

Electronic Supplementary Information for
Anion Ratio-Directed Design of $\text{CaB}_4\text{O}_5\text{F}_4$ and $\text{CaB}_6\text{O}_8\text{F}_4$:
 $[\text{BO}_3]$ / $[\text{BO}_2\text{F}_2]$ Hybridization Tailoring Deep-Ultraviolet
Nonlinear Optical Performance

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Table S1. All predicted $\text{CaB}_4\text{O}_5\text{F}_4$ structures with E_{hull} values <0.1 eV/atom.

No.	Formula	Symmetry	Space groups	Anion groups	Anionic framework dimensions	E_{hull} (eV/atom)
1	$\text{Ca}_4\text{B}_{16}\text{O}_{20}\text{F}_{16}$	CS	$C2/c$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.011
2	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.013
3	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	$Pnn2$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	3D	0.030
4	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	1D	0.040
5	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.060
6	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	1D	0.063
7	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	Pc	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.066
8	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	$P2_1$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.067
9	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$[\text{BO}_3] + [\text{BO}_4] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.071
10	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	Pc	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.073
11	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	$P2_1$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.073
12	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	$P2_1$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.076
13	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	1D	0.078
14	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	Pc	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.078
15	$\text{Ca}_4\text{B}_{16}\text{O}_{20}\text{F}_{16}$	NCS	Cc	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	3D	0.078
16	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	1D	0.079
17	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	$P2_1$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.079
18	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.082
19	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.083
20	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.083
21	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	1D	0.086
22	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	$P2_1$	$2^*[\text{BO}_3] + [\text{BO}_3\text{F}]$	2D	0.086
23	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	Pc	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	1D	0.090
24	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	$P2_1$	$2^*[\text{BO}_3] + [\text{BO}_3\text{F}] + [\text{BOF}_3]$	2D	0.091
25	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	CS	$P\bar{1}$	$2^*[\text{BO}_3] + 2^*[\text{BO}_2\text{F}_2]$	2D	0.093
26	$\text{Ca}_2\text{B}_8\text{O}_{10}\text{F}_8$	NCS	Pc	$2^*[\text{BO}_3] + [\text{BO}_3\text{F}] + [\text{BOF}_3]$	2D	0.094

27	Ca ₂ B ₈ O ₁₀ F ₈	NCS	<i>P</i> 2 ₁	6*[BO ₃] + 2*[BO ₃ F]	2D	0.096
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Table S2. All predicted CaB₆O₈F₄ structures with E_{hull} values <0.1 eV/atom.

No.	Formula	Symmetry	Space group s	Anion groups	Anionic framework dimensions	E_{hull} (eV/atom)
1	Ca ₂ B ₁₂ O ₁₆ F ₈	NCS	<i>C</i> 2	2*[BO ₃] + [BO ₂ F ₂]	1D	0.026
2	Ca ₂ B ₁₂ O ₁₆ F ₈	NCS	<i>P</i> c	2*[BO ₃] + [BO ₂ F ₂]	2D	0.046
3	Ca ₂ B ₁₂ O ₁₆ F ₈	CS	<i>P</i> 2 ₁ / <i>c</i>	2*[BO ₃] + [BO ₂ F ₂]	1D	0.050
4	Ca ₂ B ₁₂ O ₁₆ F ₈	NCS	<i>P</i> 2	2*[BO ₃] + [BO ₂ F ₂]	2D	0.066
5	Ca ₂ B ₁₂ O ₁₆ F ₈	NCS	<i>P</i> c	2*[BO ₃] + [BO ₂ F ₂]	2D	0.072
6	Ca ₂ B ₁₂ O ₁₆ F ₈	NCS	<i>P</i> c	2*[BO ₃] + 2*[BO ₄] + 2*[BO ₂ F ₂]	2D	0.073

Table S3. The crystallographic data of CaB₄O₅F₄(I-IV) and CaB₆O₈F₄, including cell parameters, fractional coordinates, bond lengths.

CaB ₄ O ₅ F ₄ -I (C2/c)					
Cell parameter					
<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	<i>α</i> (°)	<i>β</i> (°)	<i>γ</i> (°)
9.9295	8.4662	8.5104	90	114.7699	90
Fractional coordinate					
Atoms	<i>x/a</i>		<i>y/b</i>		<i>z/c</i>
Ca1	0		0.3624		1.25
B1	0.79343		0.68209		1.28010
B2	0.36976		0.45374		1.24252
O1	0.26659		0.34869		1.24844
O2	0.65587		0.61343		1.26854
O3	0		0.89452		1.25
F1	0.90857		0.65585		1.45559
F2	0.84567		0.60523		1.16819
Bond lengths (Å)					
Ca1- O1	2.655		B1-O1		1.45
Ca1- O2	2.581		B1-O2		1.44
Ca1- O2	2.581		B1-F1		1.468
Ca1- O1	2.656		B1-F2		1.418
Ca1- F1	2.285		B2-O1		1.371
Ca1- F1	2.285		B2-O2		1.364
Ca1- F2	2.483		B2-O3		1.373
Ca1- F2	2.483				

CaB ₄ O ₅ F ₄ -II (<i>P</i> $\bar{1}$)					
Cell parameter					
<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	α (°)	β (°)	γ (°)
6.5119	6.5208	8.4513	70.1333	71.3184	80.9561
Fractional coordinate					
Atoms	<i>x/a</i>		<i>y/b</i>		<i>z/c</i>
Ca1	0.36679		0.13891		0.75238
B1	0.47844		0.61221		0.72200
B2	0.82691		0.41750		0.75889
B3	0.08650		0.67825		0.74484
B4	0.89336		0.02844		0.77567
O1	0.61765		0.41737		0.75511
O2	0.27121		0.54340		0.73518
O3	0.89619		0.60718		0.75312
O4	0.08551		0.88664		0.74977
O5	0.96305		0.23360		0.76631
F1	0.56849		0.75508		0.54293
F2	0.45603		0.74105		0.83287
F3	0.25628		0.06238		0.04872
F4	0.76956		0.05792		0.65796
Bond lengths (Å)					
Ca1- O1	2.637		B1-F1		1.465
Ca1- O2	2.578		B1-F2		1.465
Ca1- O4	2.657		B2-O1		1.373
Ca1- O5	2.578		B2-O3		1.362
Ca1- F1	2.265		B2-O5		1.371
Ca1- F2	2.472		B3-O2		1.371
Ca1- F3	2.269		B3-O3		1.364
Ca1- F4	2.511		B3-O4		1.373
B1-O1	1.447		B4-O4		1.438
B1-O2	1.440		B4-O5		1.448
B4-F3	1.47		B4-F4		1.418
CaB ₄ O ₅ F ₄ -III (<i>Pnn</i> 2)					
Cell parameter					
<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	α (°)	β (°)	γ (°)
5.0255	9.1129	6.8102	90	90	90
Fractional coordinate					
Atoms	<i>x/a</i>		<i>y/b</i>		<i>z/c</i>

Ca1	0	0.5	0.72345		
B1	0.34923	0.37974	0.30839		
B2	0.54707	0.29291	0.98205		
O1	0.60268	0.71874	0.16159		
O2	0.64842	0.14748	0.94078		
O3	0.5	0.5	0.34674		
F1	0.61917	0.65352	0.82652		
F2	0.76721	0.39492	0.99399		
Bond lengths (Å)					
Ca1- O1	2.648	B2-O1	1.376		
Ca1- O1	2.648	B2-O3	1.358		
Ca1- O2	2.463	B1-O3	1.365		
Ca1- O2	2.463	B2-O1	1.439		
Ca1- F1	2.473	B3-O3	1.439		
Ca1- F1	2.472	B3-F1	1.435		
Ca1- F2	2.384	B3-F3	1.447		
Ca1- F2	2.384				
CaB ₄ O ₅ F ₄ -IV (<i>P</i> $\bar{1}$)					
Cell parameter					
<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	<i>α</i> (°)	<i>β</i> (°)	<i>γ</i> (°)
4.4196	9.3701	9.7535	63.3899	89.5219	89.7503
Fractional coordinate					
Atoms	<i>x/a</i>	<i>y/b</i>	<i>z/c</i>		
Ca1	0.26666	0.99768	0.75163		
B1	0.70266	0.21794	0.83727		
B2	0.80264	0.64085	0.23821		
B3	0.70042	0.78056	0.66220		
B4	0.80547	0.36194	0.26549		
O1	0.89331	0.65516	0.75017		
O2	0.61427	0.23496	0.29224		
O3	0.39047	0.23195	0.79014		
O4	0.10252	0.65868	0.25426		
O5	0.67950	0.50118	0.25222		
F1	0.71550	0.18814	0.99746		
F2	0.20246	0.93698	0.15743		
F3	0.79103	0.93202	0.66553		
F4	0.27769	0.18116	0.49998		
Bond lengths (Å)					

Ca1- O2	2.456	B1-F2	1.487
Ca1- O3	2.452	B2-O3	1.388
Ca1- F1	2.283	B2-O4	1.356
Ca1- F2	2.430	B2-O5	1.368
Ca1- F2	2.683	B3-O1	1.394
Ca1- F3	2.451	B3-O2	1.444
Ca1- F3	2.621	B3-F3	1.491
Ca1- F4	2.281	B3-F4	1.460
B1-O3	1.445	B4-O1	1.356
B1-O4	1.395	B4-O2	1.387
B1-F1	1.460	B4-O5	1.368

CaB ₆ O ₈ F ₄ -I (C2)					
Cell parameter					
<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	<i>α</i> (°)	<i>β</i> (°)	<i>γ</i> (°)
10.4878	8.3208	6.9613	90	130.8993	90

Fractional coordinate				
Atoms	<i>x/a</i>	<i>y/b</i>	<i>z/c</i>	
Ca1	0	0.5725	0	
B1	0.78737	0.04049	0.69584	
B2	0.20540	0.80136	0.50955	
B3	0.28837	0.75914	0.92584	
O1	0.24460	0.86599	0.72131	
O2	0.83463	0.10076	0.91275	
O3	0.67526	0.38574	0.31610	
O4	0.69630	0.13506	0.47487	
F1	0.15093	0.74400	0.92405	
F2	0.42497	0.84114	0.15393	

Bond lengths (Å)			
Ca1- O1	2.662	B2-O1	1.355
Ca1- O1	2.662	B2-O3	1.360
Ca1- O4	2.555	B2-O4	1.397
Ca1- O4	2.554	B3-O1	1.474
Ca1- F1	2.432	B3-O2	1.428
Ca1- F1	2.433	B3-F1	1.439
Ca1- F2	2.565	B3-F2	1.435
Ca1- F2	2.564	B1-O2	1.364
B1-O3	1.405	B1-O4	1.34

CaB ₆ O ₈ F ₄ -II (<i>Pc</i>)					
Cell parameter					
<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	<i>α</i> (°)	<i>β</i> (°)	<i>γ</i> (°)
5.1298	10.7150	11.6699	90	119.2582	90
Fractional coordinate					
Atoms	<i>x/a</i>		<i>y/b</i>		<i>z/c</i>
Ca1	-0.39690		-0.12773		0.24054
B1	1.30112		-0.01632		0.94811
B2	1.10524		-0.68340		0.81508
B3	1.35672		-0.30888		0.72630
B4	0.26925		-0.18920		0.52555
B5	1.25044		-0.45305		0.85404
B6	1.34648		-0.23902		0.91768
O1	0.37438		-0.28257		0.61652
O2	-0.61954		-0.14162		0.00164
O3	1.15967		-0.56458		0.87204
O4	1.27700		-0.35619		0.93925
O5	1.07785		-0.78067		0.89654
O6	-0.65769		-0.93488		0.05484
O7	1.31088		-0.42887		0.75246
O8	1.37696		-0.21318		0.80922
F1	0.34000		-0.27657		0.28490
F2	-0.00333		-0.98069		0.33982
F3	-0.17096		-0.30450		0.19371
F4	0.48354		-0.02825		0.39292
Bond lengths (Å)					
Ca1-O2	2.447		B3-O1	1.357	
Ca1-O5	2.424		B3-O7	1.368	
Ca1-O6	2.815		B3-O8	1.379	
Ca1-F1	2.306		B4-O1	1.364	
Ca1-F2	2.369		B4-O5	1.375	
Ca1-F3	2.418		B4-O6	1.378	
Ca1-F4	2.396		B5-O3	1.336	
B1-O2	1.453		B5-O4	1.397	
B1-O6	1.449		B5-O7	1.388	
B1-F2	1.452		B6-O2	1.383	
B1-F4	1.452		B6-O4	1.362	
B2-O3	1.400		B6-O8	1.377	
B2-O5	1.463		B2-F3	1.438	

B2-F1	1.474
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Table S4. Calculated band gap, birefringence, the shortest SHG phase-matching wavelengths (λ_{PM}) and the effective SHG coefficients for the predicted $\text{CaB}_4\text{O}_5\text{F}_4$ (V-XI) bulk structures.

Formula	Space groups	HSE06 (eV)	GGA (eV)	Birefringence (@1064 nm)	Shortest λ_{PM} (nm)	SHG effect (pm/V)	E_{hull} (eV/atom)
$\text{CaB}_4\text{O}_5\text{F}_4$ -V	$P2_1$	7.57	6.03	0.092	167	$d_{16}=0.098$, $d_{22}=-0.185$ (0.47×KDP), $d_{23}=-0.091$ $d_{16}=0.0735$,	0.067
$\text{CaB}_4\text{O}_5\text{F}_4$ -VI	$P2_1$	8.02	6.31	0.097	157	$d_{14}=0.134$ (0.34×KDP), $d_{23}=-0.134$ $d_{16}=0.233$	0.073
$\text{CaB}_4\text{O}_5\text{F}_4$ -VII	$P2_1$	7.34	6.00	0.074	184	(0.6×KDP), $d_{22}=0.056$, $d_{23}=0.208$ $d_{11}=-0.360$, $d_{15}=0.237$, $d_{12}=0.418$,	0.076
$\text{CaB}_4\text{O}_5\text{F}_4$ -VIII	Pc	7.50	6.00	0.071	185	$d_{13}=-0.134$, $d_{24}=-0.086$, $d_{33}=-0.591$ (1.5×KDP) $d_{11}=-$ 0.342 (0.88×KDP)) ,	0.078
$\text{CaB}_4\text{O}_5\text{F}_4$ -IX	Cc	8.20	6.52	0.048	226	$d_{15}=0.303$, $d_{12}=-0.22$, $d_{13}=0.213$, $d_{24}=-0.107$ $d_{16}=-$ 0.482(1.23×KDP),	0.078
$\text{CaB}_4\text{O}_5\text{F}_4$ -X	$P2_1$	7.65	6.17	0.045	226	$d_{14}=0.247$, $d_{22}=-0.261$, $d_{23}=0.268$ $d_{11}=-$ 0.455 (1.17×KDP) ,	0.079
$\text{CaB}_4\text{O}_5\text{F}_4$ -XI	Pc	7.65	5.95	0.026	264	$d_{15}=0.120$, $d_{12}=-0.204$,	0.090

$$d_{13}=0.093,$$

$$d_{24}=0.054,$$

$$d_{33}= -0.116$$

Table S5. Calculated band gap, birefringence, the shortest SHG phase-matching wavelengths (λ_{PM}) and the effective SHG coefficients for the predicted $\text{CaB}_6\text{O}_8\text{F}_4$ (II-VI) bulk structures.

Crystals	Space groups	HSE06 (eV)	GGA (eV)	Birefringence (@1064 nm)	Shortest λ_{PM} (nm)	SHG effect (pm/V)	E_{hull} (eV/atom)
$\text{CaB}_6\text{O}_8\text{F}_4$ -III	$P2_1/c$	7.16	5.80	0.074	/	/	0.050
$\text{CaB}_6\text{O}_8\text{F}_4$ -IV	$P2$	7.04	5.76	0.018	345	$d_{16}= -0.408,$ $d_{14}=0.704$ (1.8×KDP), $d_{22}=0.340,$ $d_{23}=0.508$ $d_{11}=0.295,$ $d_{15}=0.412$	0.066
$\text{CaB}_6\text{O}_8\text{F}_4$ -V	Pc	6.76	5.52	0.059	215	(1×KDP), $d_{12}=-0.193,$ $d_{24}=-0.395$ $d_{11}=-0.48$ (1.23×KDP)	0.072
$\text{CaB}_6\text{O}_8\text{F}_4$ -VI	Pc	5.65	6.94	0.053	215	$d_{12}=-0.333$ $d_{13}=-0.242,$ $d_{24}=0.06$ $d_{33}=0.166$	0.073

Table S6. SHG response and the shortest phase-matching wavelength of the synthesized deep-UV materials.

Crystal	Space group	Absorption edge (nm)	SHG effect ($\times$ KDP)	Birefringence (@1064 nm)	Shortest phase-matching wavelength (nm)	Refs.
KBe ₂ BO ₃ F ₂	<i>R</i> 32	147	1.26	0.077	161	1
RbBe ₂ BO ₃ F ₂	<i>R</i> 32	152	1.15	0.073	170	2
NH ₄ Be ₂ BO ₃ F ₂	<i>R</i> 32	153	1.2	0.057@400 nm	173.9	3
NaBe ₂ BO ₃ F ₂	<i>C</i> 2	155	1.4	0.091@200 nm	185	4
BaBe ₂ BO ₃ F ₃	<i>P</i> 6 ₃	<185	0.1	0.081@200 nm	196	5
Be ₂ BO ₃ F	<i>C</i> 2	150	0.1	0.0915	180	6
Be ₂ BO ₃ F	<i>R</i> 32	144.8	2.3	0.0989	146	3
NH ₄ B ₄ O ₆ F	<i>Pna</i> 2 ₁	156	3	0.1171	158	7
NaB ₄ O ₆ F	<i>C</i> 2	<180	0.9	0.12	166	8
RbB ₄ O ₆ F	<i>Pna</i> 2 ₁	<190	0.8	0.102	165	9
CsB ₄ O ₆ F	<i>Pna</i> 2 ₁	155	1.9	0.114	171.6	10
CsKB ₈ O ₁₂ F ₂	<i>P</i> 321	<190	1.9	0.105	170	11
CaB ₅ O ₇ F ₃	<i>Cmc</i> 2 ₁	<180	2	0.07	183	12
SrB ₅ O ₇ F ₃	<i>Cmc</i> 2 ₁	<180	1.6	0.072@589 nm	180	13
MgB ₅ O ₇ F ₃	<i>Cmc</i> 2 ₁	<200	2.4	0.07	189	14
Li ₂ B ₆ O ₉ F ₂	<i>Cc</i>	<190	0.9	0.07	192	15
CsAlB ₃ O ₆ F	<i>Pna</i> 2 ₁	<190	2	0.091	182	16
RbAlB ₃ O ₆ F	<i>Pna</i> 2 ₁	<200	0.2	0.095	174	17
C(NH ₂) ₃ BF ₄	<i>R</i> 3 <i>m</i>	193	3.6	0.11	193.2	18
Cs ₂ Al ₂ (B ₃ O ₆) ₂ O	<i>P</i> 6 ₃	185	0.5	0.136@177.3 nm	185	19
Sr ₂ Be ₂ B ₂ O ₇	<i>P</i> 2 <i>c</i>	155	3.8	0.062@589 nm	200	20
SrB ₈ O ₁₅ H ₄	<i>P</i> 2 ₁	<200	1.8	0.109	185	21
CaB ₈ O ₁₅ H ₄	<i>P</i> 2 ₁	<200	2	0.093	174	21
[C(NH ₂) ₃] ₂ [B ₃ O ₃ F ₄ (OH)]	<i>P</i> ₁	190	0.9	0.173	190	22
[C(NH ₂) ₃] ₂ [B ₃ O ₃ F ₄ (OH)]	<i>P</i> ₁	195	1.4	0.161	195	23
Cs ₂ KY(B ₃ O ₆) ₂	<i>Pc</i> 2	< 190	4.8	0.078@1064	<200	24

Table S7. $\Delta\rho^b$, group contribution and corresponding birefringence of CaB₄O₅F₄-I, II and CaB₆O₈F₄-I, II.

Structure	Group	$\Delta\rho^b$	Group contribution	Birefringence
CaB ₄ O ₅ F ₄ -I	[BO ₃]	0.0187	87.04%	0.084
	[BO ₂ F ₂]	0.0035	16.46%	
	[CaO ₄ F ₄]	-0.0008	-3.5%	
CaB ₄ O ₅ F ₄ -II	[BO ₃]	0.0191	87%	0.086
	[BO ₂ F ₂]	0.0006	2.61%	
	[CaO ₄ F ₄]	0.0023	10.38%	
CaB ₄ O ₅ F ₄ -III	[BO ₃]	0.0017	44.88%	0.035
	[BO ₂ F ₂]	0.0007	17.44%	

CaB ₄ O ₅ F ₄ -IV	[CaO ₄ F ₄]	0.0014	37.68%	0.07
	[BO ₃]	0.0166	78.36%	
	[BO ₂ F ₂]	0.0029	13.50%	
CaB ₆ O ₈ F ₄ -I	[CaO ₂ F ₆]	0.0017	8.14%	0.106
	[BO ₃]	0.04936	91.70%	
	[BO ₂ F ₂]	0.0039	7.20%	
CaB ₆ O ₈ F ₄ -II	[CaO ₄ F ₄]	0.0006	1.10%	0.083
	[BO ₃]	0.0147	67.21%	
	[BO ₂ F ₂]	0.0054	24.44%	
	[CaO ₃ F ₄]	0.0018	8.36%	

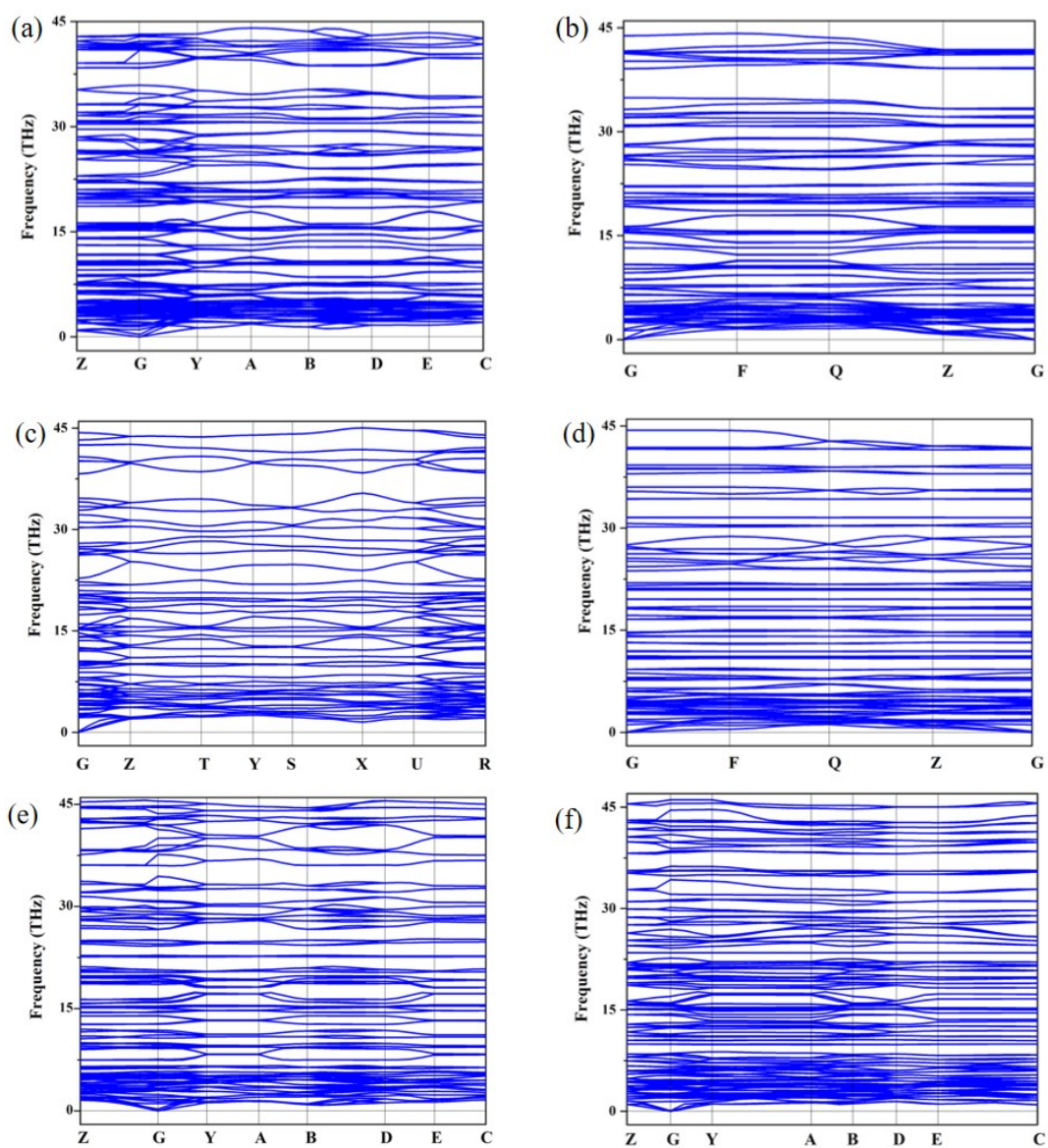


Figure S1. Phonon dispersion spectra of CaB₄O₅F₄-I (a), II (b), III (c), IV(d), CaB₆O₈F₄-I (e) and II (f).

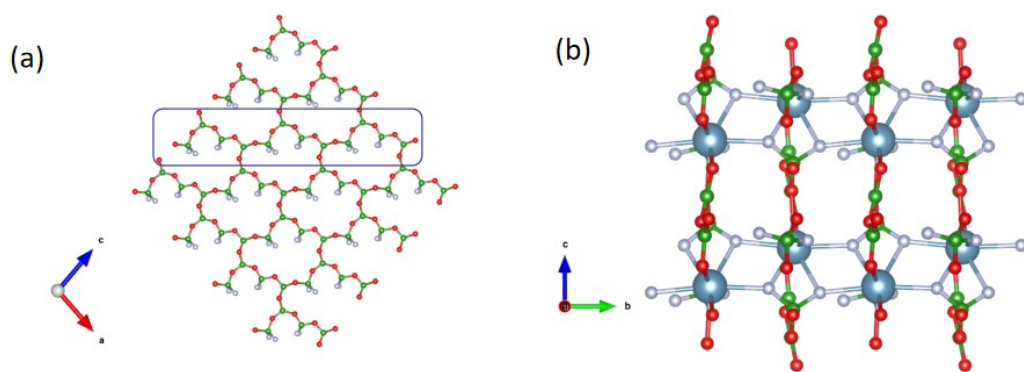


Figure S2. (a) [B₄O₅F₄]_∞ chain and (b) three-dimensional structure of CaB₄O₅F₄-VI.

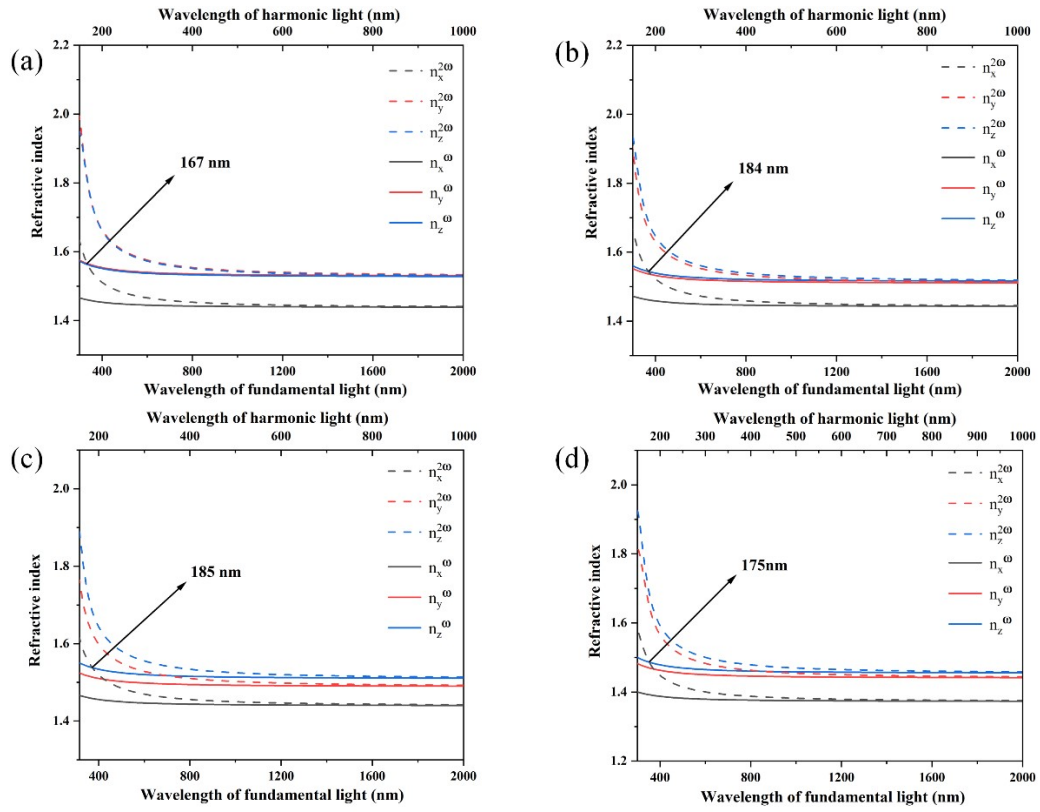


Figure S3. Refractive index dispersion curves and shortest SHG PM wavelengths of $\text{CaB}_4\text{O}_5\text{F}_4$ -V (a), VII (b), VIII(c), and $\text{CaB}_6\text{O}_8\text{F}_4$ -II (d).

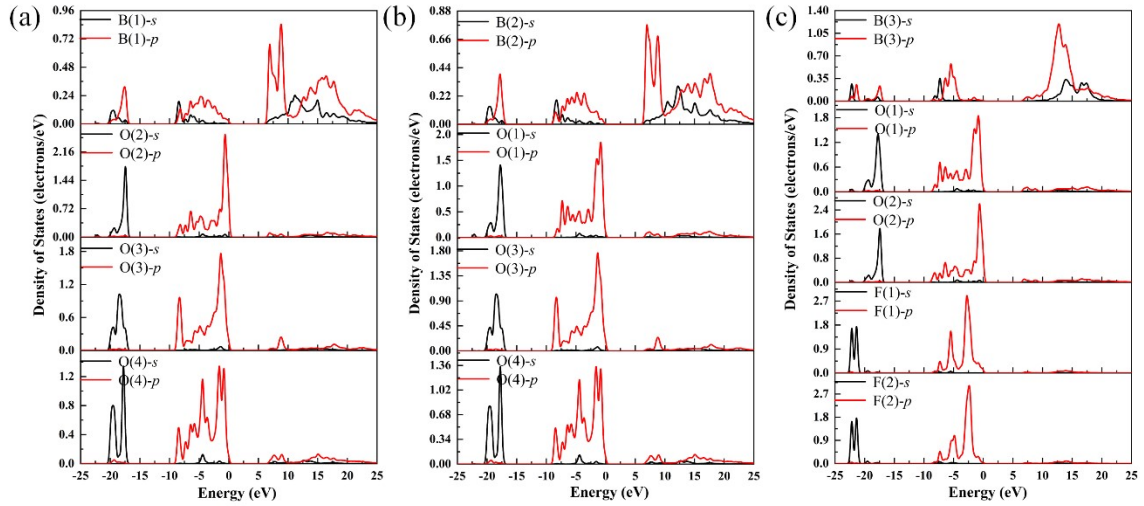


Figure S4. PDOS plot of each atom in the $[\text{B}(1)\text{O}_3]$, $[\text{B}(2)\text{O}_3]$ and $[\text{B}(3)\text{O}_2\text{F}_2]$ groups of $\text{CaB}_6\text{O}_8\text{F}_4$ -I.

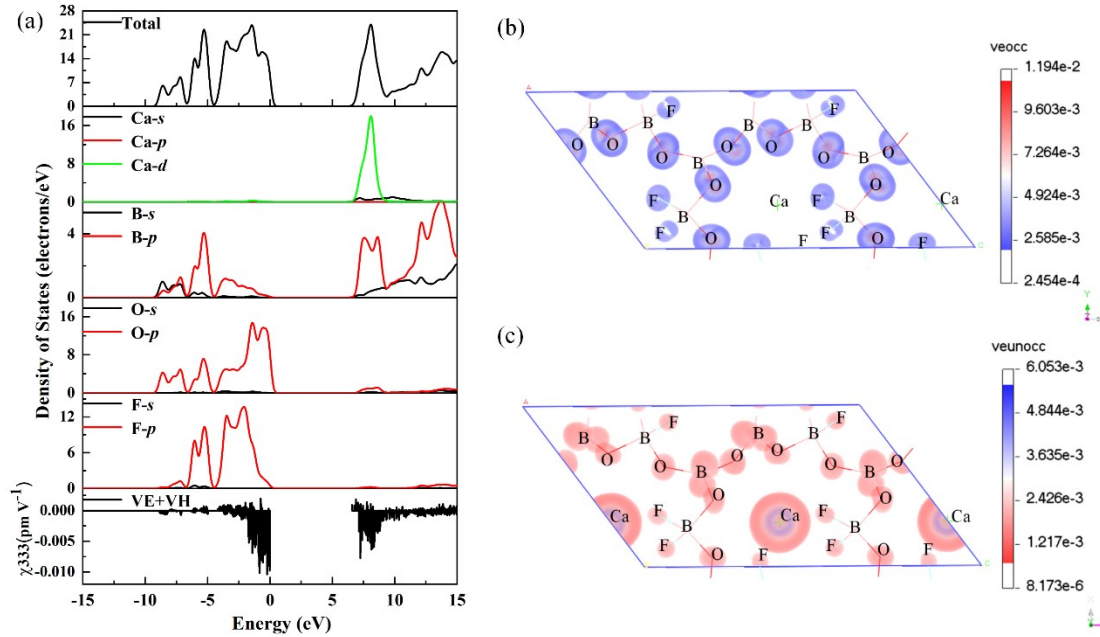


Figure S5. Occupied and unoccupied SHG-density of $\text{CaB}_4\text{O}_5\text{F}_4$ -III in VE process.

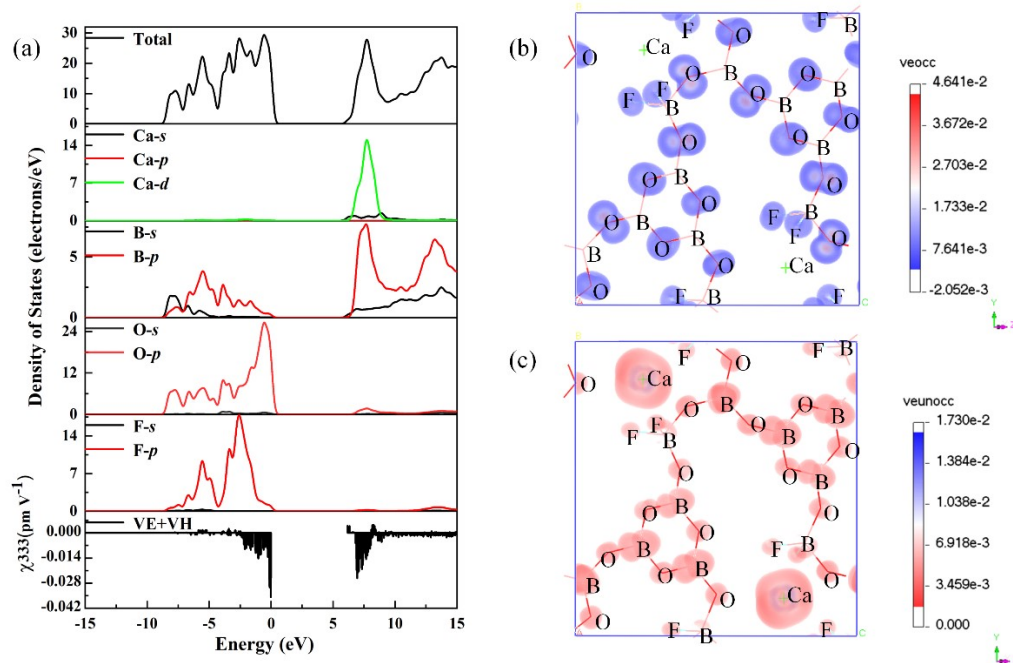


Figure S6. Occupied and unoccupied SHG-density of $\text{CaB}_6\text{O}_8\text{F}_4$ -II in VE process.

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