

Supporting Information for

## Monte Carlo Simulations of Ion Correlations and Transport in Highly Concentrated Liquid Electrolytes

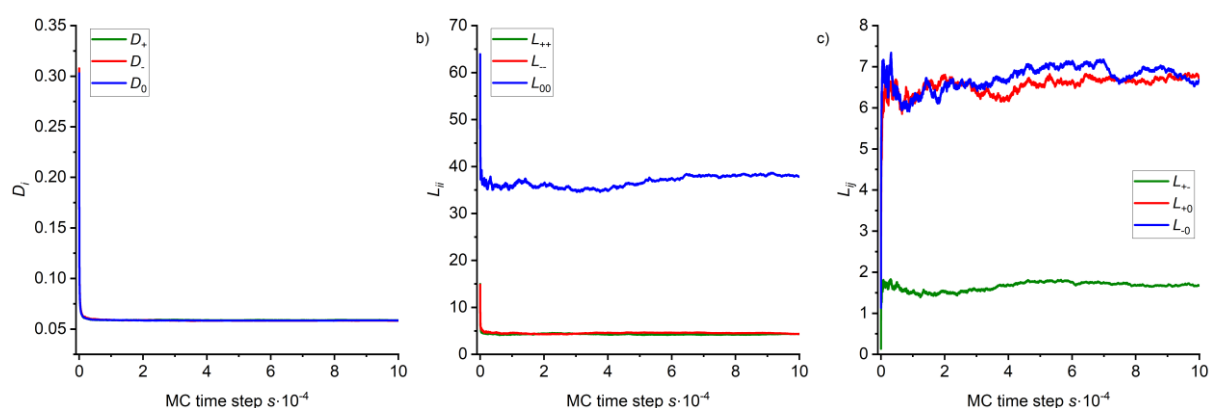
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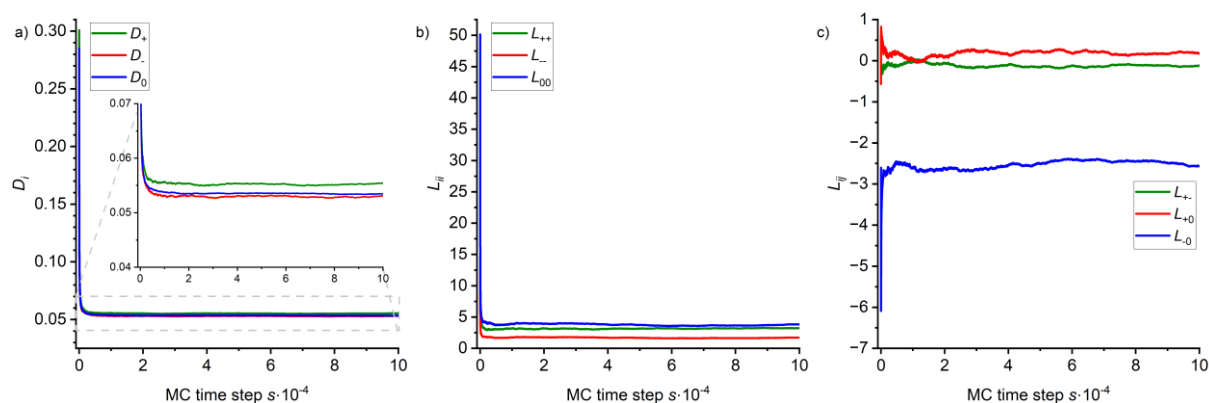
*Marburg Center for Quantum Materials and Sustainable Technologies (mar.quest),*

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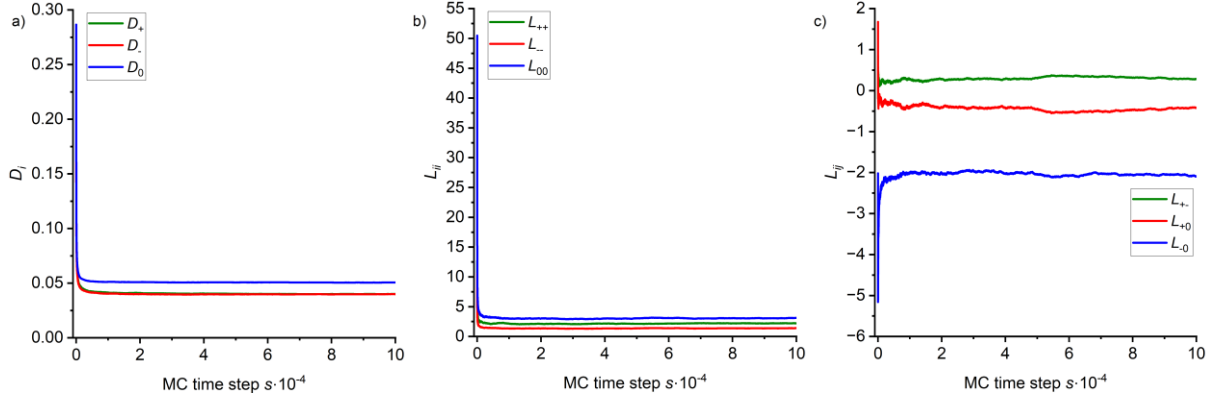
### Exemplary results for time-dependent transport coefficients



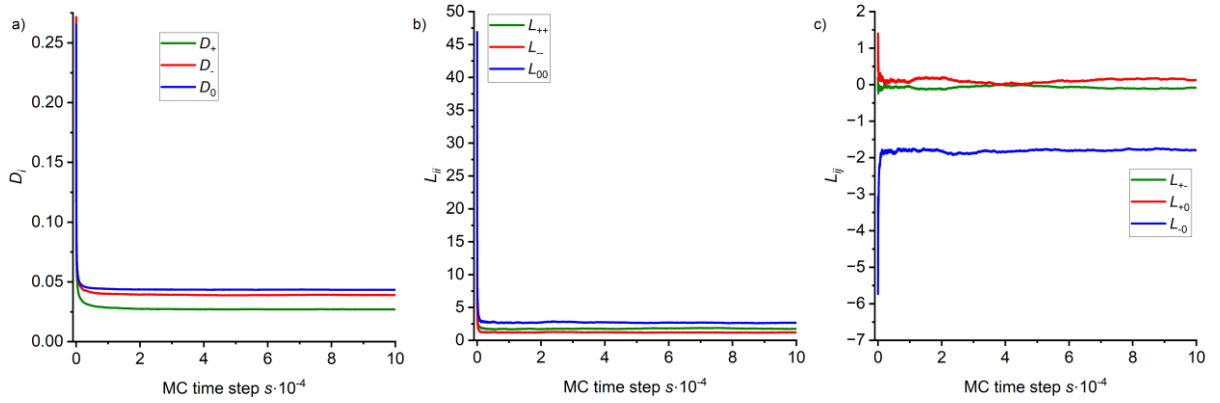
**Fig. S1:** Time-dependent diffusion coefficients and Onsager coefficients for a system with  $1/x = 0.25$  and only hard-core interactions.



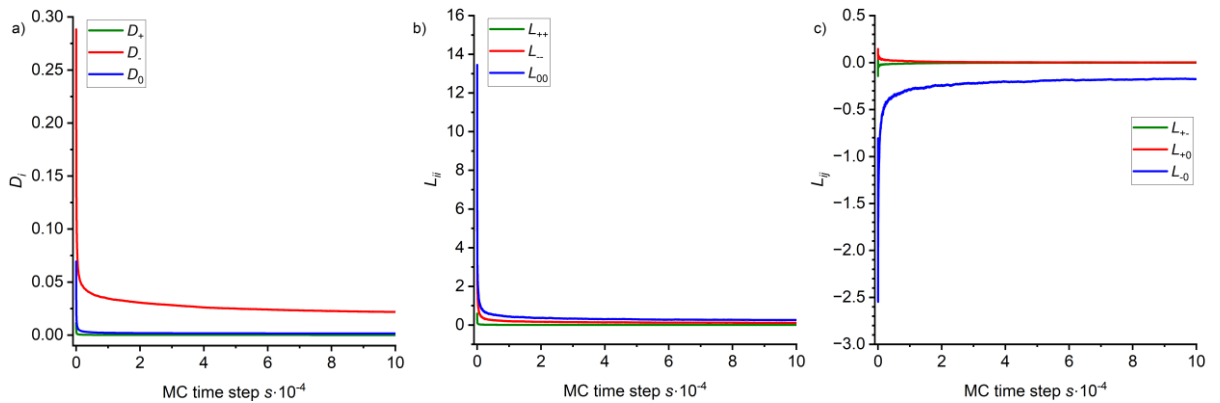
**Fig. S2:** Time-dependent diffusion coefficients and Onsager coefficients for a system with  $1/x = 0.25$ , hard-core interactions, and volume conservation with  $U_{CV} = 1000$  and  $v_0/v_- = 0.67$ .



**Fig. S3:** Time-dependent diffusion coefficients and Onsager coefficients for a system with  $1/x = 0.25$ , hard-core interactions, and volume conservation with  $U_{CV} = 1000$  and  $v_0/v_- = 0.67$ , and Coulomb interactions with  $U_{Coul} = 5$ .



**Fig. S4:** Time-dependent diffusion coefficients and Onsager coefficients for a system with  $1/x = 0.25$ , hard-core interactions, and volume conservation with  $U_{CV} = 1000$  and  $v_0/v_- = 0.67$ , Coulomb interactions with  $U_{Coul} = 5$ , and cation-solvent interactions with  $U_{cat-sol} = -2.5$ .



**Fig. S5:** Time-dependent diffusion coefficients and Onsager coefficients for a system with  $1/x = 0.25$ , hard-core interactions, and volume conservation with  $U_{CV} = 1000$  and  $v_0/v_- = 0.67$ , Coulomb interactions with  $U_{Coul} = 5$ , and cation-solvent interactions with  $U_{cat-sol} = -7.0$ .

## Self and distinct parts of Onsager coefficients and jump rates of particles

**Tab. S1:** Self parts of Onsager coefficients for systems with only hard-core interactions.

$\frac{1}{x}$	$L_+^{\text{self}}$	$L_-^{\text{self}}$	$L_0^{\text{self}}$
0.1	$1.40 \pm 0.01$	$1.39 \pm 0.01$	$13.99 \pm 0.03$
0.25	$2.82 \pm 0.01$	$2.80 \pm 0.02$	$11.23 \pm 0.03$
0.5	$4.18 \pm 0.02$	$4.20 \pm 0.02$	$8.38 \pm 0.03$
1.0	$5.60 \pm 0.01$	$5.64 \pm 0.02$	$5.59 \pm 0.02$

**Tab. S2:** Distinct parts of Onsager coefficients and  $L_{-0}$  for systems with only hard-core interactions.

$\frac{1}{x}$	$L_{++}^{\text{distinct}}$	$L_{--}^{\text{distinct}}$	$L_{00}^{\text{distinct}}$	$L_{-0}$
0.1	$0.38 \pm 0.08$	$0.39 \pm 0.05$	$41 \pm 2$	$3.9 \pm 0.3$
0.25	$1.4 \pm 0.2$	$1.7 \pm 0.2$	$27 \pm 2$	$6.8 \pm 0.5$
0.5	$3.9 \pm 0.4$	$3.9 \pm 0.2$	$15 \pm 1$	$7.7 \pm 0.5$
1.0	$5.8 \pm 0.5$	$6.1 \pm 0.3$	$5.9 \pm 0.4$	$6.2 \pm 0.3$

**Tab. S3:** Jump rates of particles for systems with only hard-core interactions.

$\frac{1}{x}$	jump rate of the cations	jump rate of the anions	jump rate of the solvent
0.1	$0.33 \pm 0.00$	$0.33 \pm 0.00$	$0.33 \pm 0.00$
0.25	$0.33 \pm 0.00$	$0.33 \pm 0.00$	$0.33 \pm 0.00$
0.5	$0.33 \pm 0.00$	$0.33 \pm 0.00$	$0.33 \pm 0.00$
1.0	$0.33 \pm 0.00$	$0.33 \pm 0.00$	$0.33 \pm 0.00$

**Tab. S4:** Self parts of Onsager coefficients for systems with hard-core interactions and volume conservation with  $U_{\text{CV}} = 1000$ .

$\frac{v_0}{v_-}$	$\frac{1}{x}$	$L_+^{\text{self}}$	$L_-^{\text{self}}$	$L_0^{\text{self}}$
0.67	0.1	$1.31 \pm 0.01$	$1.27 \pm 0.01$	$12.87 \pm 0.01$
	0.25	$2.65 \pm 0.01$	$2.54 \pm 0.01$	$10.26 \pm 0.03$
	0.5	$3.96 \pm 0.02$	$3.79 \pm 0.02$	$7.68 \pm 0.02$
	1.0	$5.26 \pm 0.02$	$5.02 \pm 0.02$	$5.12 \pm 0.02$
0.90	0.1	$1.32 \pm 0.01$	$1.28 \pm 0.01$	$12.83 \pm 0.02$
	0.25	$2.64 \pm 0.02$	$2.56 \pm 0.01$	$10.24 \pm 0.02$
	0.5	$3.93 \pm 0.02$	$3.83 \pm 0.02$	$7.67 \pm 0.02$
	1.0	$5.29 \pm 0.01$	$5.06 \pm 0.02$	$5.08 \pm 0.02$
1.05	0.1	$1.31 \pm 0.01$	$1.27 \pm 0.01$	$12.85 \pm 0.03$
	0.25	$2.66 \pm 0.02$	$2.58 \pm 0.01$	$10.23 \pm 0.03$
	0.5	$3.96 \pm 0.01$	$3.81 \pm 0.01$	$7.64 \pm 0.02$
	1.0	$5.29 \pm 0.02$	$5.07 \pm 0.01$	$5.08 \pm 0.01$

**Tab. S5:** Distinct parts of Onsager coefficients and  $L_{-0}$  for systems with hard-core interactions and volume conservation with  $U_{CV} = 1000$ .

$\frac{v_0}{v_-}$	$\frac{1}{x}$	$L_{++}^{\text{distinct}}$	$L_{--}^{\text{distinct}}$	$L_{00}^{\text{distinct}}$	$L_{-0}$
0.67	0.1	$0.20 \pm 0.04$	$-0.26 \pm 0.03$	$-10.61 \pm 0.07$	$-1.51 \pm 0.05$
	0.25	$0.6 \pm 0.2$	$-0.88 \pm 0.06$	$-6.6 \pm 0.1$	$-2.47 \pm 0.09$
	0.5	$1.2 \pm 0.2$	$-1.88 \pm 0.05$	$-3.4 \pm 0.1$	$-2.85 \pm 0.07$
	1.0	$2.2 \pm 0.3$	$-3.46 \pm 0.05$	$-1.64 \pm 0.09$	$-2.33 \pm 0.06$
0.90	0.1	$0.08 \pm 0.04$	$-0.15 \pm 0.04$	$-11.45 \pm 0.06$	$-1.25 \pm 0.04$
	0.25	$0.35 \pm 0.09$	$-0.56 \pm 0.07$	$-7.77 \pm 0.09$	$-2.23 \pm 0.08$
	0.5	$1.0 \pm 0.2$	$-1.30 \pm 0.08$	$-4.6 \pm 0.1$	$-2.80 \pm 0.09$
	1.0	$1.6 \pm 0.3$	$-2.84 \pm 0.07$	$-2.35 \pm 0.09$	$-2.46 \pm 0.08$
1.05	0.1	$0.07 \pm 0.04$	$-0.12 \pm 0.04$	$-11.81 \pm 0.05$	$-1.09 \pm 0.04$
	0.25	$0.5 \pm 0.1$	$-0.42 \pm 0.09$	$-8.26 \pm 0.08$	$-2.06 \pm 0.08$
	0.5	$0.8 \pm 0.2$	$-1.07 \pm 0.08$	$-5.16 \pm 0.07$	$-2.61 \pm 0.07$
	1.0	$1.8 \pm 0.3$	$-2.5 \pm 0.1$	$-2.75 \pm 0.09$	$-2.45 \pm 0.09$

**Tab. S6:** Jump rates of particles for systems for systems with hard-core-interactions and volume conservation with  $U_{CV} = 1000$ .

$\frac{v_0}{v_-}$	$\frac{1}{x}$	jump rate of the cations	jump rate of the anions	jump rate of the solvent
0.67	0.1	$0.33 \pm 0.01$	$0.30 \pm 0.01$	$0.31 \pm 0.01$
	0.25	$0.33 \pm 0.01$	$0.30 \pm 0.01$	$0.31 \pm 0.01$
	0.5	$0.33 \pm 0.01$	$0.30 \pm 0.01$	$0.31 \pm 0.01$
	1.0	$0.33 \pm 0.01$	$0.30 \pm 0.01$	$0.31 \pm 0.01$
0.90	0.1	$0.33 \pm 0.01$	$0.31 \pm 0.01$	$0.31 \pm 0.01$
	0.25	$0.33 \pm 0.01$	$0.31 \pm 0.01$	$0.31 \pm 0.01$
	0.5	$0.33 \pm 0.01$	$0.30 \pm 0.01$	$0.31 \pm 0.01$
	1.0	$0.33 \pm 0.01$	$0.30 \pm 0.01$	$0.30 \pm 0.01$
1.05	0.1	$0.33 \pm 0.01$	$0.31 \pm 0.01$	$0.31 \pm 0.01$
	0.25	$0.33 \pm 0.01$	$0.31 \pm 0.01$	$0.31 \pm 0.01$
	0.5	$0.33 \pm 0.01$	$0.31 \pm 0.01$	$0.30 \pm 0.01$
	1.0	$0.33 \pm 0.01$	$0.30 \pm 0.01$	$0.30 \pm 0.01$

**Tab. S7:** Self parts of Onsager coefficients for systems with hard-core-interactions, volume conservation with  $U_{CV} = 1000$  and Coulomb interactions with  $U_{Coul} = 5$ .

$\frac{v_0}{v_-}$	$\frac{1}{x}$	$L_+^{\text{self}}$	$L_-^{\text{self}}$	$L_0^{\text{self}}$
0.67	0.1	$1.02 \pm 0.01$	$0.99 \pm 0.01$	$12.61 \pm 0.01$
	0.25	$1.92 \pm 0.01$	$1.91 \pm 0.01$	$9.71 \pm 0.02$
	0.5	$2.77 \pm 0.01$	$2.73 \pm 0.01$	$6.98 \pm 0.02$
	1.0	$3.48 \pm 0.01$	$3.43 \pm 0.01$	$4.45 \pm 0.02$
0.90	0.1	$1.02 \pm 0.01$	$1.00 \pm 0.01$	$12.51 \pm 0.03$
	0.25	$1.94 \pm 0.01$	$1.92 \pm 0.01$	$9.66 \pm 0.01$
	0.5	$2.77 \pm 0.01$	$2.72 \pm 0.01$	$7.00 \pm 0.01$
	1.0	$3.50 \pm 0.02$	$3.44 \pm 0.01$	$4.42 \pm 0.01$
1.05	0.1	$1.02 \pm 0.01$	$1.01 \pm 0.01$	$12.58 \pm 0.03$

0.25	$1.94 \pm 0.01$	$1.93 \pm 0.01$	$9.69 \pm 0.04$
0.5	$2.77 \pm 0.02$	$2.75 \pm 0.01$	$6.97 \pm 0.02$
1.0	$3.49 \pm 0.01$	$3.44 \pm 0.01$	$4.41 \pm 0.02$

**Tab. S8:** Distinct parts of Onsager coefficients and  $L_{-0}$  for systems with hard-core-interactions, volume conservation with  $U_{CV} = 1000$  and Coulomb interactions with  $U_{Coul} = 5$ .

$\frac{v_0}{v_-}$	$\frac{1}{\chi}$	$L_{++}^{\text{distinct}}$	$L_{--}^{\text{distinct}}$	$L_{00}^{\text{distinct}}$	$L_{-0}$
0.67	0.1	$0.04 \pm 0.03$	$-0.08 \pm 0.04$	$-10.59 \pm 0.08$	$-1.35 \pm 0.06$
	0.25	$0.30 \pm 0.07$	$-0.54 \pm 0.05$	$-6.7 \pm 0.1$	$-2.05 \pm 0.07$
	0.5	$0.4 \pm 0.1$	$-1.13 \pm 0.07$	$-3.4 \pm 0.2$	$-2.4 \pm 0.1$
	1.0	$0.59 \pm 0.07$	$-2.19 \pm 0.05$	$-1.7 \pm 0.1$	$-1.85 \pm 0.08$
0.90	0.1	$0.11 \pm 0.04$	$-0.04 \pm 0.02$	$-11.33 \pm 0.04$	$-1.06 \pm 0.03$
	0.25	$0.23 \pm 0.09$	$-0.35 \pm 0.05$	$-7.72 \pm 0.07$	$-1.74 \pm 0.06$
	0.5	$0.56 \pm 0.07$	$-0.87 \pm 0.07$	$-4.72 \pm 0.09$	$-2.05 \pm 0.08$
	1.0	$1.1 \pm 0.2$	$-1.70 \pm 0.06$	$-2.28 \pm 0.08$	$-1.93 \pm 0.07$
1.05	0.1	$0.06 \pm 0.03$	$-0.07 \pm 0.04$	$-11.72 \pm 0.05$	$-0.89 \pm 0.04$
	0.25	$0.31 \pm 0.07$	$-0.18 \pm 0.08$	$-8.10 \pm 0.08$	$-1.66 \pm 0.07$
	0.5	$0.5 \pm 0.1$	$-0.61 \pm 0.04$	$-5.02 \pm 0.04$	$-2.04 \pm 0.04$
	1.0	$0.9 \pm 0.1$	$-1.35 \pm 0.07$	$-2.52 \pm 0.07$	$-1.99 \pm 0.07$

**Tab. S9:** Jump rates of particles for systems with hard-core-interactions, volume conservation with  $U_{CV} = 1000$  and Coulomb interactions with  $U_{Coul} = 5$ .

$\frac{v_0}{v_-}$	$\frac{1}{\chi}$	jump rate of the cations	jump rate of the anions	jump rate of the solvent
0.67	0.1	$0.29 \pm 0.01$	$0.28 \pm 0.01$	$0.31 \pm 0.01$
	0.25	$0.29 \pm 0.01$	$0.27 \pm 0.01$	$0.31 \pm 0.01$
	0.5	$0.28 \pm 0.01$	$0.27 \pm 0.01$	$0.31 \pm 0.01$
	1.0	$0.28 \pm 0.01$	$0.27 \pm 0.01$	$0.31 \pm 0.01$
0.90	0.1	$0.29 \pm 0.01$	$0.28 \pm 0.01$	$0.31 \pm 0.01$
	0.25	$0.29 \pm 0.01$	$0.28 \pm 0.01$	$0.31 \pm 0.01$
	0.5	$0.28 \pm 0.01$	$0.27 \pm 0.01$	$0.31 \pm 0.01$
	1.0	$0.28 \pm 0.01$	$0.27 \pm 0.01$	$0.31 \pm 0.01$
1.05	0.1	$0.29 \pm 0.01$	$0.29 \pm 0.01$	$0.31 \pm 0.01$
	0.25	$0.29 \pm 0.01$	$0.28 \pm 0.01$	$0.31 \pm 0.01$
	0.5	$0.28 \pm 0.01$	$0.28 \pm 0.01$	$0.31 \pm 0.01$
	1.0	$0.28 \pm 0.01$	$0.27 \pm 0.01$	$0.31 \pm 0.01$

**Tab. S10:** Self parts of Onsager coefficients for systems with hard-core interactions, volume conservation with  $U_{CV} = 1000$ , Coulomb interactions with  $U_{Coul} = 5$ , and cation-solvent interactions with  $U_{\text{cat-sol}} = -2.5$ .

$\frac{v_0}{v_-}$	$\frac{1}{\chi}$	$L_+^{\text{self}}$	$L_-^{\text{self}}$	$L_0^{\text{self}}$
0.67	0.1	$0.68 \pm 0.01$	$0.98 \pm 0.01$	$11.51 \pm 0.03$
	0.25	$1.30 \pm 0.01$	$1.88 \pm 0.01$	$8.34 \pm 0.02$
	0.5	$2.00 \pm 0.01$	$2.63 \pm 0.01$	$5.63 \pm 0.02$

	1.0	$2.81 \pm 0.01$	$3.33 \pm 0.01$	$3.37 \pm 0.02$
0.90	0.1	$0.67 \pm 0.01$	$0.99 \pm 0.01$	$11.55 \pm 0.04$
	0.25	$1.31 \pm 0.01$	$1.89 \pm 0.01$	$8.36 \pm 0.02$
	0.5	$2.02 \pm 0.01$	$2.67 \pm 0.01$	$5.60 \pm 0.02$
	1.0	$2.78 \pm 0.01$	$3.34 \pm 0.01$	$3.34 \pm 0.01$
1.05	0.1	$0.668 \pm 0.006$	$1.012 \pm 0.005$	$11.59 \pm 0.03$
	0.25	$1.30 \pm 0.01$	$1.89 \pm 0.01$	$8.32 \pm 0.01$
	0.5	$2.01 \pm 0.01$	$2.66 \pm 0.01$	$5.62 \pm 0.01$
	1.0	$2.80 \pm 0.01$	$3.35 \pm 0.01$	$3.34 \pm 0.01$

**Tab. S11:** Distinct parts of Onsager coefficients and  $L_{-0}$  for systems with hard-core interactions, volume conservation with  $U_{CV} = 1000$ , Coulomb interactions with  $U_{Coul} = 5$ , and cation-solvent interactions with  $U_{cat-sol} = -2.5$ .

$\frac{v_0}{v_-}$	$\frac{1}{x}$	$L_{++}^{\text{distinct}}$	$L_{--}^{\text{distinct}}$	$L_{00}^{\text{distinct}}$	$L_{-0}$
0.67	0.1	$0.16 \pm 0.02$	$-0.11 \pm 0.02$	$-9.57 \pm 0.05$	$-1.30 \pm 0.03$
	0.25	$0.51 \pm 0.06$	$-0.69 \pm 0.03$	$-5.68 \pm 0.08$	$-1.78 \pm 0.05$
	0.5	$0.68 \pm 0.06$	$-1.42 \pm 0.03$	$-2.92 \pm 0.07$	$-1.81 \pm 0.05$
	1.0	$0.7 \pm 0.1$	$-2.36 \pm 0.04$	$-1.21 \pm 0.08$	$-1.44 \pm 0.05$
0.90	0.1	$0.13 \pm 0.02$	$-0.06 \pm 0.04$	$-10.40 \pm 0.06$	$-1.04 \pm 0.04$
	0.25	$0.46 \pm 0.06$	$-0.47 \pm 0.04$	$-6.61 \pm 0.06$	$-1.57 \pm 0.05$
	0.5	$0.44 \pm 0.08$	$-1.18 \pm 0.06$	$-3.76 \pm 0.07$	$-1.65 \pm 0.06$
	1.0	$0.8 \pm 0.1$	$-1.91 \pm 0.07$	$-1.58 \pm 0.08$	$-1.59 \pm 0.07$
1.05	0.1	$0.16 \pm 0.03$	$-0.08 \pm 0.02$	$-10.75 \pm 0.04$	$-0.88 \pm 0.02$
	0.25	$0.45 \pm 0.06$	$-0.37 \pm 0.04$	$-6.94 \pm 0.04$	$-1.45 \pm 0.04$
	0.5	$0.68 \pm 0.08$	$-0.94 \pm 0.05$	$-4.06 \pm 0.04$	$-1.64 \pm 0.04$
	1.0	$1.0 \pm 0.2$	$-1.70 \pm 0.06$	$-1.84 \pm 0.05$	$-1.58 \pm 0.06$

**Tab. S12:** Jump rates of particles for systems with hard-core interactions, volume conservation with  $U_{CV} = 1000$ , Coulomb interactions with  $U_{Coul} = 5$ , and cation-solvent interactions with  $U_{cat-sol} = -2.5$ .

$\frac{v_0}{v_-}$	$\frac{1}{x}$	jump rate of the cations	jump rate of the anions	jump rate of the solvent
0.67	0.1	$0.20 \pm 0.01$	$0.29 \pm 0.01$	$0.30 \pm 0.01$
	0.25	$0.22 \pm 0.01$	$0.29 \pm 0.01$	$0.29 \pm 0.01$
	0.5	$0.24 \pm 0.01$	$0.29 \pm 0.01$	$0.28 \pm 0.01$
	1.0	$0.25 \pm 0.01$	$0.29 \pm 0.01$	$0.27 \pm 0.01$
0.90	0.1	$0.20 \pm 0.01$	$0.30 \pm 0.01$	$0.30 \pm 0.01$
	0.25	$0.22 \pm 0.01$	$0.30 \pm 0.01$	$0.29 \pm 0.01$
	0.5	$0.24 \pm 0.01$	$0.29 \pm 0.01$	$0.28 \pm 0.01$
	1.0	$0.25 \pm 0.01$	$0.29 \pm 0.01$	$0.27 \pm 0.01$
1.05	0.1	$0.20 \pm 0.01$	$0.30 \pm 0.01$	$0.30 \pm 0.01$
	0.25	$0.22 \pm 0.01$	$0.30 \pm 0.01$	$0.29 \pm 0.01$
	0.5	$0.24 \pm 0.01$	$0.30 \pm 0.01$	$0.28 \pm 0.01$
	1.0	$0.25 \pm 0.01$	$0.29 \pm 0.01$	$0.26 \pm 0.01$

**Tab. S13:** Self parts of Onsager coefficients for systems with hard-core interactions, volume conservation with  $U_{CV} = 1000$ , Coulomb interactions with  $U_{Coul} = 5$ , and cation-solvent interactions with  $U_{cat-sol} = -7$ .

$\frac{v_0}{v_-}$	$\frac{1}{x}$	$L_+^{self}$	$L_-^{self}$	$L_0^{self}$
0.67	0.1	$0.00131 \pm 0.00006$	$1.29 \pm 0.02$	$4.86 \pm 0.03$
	0.25	$0.00207 \pm 0.00004$	$1.08 \pm 0.01$	$0.295 \pm 0.004$
	0.5	$0.0035 \pm 0.0001$	$0.95 \pm 0.01$	$0.0230 \pm 0.0005$
	1.0	$0.0185 \pm 0.0004$	$1.12 \pm 0.01$	$0.0065 \pm 0.0001$
0.90	0.1	$0.00118 \pm 0.00005$	$1.32 \pm 0.02$	$4.83 \pm 0.01$
	0.25	$0.00208 \pm 0.00003$	$1.12 \pm 0.01$	$0.301 \pm 0.004$
	0.5	$0.0035 \pm 0.0001$	$0.98 \pm 0.01$	$0.0229 \pm 0.0005$
	1.0	$0.0187 \pm 0.0003$	$1.13 \pm 0.01$	$0.0065 \pm 0.0002$
1.05	0.1	$0.0013 \pm 0.0001$	$1.33 \pm 0.01$	$4.74 \pm 0.02$
	0.25	$0.00210 \pm 0.00004$	$1.13 \pm 0.01$	$0.297 \pm 0.004$
	0.5	$0.0035 \pm 0.0001$	$0.99 \pm 0.01$	$0.023 \pm 0.001$
	1.0	$0.0196 \pm 0.0004$	$1.15 \pm 0.01$	$0.0068 \pm 0.0001$

**Tab. S14:** Distinct parts of Onsager coefficients and  $L_{-0}$  for systems with hard-core interactions, volume conservation with  $U_{CV} = 1000$ , Coulomb interactions with  $U_{Coul} = 5$ , and cation-solvent interactions with  $U_{cat-sol} = -7$ .

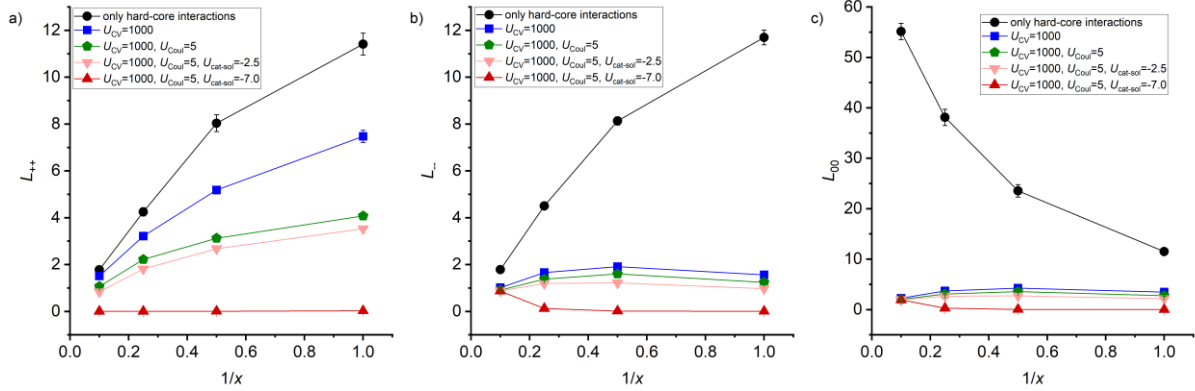
$\frac{v_0}{v_-}$	$\frac{1}{x}$	$L_{++}^{distinct}$	$L_{--}^{distinct}$	$L_{00}^{distinct}$	$L_{-0}$
0.67	0.1	$0.0004 \pm 0.0001$	$-0.42 \pm 0.05$	$-2.9 \pm 0.1$	$-1.30 \pm 0.07$
	0.25	$0.0008 \pm 0.0001$	$-0.96 \pm 0.01$	$-0.03 \pm 0.01$	$-0.18 \pm 0.01$
	0.5	$0.0012 \pm 0.0002$	$-0.93 \pm 0.01$	$0.006 \pm 0.001$	$-0.019 \pm 0.001$
	1.0	$0.006 \pm 0.001$	$-1.12 \pm 0.01$	$0.0032 \pm 0.0003$	$-0.0064 \pm 0.0002$
0.90	0.1	$0.0005 \pm 0.0002$	$-0.21 \pm 0.04$	$-3.45 \pm 0.05$	$-1.23 \pm 0.04$
	0.25	$0.0006 \pm 0.0001$	$-0.92 \pm 0.02$	$-0.05 \pm 0.01$	$-0.23 \pm 0.01$
	0.5	$0.0013 \pm 0.0003$	$-0.95 \pm 0.01$	$0.003 \pm 0.001$	$-0.023 \pm 0.001$
	1.0	$0.005 \pm 0.001$	$-1.12 \pm 0.01$	$0.0027 \pm 0.0004$	$-0.0082 \pm 0.0003$
1.05	0.1	$0.0005 \pm 0.0001$	$-0.20 \pm 0.03$	$-3.77 \pm 0.05$	$-1.02 \pm 0.04$
	0.25	$0.0008 \pm 0.0001$	$-0.78 \pm 0.01$	$-0.07 \pm 0.01$	$-0.24 \pm 0.01$
	0.5	$0.0011 \pm 0.0002$	$-0.97 \pm 0.01$	$0.004 \pm 0.001$	$-0.028 \pm 0.001$
	1.0	$0.006 \pm 0.001$	$-0.99 \pm 0.01$	$0.0030 \pm 0.0004$	$-0.0103 \pm 0.0004$

**Tab. S15:** Jump rates of particles for systems with hard-core interactions, volume conservation with  $U_{CV} = 1000$ , Coulomb interactions with  $U_{Coul} = 5$ , and cation-solvent interactions with  $U_{cat-sol} = -7$ .

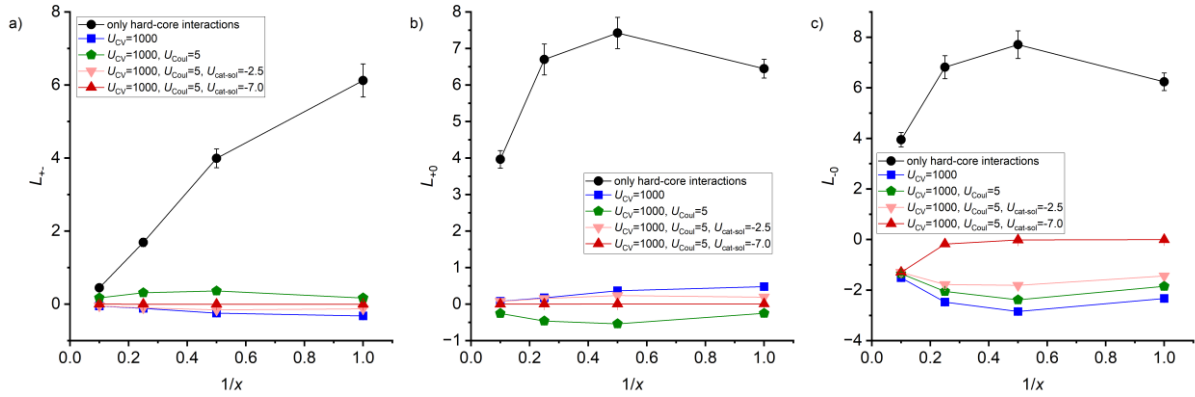
$\frac{v_0}{v_-}$	$\frac{1}{x}$	jump rate of the cations	jump rate of the anions	jump rate of the solvent
0.67	0.1	$0.01 \pm 0.01$	$0.40 \pm 0.01$	$0.17 \pm 0.01$
	0.25	$0.01 \pm 0.01$	$0.31 \pm 0.01$	$0.08 \pm 0.01$
	0.5	$0.02 \pm 0.01$	$0.25 \pm 0.01$	$0.04 \pm 0.01$
	1.0	$0.04 \pm 0.01$	$0.22 \pm 0.01$	$0.03 \pm 0.01$
0.90	0.1	$0.01 \pm 0.01$	$0.41 \pm 0.01$	$0.17 \pm 0.01$
	0.25	$0.01 \pm 0.01$	$0.31 \pm 0.01$	$0.07 \pm 0.01$

	0.5	$0.02 \pm 0.01$	$0.25 \pm 0.01$	$0.04 \pm 0.01$
	1.0	$0.04 \pm 0.01$	$0.22 \pm 0.01$	$0.03 \pm 0.01$
1.05	0.1	$0.01 \pm 0.01$	$0.41 \pm 0.01$	$0.19 \pm 0.01$
	0.25	$0.01 \pm 0.01$	$0.31 \pm 0.01$	$0.07 \pm 0.01$
	0.5	$0.02 \pm 0.01$	$0.25 \pm 0.01$	$0.04 \pm 0.01$
	1.0	$0.04 \pm 0.01$	$0.22 \pm 0.01$	$0.03 \pm 0.01$

### Composition-dependent Onsager coefficients for systems with $\frac{v_0}{v_-} = 0.67$

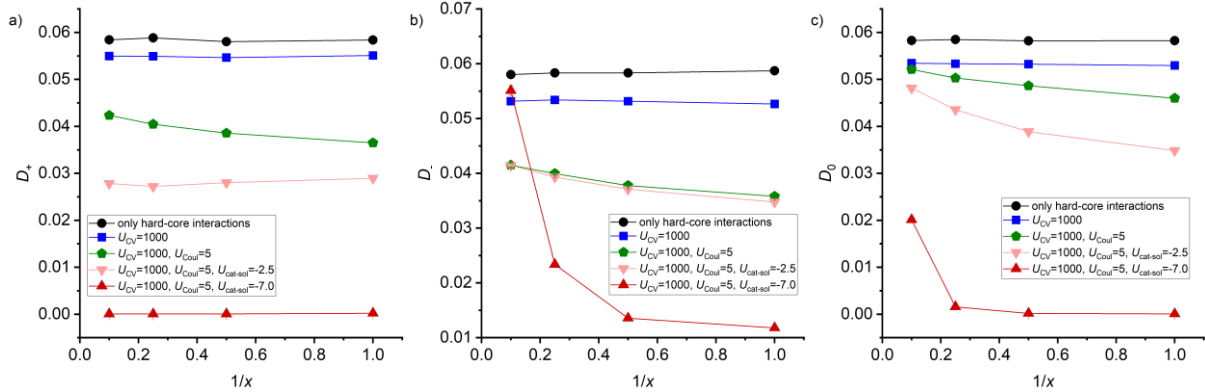


**Fig. S6:** Plots of the Onsager coefficients  $L_{++}$ ,  $L_{--}$  and  $L_{00}$  vs. molar ratio  $1/x$  for different energy parameters.

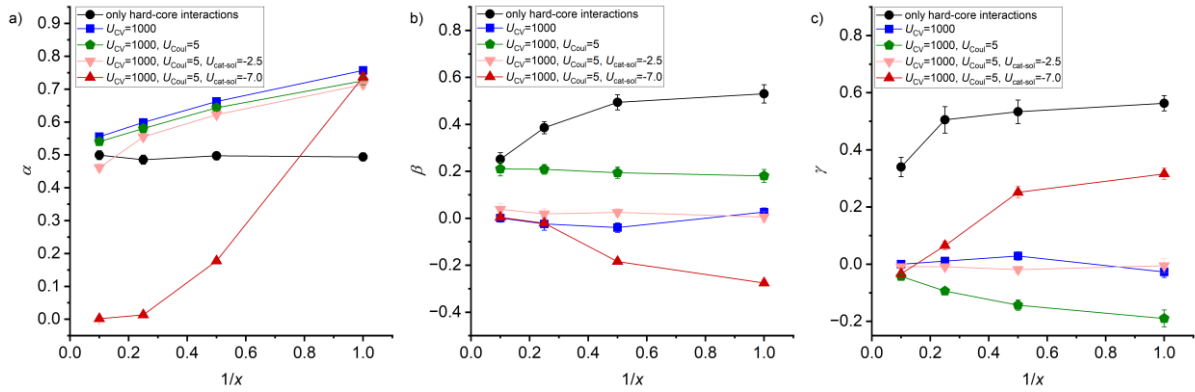


**Fig. S7:** Plots of the Onsager coefficients  $L_{+-}$ ,  $L_{+0}$  and  $L_{-0}$  vs. molar ratio  $1/x$  for different energy parameters.

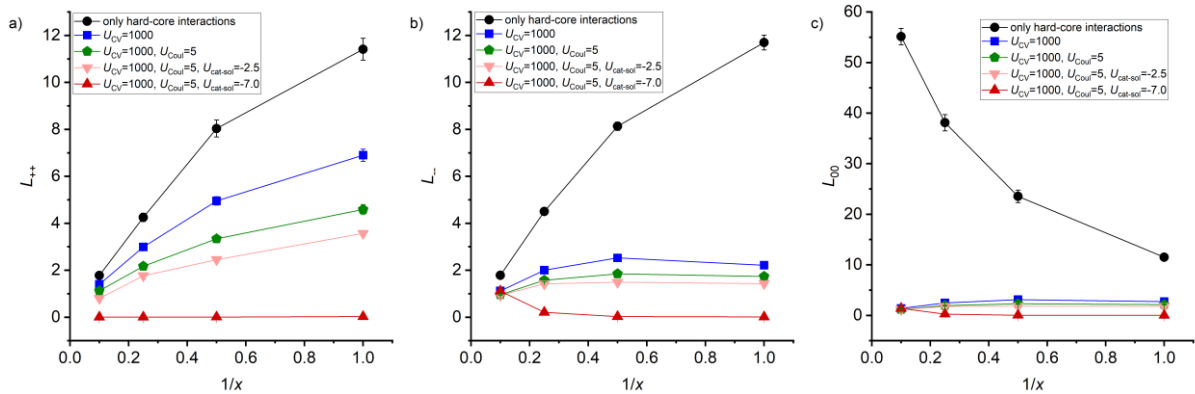
## Composition-dependent diffusion coefficients and correlation parameters for systems with $\frac{v_0}{v_-} = 0.90$



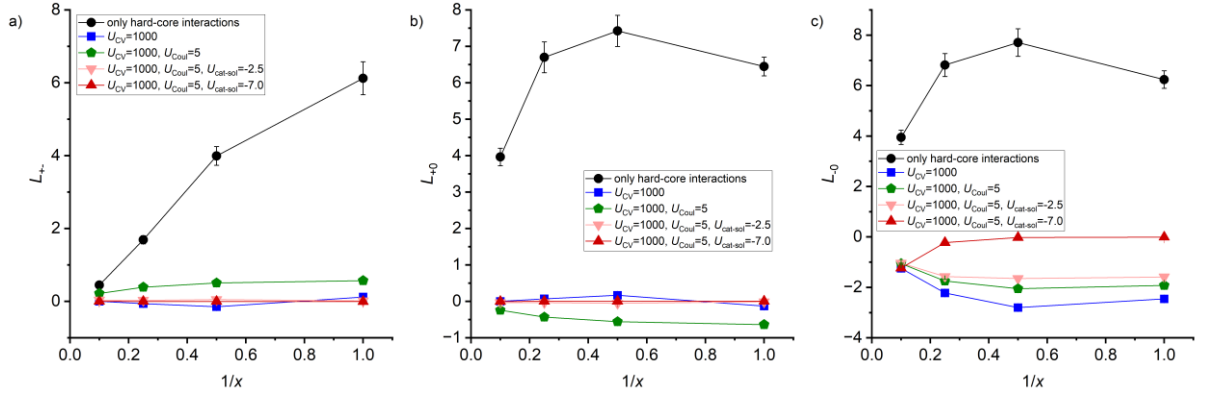
**Fig. S8:** Plots of the diffusion coefficients of  $D_+$ ,  $D_-$ , and  $D_0$  vs. the molar ratio  $1/x$  for different energy parameters.



**Fig. S9:** Plots of correlation parameters  $\alpha$ ,  $\beta$  and  $\gamma$  vs. the molar ratio  $1/x$  for different energy parameters.

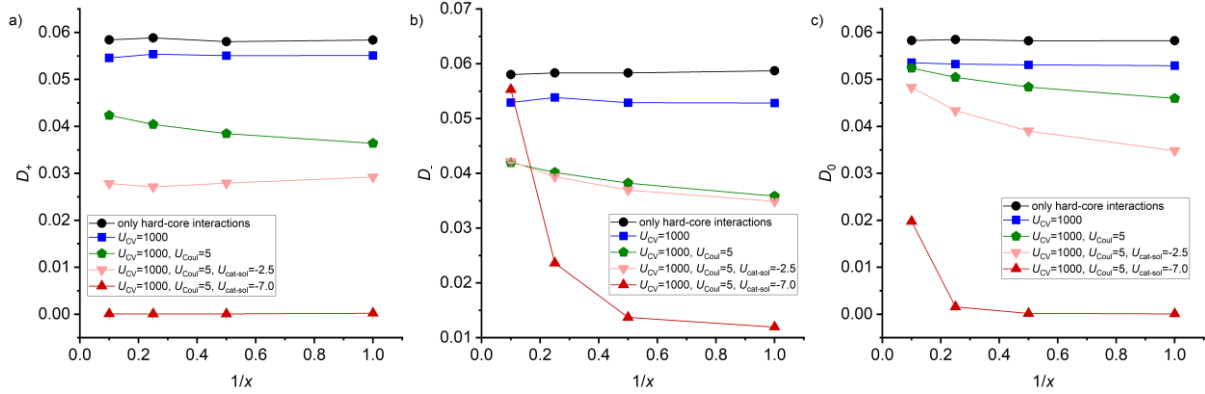


**Fig. S10:** Plots of the Onsager coefficients  $L_{++}$ ,  $L_{--}$ , and  $L_{00}$  vs. the molar ratio  $1/x$  for different energy parameters.

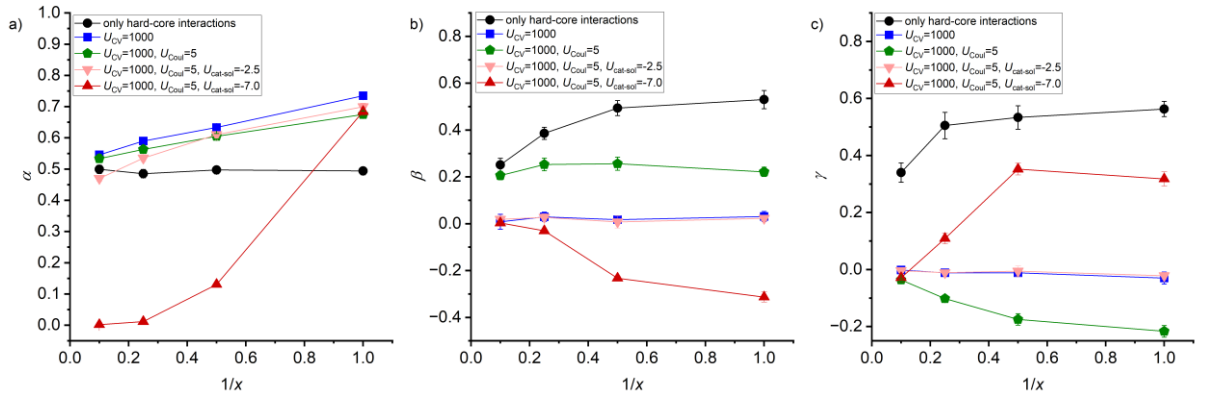


**Fig. S11:** Plots of the Onsager coefficients  $L_{+-}$ ,  $L_{+0}$ , and  $L_{-0}$  vs. the molar ratio  $1/x$  for different energy parameters.

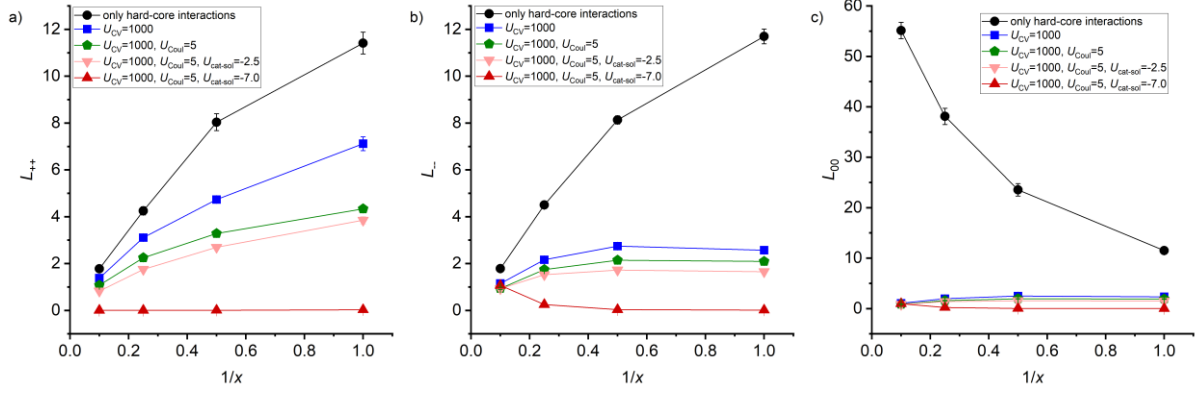
### Composition-dependent diffusion coefficients and correlation parameters for systems with $\frac{v_0}{v_-} = 1.05$



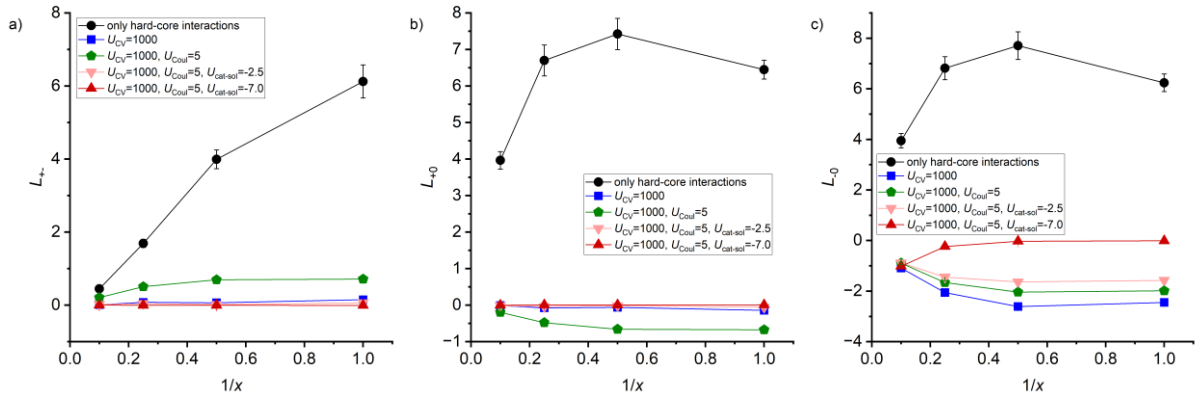
**Fig. S12:** Plots of the diffusion coefficients of  $D_{+}$ ,  $D_{-}$ , and  $D_0$  vs. the molar ratio  $1/x$  for different energy parameters.



**Fig. S13:** Plots of correlation parameters  $\alpha$ ,  $\beta$  and  $\gamma$  vs. the molar ratio  $1/x$  for different energy parameters.

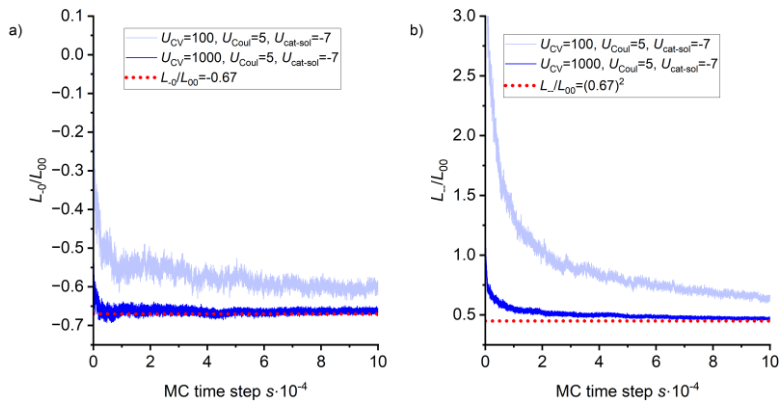


**Fig. S14:** Plots of the Onsager coefficients  $L_{++}$ ,  $L_{--}$ , and  $L_{00}$  vs. the molar ratio  $1/x$  for different energy parameters.



**Fig. S15:** Plots of the Onsager coefficients  $L_{+-}$ ,  $L_{+0}$ , and  $L_{-0}$  vs. the molar ratio  $1/x$  for different energy parameters.

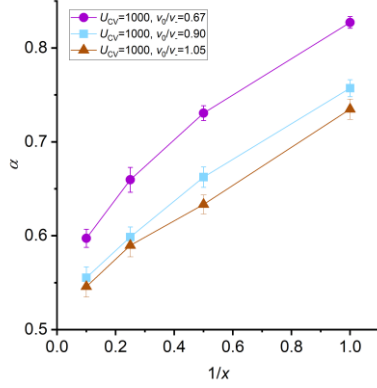
### Simulation results for different energy penalty parameter for center-of-volume shifts $U_{CV}$



**Fig. S16:** Time-dependent ratio of the Onsager coefficients (a)  $L_{-0}/L_{00}$  and (b)  $L_{--}/L_{00}$  for a system with a molar ratio of  $1/x = 0.5$  and with different values of  $U_{CV}$ . For comparison, theoretical results for strict volume conservation are shown as dotted lines. Volume conservation is considered as sufficiently strict, if the mean value of the ratios  $L_{-0}/L_{00}$  and (b)

$L_{--}/L_{00}$  deviate by less than 5% from the predictions of Eq. (17) and (18) over the last  $3 \cdot 10^4$  MC time steps of the equilibrium simulations.

### Influence of the volume ratio $v_0/v_-$ on the parameter $\alpha$



**Fig. S17:** Plot of the parameter  $\alpha$  vs. the molar ratio  $1/x$  for the systems with only volume conservation and different volume ratios  $v_0/v_-$ .

### Derivation of Eq. (20) for analyzing the relative contributions of anions and solvent molecules to volume conservation

The sum over all displacement vectors of the anions is given by:

$$\sum_i^{N_-} \Delta \vec{r}_i(t) \quad (\text{S1})$$

The sum over all displacement vectors of the solvent molecules is given by:

$$\sum_j^{x \cdot N_-} \Delta \vec{r}_j(t) \quad (\text{S2})$$

In the case of strict volume conservation, the following equation must hold:

$$\frac{v_-}{v_0} \cdot \sum_i^{N_-} \Delta \vec{r}_i(t) = - \sum_j^{x \cdot N_-} \Delta \vec{r}_j(t) \quad (\text{S3})$$

which can be rewritten as:

$$\frac{v_-}{v_0} \cdot \sum_i^{N_-} \Delta \vec{r}_i(t) + \sum_j^{x \cdot N_-} \Delta \vec{r}_j(t) = 0 \quad (\text{S4})$$

In Monte Carlo units, the displacement vectors of the species  $i$  and  $j$  are linked to the transport coefficients  $L_{ij}$  by:

$$L_{ij} = \lim_{t \rightarrow \infty} \frac{d}{dt} \left[ \left( \sum_i^{N_i} \Delta \vec{r}_i(t) \right) \left( \sum_j^{N_j} \Delta \vec{r}_j(t) \right) \right] \quad (\text{S5})$$

Squaring Eq. (S4) yields:

$$\left(\frac{v_-}{v_0}\right)^2 \cdot \left[ \left( \sum_i^{N_-} \Delta \vec{r}_i(t) \right)^2 \right] + \left[ \left( \sum_j^{x \cdot N_-} \Delta \vec{r}_j(t) \right)^2 \right] - 2 \cdot \frac{v_-}{v_0} \cdot \sum_i^{N_-} \Delta \vec{r}_i(t) \cdot \sum_j^{x \cdot N_-} \Delta \vec{r}_j(t) = 0 \quad (\text{S6})$$

Taking into account Eq. (S5) results in:

$$\left(\frac{v_-}{v_0}\right)^2 \cdot L_{--} + L_{00} + 2 \cdot \frac{v_-}{v_0} L_{-0} = 0 \quad (\text{S7})$$

$$\frac{v_-}{v_0} \cdot L_{--} + \frac{v_0}{v_-} L_{00} + 2 \cdot L_{-0} = 0 \quad (\text{S8})$$

Next the Onsager coefficients  $L_{--}$  and  $L_{00}$  are split into self and distinct parts:

$$\frac{v_-}{v_0} \cdot L_{--}^{\text{self}} + \frac{v_0}{v_-} L_{00}^{\text{self}} + \frac{v_-}{v_0} \cdot L_{--}^{\text{distinct}} + \frac{v_0}{v_-} L_{00}^{\text{distinct}} + 2 \cdot L_{-0} = 0 \quad (\text{S9})$$

and the equation is divided by  $\left(\frac{v_-}{v_0} \cdot L_{--}^{\text{self}} + \frac{v_0}{v_-} L_{00}^{\text{self}}\right)$ :

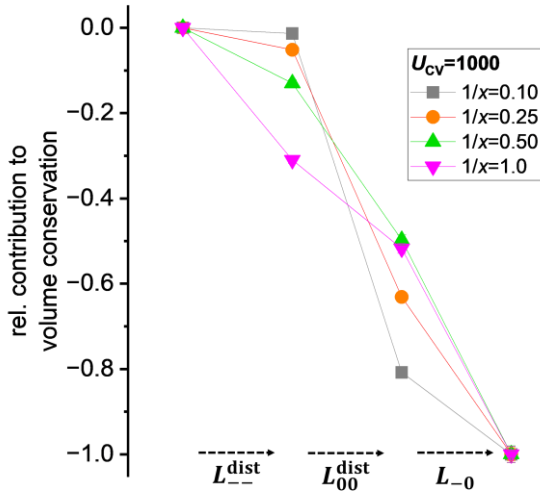
$$0 = \frac{\frac{v_-}{v_0} \cdot L_{--}^{\text{self}} + \frac{v_0}{v_-} L_{00}^{\text{self}}}{\frac{v_-}{v_0} \cdot L_{--}^{\text{self}} + \frac{v_0}{v_-} L_{00}^{\text{self}}} + \frac{\frac{v_-}{v_0} \cdot L_{--}^{\text{distinct}}}{\frac{v_-}{v_0} \cdot L_{--}^{\text{self}} + \frac{v_0}{v_-} L_{00}^{\text{self}}} + \frac{\frac{v_0}{v_-} L_{00}^{\text{distinct}}}{\frac{v_-}{v_0} \cdot L_{--}^{\text{self}} + \frac{v_0}{v_-} L_{00}^{\text{self}}} + \frac{2 \cdot L_{-0}}{\frac{v_-}{v_0} \cdot L_{--}^{\text{self}} + \frac{v_0}{v_-} L_{00}^{\text{self}}} \quad (\text{S10})$$

$$0 = 1 + \frac{L_{--}^{\text{distinct}}}{L_{--}^{\text{self}} + \left(\frac{v_0}{v_-}\right)^2 L_{00}^{\text{self}}} + \frac{\left(\frac{v_0}{v_-}\right)^2 L_{00}^{\text{distinct}}}{L_{--}^{\text{self}} + \left(\frac{v_0}{v_-}\right)^2 L_{00}^{\text{self}}} + \frac{2 \frac{v_0}{v_-} \cdot L_{-0}}{L_{--}^{\text{self}} + \left(\frac{v_0}{v_-}\right)^2 L_{00}^{\text{self}}} \quad (\text{S11})$$

Finally, we obtain:

$$-1 = \frac{L_{--}^{\text{distinct}}}{L_{--}^{\text{self}} + \left(\frac{v_0}{v_-}\right)^2 L_{00}^{\text{self}}} + \frac{\left(\frac{v_0}{v_-}\right)^2 L_{00}^{\text{distinct}}}{L_{--}^{\text{self}} + \left(\frac{v_0}{v_-}\right)^2 L_{00}^{\text{self}}} + \frac{2 \frac{v_0}{v_-} \cdot L_{-0}}{L_{--}^{\text{self}} + \left(\frac{v_0}{v_-}\right)^2 L_{00}^{\text{self}}} \quad (\text{20})$$

**Relative contributions to the volume conservation for systems with  $\frac{v_0}{v_-} = 0.9$**



**Fig. S18:** Relative contributions of  $L_{--}^{\text{dist}}$ ,  $L_{00}^{\text{dist}}$  and  $L_{-0}$  to volume conservation for different molar ratios  $1/x$  in systems with hard-core interactions between the particles and with strict volume conservation ( $U_{\text{CV}} = 1000$ ) at a volume ratio of  $v_0/v_- = 0.90$ .

### Derivation of Eq. (23) for the ratio $L_{\text{salt}} / L_{\text{ion}}$

The combination of equations (23) and (24) yields:

$$\frac{L_{\text{salt}}}{L_{\text{ion}}} = \frac{L_{++} \cdot L_{--} - L_{+-}^2}{(L_{++} + L_{--} - 2L_{+-})^2} \quad (\text{S12})$$

Dividing all Onsager coefficients in Eq. (S12) by  $(L_{++} + L_{--})$  and taking into account that

$$\alpha = \frac{L_{++}}{L_{++} + L_{--}} \quad (14)$$

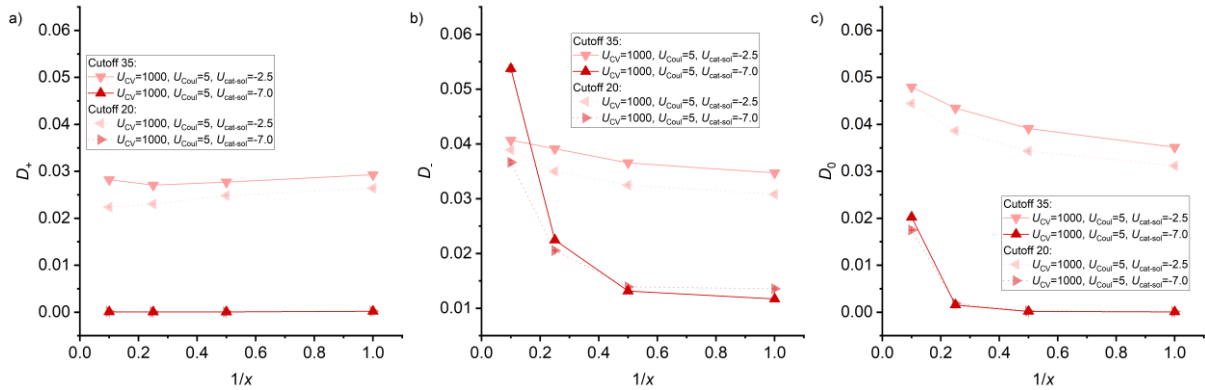
$$1 - \alpha = \frac{L_{--}}{L_{++} + L_{--}} \quad (\text{S13})$$

$$\beta = \frac{2 \cdot L_{+-}}{L_{++} + L_{--}} \quad (15)$$

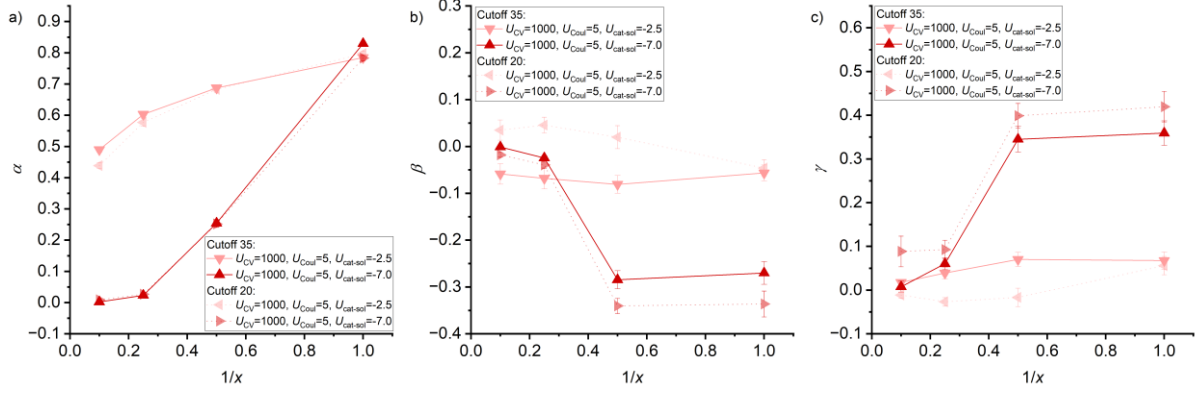
results in:

$$\frac{L_{\text{salt}}}{L_{\text{ion}}} = \frac{\alpha(1 - \alpha) - (0.5 \cdot \beta)^2}{(1 - \beta)^2} \quad (23)$$

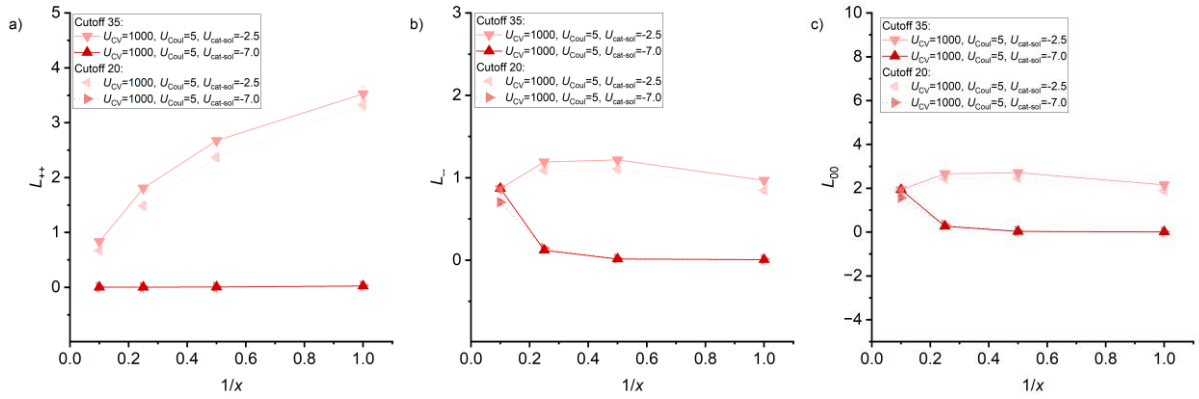
### Comparison of two different cutoffs for the attractive cation-solvent interaction for systems with $\frac{v_0}{v_-} = 0.67$



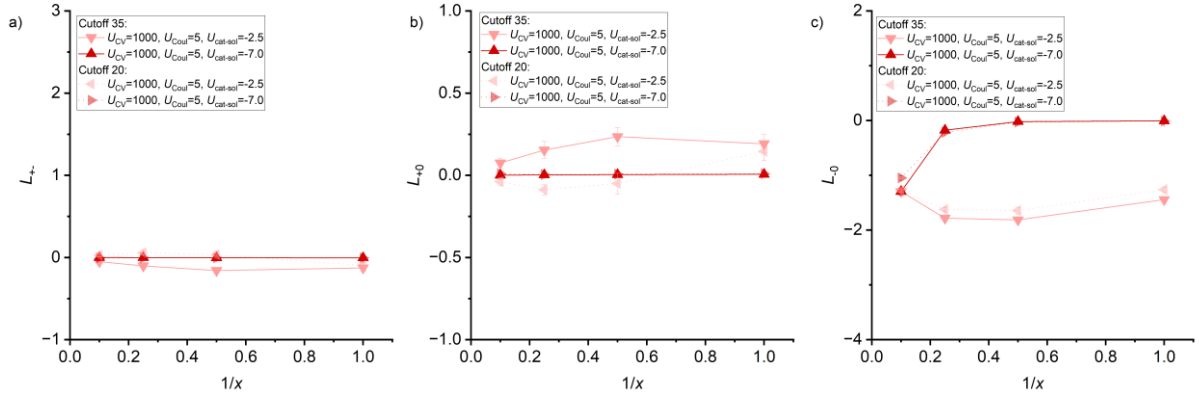
**Fig. S19:** Plots of the diffusion coefficients of  $D_+$ ,  $D_-$ , and  $D_0$  vs. the molar ratio  $1/x$  for different cutoffs for the attractive cation-solvent interaction.



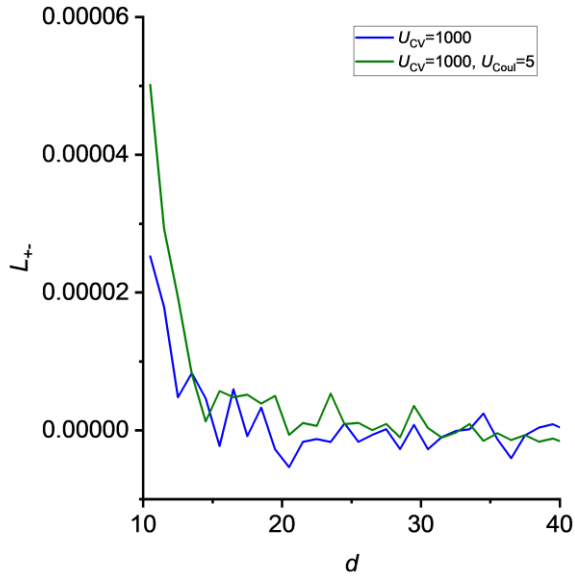
**Fig. S20:** Plots of correlation parameters  $\alpha$ ,  $\beta$  and  $\gamma$  vs. the molar ratio  $1/x$  for different cutoffs for the attractive cation-solvent interaction.



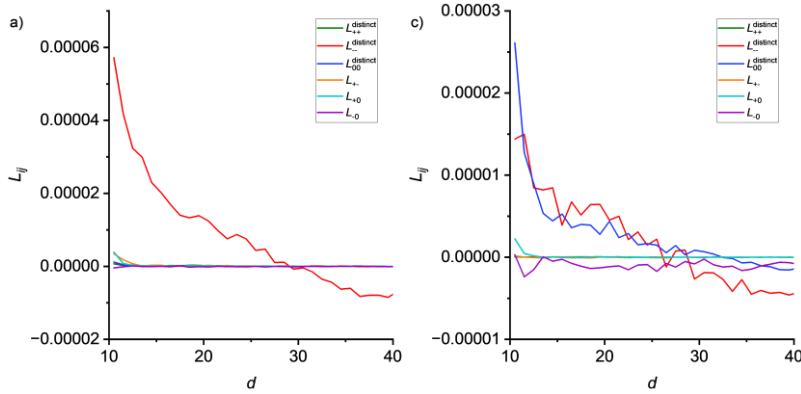
**Fig. S21:** Plots of the Onsager coefficients  $L_{++}$ ,  $L_{--}$ , and  $L_{00}$  vs. the molar ratio  $1/x$  for different cutoffs for the attractive cation-solvent interaction.



**Fig. S22:** Plots of the Onsager coefficients  $L_{+-}$ ,  $L_{+0}$ , and  $L_{-0}$  vs. the molar ratio  $1/x$  for different cutoffs for the attractive cation-solvent interaction.



**Fig. S23:** Dependence of the Onsager coefficient  $L_{+-}$  on the initial cation-anion distance  $d$  for two systems with a molar ratio of  $1/x = 1$ ,  $\frac{v_0}{v_-} = 0.67$  and with strict volume conservation ( $U_{CV} = 1000$ ). Coulomb interactions with  $U_{Coul} = 5$  lead to enhanced positive cation-anion correlations when the initial separation distance of cations and anion is small.



**Fig. S24:** Dependence of Onsager coefficients  $L_{++}^{\text{distinct}}$ ,  $L_{--}^{\text{distinct}}$ ,  $L_{00}^{\text{distinct}}$ ,  $L_{+-}$ ,  $L_{+0}$ , and  $L_{-0}$  on the initial distance between the respective particles,  $d$ , for systems with a molar ratio of a)  $1/x = 1$  and of b)  $1/x = 0.25$  and  $\frac{v_0}{v_-} = 0.67$  with hard-core interactions, volume conservation with  $U_{CV} = 1000$ , Coulomb interactions with  $U_{Coul} = 5$ , and cation-solvent interactions with  $U_{\text{cat-sol}} = -7$ .