Table S1. Single-ion principal components of the g matrix of the Mn (III) centres in $\mathbf{1}$ and 2 and orientations with respect to the crystallographic frame of reference $X Y Z$ by means of Euler angles.

|  | $\mathrm{g}_{\mathrm{xx}}$ | $\mathrm{g}_{\mathrm{yy}}$ | $\mathrm{g}_{\mathrm{zz}}$ | $\alpha /^{\circ}$ | $\beta /^{\circ}$ | $\gamma^{\circ}$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mn 1 (1) <br> (2) | 1.978 |  |  |  |  |  |
| 1.977 | 1.992 | 1.999 <br> 1.998 | 60.10 <br> 83.97 | 100.64 <br> 89.70 | 345.98 <br> 315.67 |  |
| Mn2 (1) | 1.982 |  |  |  |  |  |
| (2) | 1.978 | 1.994 | 1.992 | 1.998 | 38.01 <br> 144.19 | 141.29 <br> 117.42 |
| Mn3 (1) <br> (2) | 1.980 | 1.978 | 1.992 |  |  |  |

Table S2. Angles, in degrees, between the Jahn-Teller orientation and the AOM calculated $D_{Z Z}$ component of the anisotropy tensor for the $\mathrm{Mn}(\mathrm{III})$ sites $\mathrm{Mn} 1, \mathrm{Mn2}$, and Mn 3 , for compounds $\mathbf{1}$ and 2.

|  | Mn1 | Mn2 | Mn3 |
| :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | $4^{\circ \circ}$ | $7^{\circ}$ | $4^{\circ}$ |
| $\mathbf{2}$ | $15^{\circ}$ | $14^{\circ}$ | $13^{\circ}$ |



Figure S1. Field dependence of the eigenvalues of the twenty eight lowest lying eigenstates of $\mathbf{1}$ calculated as described in the text. The magnetic field is applied along the quantization axis (Z-axis).


Figure S2. Field dependence of the Boltzmann population of the twenty eight lowest lying eigenstates of $\mathbf{1}$ (top) and of the forty eight eigenstates of $\mathbf{2}$ (bottom) determined by diagonalisation of the anisotropic spin-Hamiltonian (5) at 4.2 K.


Figure S3. Field dependence of the eigenvalues of the forty eight lowest lying eigenstates of 2 calculated as described in the text. The magnetic field is applied along the quantization axis (Z-axis)

