Supplemental Informations for A computational and Raman spectroscopic study of successive phase transitions in Co₃TeO₆ under high pressure and high temperature

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TABLE S1: Crystal structure parameters of the Rietveld refinements of the PXD data of the AP Co₃TeO₆. Monoclinic, space group C2/c (No. 12), a = 14.8009(1) Å, b = 8.8380(7) Å, c = 10.3429(1) Å, $\beta = 94.835(5)^{\circ}$, V = 1348.14(2) Å³, $Z = 12, R_p/R_{wp} = 0.81/1.07\%$.

Atom	Position	x	у	z	Occ.	$B_{eq}(Å^2)$	
Col	4e	0.5	-0.1891(2)	0.25	1	0.67(2)	
Co2	8f	0.8591(8)	-0.3559(9)	0.2338(9)	1	0.76(3)	
Co3	8f	0.5231(6)	-0.6518(9)	0.0393(7)	1	0.74(3)	
Co4	8f	0.6638(6)	-0.2894(8)	0.0574(7)	1	0.58(5)	
Co5	8f	0.7999(6)	-0.3641(9)	0.5730(8)	1	0.52(3)	
Te1	4b	0	0.5	0.5	1	0.77(8)	
Te2	8f	0.6590(2)	-0.4995(6)	0.2994(3)	1	1.01(6)	
O1	8f	0.9318(5)	-0.3419(4)	0.5742(7)	1	0.81(7)	
O2	8f	0.5978(1)	-0.3378(7)	0.2018(1)	1	0.95(2)	
O3	8f	0.5991(1)	-0.6623(1)	0.1967(3)	1	0.87(3)	
O4	8f	0.7482(5)	-0.5225(3)	0.6698(3)	1	0.75(3)	
05	8f	0.9347(2)	-0.5119(3)	0.3345(7)	1	0.94(5)	
O6	8f	0.5889(7)	-0.5171(5)	0.4380(5)	1	0.89(3)	
07	8f	0.9289(3)	-0.6567(2)	0.5605(3)	1	0.96(8)	
08	8f	0.7341(3)	-0.3379(3)	0.3872(1)	1	0.86(6)	
09	8 <i>f</i>	0.7282(5)	-0.6521(5)	0.3905(2)	1	0.81(2)	

TABLE S2: Crystallographic parameters of the synthesized Co₃TeO₆ samples obtained at 5 GPa 1073 K, refined from the SPXD data. Trigonal, space group *R*3 (No. 146), a = 5.1910(8) Å, c = 13.8187(2) Å, V = 322.46(1) Å³, $Z = 3, R_p/R_{wp} = 5.96/7.36\%$.

Atom	Position	x	у	Z	Occ.	$B_{eq}(Å^2)$	
Col	3a	0	0	0.1988(2)	1	0.73(4)	
Co1 Co2	3a	0	0	0.1988(2) 0.4791(3)	1	0.73(4) 0.70(4)	
Co3	3 <i>a</i>	0	0	0.6837(2)	1	0.65(3)	
Te1	3 <i>a</i>	0	0	-0.0121(1)	1	1.06(6)	
O1	9 <i>b</i>	0.1438(7)	0.1903(1)	-0.0418(3)	1	0.54(8)	
O2	9 <i>b</i>	0.6264(2)	-0.0107(1)	0.2779(6)	1	0.67(1)	

TABLE S3: Crystallographic parameters of the synthesized Co₃TeO₆ samples obtained at 20 GPa 1473 K, refined from the SPXD data. Monoclinic, space group $P2_1/n$ (No. 14), a = 5.0232(4) Å, b = 5.1861(7) Å, c = 7.1854(8) Å, $\beta = 94.09(1)^{\circ}$, V = 186.71(1) Å³, Z = 2, $R_p/R_{wp} = 2.77/3.58\%$.

Atom	Position	x	у	Z	Occ.	$B_{eq}(Å^2)$	
Col	4e	0.6809(2)	0.1185(6)	0.2374(3)	1	0.51(3)	
Co2	2d	0.5	0	0	1	0.64(5)	
Te1	2c	0	0.5	0	1	0.46(2)	
01	4e	0.1517(5)	1.1783(3)	0.2105(1)	1	0.52(1)	
O2	4e	0.5117(6)	0.5257(8)	0.1511(3)	1	0.41(2)	
O3	4 <i>e</i>	0.7827(2)	0.0145(7)	0.0671(6)	1	0.62(5)	



FIG. S1: Refinement of the (a) PXD data of Co_3TeO_6 in C2/c and (b) SPXD data of Co_3TeO_6 in R3 (obtained at 5 GPa 1073 K), respectively. The experimental, calculated, difference curves, and Bragg-reflection positions are shown in red, black, blue and green, respectively.



FIG. S2: The optimized unit cells of Co_3TeO_6 in (a) $P2_1/n$ and (b) R3 (with cell volumes V = 202 and 101 Å³, respectively), with the minimum distance between Co_A and Co_B indicated.

TABLE S4: The typical structural parameters and atomic Wyckoff positions of $Mn_3 TeO_6$ at AP $(R\overline{3})^1$ and HP $(P2_1/n)^2$, $Co_3 TeO_6$ at AP $(C2/c)^3$, HP $(R3)^{4,5}$ and of the optimized $P2_1/n$ structure⁶. Note that the *B* (Mn_B or Co_B) and *B'* (Te) sites are interchanged between Mn_3 TeO_6 and Co_3 TeO_6 in $P2_1/n$ structure, whose Wyckoff positions are named by choosing *b* as unique axis with cell choice 2^7 .

system	space group	a(Å)	$b(\AA)$	c(Å)	$oldsymbol{eta}(^\circ)$	atom	x	у	Z
Mn ₃ TeO ₆	<i>P</i> 2 ₁ / <i>n</i>	5.295	5.453	7.809	90.370	$ \begin{array}{c} {\rm Mn}_A \ (4e) \\ {\rm Mn}_B \ (2c) \\ {\rm Te} \ (2d) \\ {\rm O1} \ (4e) \\ {\rm O2} \ (4e) \\ {\rm O3} \ (4e) \end{array} $	$\begin{array}{c} 0.0107 \\ 0 \\ 0.5 \\ 0.3383 \\ 0.1946 \\ -0.1308 \end{array}$	$\begin{array}{c} 0.0475 \\ 0.5 \\ 0 \\ 0.3018 \\ 0.8243 \\ 0.4303 \end{array}$	$\begin{array}{c} 0.2407 \\ 0 \\ 0 \\ 0.0831 \\ 0.0463 \\ 0.2707 \end{array}$
	R3	8.867	-	10.673	-	Mn (18 <i>f</i>) Te1 (3 <i>b</i>) Te2 (3 <i>a</i>) O1 (18 <i>f</i>) O2 (18 <i>f</i>)	0.0384 0 0 0.0307 0.1828	0.2643 0 0 0.1963 0.1562	0.2130 0.5 0 0.4028 0.1105
Co ₃ TeO ₆	C2/c	14.817	8.851	10.363	94.900	Co1 $(4e)$ Co2 $(8f)$ Co3 $(8f)$ Co4 $(8f)$ Co5 $(8f)$ Te1 $(4b)$ Te2 $(8f)$ O1 $(8f)$ O2 $(8f)$ O3 $(8f)$ O4 $(8f)$ O5 $(8f)$ O6 $(8f)$ O7 $(8f)$ O8 $(8f)$ O9 $(8f)$	$\begin{array}{c} 0.5\\ 0.8583\\ 0.5231\\ 0.6647\\ 0.7968\\ 1.0\\ 0.6614\\ 0.9274\\ 0.5935\\ 0.6030\\ 0.7484\\ 0.9293\\ 0.5818\\ 0.9269\\ 0.7377\\ 0.7272\end{array}$	$\begin{array}{r} -0.1878 \\ -0.3540 \\ -0.6546 \\ -0.2935 \\ -0.3634 \\ -0.5 \\ -0.4985 \\ -0.3351 \\ -0.3450 \\ -0.6554 \\ -0.5267 \\ -0.5144 \\ -0.5117 \\ -0.6591 \\ -0.3503 \\ -0.6611 \end{array}$	$\begin{array}{c} 0.25\\ 0.2336\\ 0.0400\\ 0.0550\\ 0.5724\\ 0.5\\ 0.3004\\ 0.5611\\ 0.2024\\ 0.1980\\ 0.6687\\ 0.3377\\ 0.4377\\ 0.5662\\ 0.3932\\ 0.3887\\ \end{array}$
	R3	5.190	-	13.820	-	Co1 (3 <i>a</i>) Co2 (3 <i>a</i>) Co3 (3 <i>a</i>) Te (3 <i>a</i>) O1 (9 <i>b</i>) O2 (9 <i>b</i>)	0 0 0 0.2870 0.6690	$0 \\ 0 \\ 0 \\ -0.0050 \\ -0.0220$	0.3688 0.6490 0.8609 0.1606 0.2470 0.7570
	$P2_{1}/n$	5.240	5.167	7.461	90.346	$\begin{array}{c} \text{Co}_{A} \ (4e) \\ \text{Co}_{B} \ (2d) \\ \text{Te} \ (2c) \\ \text{O1} \ (4e) \\ \text{O2} \ (4e) \\ \text{O3} \ (4e) \end{array}$	0.4879 0.5 0 0.1205 0.6757 0.8407	0.4668 0 0.5 0.5895 0.6653 0.1853	$\begin{array}{c} 0.2288 \\ 0 \\ 0.2398 \\ 0.0430 \\ 0.0849 \end{array}$



FIG. S3: The simulated X-ray powder diffraction patterns of $Co_3 TeO_6$ in R3 and $P2_1/n$, respectively, by VESTA⁸.



FIG. S4: The variation of total energies of $Co_3 TeO_6$ in *R*3 phase with lattice constant a_R in different magnetic structures. The volume of the unit cell is fixed at (a) V = 210 and (b) V = 214.92 Å³, respectively.



FIG. S5: The pressure dependence of the phonon frequencies of Raman spectrum of $Co_3 TeO_6$ in C2/c and R3 phases, obtained from Fig.6 in main text. The frequencies of five highest peaks of C2/c are shown.

TABLE S5: The maximum change of lattice parameters of $A_2BB'O_6$ with small A-site cations extracted from experimental reports. ΔT is the measured temperature range.

system	space group	P (GPa)	$T_N(K)$	$\Delta a(\AA)$	$\Delta b(\AA)$	$\Delta c(Å)$	$\Delta oldsymbol{eta}(^{\circ})$	$\Delta T(K)$	$\Delta V(Å^3)$	$\Delta \overline{d}_{B-O}(\mathring{A})$	$\Delta \overline{d}_{B'-O}(\mathring{A})$
0											
$Mn_3ReO_6^9$	$P2_1/n$	5	110, 50	0.008	0.015	0.010	0.04	[5, 300]	1.22	-	-
Mn ₂ FeReO ₆ ¹⁰	$P2_1/n$	5	520,75 (FM)	0.012	0.012	0.017	0.15	[4, 300]	1.22	0.03	0.03
Mn ₂ CoReO ₆ ¹¹	$P2_1/n$	8	94	0.008	0.006	0.002	0.09	[2, 130]	0.60	-	-
$Mn_3WO_6^{12}$	<i>R</i> 3	8	58	0.004	-	0.02	-	[5, 100]	0.70	0.1	0.02
Mn ₂ InSbO ₆ ¹³	<i>R</i> 3	5	38, 17, 8	0.001	-	0.001	-	[4, 30]	-	0.08	0.09^{*}
Mn ₂ FeMoO ₆ ¹⁴	$P2_1/n$	8	194,45	0.011	0.010	0.011	0.01	[10, 300]	1.14	0.09	0.14
Mn ₃ TeO ₆ ¹	$R\overline{3}$	AP	23	0.016	-	0.023	-	[5, 295]	-	0.01	0.00
Co ₃ TeO ₆ ¹⁵	C2/c	AP	26,17.4	0.028	0.006	0.015	0.18	[1.6, 295]	-	0.10	0.04
Ni ₃ TeO ₆ ¹⁶	<i>R</i> 3	AP	54	0.008	-	0.02	-	[15, 300]	-	0.04	-
Co ₃ TeO ₆ ¹⁷	<i>R</i> 3	5	58,24	0.01	-	0.006	-	[5, 90]	0.20	0.01	0.01
Ni ₂ InSbO ₆ ¹⁸	<i>R</i> 3	AP	76	0.006	-	0.007	-	[1.7, 295]	-	0.01	0.02
Ni ₂ ScSbO ₆ ¹⁸	<i>R</i> 3	AP	60	0.005	-	0.007	-	[1.7, 295]	-	0.03	0.03

* Measured between 2 and 100 K.

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