* is set to be 0.1.

Table S1. Key superconducting parameters for dynamically stable ABH_3 , ABH_6 and AB_2H_6 at different pressures

Phase	Pressure (GPa)	λ	ω_{log}	T_c (K)
BeZrH_3	50	1.9	297	41
BeHfH_3	50	1.8	292	39
MgSrH_3	0	1.8	252	34
MgSrH_3	10	1.3	290	30
MgSrH_3	50	0.7	363	14
LiCsH_3	50	1.0	334	26
LiZrH_3	50	0.9	323	21
LiHfH_3	50	1.0	276	20
MgBaH_3	0	1.5	160	19
MgBaH_3	10	1.5	162	19
LiYH_3	0	0.6	335	8
LiYH_3	10	0.5	389	5
LiYH_3	50	0.3	452	0.2
LiLaH_3	0	0.4	255	3
LiLaH_3	10	0.4	279	1
LiLaH_3	50	0.4	281	2
LiScH_3	50	0.3	627	0.4
LiTiH_6	50	2.3	547	87
LiZrH_6	10	3.0	324	58
LiZrH_6	50	1.7	637	82
LiHfH_6	0	3.5	196	37
LiHfH_6	10	2.8	333	58

LiHfH ₆	50	1.6	629	80
MgScH ₆	50	1.7	410	55
MgYH ₆	0	2.8	173	31
MgYH ₆	10	2.0	271	40
MgYH ₆	50	1.4	446	49
NaZrH ₆	50	1.2	396	37
CaYH ₆	0	1.4	324	35
CaYH ₆	10	1.0	426	33
CaYH ₆	50	0.9	450	30
NaHfH ₆	10	3.1	73	14
NaHfH ₆	50	1.2	353	33
CaLaH ₆	0	1.1	281	25
CaLaH ₆	10	1.2	262	24
SrLaH ₆	0	1.4	135	15
MgZr ₂ H ₆	50	1.1	300	27
LiBa ₂ H ₆	0	0.6	186	5
LiBa ₂ H ₆	10	0.8	143	7
LiBa ₂ H ₆	50	1.2	276	26
CaLa ₂ H ₆	10	1.0	219	17
MgY ₂ H ₆	0	0.7	365	17
MgY ₂ H ₆	10	0.5	395	9
MgY ₂ H ₆	50	0.3	547	0.2
LiHf ₂ H ₆	10	0.8	298	14
LiHf ₂ H ₆	50	0.4	387	2
NaSc ₂ H ₆	50	0.5	664	13
LiSr ₂ H ₆	0	0.7	339	13
LiSr ₂ H ₆	10	0.7	300	11
LiTi ₂ H ₆	10	0.7	347	12
LiTi ₂ H ₆	50	0.3	535	1.1
NaLa ₂ H ₆	0	0.6	320	9
NaLa ₂ H ₆	10	0.3	502	0.5
BeY ₂ H ₆	0	0.6	285	7
BeY ₂ H ₆	10	0.4	356	4
BeY ₂ H ₆	50	0.4	419	2
LiSc ₂ H ₆	0	0.5	472	6
LiSc ₂ H ₆	10	0.3	620	1
BeLa ₂ H ₆	10	0.4	263	3
BeLa ₂ H ₆	50	0.5	302	5
NaZr ₂ H ₆	50	0.4	473	4
LiY ₂ H ₆	0	0.4	446	3
LiY ₂ H ₆	10	0.2	569	0.2
MgSc ₂ H ₆	50	0.3	676	0.6
BeSc ₂ H ₆	50	0.3	615	0.6

NaY ₂ H ₆	50	0.3	754	0.6
LiZr ₂ H ₆	50	0.3	458	0.5
LiLa ₂ H ₆	0	0.3	355	0.2

Table S2. Possible reaction routes and formation enthalpies for LiTiH₆, LiZrH₆ and LiHfH₆

Material	Reaction routes	Formation enthalpy (eV)
LiTiH ₆	LiH+TiH+2H ₂	-0.618
LiZrH ₆	LiH+ZrH+2H ₂	-0.990
LiHfH ₆	Li+HfH ₃ +3/2H ₂	-1.375

Table S3. Computed superconducting parameters for BeZrH₃ and MgHCu₃.

Material	Pressure (GPa)	λ	ω_{log} (K)	T_c (K)
BeZrH ₃	50	1.91	297.31	41.5
MgHCu ₃	0	0.83	402.19	42.0