

Electronic Supplementary Information

Data-driven exploration of  $AB_2X_4$  ( $X=O, S, Se, Te$ ) spinel chemical space

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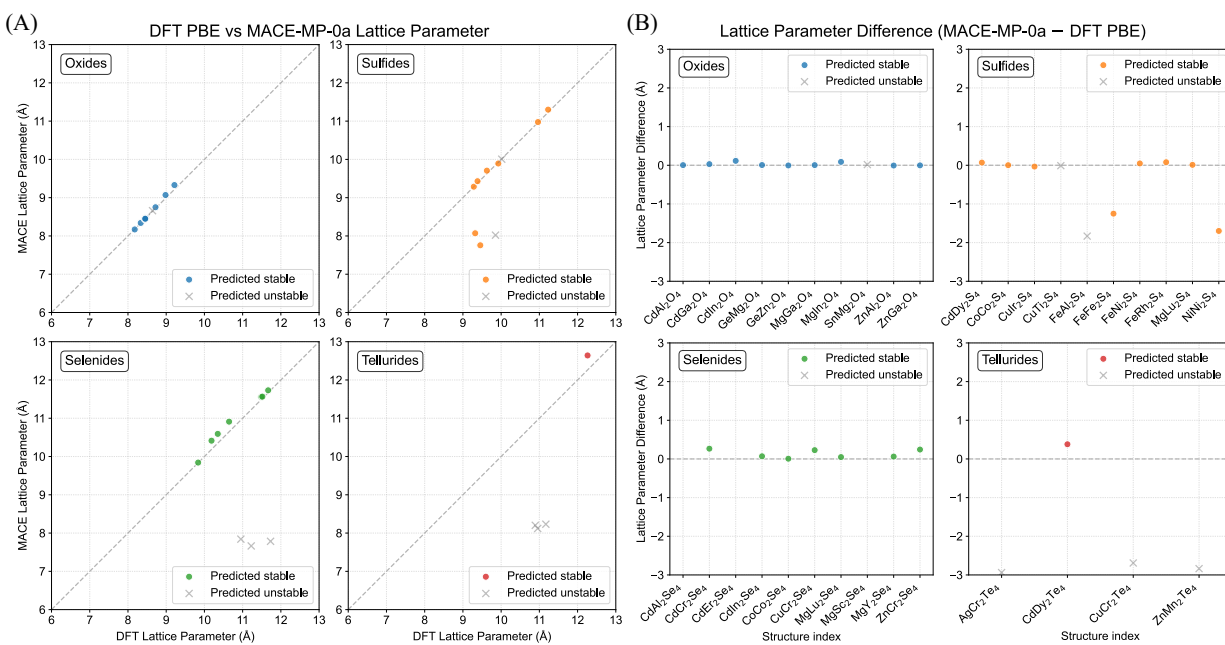


Fig. S1 (A) Parity and (B) difference plots of DFT and MACE-MP-0a calculated lattice parameters of experimentally known oxide and chalcogenide spinels. Predicted stable compositions are shown in colored while predicted unstable ones are shown in grey crossed symbol.

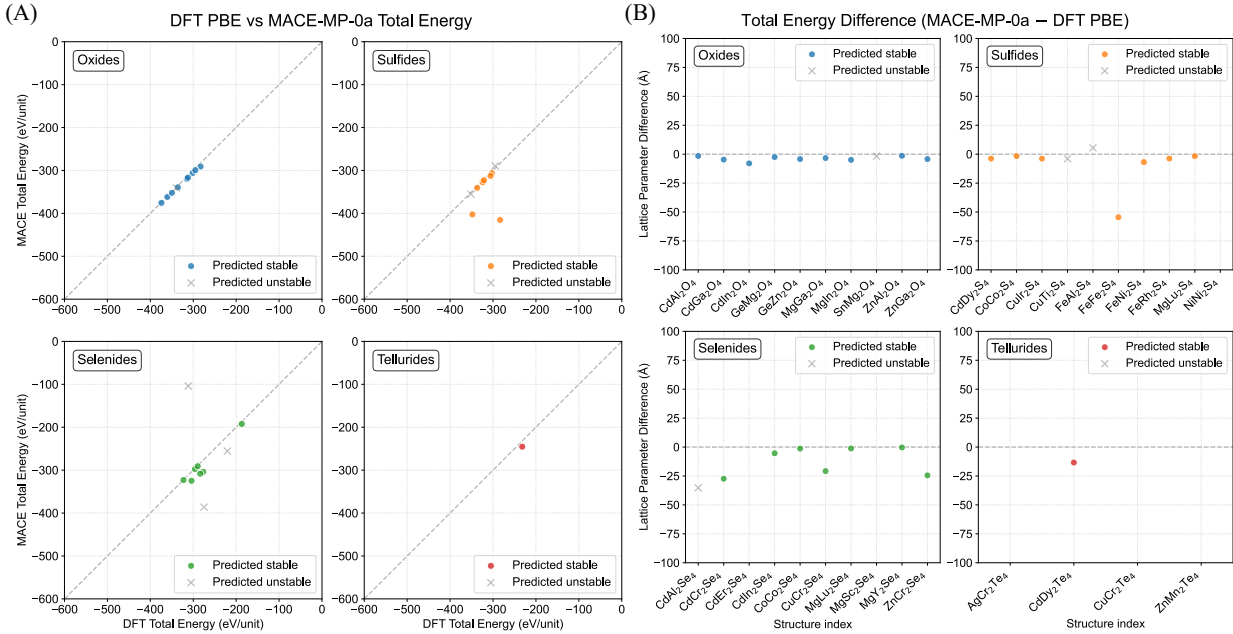


Fig. S2 (A) Parity and (B) difference plots of DFT and MACE-MP-0a calculated total energies per unit of experimentally known oxide and chalcogenide spinels.

To compare results from MACE-MP-0a against Density Functional Theory (DFT)<sup>1,2</sup> first-principles calculations using DFT framework were employed with Generalized Gradient Approximation (GGA) by Perdew-Berke-Ernzerhof (PBE)<sup>3</sup>. The Projector Augmented Wave (PAW)<sup>4,5</sup> pseudopotentials as defined within Vienna Ab initio Simulation Package (VASP)<sup>6,7</sup> were used to describe the interactions between ion cores and valence electrons. An energy cutoff of 520 eV was selected to optimise the structures until the force on each atom is less than 0.01 eV/Å and the energy convergence reaches  $10^{-6}$  eV with Gamma  $4 \times 4 \times 4$   $k$ -point for all systems alongside Gaussian smearing with a width of 0.05 eV. For MACE<sup>8-10</sup> calculations, the settings are mentioned in the main manuscript. The results are shown in Fig. S1 and Fig. S2.

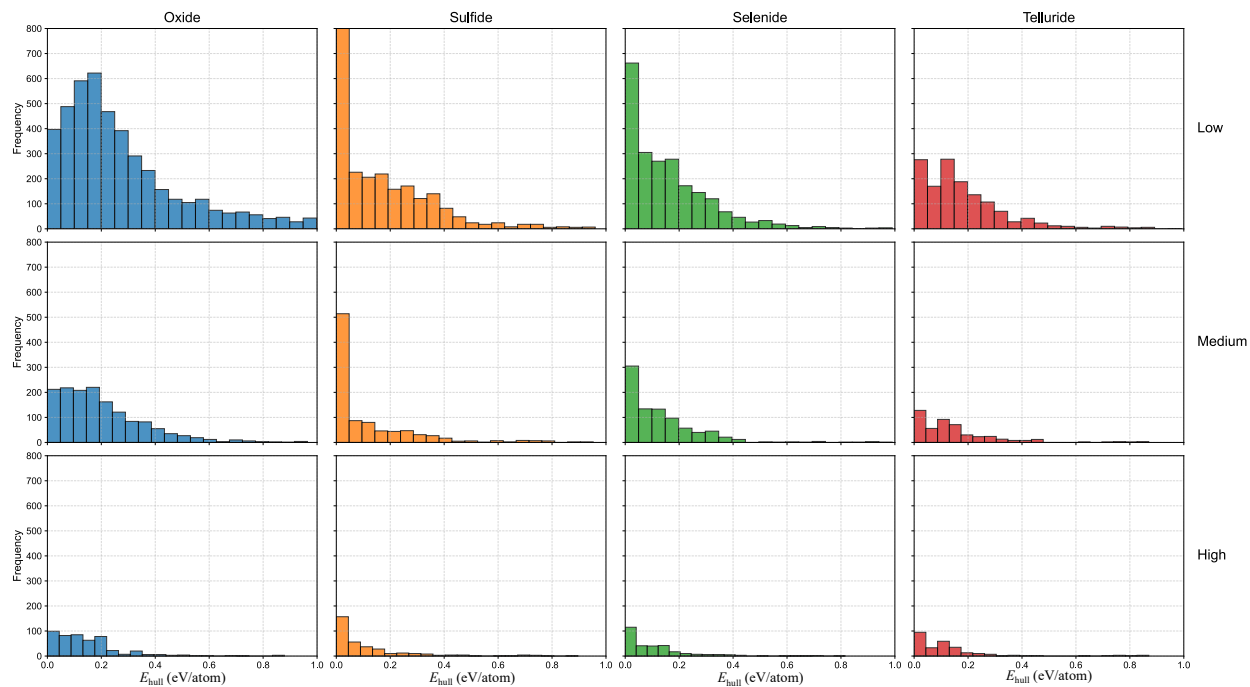


Fig. S3  $E_{\text{hull}}$  distribution for four types of anions with different oxidation state thresholds

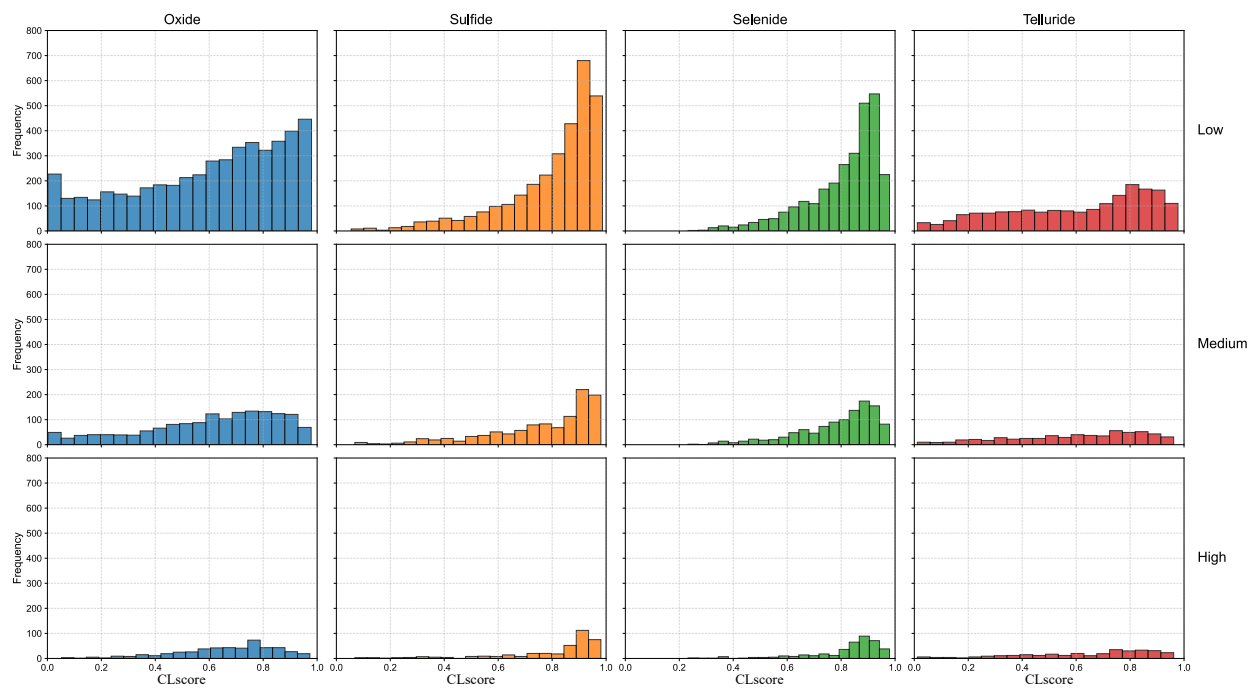


Fig. S4 CLscore distribution for four types of anions with different oxidation state thresholds

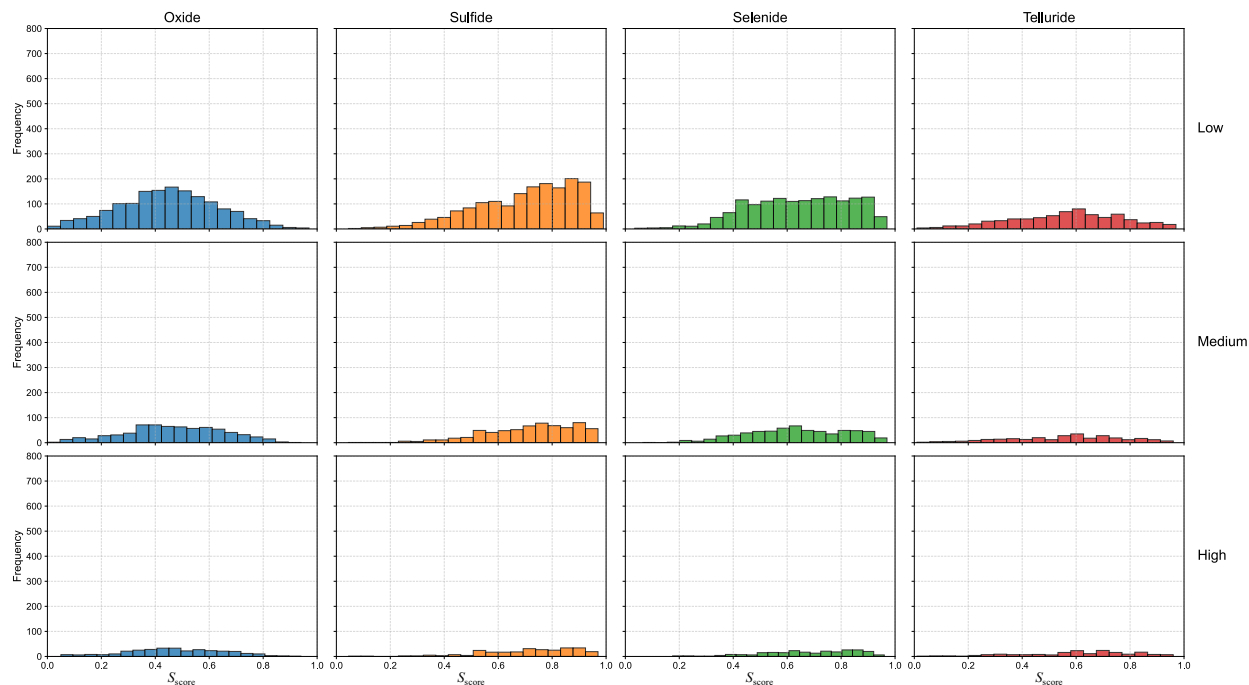


Fig. S5  $S_{\text{score}}$  distribution for four types of anions with different oxidation state thresholds

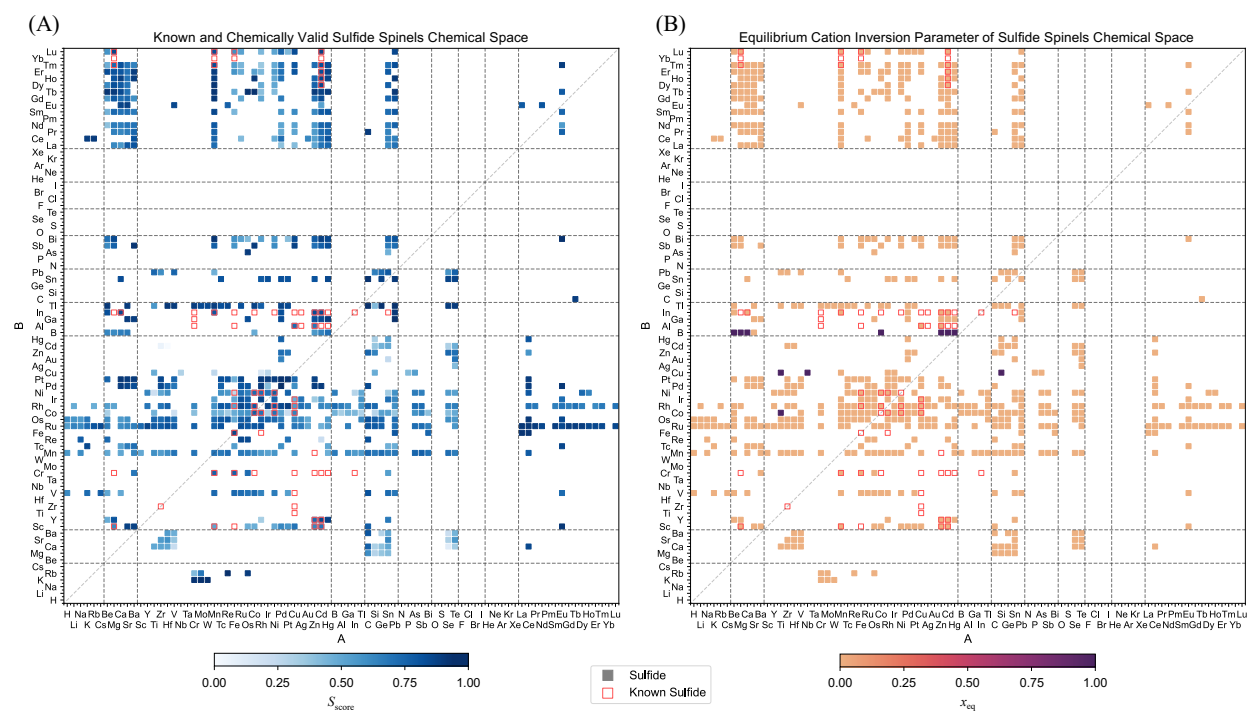


Fig. S6 Chemical space of sulfide spinels that satisfy both  $E_{\text{hull}} \leq 0.2$  eV/atom AND  $\text{CLscore} \geq 0.5$ . (A) The blue gradient indicates  $S_{\text{score}}$ , where lighter and darker shades designate lower and higher crystal likelihood, respectively. (B) The colourmap represents the equilibrium cation inversion

parameter  $x_{eq}$ , where lighter orange designates the normal configuration, and darker purple represents the inverse configuration. The red square markers denote the experimentally known spinel compositions.

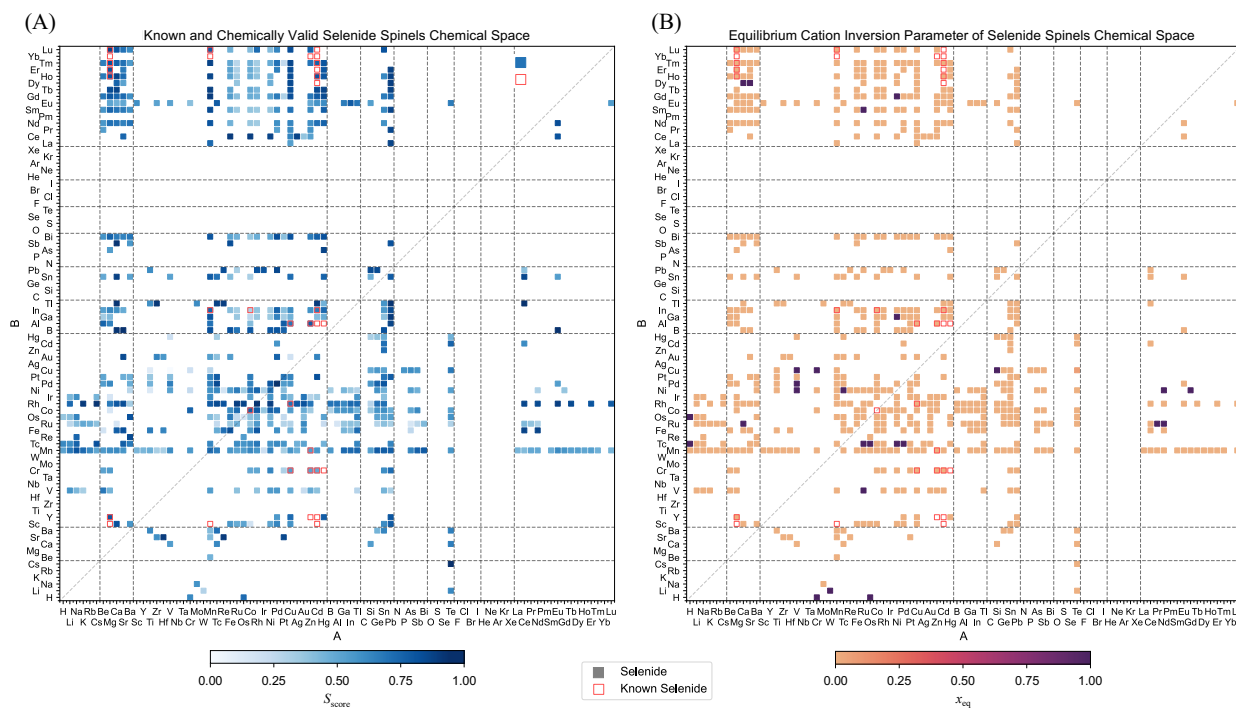


Fig. S7 Chemical space of selenide spinels that satisfy both  $E_{hull} \leq 0.2$  eV/atom AND  $CLscore \geq 0.5$ . (A) The blue gradient indicates  $S_{score}$ , where lighter and darker shades designate lower and higher crystal likelihood, respectively. (B) The colourmap represents the equilibrium cation inversion parameter  $x_{eq}$ , where lighter orange designates the normal configuration, and darker purple represents the inverse configuration. The red square markers denote the experimentally known spinel compositions.

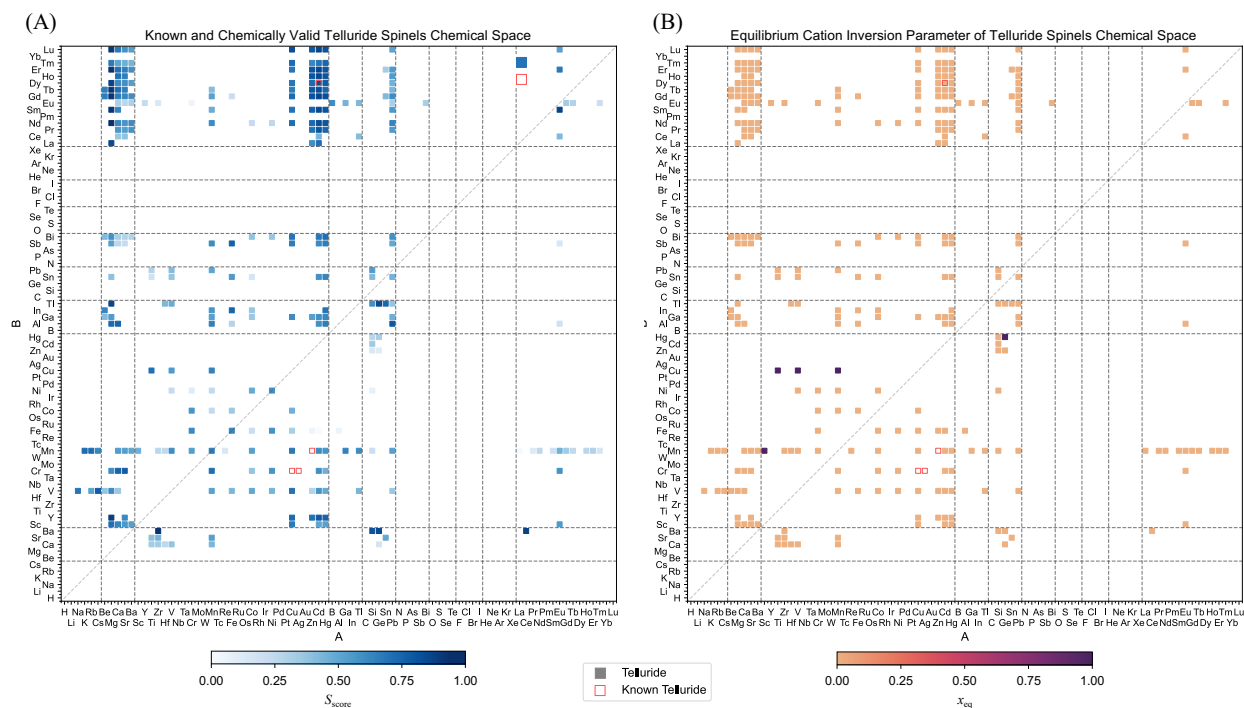


Fig. S8 Chemical space of telluride spinels that satisfy both  $E_{\text{hull}} \leq 0.2$  eV/atom AND  $\text{CLscore} \geq 0.5$ . (A) The blue gradient indicates  $S_{\text{score}}$ , where lighter and darker shades designate lower and higher crystal likelihood, respectively. (B) The colourmap represents the equilibrium cation inversion parameter  $x_{\text{eq}}$ , where lighter orange designates the normal configuration, and darker purple represents the inverse configuration. The red square markers denote the experimentally known spinel compositions.

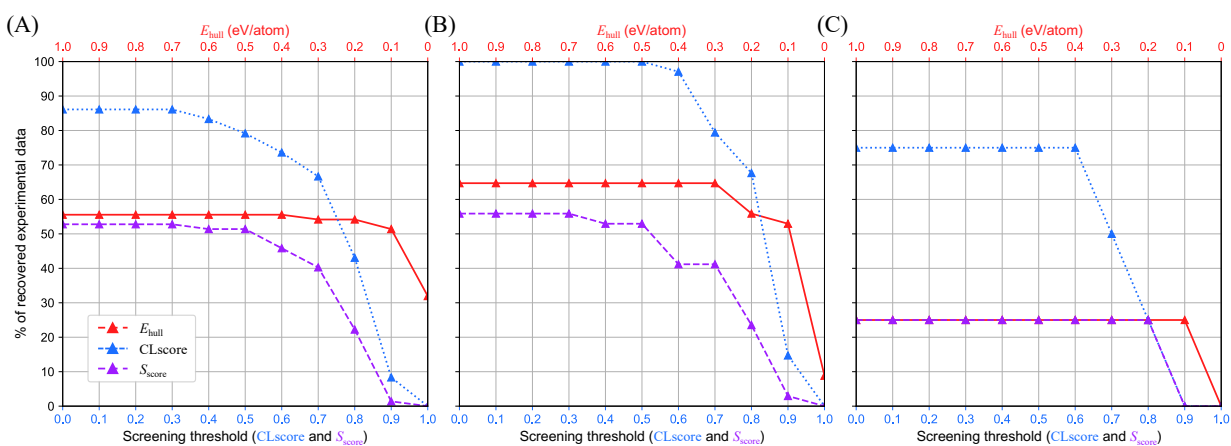


Fig. S9 Fraction of recovered experimental known (A) sulfide, (B) selenide, and (C) telluride spinels with medium oxidation state threshold for the initial chemical filter.

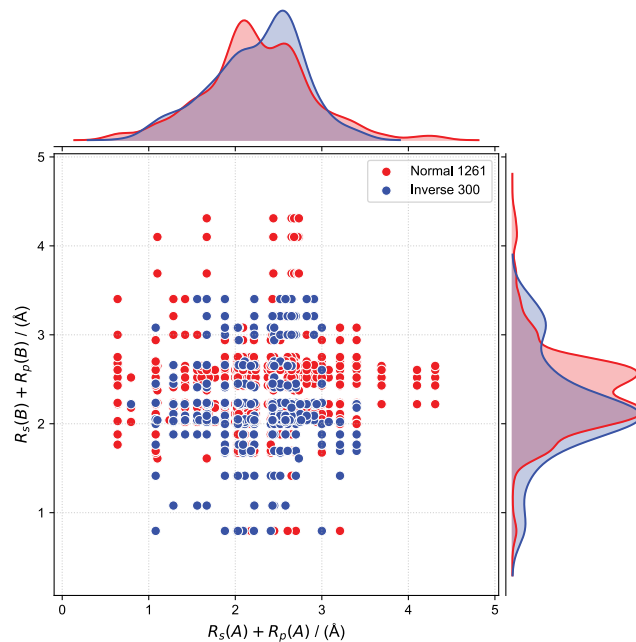


Fig. S10 Orbital-radii separation map of  $AB_2X_4$  spinels ( $X=O, S, Se, Te$ ) with preferred normal and inverse configurations, determined by  $E_{\text{hull}}$ , in red and blue, respectively.

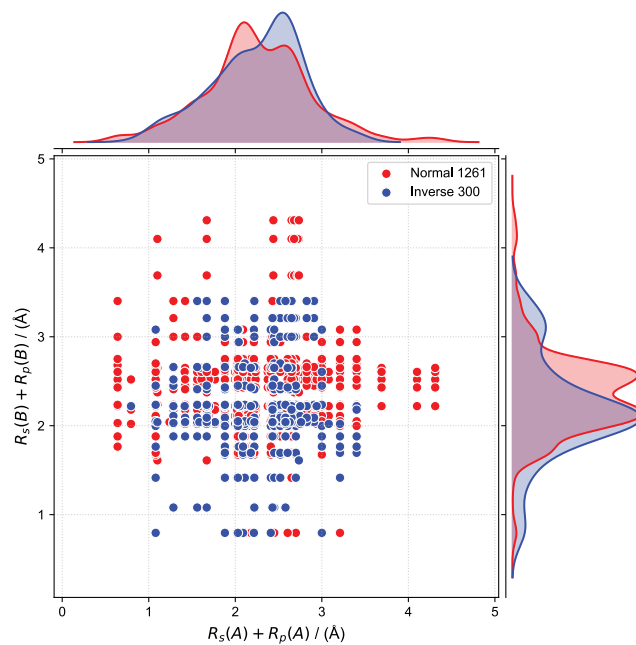


Fig. S11 Orbital-radii separation map of  $AB_2X_4$  spinels ( $X=O, S, Se, Te$ ) with preferred normal and inverse configurations, determined by  $x_{\text{eq}}$ , in red and blue, respectively.

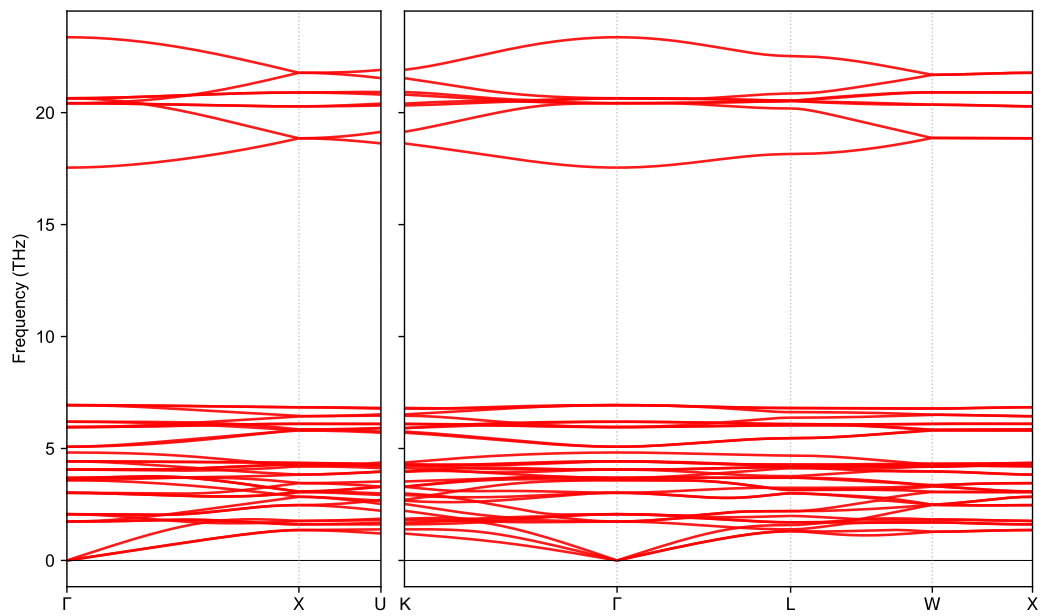


Fig. S12 Phonon band structure of  $\text{ReK}_2\text{O}_4$

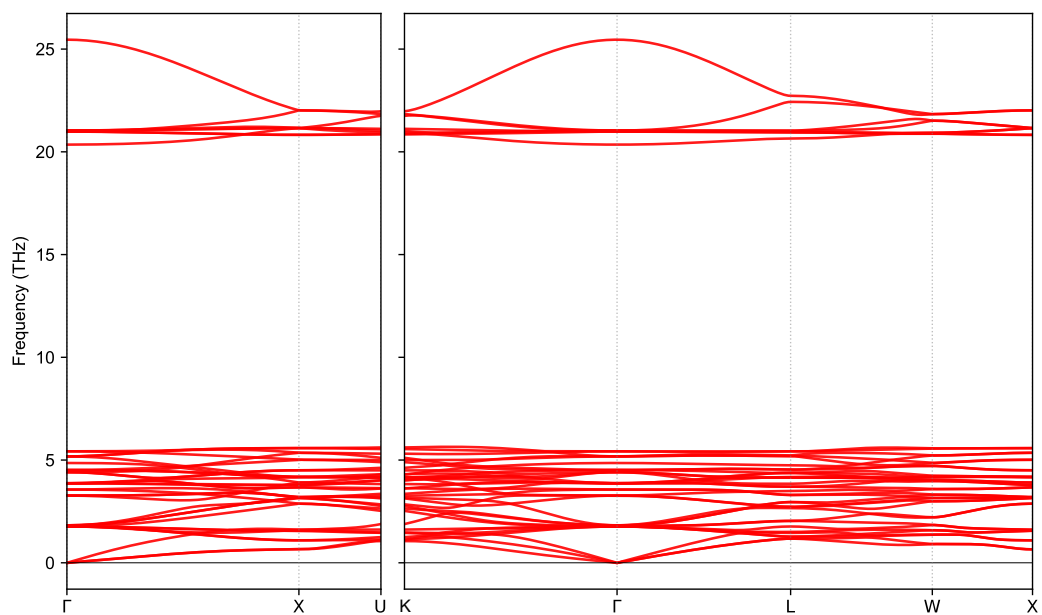


Fig. S13 Phonon band structure of  $\text{OsK}_2\text{O}_4$

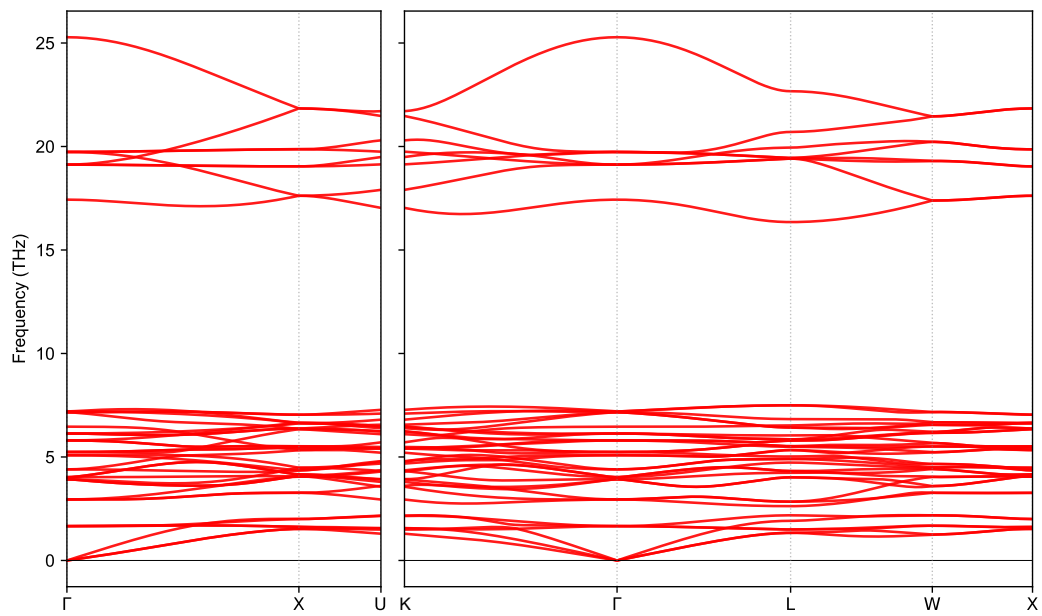


Fig. S14 Phonon band structure of  $\text{ReNa}_2\text{O}_4$

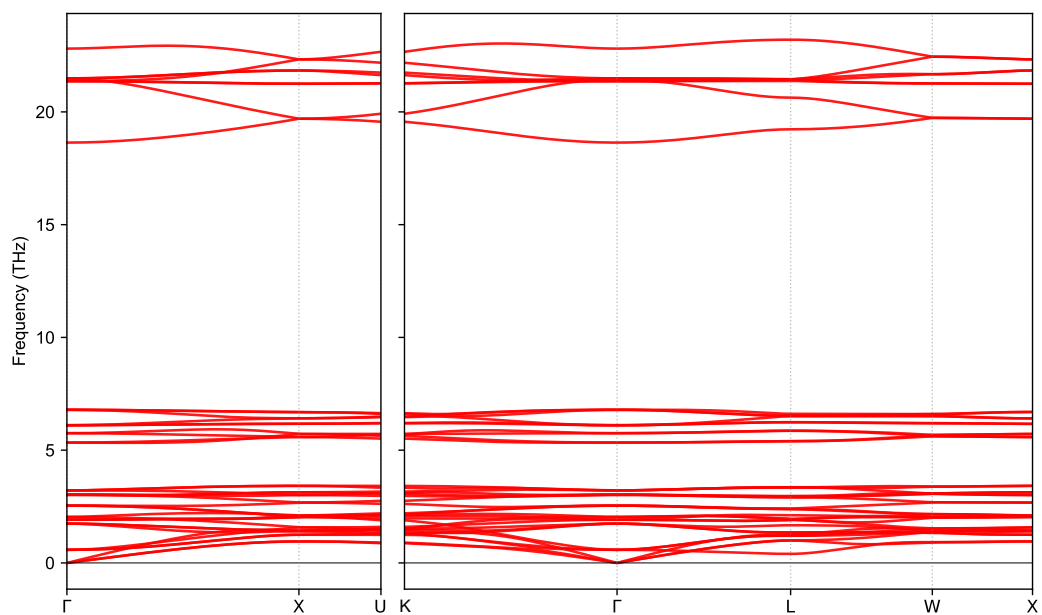


Fig. S15 Phonon band structure of  $\text{ReRb}_2\text{O}_4$

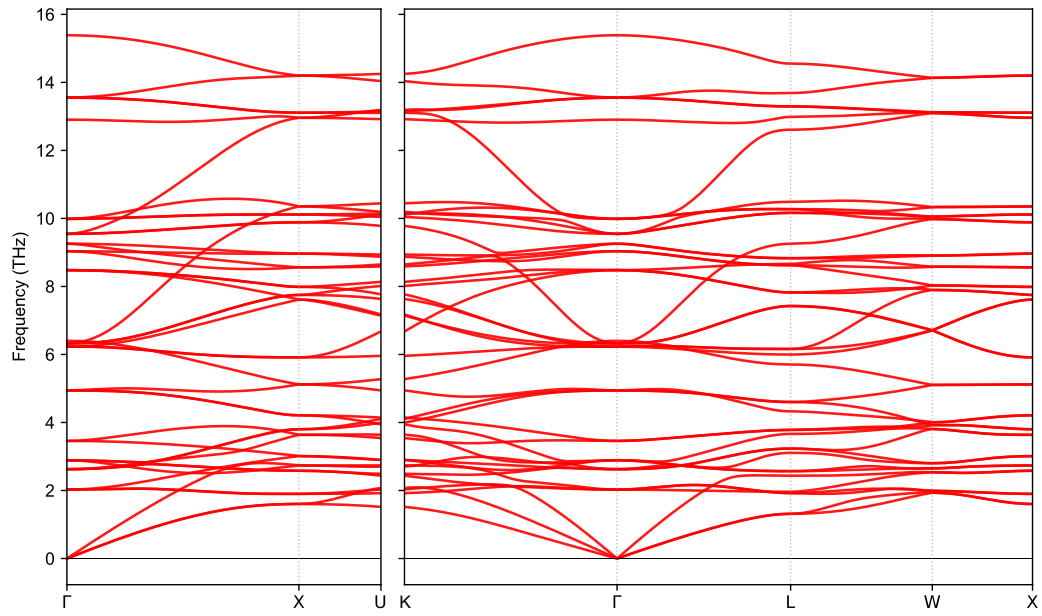


Fig. S16 Phonon band structure of BaNd<sub>2</sub>O<sub>4</sub>

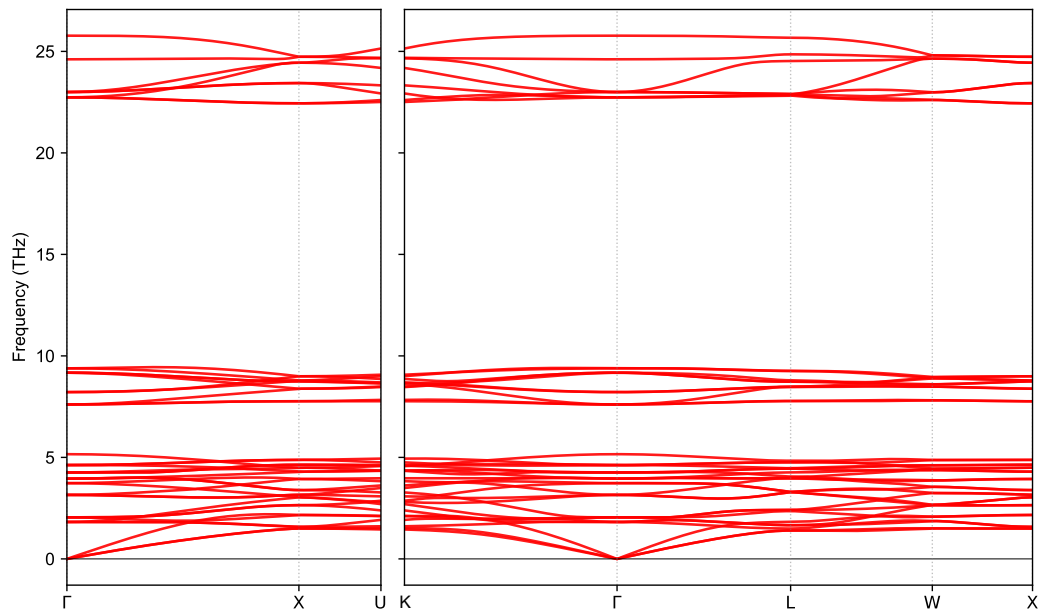


Fig. S17 Phonon band structure of WK<sub>2</sub>O<sub>4</sub>

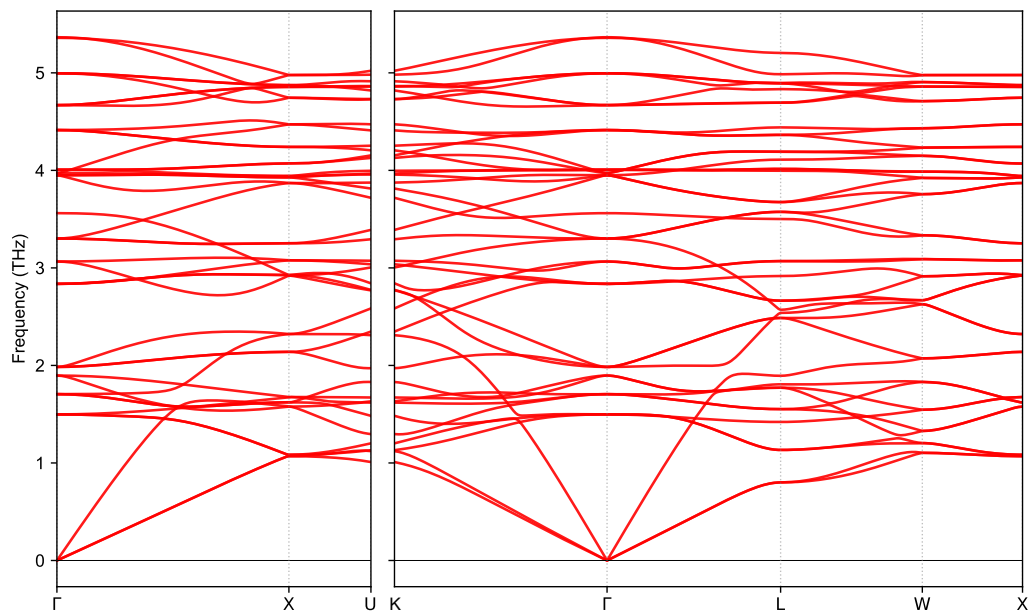


Fig. S18 Phonon band structure of Pd<sub>3</sub>Se<sub>4</sub>

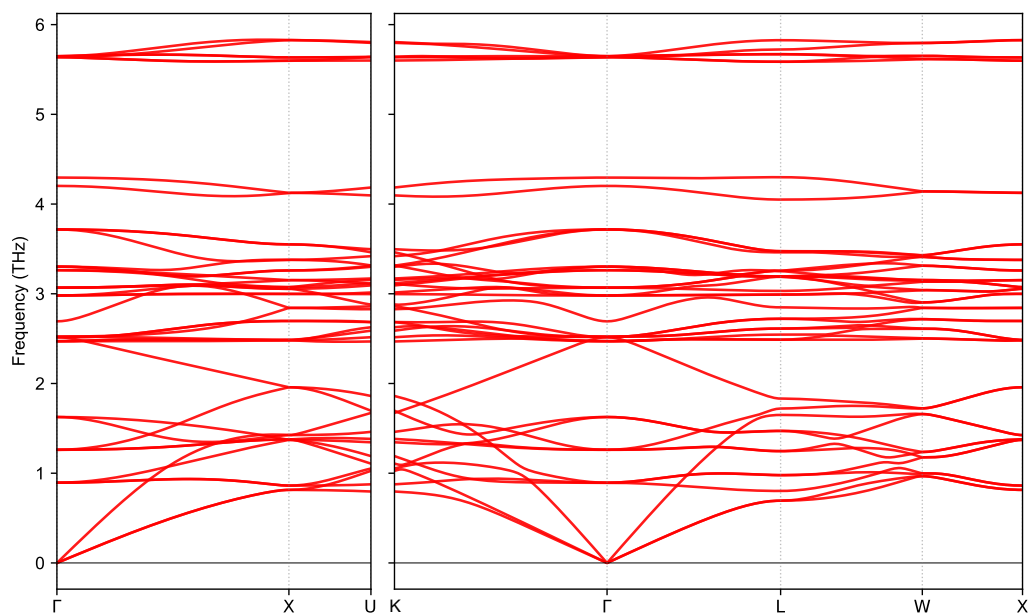


Fig. S19 Phonon band structure of MgNd<sub>2</sub>Te<sub>4</sub>

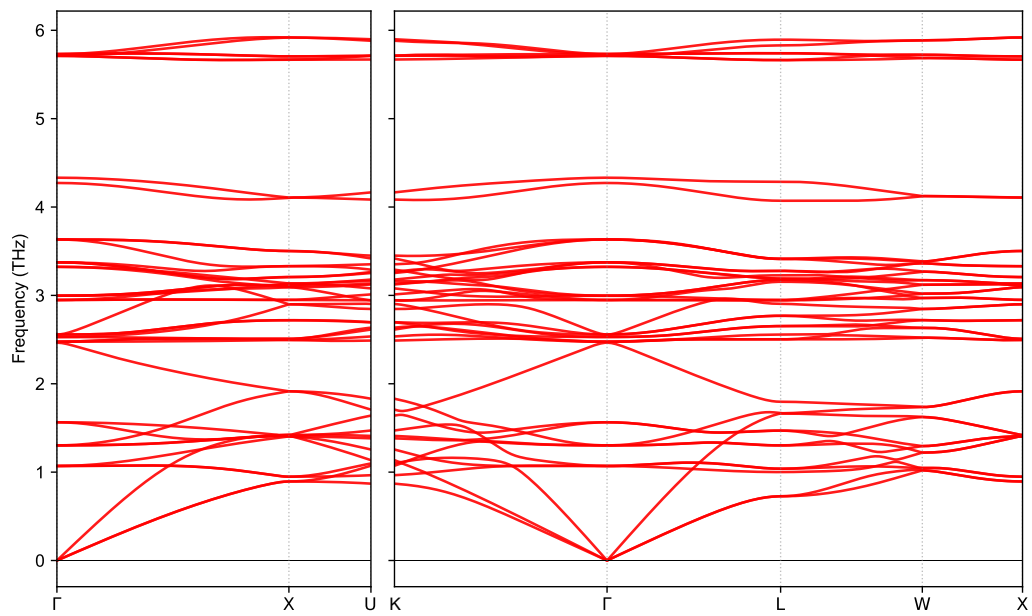


Fig. S20 Phonon band structure of MgEr<sub>2</sub>Te<sub>4</sub>

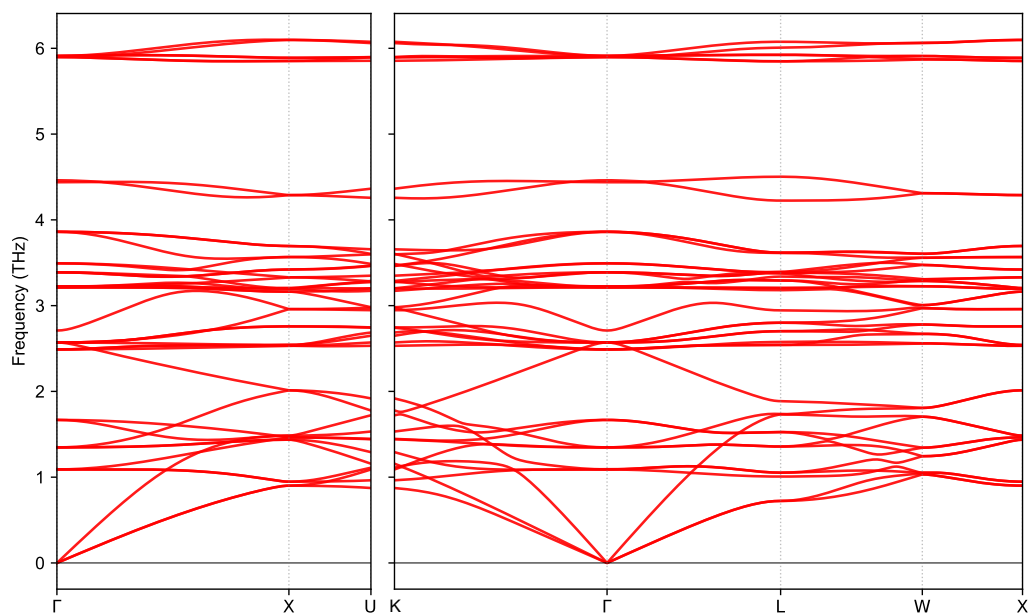


Fig. S21 Phonon band structure of MgTb<sub>2</sub>Te<sub>4</sub>

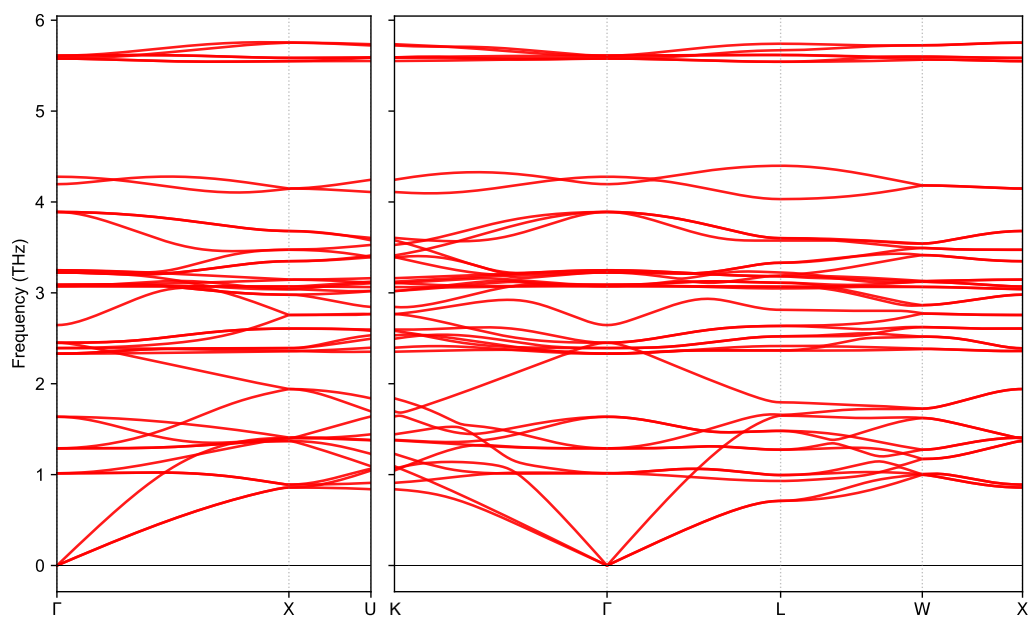


Fig. S22 Phonon band structure of MgGd<sub>2</sub>Te<sub>4</sub>

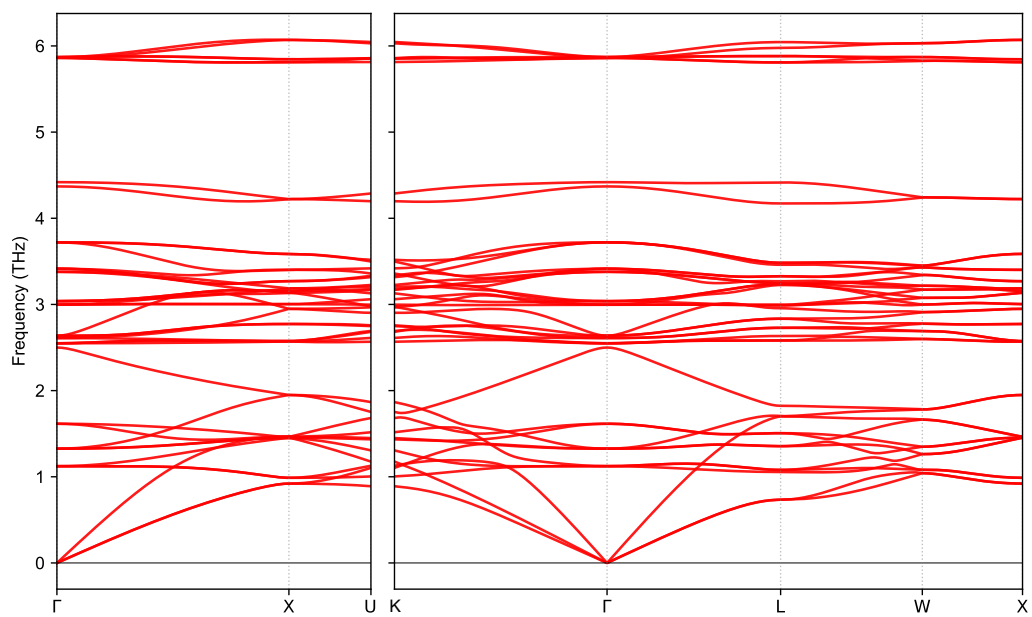


Fig. S23 Phonon band structure of MgLu<sub>2</sub>Te<sub>4</sub>

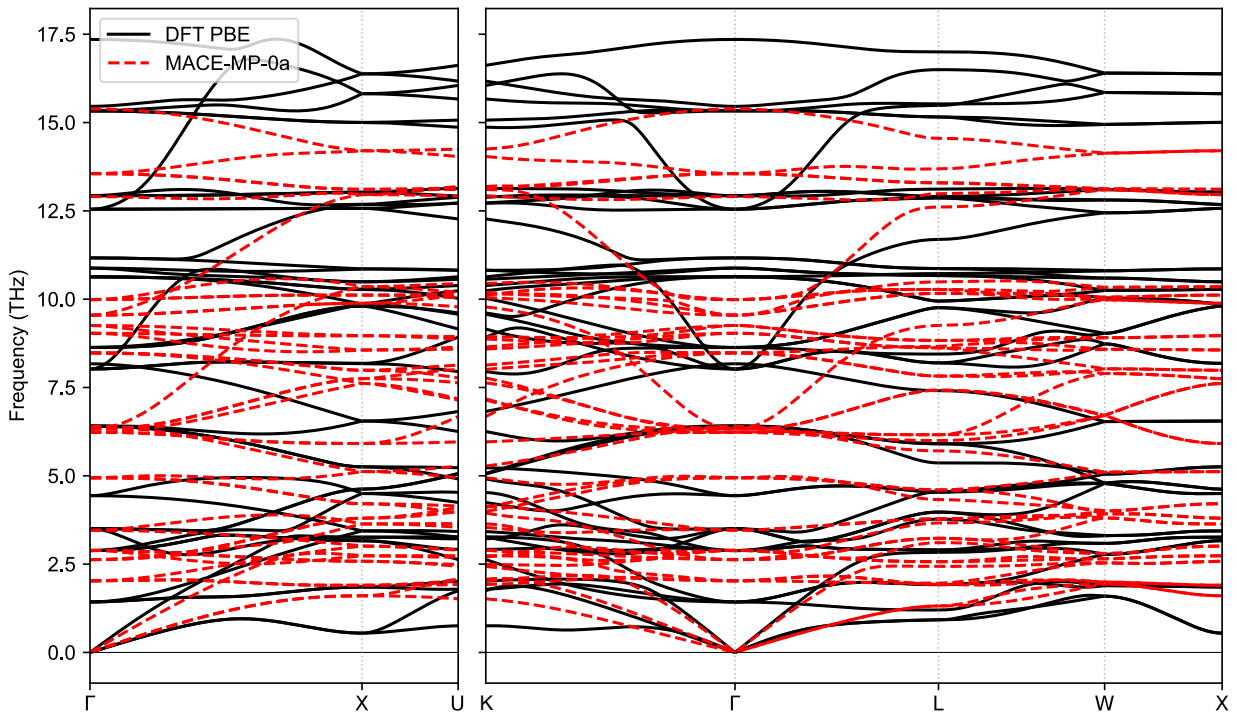


Fig. S24 Phonon band structure of  $\text{BaNd}_2\text{O}_4$

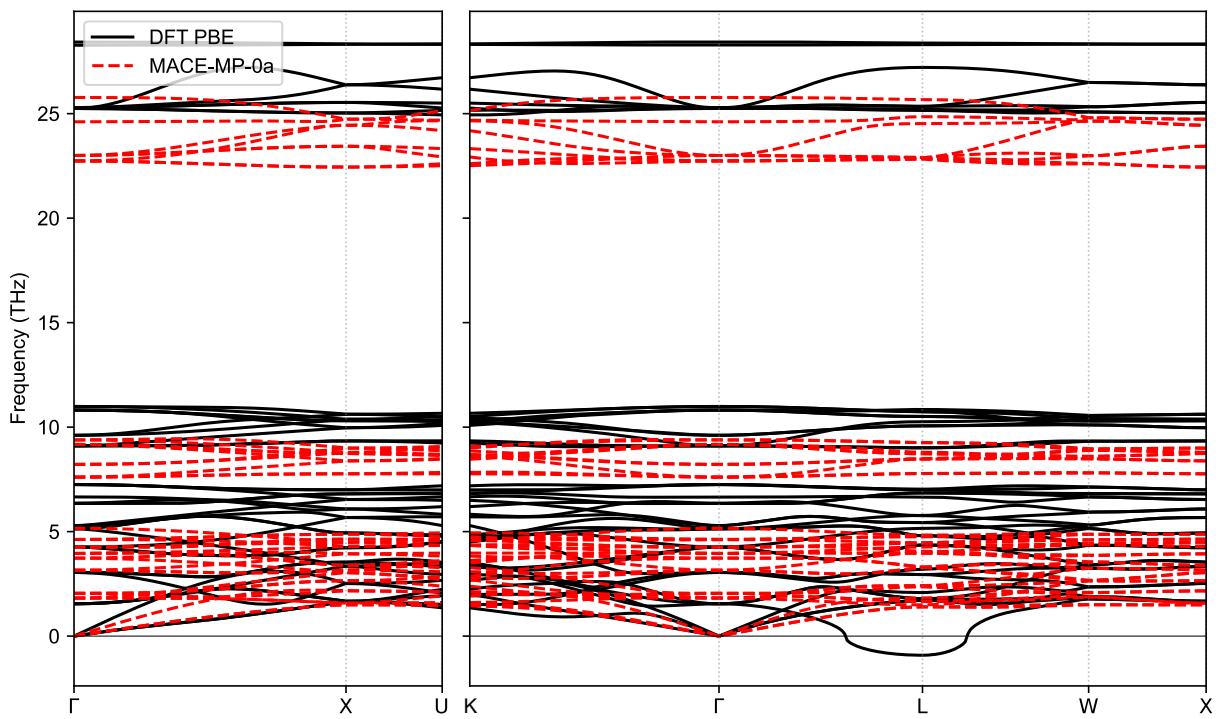


Fig. S25 Phonon band structure of  $\text{WK}_2\text{O}_4$

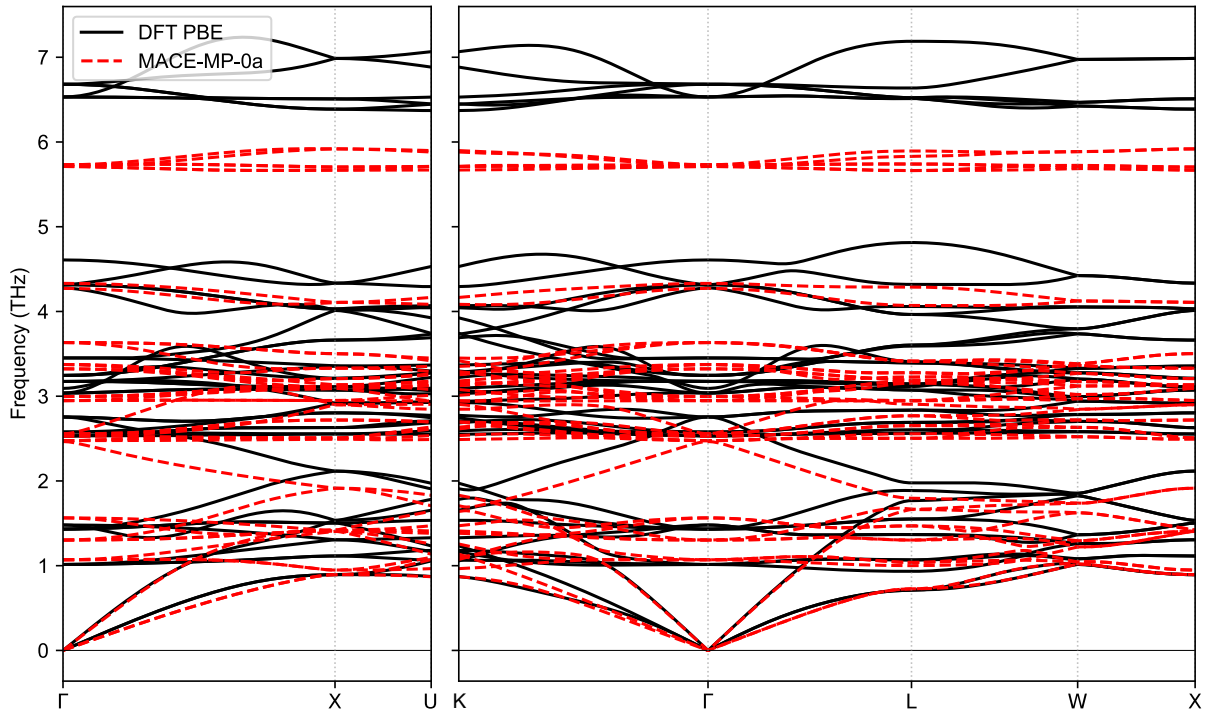


Fig. S26 Phonon band structure of  $\text{MgEr}_2\text{Te}_4$

DFT phonon calculations were carried out using VASP. The analysis was performed using Phonopy<sup>11,12</sup> package. The calculations were carried out using PBE functional with PAW pseudopotentials. The energy cutoff of 520 eV was applied for all systems. The electronic energy convergence criterion was set to  $10^{-8}$  eV. The calculations were performed on a  $2 \times 2 \times 2$  supercell containing a total of 448 atoms using Gamma-centred  $2 \times 2 \times 2$   $k$ -points alongside Gaussian smearing with a width of 0.05 eV. The results are shown in Fig. S24 to Fig. S26.

## Supporting References

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