

Electronic Supplementary Information:

The expressions for thermodynamic properties of FeSe at high pressure and high temperature

The thermal equation of state $V(P,T)$ can be obtained by solving the non-equilibrium Gibbs function with respect to volume V

$$\left(\frac{\partial G^*(V;P,T)}{\partial V} \right)_{P,T} = 0 \quad (\text{A1})$$

From equation A1, one can get the thermal equation of state. Then, the isothermal bulk modulus B_T , the vibrational internal energy U_{vib} , the heat capacity of constant volume C_V , the heat capacity at constant pressure C_P , the vibrational entropy S_{vib} and the thermal expansion coefficient α can be derived as

$$B_T(P,T) = V \left(\frac{\partial^2 G^*(V;P,T)}{\partial V^2} \right)_{P,T} = 0, \quad (\text{A2})$$

$$U_{\text{vib}} = nk \left[\frac{9}{8} \frac{\Theta}{T} + 3D(3\Theta/T) \right], \quad (\text{A3})$$

$$C_V = 3nk \left[4D\left(\frac{\Theta}{T}\right) - \frac{3\Theta/T}{e^{\Theta/T} - 1} \right], \quad (\text{A4})$$

$$C_P = C_V(1 + \alpha\gamma T), \quad (\text{A5})$$

$$S_{\text{vib}} = nk \left[4D(3\Theta/T) - 3\ln(1 - e^{-\Theta/T}) \right], \quad (\text{A6})$$

$$\alpha = \frac{\gamma C_V}{B_T V}, \quad (\text{A7})$$

where the Grüneisen parameter γ is defined as

$$\gamma = - \frac{d \ln \Theta(V)}{\ln V} \quad (\text{A8})$$