

**Gadolinium(III) Complexes of 1,4,7-triazacyclononane Based Picolinate Ligands:
Simultaneous Optimization of Water Exchange Kinetics and Electronic Relaxation**

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Table S1: Influence of the synthesis conditions on the yield of bisubstituted tacn.

N°	Base	Base eq	Tacn eq	Solvent	C (M)	Yield in TRI (%)	Yield in BI (%)	Yield in MON	Global Yield (%)
<i>Influence of the solvent</i>									
1	iPr ₂ EtN	7.5	1.5	CH ₃ CN	0.05	36	39	10	85
2	iPr ₂ EtN	7.5	1.5	EtOH	0.05	10	55	22	87
3	iPr ₂ EtN	7.5	1.5	CHCl ₃	0.05	21	41	20	81
4	iPr ₂ EtN	7.5	1.5	DMF	0.05	18	48	14	80
<i>Influence of the base</i>									
5	iPr ₂ EtN	7.5	1.5	EtOH	0.05	10	55	22	87
6	Et ₃ N	7.5	1.5	EtOH	0.05	6	54	20	80
7	Me ₅ NC	7.5	1.5	EtOH	0.05	-			
8	iPr ₂ EtN	4.5	1.5	EtOH	0.05	3	36	13	52
9	K ₂ CO ₃	4.5	1.5	EtOH	0.05	17	19	9	45
10	CsCO ₃	4.5	1.5	EtOH	0.05	21	27	11	59
<i>Influence of the base stoichiometry</i>									
11	iPr ₂ EtN	4.5	1.5	EtOH	0.05	3	36	13	52
12	iPr ₂ EtN	6	1.5	EtOH	0.05	8	53	9	70
13	iPr ₂ EtN	7.5	1.5	EtOH	0.05	10	55	22	87
14	iPr ₂ EtN	8	1.5	EtOH	0.05	12	52	11	75
<i>Influence of the 1,4,7-triazacyclononane (tacn) stoichiometry</i>									
15	iPr ₂ EtN	7.5	3	EtOH	0.05	0	49	27	76
16	iPr ₂ EtN	7.5	2.5	EtOH	0.05	2	53	24	79
17	iPr ₂ EtN	7.5	2	EtOH	0.05	3	59	19	81
18	iPr ₂ EtN	7.5	1.5	EtOH	0.05	10	55	22	87
19	iPr ₂ EtN	7.5	1	EtOH	0.05	29	44	7	20
<i>Influence of the concentration</i>									
20	iPr ₂ EtN	7.5	1.5	EtOH	0.01	0	32	25	57
21	iPr ₂ EtN	7.5	1.5	EtOH	0.05	10	55	22	87
22	iPr ₂ EtN	7.5	1.5	EtOH	0.1	10	56	17	83
23	iPr ₂ EtN	7.5	1.5	EtOH	0.5	16	58	13	87
<i>Optimal conditions</i>									
24	iPr ₂ EtN	7.5	2	EtOH	0.5	5	62	18	85

2. NMR spectra of ligands and Ln complexes at different temperatures

Figure S1: ^1H NMR spectrum of $\text{H}_3\text{ebpatchn}$, D_2O , 298 K, $\text{pD}=2.4$.

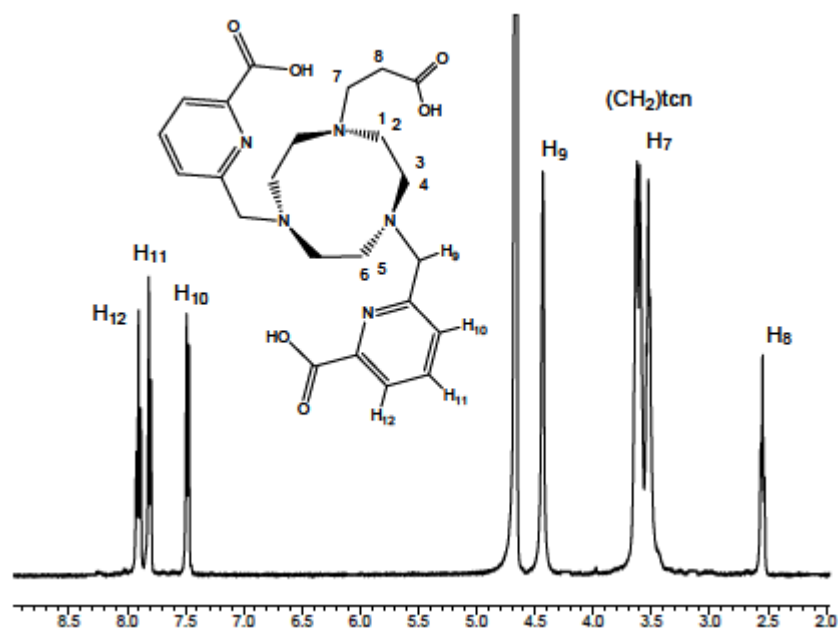


Figure S2: ^1H NMR spectrum of $\text{H}_4\text{pbpatchn}$, D_2O , 298 K, $\text{pD}=2.2$.

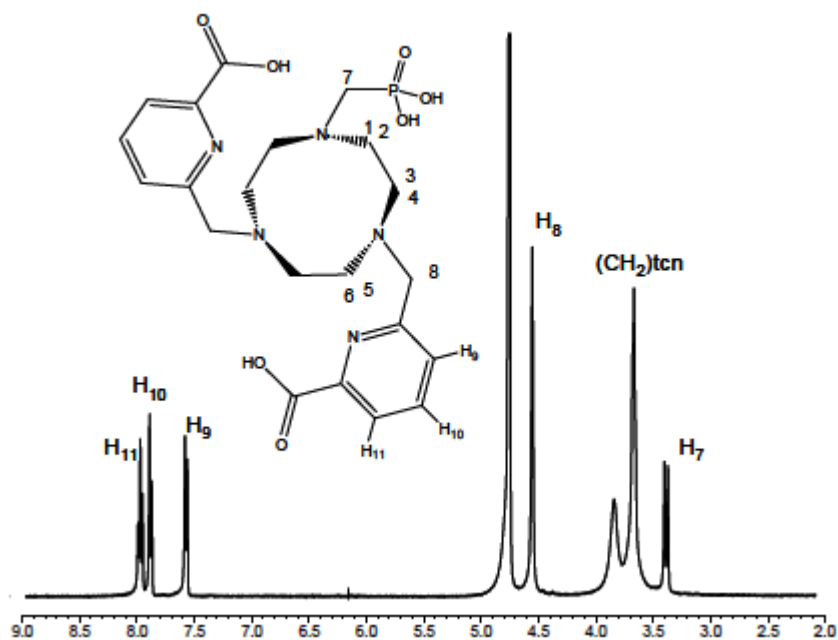


Figure S3: ^1H NMR spectrum of $[\text{Eu}(\text{ebpatchn})]$, D_2O , 278 K, 500 MHz, $\text{pD}=7.4$.

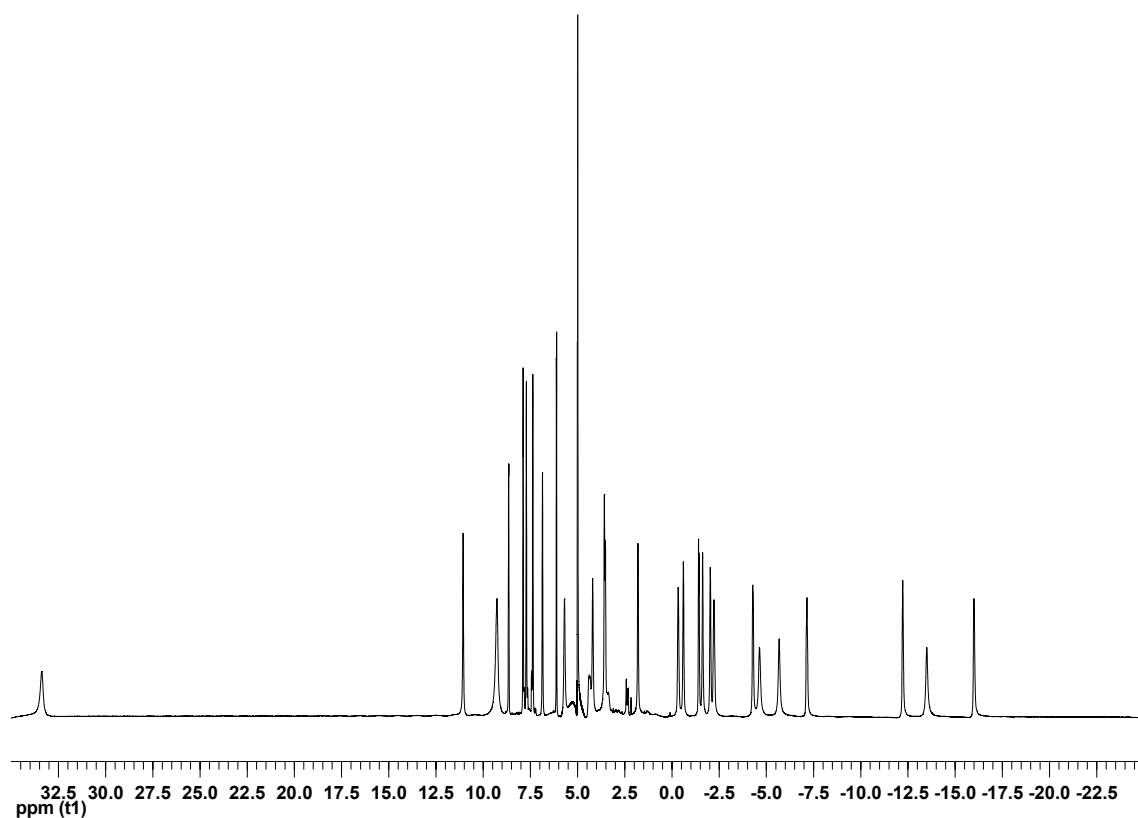


Figure S4: ^1H NMR spectrum of $[\text{La}(\text{pbpatchn})]$, D_2O , 278 K, 500 MHz, $\text{pD}=7.2$.

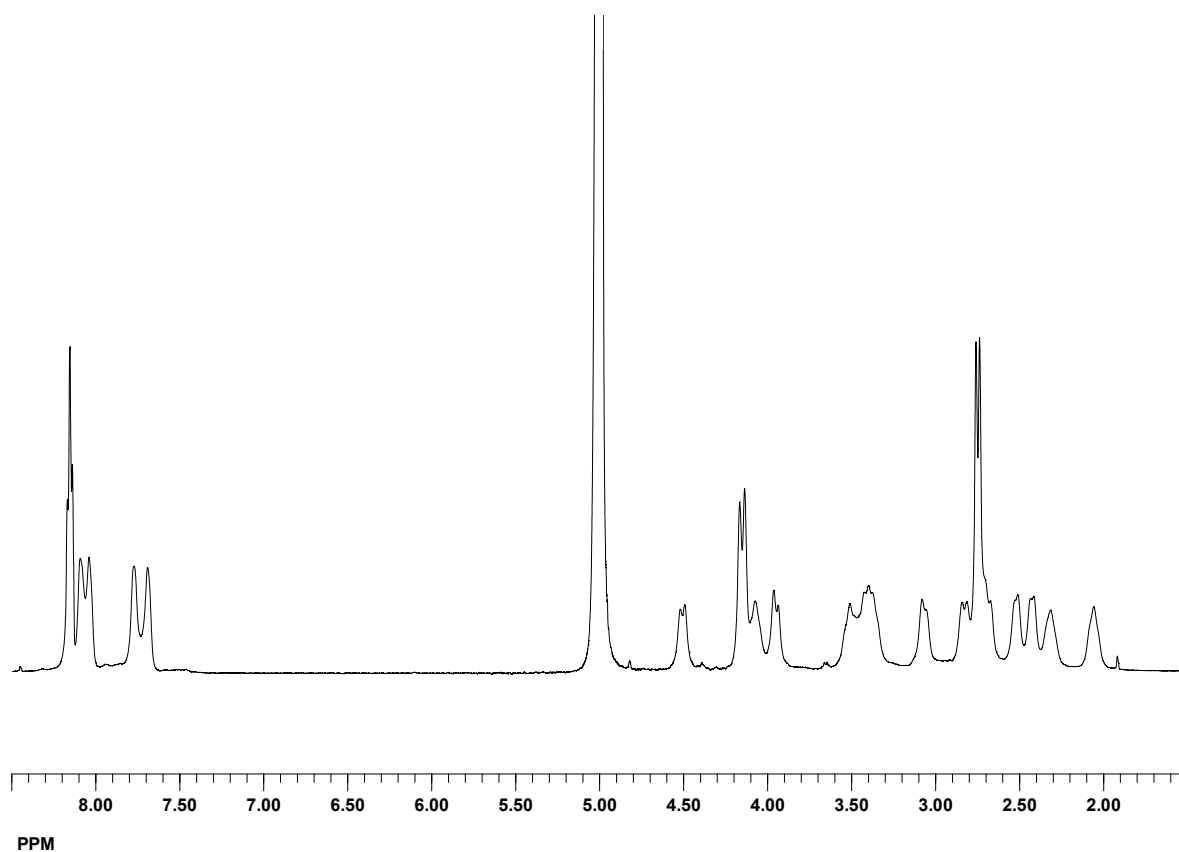


Figure S5: ^1H NMR spectrum of $[\text{La}(\text{pbpatchn})]$, D_2O , 298 K, 500 MHz, $\text{pD}=7.2$.

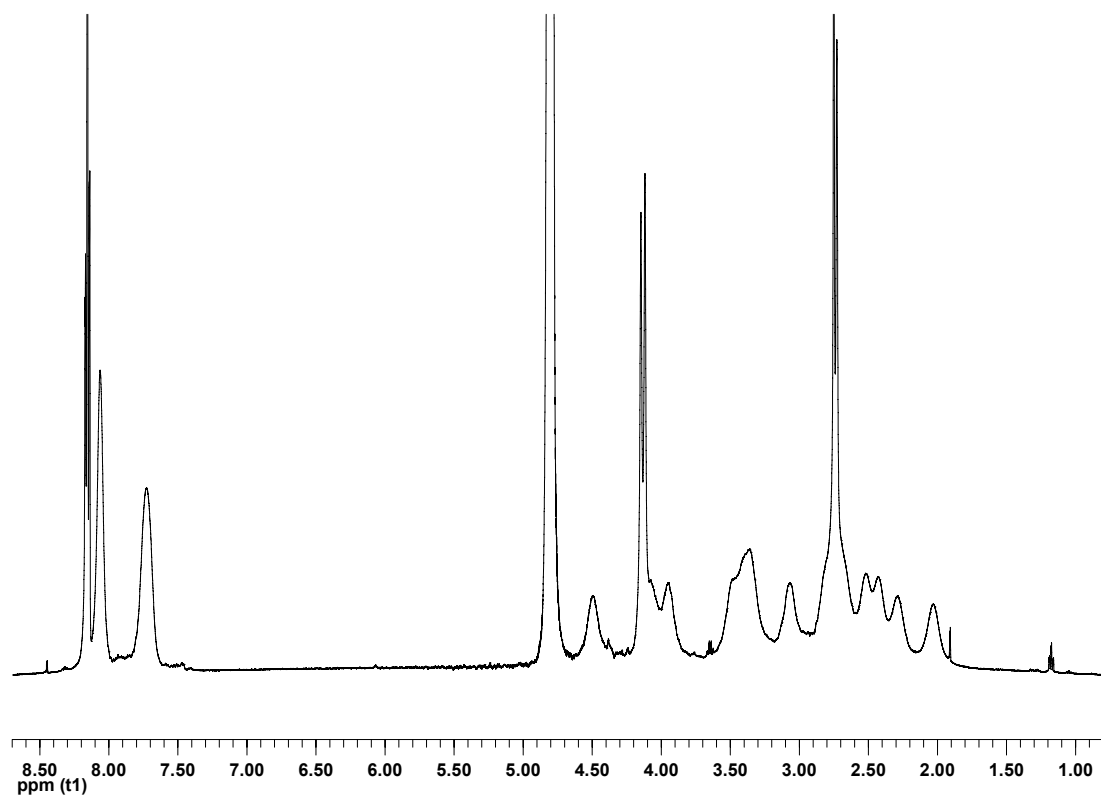


Figure S6: ^1H NMR spectrum of $[\text{La}(\text{pbpatchn})]$, D_2O , 343 K, 500 MHz, $\text{pD}=7.2$.

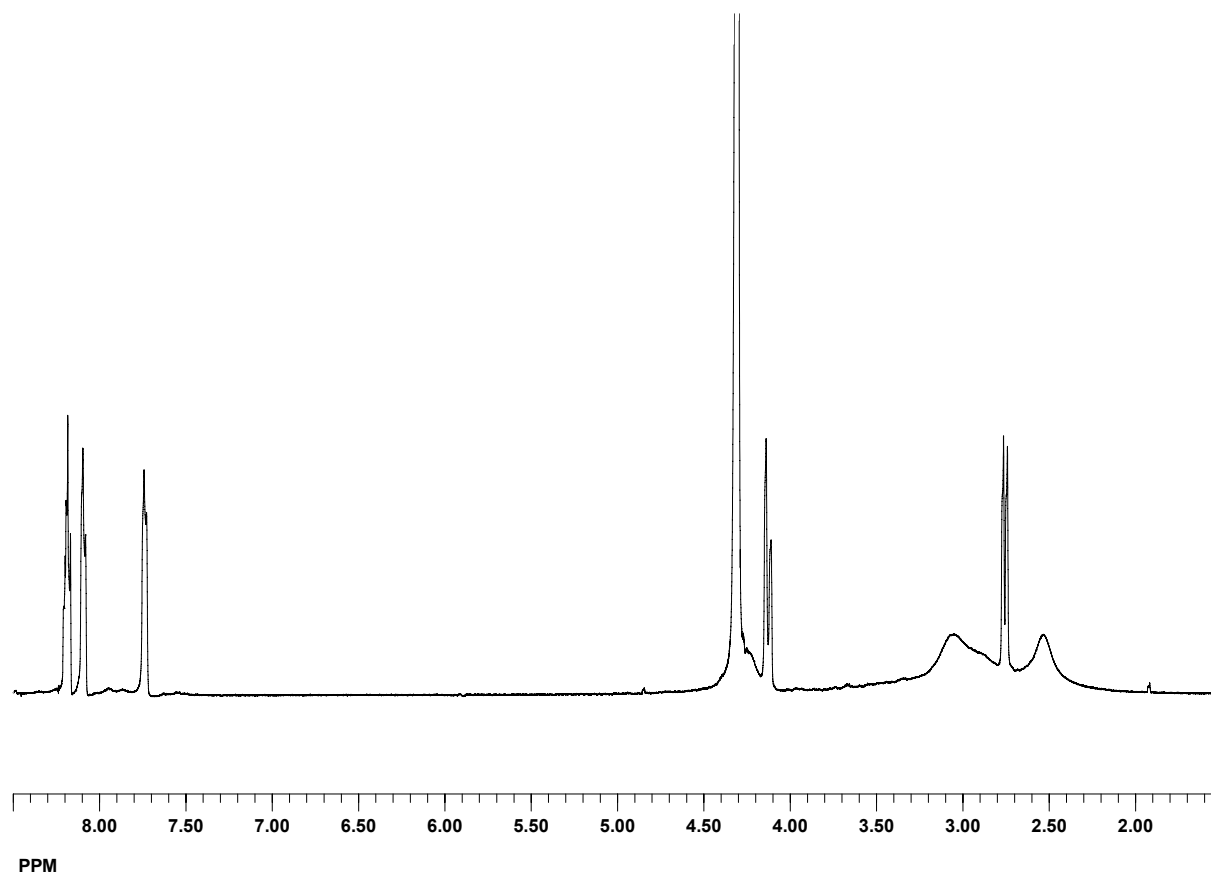


Figure S7: ^1H NMR spectrum of $[\text{Eu}(\text{pbpatcn})]$, D_2O , 278 K, 500 MHz, $\text{pD}=5.5$.

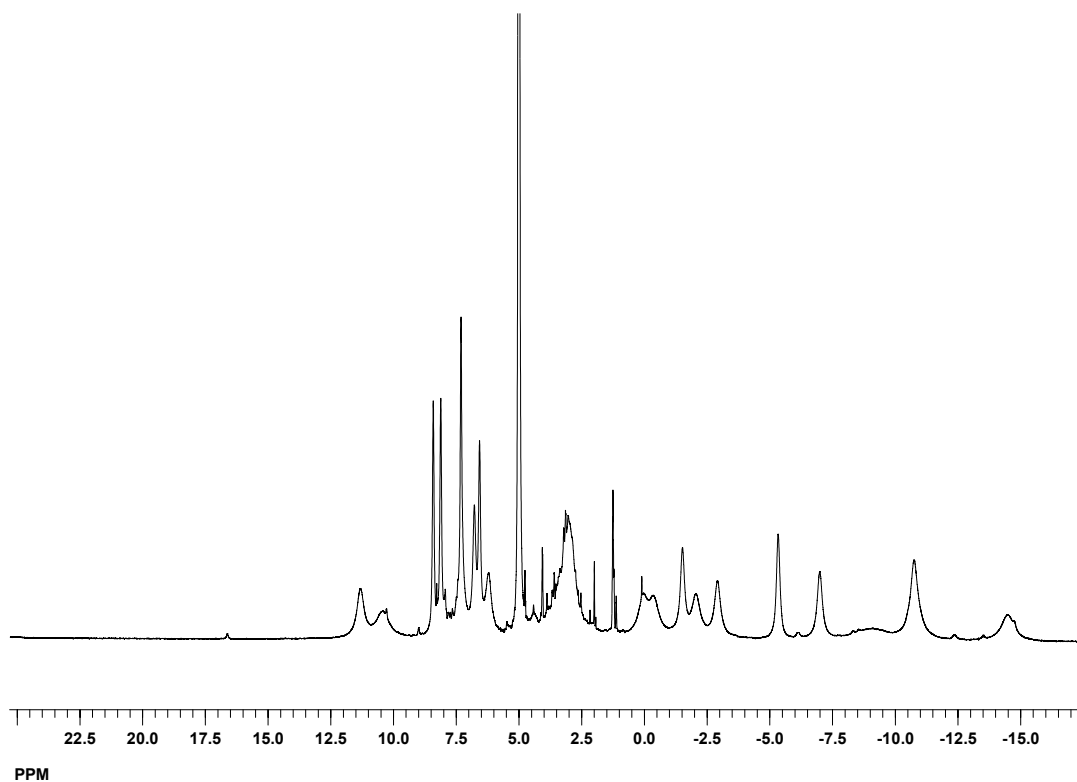


Figure S8: ^1H NMR spectrum of $[\text{Lu}(\text{pbpatcn})]$, D_2O , 298 K, 500 MHz, $\text{pD}=6.8$.

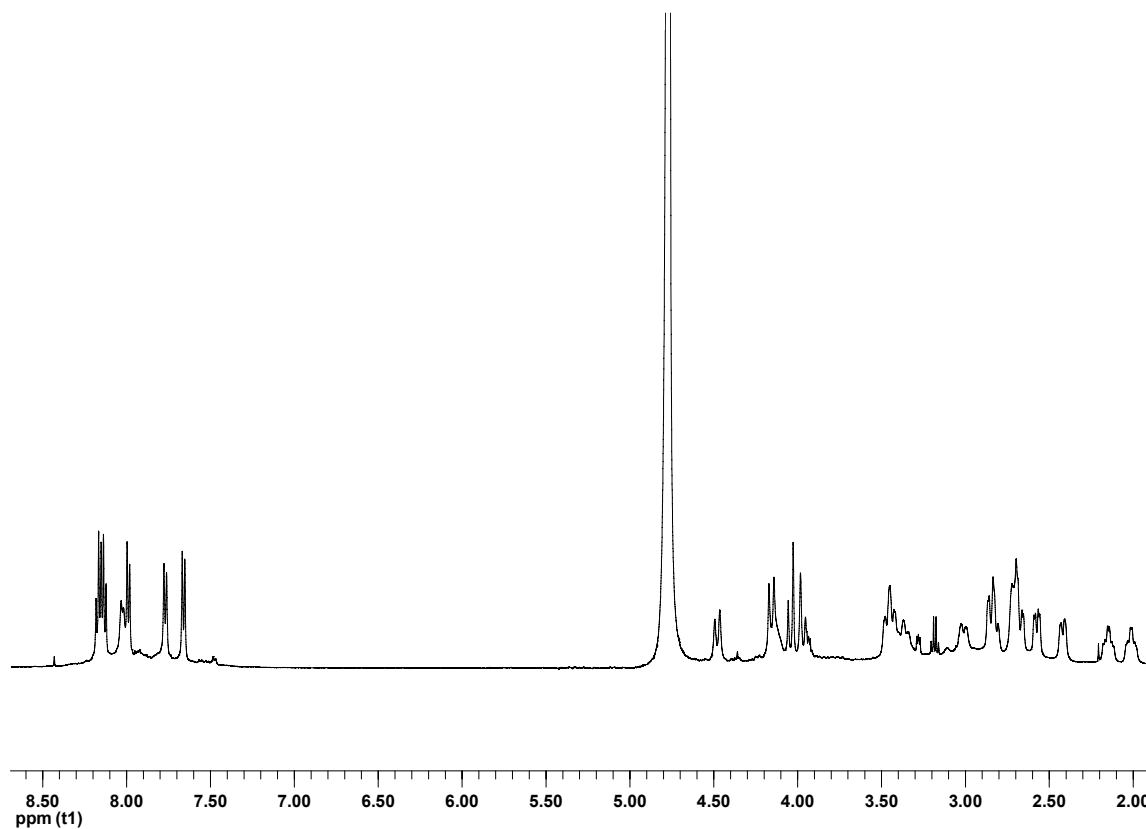
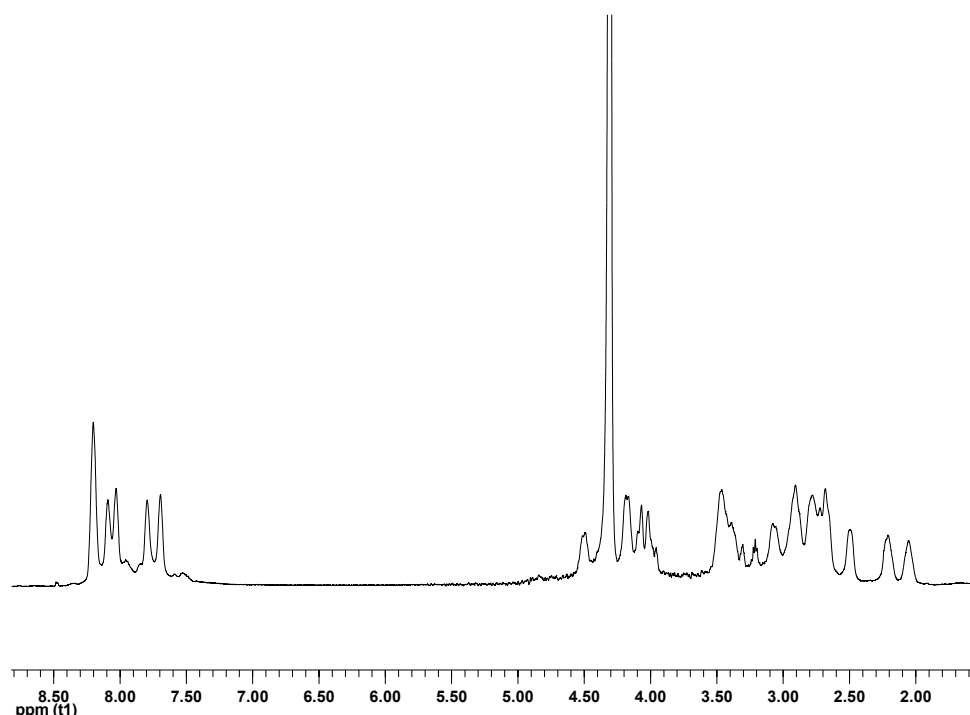


Figure S9: ^1H NMR spectrum of $[\text{Lu}(\text{pbpatcn})]$, D_2O , 343 K, 500 MHz, $\text{pD}=6.8$.



3. Data analysis of the variable temperature ^{17}O NMR

The reduced relaxation rates and chemical shift ($1/T_{1r}$, $1/T_{2r}$ and $\Delta\omega_r$) can be calculated from the measured ^{17}O NMR relaxation rates and angular frequencies of the Gd^{3+} containing solutions, $1/T_1$, $1/T_2$, and ω , and of the diamagnetic water reference, $1/T_{1d}$, $1/T_{2d}$, and ω_d with equations 1-3 where $1/T_{1m}$, $1/T_{2m}$ are the relaxations rates in the bound water, $\Delta\omega_m$ is the chemical shift difference between bound water and bulk water, P_m is the mole fraction of bound water, and τ_m is the mean residence time of water molecule in the inner-coordination sphere ($k_{\text{ex}} = 1/\tau_m$). It has been shown that the outer-sphere contributions to longitudinal and transversal relaxivities can be neglected.

$$\frac{1}{T_{1r}} = \frac{1}{P_m} \left[\frac{1}{T_1} - \frac{1}{T_{1d}} \right] = \frac{1}{T_{1m} + \tau_m} \quad (1)$$

$$\frac{1}{T_{2r}} = \frac{1}{P_m} \left[\frac{1}{T_2} - \frac{1}{T_{2d}} \right] = \frac{1}{\tau_m} \frac{T_{2m}^{-2} + \tau_m^{-1} T_{2m}^{-1} + \Delta\omega_m^2}{(\tau_m^{-1} + T_{2m}^{-1})^2 + \Delta\omega_m^2} \quad (2)$$

$$\Delta\omega_r = \frac{1}{P_m} (\omega - \omega_d) = \frac{\Delta\omega_m}{(1 + \tau_m T_{2m}^{-1})^2 + \tau_m^2 \Delta\omega_m^2} \quad (3)$$

At high temperatures, the inner-sphere contribution to $\Delta\omega_r$ is given by the chemical shift of the bound water molecules, which is determined by the hyperfine interaction between the Gd^{3+} electron spin and the ^{17}O nucleus via equation 4 where g_L is the isotropic Landé

factor, μ_B the Bohr magneton, S the electron spin, $A/\hbar$ the scalar coupling constant and B_0 the magnetic field.

$$\Delta\omega_m = \frac{g_L \mu_B S(S+1) B_0}{3k_B T} \frac{A}{\hbar} \quad (4)$$

When it is not negligible, the outer-sphere contribution has a similar temperature dependence to $\Delta\omega_m$ and is given by equation 5 where C_{os} is an empirical constant ($0 < C_{os} < 0.1$).

$$\Delta\omega_{os} = C_{os} \Delta\omega_m \quad (5)$$

The ^{17}O longitudinal relaxation rates in Gd^{3+} solutions are dominated by the dipole-dipole and quadrupolar mechanisms and are given by equation 6 where γ_I is the ^{17}O nuclear magnetic ratio, r_{GdO} the mean Gd^{3+} -O distance, I the nuclear spin, χ the quadrupolar coupling constant, η an asymmetry parameter and τ_{d1} is defined by equation 7.

$$\frac{1}{T_{1m}} = \left[\frac{1}{15} \left(\frac{\mu_0}{4\pi} \right)^2 \frac{\hbar^2 \gamma_I^2 \gamma_S^2}{r_{\text{GdO}}^6} S(S+1) \right] \times 6\tau_{d1} + \frac{3\pi^2}{10} \frac{2I+3}{I^2(2I-1)} \chi^2 \left(1 + \frac{\eta^2}{3} \right) \tau_R \quad (6)$$

$$\frac{1}{\tau_{d1}} = \frac{1}{T_{1e}} + \frac{1}{\tau_R} + \frac{1}{\tau_m} \quad (7)$$

According to crystallographic studies on a series of Gd^{3+} complexes, the mean distance r_{GdO} can be considered as independent of the complex and fixed to 2.5 Å. χ and η have been fixed, considering that the quadrupolar coupling constant is the same as the one for acidified water (Equation 8).

$$\chi \left(1 + \frac{\eta^2}{3} \right)^{1/2} = 7.58 \text{ MHz} \quad (8)$$

The ^{17}O transverse relaxation rate $1/T_{2m}$ in bound water in Gd^{3+} solutions are dominated by the scalar relaxation mechanism and are given to an excellent approximation by equations 9 and 10.

$$\frac{1}{T_{2m}} = \frac{S(S+1)}{3} \left(\frac{A}{\hbar} \right)^2 \times \tau_{1s} \quad (9)$$

$$\frac{1}{\tau_{1s}} = \frac{1}{T_{1e}} + \frac{1}{\tau_m} \quad (10)$$

The longitudinal electronic relaxation rate $1/T_{1e}$ is accounted for by modulation of the zero field splitting (ZFS) either by rotation or by transient distortions of the complex. At the

experimental field, we assumed that $1/T_{1e}$ can be obtained by the approach of McLachlan (equations 11 and 12) within a good agreement.^{1,2}

$$\frac{1}{T_{1e}} = 2C \left(\frac{1}{1 + \omega_S^2 \tau_v^2} + \frac{4}{1 + 4\omega_S^2 \tau_v^2} \right) \quad (11)$$

$$C = \frac{1}{50} \Delta^2 \tau_v [4S(S+1) - 3] \quad (12)$$

Δ^2 is the mean-square zero field splitting energy and τ_v is the correlation time for modulation of the zero field splitting interaction. This modulation may result either from rotation or from transient distortions of the complex. We assume that τ_v has the simple exponential temperature dependence given by equation 13 where τ_v^{298} is the correlation time at 298.15 K and E_v is the activation energy. It should be noted that the electronic relaxation time τ_{s0} commonly used in the interpretation of the NMRD profiles corresponds to $(12\Delta^2 \tau_v)^{-1}$.

$$\tau_v = \tau_v^{298} \exp \left[\frac{E_v}{R} \left(\frac{1}{T} - \frac{1}{298.15} \right) \right] \quad (13)$$

The exchange rate of water molecules in the inner-sphere is assumed to obey the Eyring equation (equation 14) where $\Delta S^\ddagger$ and $\Delta H^\ddagger$ are respectively the entropy and the enthalpy of activation for the exchange process and k_{ex}^{298} is the exchange rate at 298.15 K.

$$k_{ex} = \frac{1}{\tau_m} = \frac{k_B T}{h} \exp \left[\frac{\Delta S^\ddagger}{R} - \frac{\Delta H^\ddagger}{RT} \right] = \frac{k_{ex}^{298} T}{298.15} \exp \left[\frac{\Delta H^\ddagger}{R} \left(\frac{1}{298.15} - \frac{1}{T} \right) \right] \quad (14)$$

4. Potentiometric titrations

Figure S10: Normalized titration curves ($\text{pH} = f(n_{\text{OH}^-}/n_{\text{Ligand}})$) for solution of $\text{H}_4\text{pbpatcn}$ (0.51 mM) and Gd-pbpatcn ($[\text{pbpatcn}] = 0.26 \text{ mM}$, $[\text{Gd}] = 0.24 \text{ mM}$).

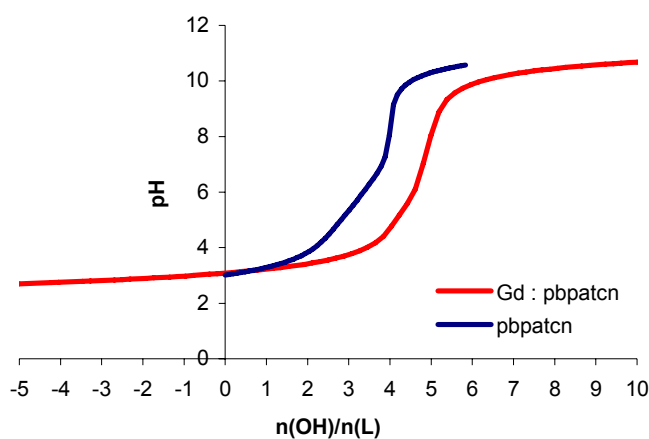
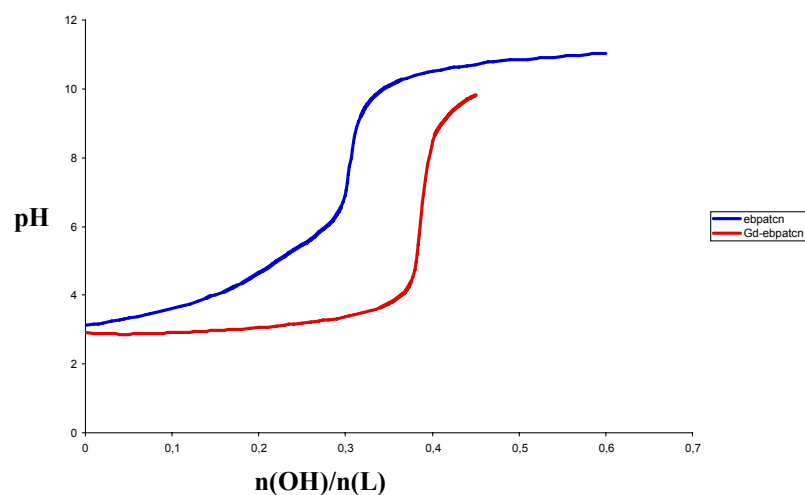


Figure S11: Normalized titration curves ($\text{pH} = f(n_{\text{OH}^-}/n_{\text{Ligand}})$) for solution of $\text{H}_3\text{ebpatcn}$ (0.91 mM, blue line), Gd-ebpatcn ($[\text{ebpatcn}] = 0.91 \text{ mM}$, $[\text{Gd}] = 0.91 \text{ mM}$, red line).



5. References

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