

Supplementary Information for:

Surface curvature effects in neutral and protonated water clusters: insights from DFT and energy decomposition analysis†

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Voronoi Deformation Density (VDD) Charge Analysis for Complexes

The VDD method⁶² provides a way to assess how electron density is redistributed upon complex formation. In this context, the change in atomic charge (ΔQ_A) for a given atom A in fragment i is obtained by integrating the deformation density over the Voronoi cell of atom A. This deformation density is defined as the difference between the total electron density of the complex, $\rho(r)$, and the sum of the densities of the isolated fragments, $\sum_{fragment,i} \rho_i(r)$:

$$\Delta Q_A = - \int_{\text{Voronoi cell of A in the complex}} \left[\rho(r) - \sum_{fragment,i} \rho_i(r) \right]$$

This analysis shows how the interaction between fragments alters the local electron density around atom A. Summing ΔQ_A over all atoms in fragment i gives the total charge transfer associated with that fragment: a negative value ($\Delta Q_{fragment,i} < 0$) indicates net electron gain, while a positive value ($\Delta Q_{fragment,i} > 0$) indicates net electron loss due to complex formation.

$$\Delta Q_{fragment,i} = \sum_{A \text{ in fragment}} \Delta Q_A$$

Non-Covalent Interactions

Non-Covalent Interactions (NCI)^{S1} plots are based on the gradients of electron density are provided to identify and visualize weak interactions through color-coded isosurfaces.

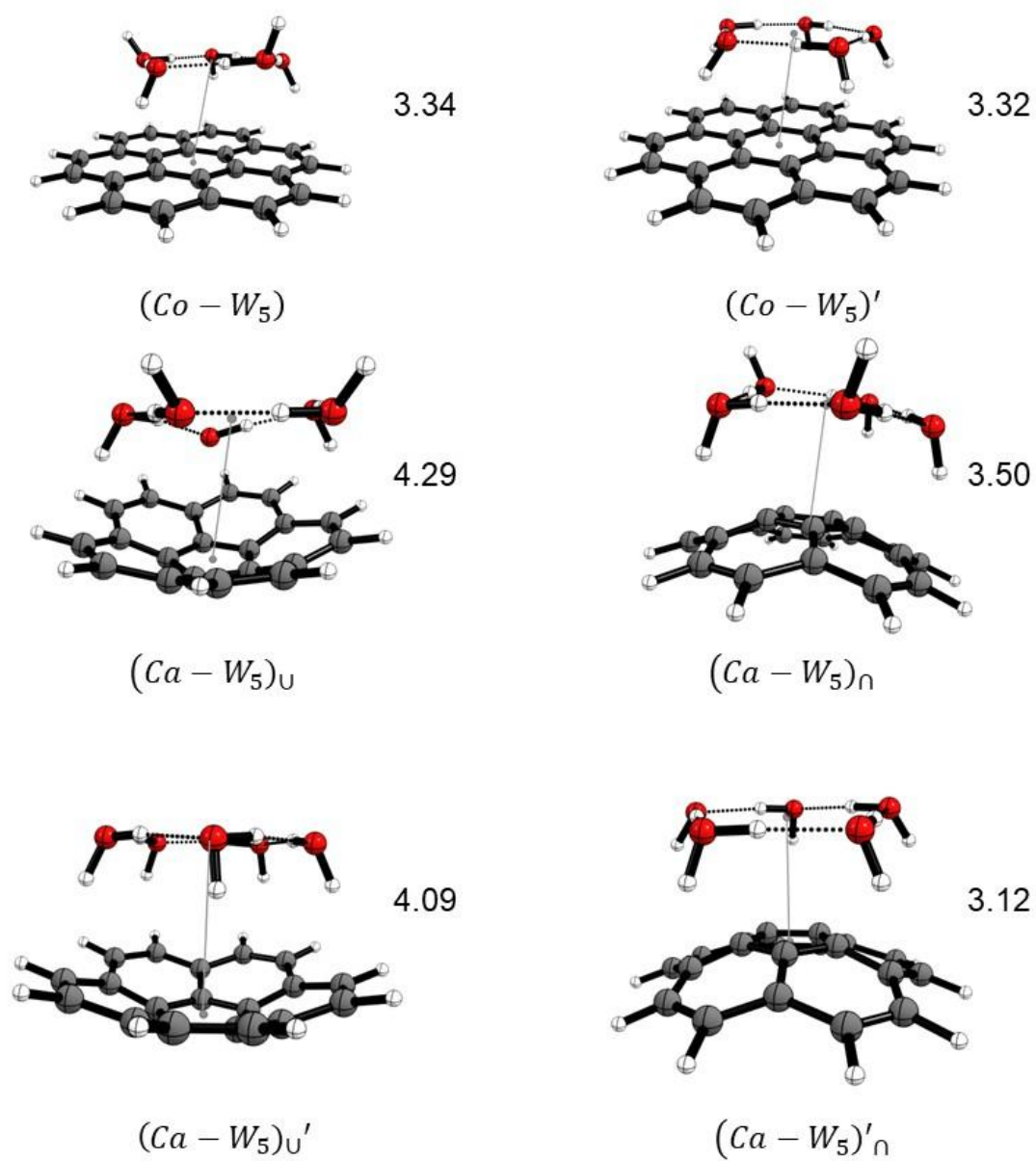


Figure S1. B3LYP-D3(BJ)/def2-TZVP optimized structures of the neutral water cluster–PAH complexes. Values in black are the intercluster distances ($Co/Ca \cdots W_5$) in Å.

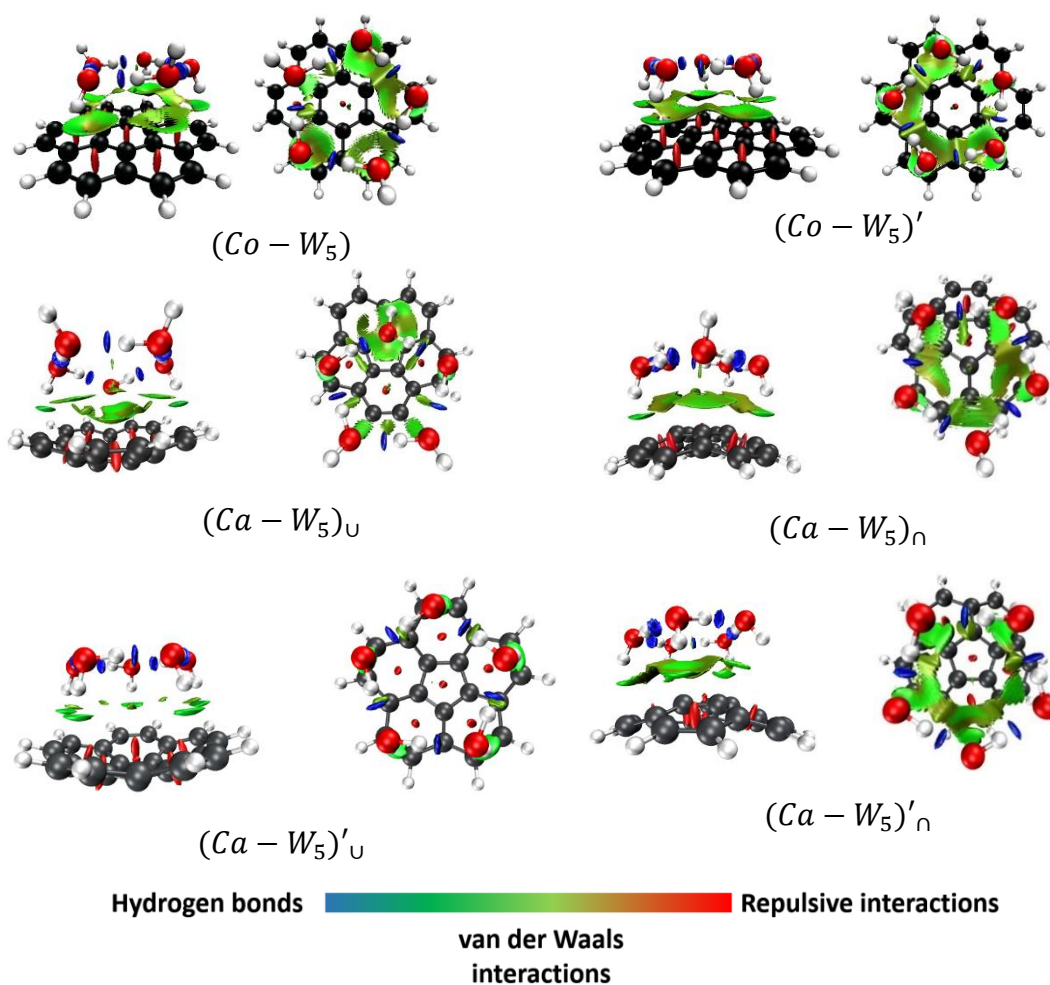


Figure S2. Optimized structures and NCI analysis for the neutral complexes involving water pentamers and corannulene. Blue, green, and red electron density regions denote conventional H-bonds, dispersion, and repulsive interactions, respectively (reduced densities isovalue contours value = 0.5). We display side view (left) and top view (right) of each complex for clarity.

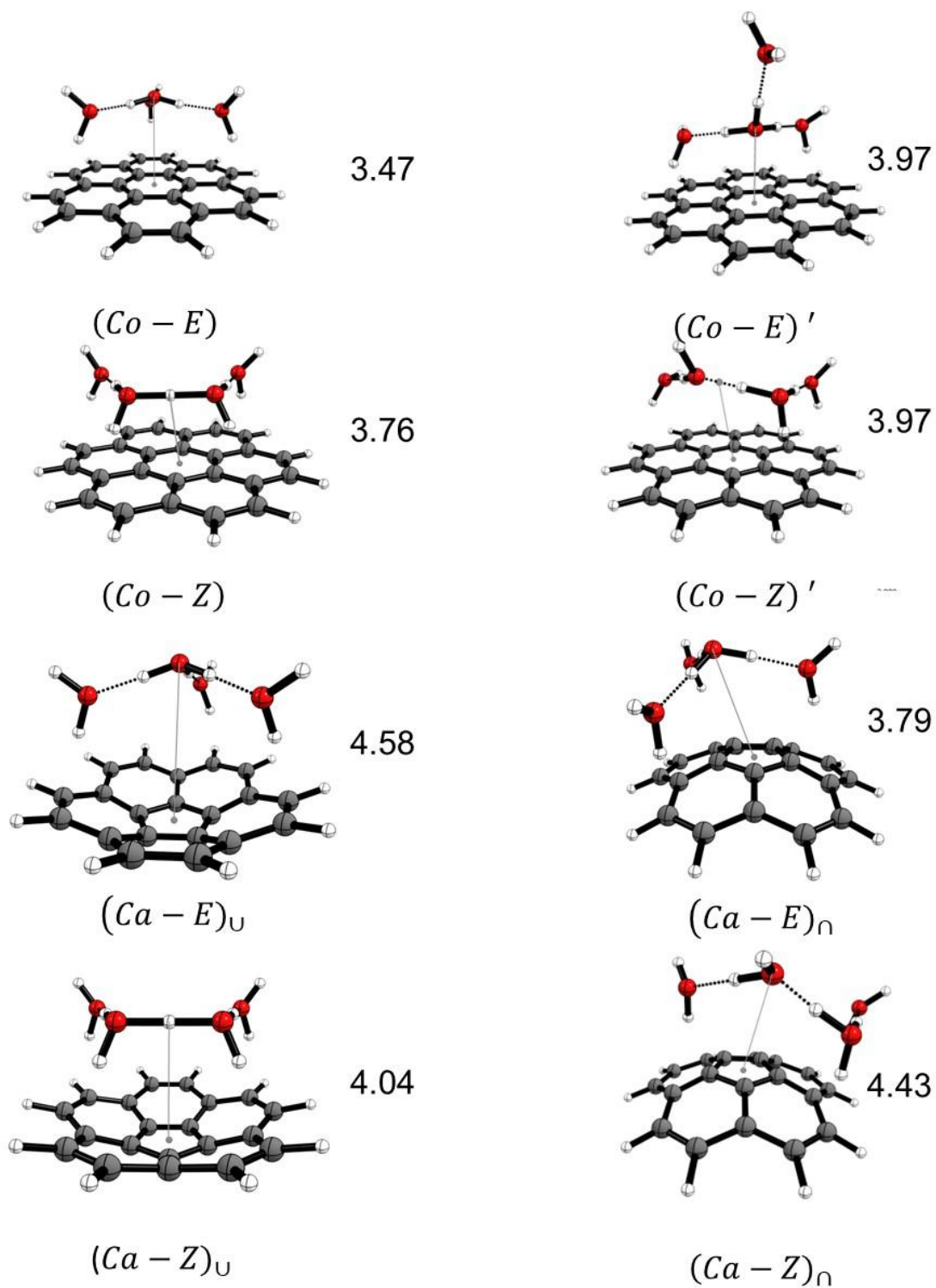


Figure S3. Some optimized structures of the cationic water cluster-PAH complexes with B3LYP-D3(BJ)/def2-TZVP. Values in black are the interclusters ($Co/Ca \cdots E/Z$) distances in Å.

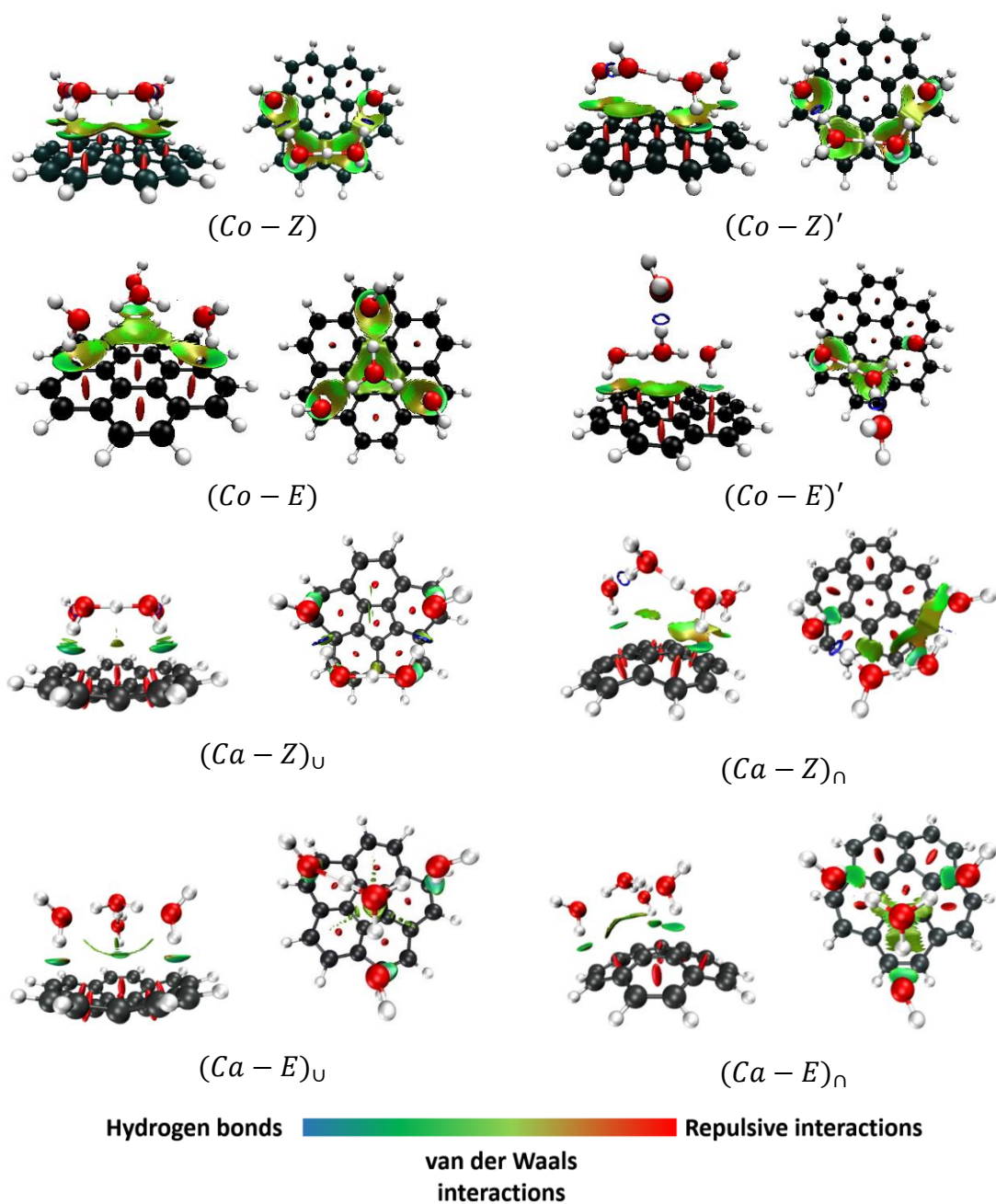


Figure S4. Some optimized structures with B3LYP-D3(BJ)/def2-TZVP and NCI analysis for the complexes involving Zundel and Eigen cations. Green and red electron density regions denote dispersion and repulsive interactions, respectively (reduced densities isovalue contours value = 0.5). We display side view (left) and top view (right) of each complex for clarity.

Table S1. Bond, interaction, and strain energies (in kcal mol⁻¹) of the neutral water cluster–PAH complexes calculated at M06-2X/TZ2P.^a

System	ΔE_{bond}^a	ΔE_{int}	ΔE_{strain}^b	ΔE_{strain}^{PAH}	$\Delta E_{strain}^{W_5}$
(Co – W ₅)	-10.6	-11.2	0.6	0.3	0.3
(Co – W ₅)'	-10.9	-14.5	3.6	0.3	3.3
(Ca – W ₅) _∪	-9.1	-11.5	2.5	0.4	2.1
(Ca – W ₅) _∩	-8.2	-8.9	0.7	0.3	0.4
(Ca – W ₅)' _∪	-6.5	-12.1	5.6	0.2	5.4
(Ca – W ₅)' _∩	-7.2	-11.5	4.3	0.6	3.7

$$^a \Delta E_{bond} = \Delta E_{strain} + \Delta E_{int} \quad ^b \Delta E_{strain} = \Delta E_{strain}^{PAH} + \Delta E_{strain}^{W_5}$$

Table S2. EDA components (in kcal mol⁻¹) for the neutral water cluster–PAH complexes calculated at M06-2X/TZ2P.^a

System	ΔE_{int}	ΔV_{elstat}	ΔE_{Pauli}	ΔE_{oi}
(Co – W ₅)	-11.2	-9.5	4.9	-6.5
(Co – W ₅)'	-14.5	-13.2	5.9	-7.3
(Ca – W ₅) _∪	-11.5	-11.6	6.3	-6.1
(Ca – W ₅) _∩	-8.9	-8.4	4.6	-5.1
(Ca – W ₅)' _∪	-12.1	-14.0	10.3	-8.4
(Ca – W ₅)' _∩	-11.5	-11.8	5.2	-5.0

$$^a \Delta E_{int} = \Delta V_{elstat} + \Delta E_{Pauli} + \Delta E_{oi}$$

Table S3. Bond, interaction, and strain energies (in kcal mol⁻¹) of the cationic water cluster–PAH complexes calculated at M06-2X/TZ2P.

System	ΔE_{bond}^a	ΔE_{int}	ΔE_{strain}^b	ΔE_{strain}^{PAH}	$\Delta E_{strain}^{Z/E}$
(Co – E)	-24.8	-25.8	1.0	0.1	0.9
(Co – Z)	-26.4	-29.4	2.9	0.2	2.7
(Ca – Z) _∪	-20.3	-24.9	4.6	0.8	3.8
(Ca – Z) _∩	-21.6	-23.9	2.3	0.1	2.2
(Ca – E) _∪	-17.1	-19.4	2.2	0.5	1.7
(Ca – E) _∩	-22.4	-24.3	2.0	0.2	1.8

$$^a \Delta E_{bond} = E_{PAH-Z/E} - E_{PAH} - E_{Z/E} \quad (\text{Note that the bonding energy of each cationic complex is computed with respect to the Eigen or Zundel cation}). \quad ^b \Delta E_{strain} = \Delta E_{strain}^{PAH} + \Delta E_{strain}^{Z/E}$$

Table S4. EDA components (in kcal mol⁻¹) for the neutral water cluster–PAH complexes calculated at M06-2X/TZ2P.^a

System	ΔE_{int}	ΔV_{elstat}	ΔE_{Pauli}	ΔE_{oi}
(Co – E)	-25.8	-17.5	9.1	-17.3
(Co – Z)	-29.4	-19.8	10.3	-19.8
(Ca – Z) _∪	-24.9	-19.2	15.4	-21.1
(Ca – Z) _∩	-23.9	-16.5	8.8	-16.2
(Ca – E) _∪	-19.4	-14.6	12.4	-17.1
(Ca – E) _∩	-24.3	-17.0	9.3	-16.6

^a $\Delta E_{\text{int}} = \Delta V_{\text{elstat}} + \Delta E_{\text{Pauli}} + \Delta E_{\text{oi}}$

Table S5. Calculated lower-frequency vibrational modes (in cm⁻¹) of the Eigen cation.

Mode	This work	MCTDH ^a	Expt. 1 ^b	Expt. 2 ^c
Global O ₄ pyramidalization	66.2	60	-	-
Water ligand wagging	242.9	240	-	236
O-O stretching	279.5	310	-	316
Water ligand rocking	343.8	370	-	-
Hydronium wagging	990.8	920	-	894
Hydronium umbrella	1165.9	970	-	1014
OH-bend water ligands	1637.4	1620	1615	1615
Hydronium O-H stretch	2974.0	2670	2653	-
Symmetric OH-stretch water ligands	3779.0	3670	3636	-
Asymmetric OH-stretch water ligands	3870.7	3800	3724	-

^a Simulations from ref. 72 in the main manuscript; ^b experimental data from supplementary ref. [2]; and ^c Experimental data from supplementary ref. [3]

Table S6. Calculated fundamentals (in cm^{-1}) of the Zundel/Eigen complexes with coronene and corannulene in comparison with the isolated cations. The shifts are given in parentheses.

Assignment	E	$(Co - E)$	$(Co - E')$
Hydronium umbrella	1166.0	1117.2 (-48.8)	1229.9 (63.9)
Hydronium + 2H ₂ O bending	1623.1	1606.5 (-16.6)	1612.1 (-11.0)
Hydronium + 2H ₂ O bending	1623.3	1606.9 (-16.4)	1616.3 (-7.0)
Water ligand O-H bending	1637.4	1627.2 (-10.2)	1631.8 (-5.6)
Hydronium bending	1687.5	1687.6 (0.1)	1707.0 (19.5)
Hydronium bending	1688.0	1688.8 (0.8)	1741.3 (53.3)
Hydronium asym. O-H stretching	2839.4	2759.9 (-79.5)	2551.4 (-288.0)
Hydronium asym. O-H stretching	2839.7	2764.1 (-75.6)	2747.3 (-92.4)
Hydronium sym. O-H stretching	2974.0	2918.7 (-55.3)	3082.0 (108.0)
Assignment	E	$(Ca - E)_U$	$(Ca - E)_N$
Hydronium umbrella	1166.0	1297.9 (+131.9)	1284.0 (+118.0)
Hydronium + 2H ₂ O bending	1623.1	1610.6 (-12.7)	1594.3 (-28.8)
Hydronium + 2H ₂ O bending	1623.3	1623.3 (0.0)	1618.7 (-4.6)
Water ligand O-H bending	1637.4	1620.0 (-1.5)	1603.2 (-34.2)
Hydronium bending	1687.5	1680.1 (-7.4)	1706.8 (+19.3)
Hydronium bending	1688.0	1716.3 (+28.3)	1712.9 (+24.9)
Hydronium asym. O-H stretching	2839.4	2710.1 (-129.3)	2728.3 (-111.1)
Hydronium asym. O-H stretching	2839.7	2743.3 (-96.4)	2780.7 (-59.4)
Hydronium sym. O-H stretching	2974.0	2933.1 (-40.9)	2952.2 (-18.8)
Assignment	Z	$(Co - Z)$	$(Co - Z')$
H ₂ O...H ⁺ ...OH ₂ bending	908.4	942.1 (33.7)	948.3 (39.9)
H ₂ O...H ⁺ ...OH ₂ bending	999.6	-	-
H ₂ O...H ⁺ ...OH ₂ bending	1058.5	1073.3 (14.8)	1030.7 (-27.8)
H ₂ O...H ⁺ ...OH ₂ bending	1416.0	1287.0 (-129.0)	1388.3 (-27.7)
H ₂ O...H ⁺ ...OH ₂ bending	1581.9	-	1613.3 (31.4)
Water ligand bending	1633.0	1611.6 (-21.4)	1627.1 (-5.9)
Water ligand bending	1636.5	1626.7 (-9.8)	1634.9 (-1.6)
Shared-proton + 2H ₂ O bending	1697.8	1685.8 (-12.0)	1722.7 (24.9)
Shared-proton + 2H ₂ O bending	1747.3	1715.1 (-32.2)	1865.9 (118.6)
H-bonded sym. O-H stretching	2992.5	3002.0 (9.5)	2782.8 (-209.7)
H-bonded asym. O-H stretching	3033.3	3039.7 (6.4)	3137.7 (104.4)
Assignment	Z	$(Ca - Z)_U$	$(Ca - Z)_N$
H ₂ O...H ⁺ ...OH ₂ bending	908.4	928.8	950.0*
H ₂ O...H ⁺ ...OH ₂ bending	999.6	-	950.4
H ₂ O...H ⁺ ...OH ₂ bending	1058.5	-	1010.9
H ₂ O...H ⁺ ...OH ₂ stretching	-	939.2	-
H ₂ O...H ⁺ ...OH ₂ stretching	-	1072.9	-
H ₂ O...H ⁺ ...OH ₂ bending	1416.0	1302.4	1402.8
H ₂ O...H ⁺ ...OH ₂ bending	1581.9	-	1448.5
Water ligand bending	1633.0	1613.6	1611.5
Water ligand bending	1636.5	1613.6	1619.8
Shared-proton + 2H ₂ O bending	1697.8	1694.5 (-3.3)	1708.3 (+10.5)
Shared-proton + 2H ₂ O bending	1747.3	1714.0 (-33.3)	1792.3 (+45.0)
H ₂ O...H ⁺ ...OH ₂ bending	-	1804.2	-
H-bonded sym. O-H stretching	2992.5	3043.3 (+50.8)	3097.8 (+105.3)
H-bonded asym. O-H stretching	3033.3	3012.7 (-20.6)	2873.6 (-159.7)

* Resonance with torsional motion of corannulene.

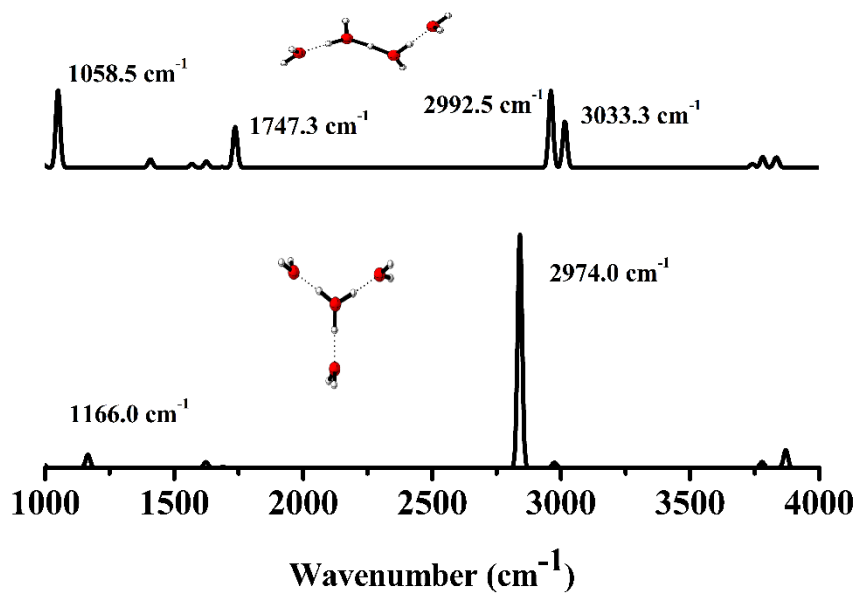


Figure S5. Calculated IR spectra of the isolated Zundel (top) and Eigen cations (bottom).

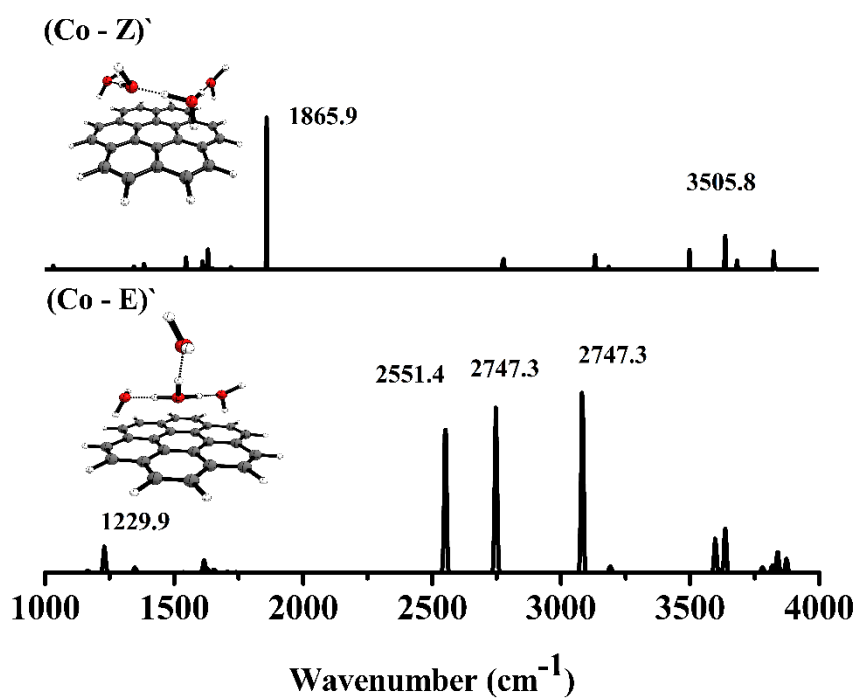


Figure S6. Calculated IR spectra of the $(Co - Z)'$ (top) and $(Co - E)'$ cations (bottom).

Supplementary references

S1. E. R. Johnson, S. Keinan, P. Mori-Sánchez, J. Contreras-García, A. J. Cohen and W. Yang, *J. Am. Chem. Soc.*, **2010**, *132*, 6498–6506.

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