

Electronic Supplementary Information

**Diffusion Mechanisms of Janus Nanoparticles in Cross-Linked
Polymer Networks**

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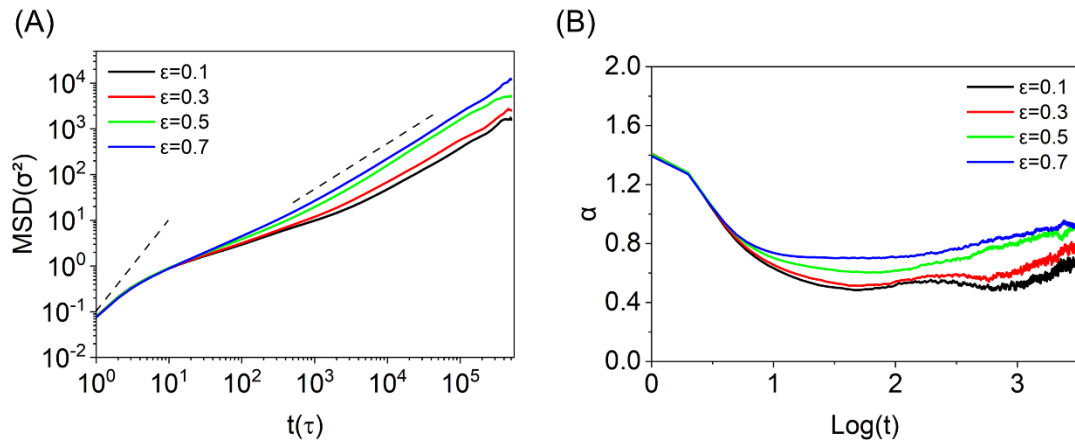


Fig. S1 Diffusion dynamics of JNPs with the adhesive component fixed at $\varepsilon=0.9k_B T$ and the non-adhesive side varied from 0.1 to $0.7k_B T$ in semi-flexible networks ($k_a = 25k_B T/\text{rad}^2$). (A) Mean square displacement (MSD); (B) anomalous diffusion exponent α corresponding to the MSD in (A).

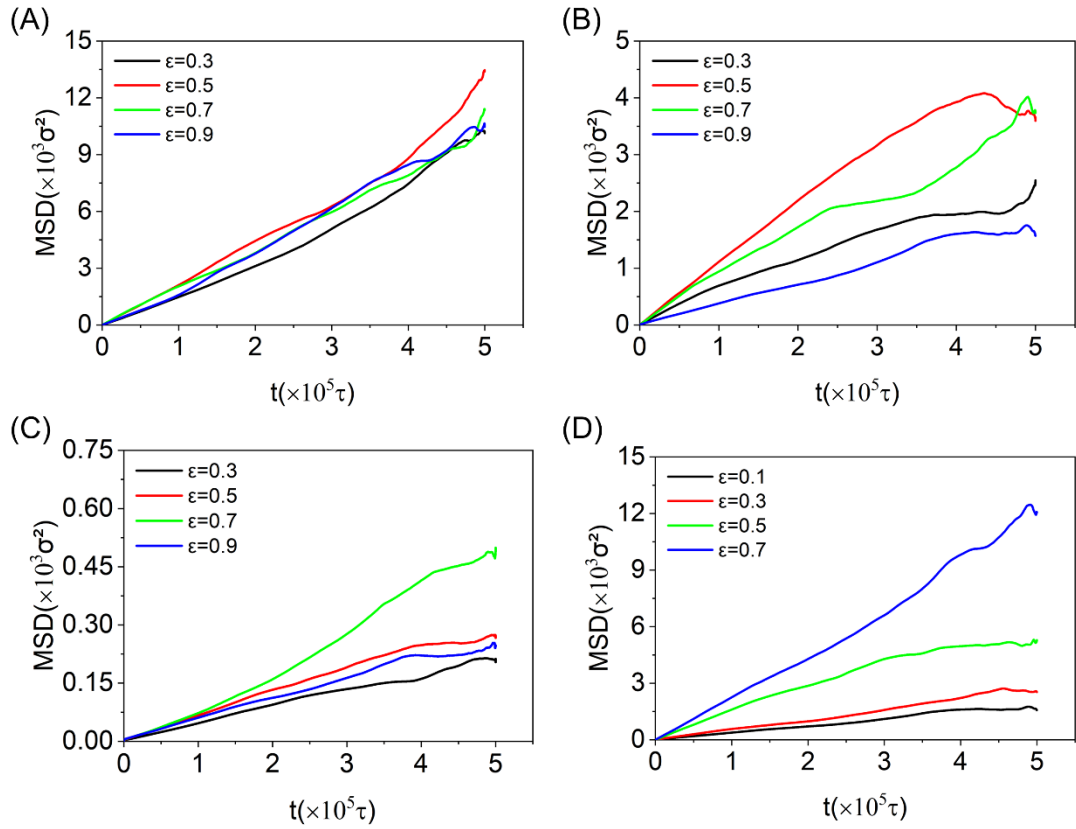


Fig. S2 Linear plots of the MSDs of the JNPs with varying interactions with cross-linked networks. (A-C) ϵ of non-adhesive component of JNP was fixed at $0.1 \text{ k}_B T$ in soft, semi-flexible and rigid networks ($k_a = 2.5, 25$ and $250 \text{ k}_B T / \text{rad}^2$, respectively); (D) ϵ of adhesive component of JNP was fixed at $0.9 \text{ k}_B T$ in semi-flexible network.

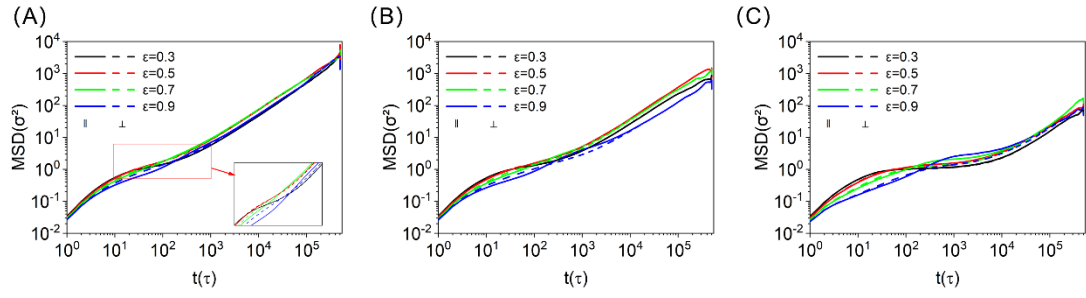


Fig. S3 MSD components of parallel and perpendicular to the major axes of JNPs with the non-adhesive component fixed at $\epsilon = 0.1k_B T$ in cross-linked networks of varying stiffness. (A) soft network ($k_a = 2.5k_B T/\text{rad}^2$), (B) semi-flexible network ($k_a = 25k_B T/\text{rad}^2$), (C) rigid network ($k_a = 250k_B T/\text{rad}^2$). The adhesive-side ϵ is varied from 0.3 to $0.9k_B T$.

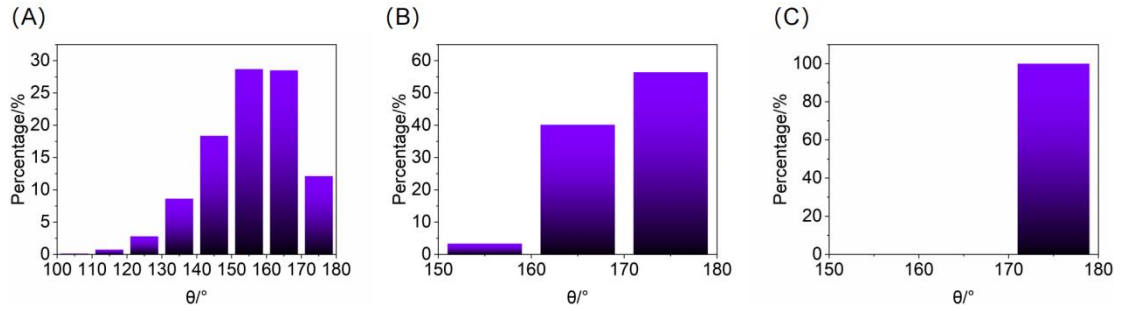


Fig. S4 Probability distribution of angles of every three consecutive CG beads in the network cell where the JNPs locate. (A) soft network ($k_a = 2.5k_B T/\text{rad}^2$), (B) semi-flexible network ($k_a = 25k_B T/\text{rad}^2$), (C) rigid network ($k_a = 250k_B T/\text{rad}^2$).

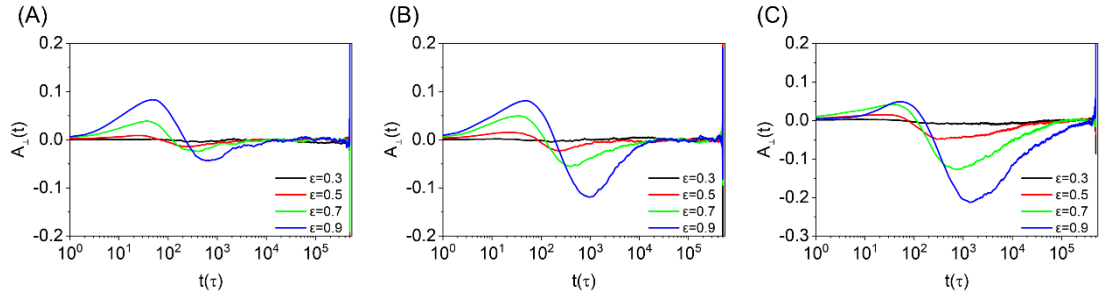


Fig. S5 Perpendicular anisotropic diffusion parameters $A_{\perp}(t)$ of JNPs with the non-adhesive component fixed at $\varepsilon = 0.1k_{\text{B}}T$ in cross-linked networks of varying stiffness. (A) soft network ($k_a = 2.5k_{\text{B}}T/\text{rad}^2$), (B) semi-flexible network ($k_a = 25k_{\text{B}}T/\text{rad}^2$), (C) rigid network ($k_a = 250k_{\text{B}}T/\text{rad}^2$). The adhesive-side ε is varied from 0.3 to $0.9k_{\text{B}}T$.

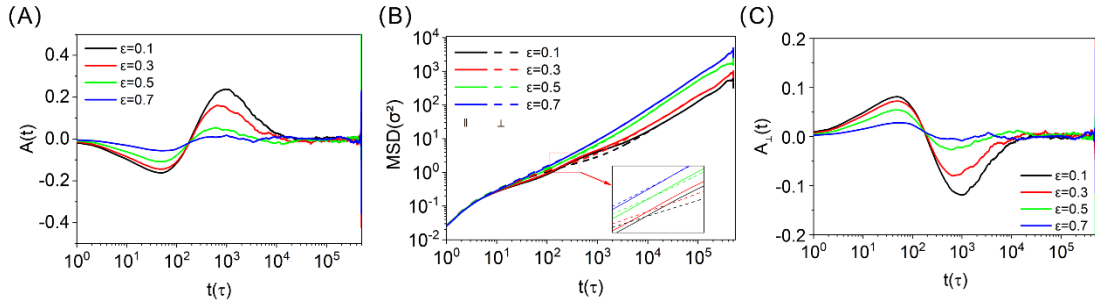


Fig. S6 Anisotropic dynamics of JNPs with the adhesive component fixed at $\varepsilon=0.9k_{\text{B}}T$ and the non-adhesive side varied from 0.1 to $0.7k_{\text{B}}T$ in semi-flexible networks ($k_a = 25k_{\text{B}}T/\text{rad}^2$). (A) Anisotropic parameter; (B) parallel and perpendicular MSDs; (C) perpendicular anisotropic parameter.

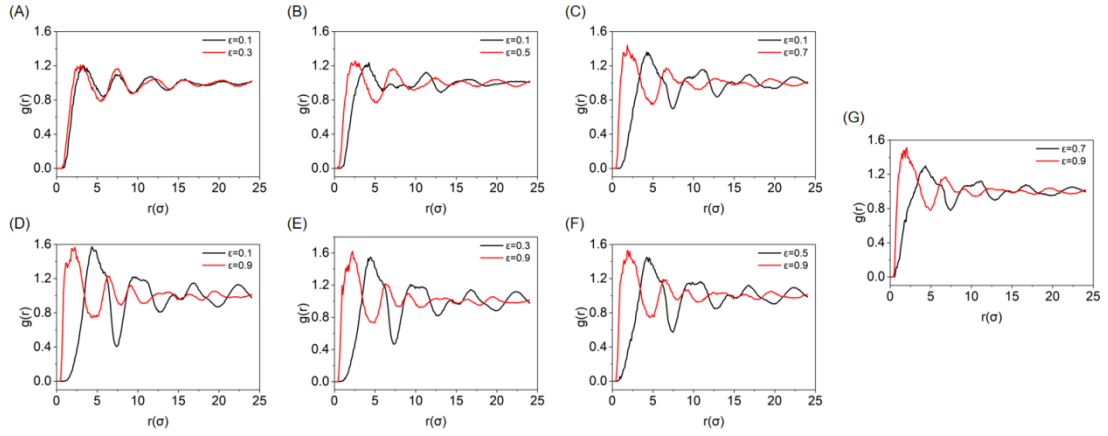


Fig. S7 Radial distribution function (RDF) plots of JNPs in cross-linked networks with $k_a = 25k_B T/\text{rad}^2$. (A) $\varepsilon = 0.1$ and $0.3k_B T$, (B) $\varepsilon = 0.1$ and $0.5k_B T$, (C) $\varepsilon = 0.1$ and $0.7k_B T$, (D) $\varepsilon = 0.1$ and $0.9k_B T$, (E) $\varepsilon = 0.3$ and $0.9k_B T$, (F) $\varepsilon = 0.5$ and $0.9k_B T$, (G) $\varepsilon = 0.7$ and $0.9k_B T$.

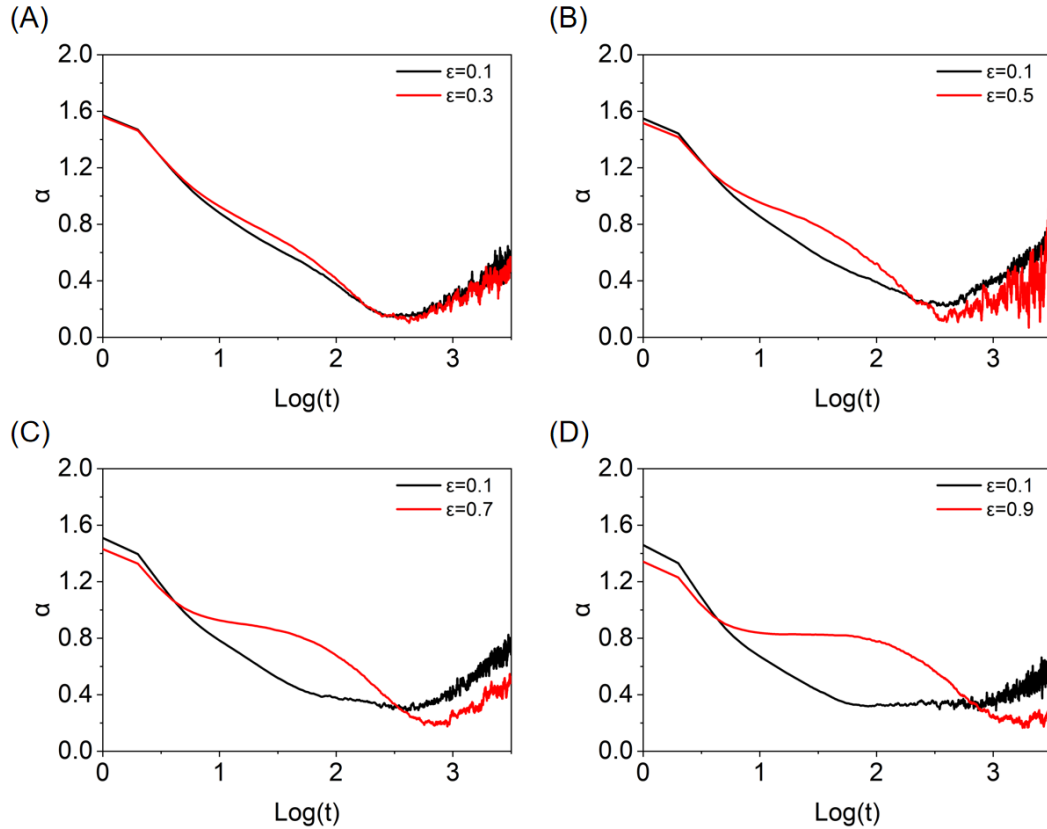


Fig. S8 Anomalous diffusion exponents α of the two vertices of JNPs in cross-linked networks with $k_a = 25k_B T/\text{rad}^2$. (A) $\varepsilon = 0.1$ and $0.3k_B T$, (B) $\varepsilon = 0.1$ and $0.5k_B T$, (C) $\varepsilon = 0.1$ and $0.7k_B T$, (D) $\varepsilon = 0.1$ and $0.9k_B T$.

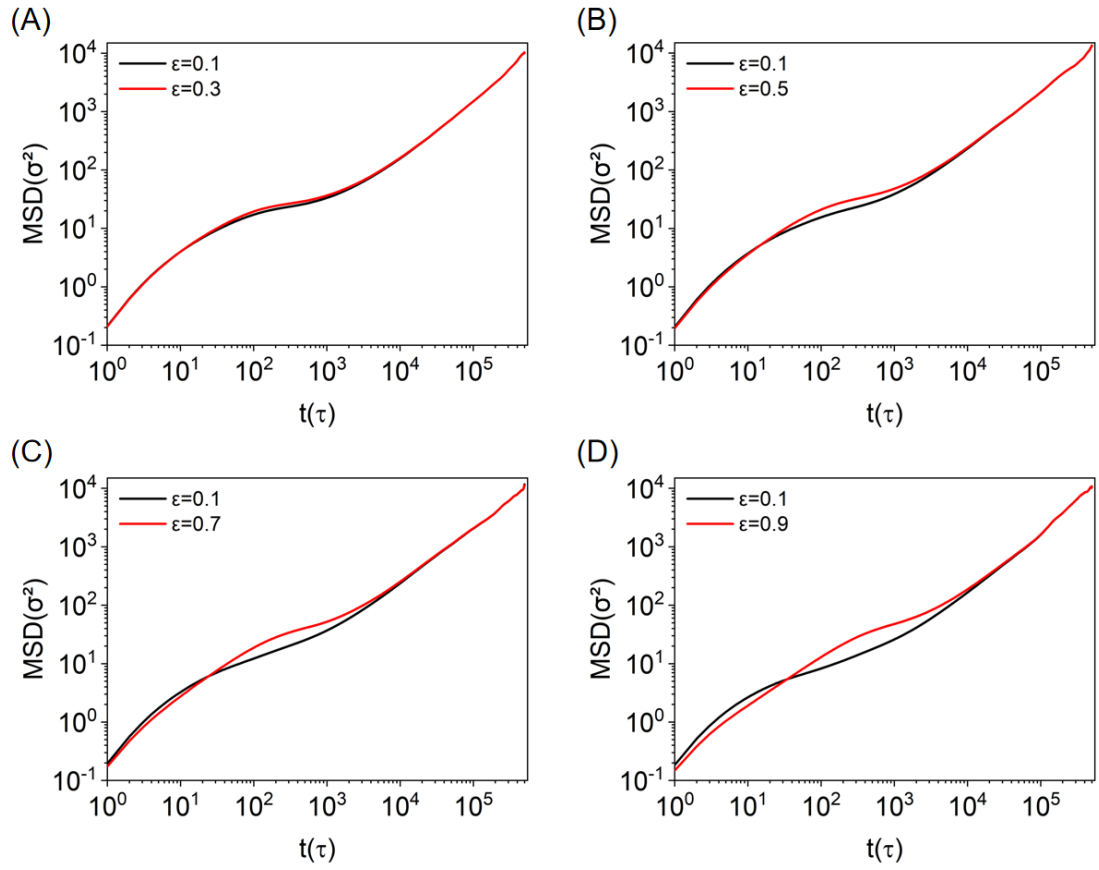


Fig. S9 MSDs of the two vertices of JNPs in cross-linked networks with $k_a = 2.5 k_B T / \text{rad}^2$. (A) $\varepsilon = 0.1$ and $0.3 k_B T$, (B) $\varepsilon = 0.1$ and $0.5 k_B T$, (C) $\varepsilon = 0.1$ and $0.7 k_B T$, (D) $\varepsilon = 0.1$ and $0.9 k_B T$.

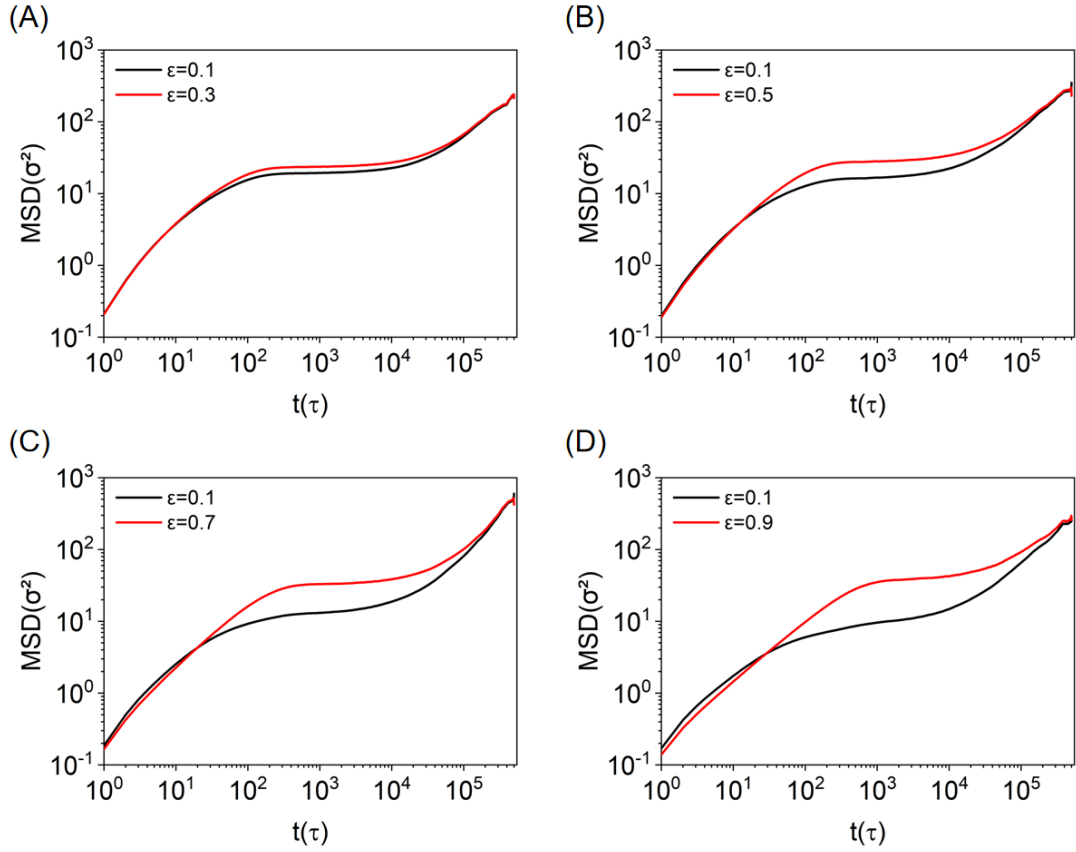


Fig. S10 MSDs of the two vertices of JNPs in cross-linked networks with $k_a = 250 k_B T / \text{rad}^2$. (A) $\varepsilon = 0.1$ and $0.3 k_B T$, (B) $\varepsilon = 0.1$ and $0.5 k_B T$, (C) $\varepsilon = 0.1$ and $0.7 k_B T$, (D) $\varepsilon = 0.1$ and $0.9 k_B T$.

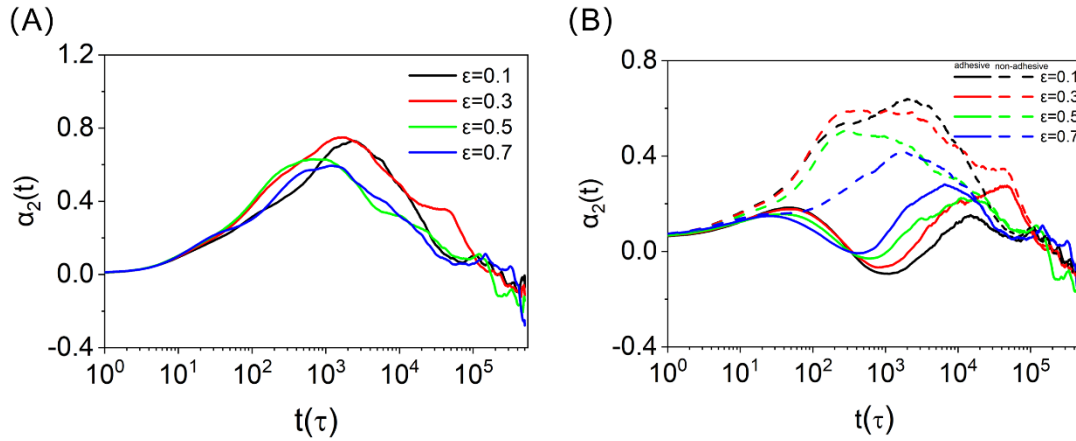


Fig. S11 Non-Gaussian parameters of JNPs with the adhesive component fixed at $\varepsilon = 0.9 k_B T$ and the non-adhesive side varied from 0.1 to $0.7 k_B T$ in semi-flexible networks ($k_a = 25 k_B T / \text{rad}^2$). (A) Results of JNP centers; (B) results of two vertices of JNPs.

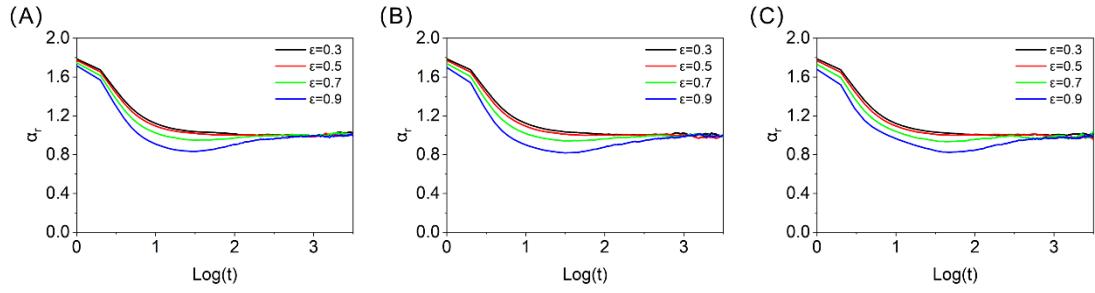


Fig. S12 Anomalous rotational diffusion exponents α_r of JNPs with the non-adhesive component fixed at $\varepsilon = 0.1k_B T$ in cross-linked networks of varying stiffness. (A) soft network ($k_a = 2.5k_B T/\text{rad}^2$), (B) semi-flexible network ($k_a = 25k_B T/\text{rad}^2$), (C) rigid network ($k_a = 250k_B T/\text{rad}^2$). The adhesive-side ε is varied from 0.3 to $0.9k_B T$.

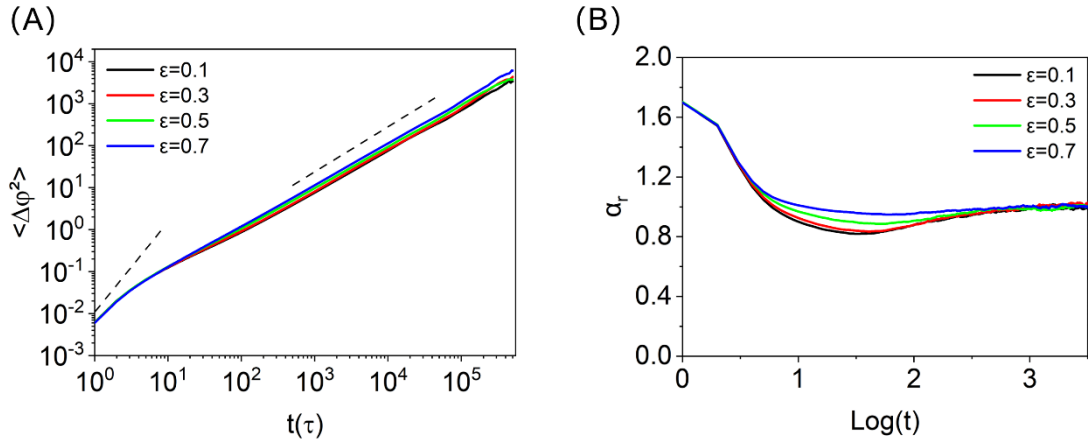


Fig. S13 Anomalous rotational diffusion exponents α_r of JNPs with the adhesive component fixed at $\varepsilon=0.9k_B T$ and the non-adhesive side varied from 0.1 to $0.7k_B T$ in semi-flexible networks ($k_a = 25k_B T/\text{rad}^2$). (A) Mean square angular displacement (MSAD); (B) anomalous rotational diffusion exponents α_r corresponding to the MSAD in (A).