

Supplementary Information

Mathematical Model Equations:

(1) Calcium Dynamics

$$\begin{aligned}
 v_{plc} &= (V_{plc} + basal) * \left(\frac{[Ca^{2+}]^2}{K_{plc}^2 + [Ca^{2+}]^2} \right) \\
 v_{deg} &= (k_{5p} + k_{3k} * \left(\frac{[Ca^{2+}]^2}{K_{3k}^2 + [Ca^{2+}]^2} \right)) * [IP3] \\
 v_{rel} &= \left(k_1 * \left([IP3r] * \frac{[Ca^{2+}]}{K_a + [Ca^{2+}]} * \frac{[IP3]}{K_p + [IP3]} \right)^3 + k_2 \right) * ([Ca^{2+}(ER)] - [Ca^{2+}]) \\
 v_{serca} &= V_{serca} * \left(\frac{[Ca^{2+}]^2}{K_{serca}^2 + [Ca^{2+}]^2} \right) \\
 v_{in} &= v_0 + \emptyset * V_{plc} * \left(\frac{1}{k_{3k} + k_{5p}} \right) \\
 v_{out} &= V_{pm} * \left(\frac{[Ca^{2+}]^2}{K_{pm}^2 + [Ca^{2+}]^2} \right) \\
 \frac{d[IP3]}{dt} &= v_{plc} - v_{deg} \\
 \frac{d[Ca^{2+}]}{dt} &= v_{rel} - v_{serca} + \varepsilon * (v_{in} - v_{out}) \\
 \frac{d[Ca^{2+}(ER)]}{dt} &= \left(\frac{1}{\beta} \right) * (v_{serca} - v_{rel}) \\
 \frac{d[IP3r]}{dt} &= \left(\frac{1}{Tr} \right) * \left(1 - [IP3r] * \frac{K_i + [Ca^{2+}]}{K_i} \right)
 \end{aligned}$$

(2) Conservation equations

R = receptor available for binding, R_{tot} = total receptor, [LR] = Ligand-Receptor Complex, G = available G-protein for activation, G_{tot} = total G-protein, [GGTP] = Active G-protein, [GGDP] = Inactive G-protein, [PLC*] = activated PLC, PLC_{tot} = total PLC, Gβγ = G-protein subunit, [LRp] = Ligand-phosphorylated Receptor complex, [Rp] = phosphorylated Receptor, [Rrec] = Recycled Receptor

$$R = R_{tot} - [LR] - [LRp] - [Rp] + R_{rec}$$

$$G = G_{tot} - [GGTP] - [GGDP] - [PLC *]$$

$$G\beta\gamma = [GGTP] + [GGDP] + [PLC *]$$
$$PLC = PLC_{tot} - [PLC *]$$

(3) Ligand, Receptor, G-protein dynamics

$$\frac{d[LR]}{dt} = k_{1L} * R * L - k_{2L} * [LR] - k_{grk1f} * [LR] + k_{grk1r} * [LRp]$$
$$\frac{d[GGTP]}{dt} = -k_4 * [GGTP] + k_5 * G * [LR] - k_6 * PLC * [GGTP] + k_3 * G$$
$$\frac{d[GGDP]}{dt} = k_4 * [GGTP] + k_4 * [PLC *] - k_7 * [GGDP] * G\beta\gamma$$
$$\frac{d[PLC *]}{dt} = k_6 * PLC * [GGTP] - k_4 * [PLC *]$$

(4) Receptor Phosphorylation Dynamics

$$\frac{d[LRp]}{dt} = k_{grk1f} * [LR] - k_{grk1r} * [LRp] + k_{grk2r} * [Rp] - k_{grk2f} * [LRp]$$
$$\frac{d[Rp]}{dt} = -k_{grk2r} * [Rp] + k_{grk2f} * [LRp] - k_{grk3r} * [Rp]$$
$$\frac{d[Rrec]}{dt} = k_{grk2r} * [Rp] - k_{1L} * L * [Rrec]$$

Model Parameters:

Parameter	Description	Value
K3k	Half-activation constant of IP3K	0.465 μM
k5p	IP3 dephosphorylation rate constant	0.56 s ⁻¹
β	Ratio of effective volumes of the ER/cytosol	0.185
Kserca	Half-activation constant for SERCA pump	0.076 μM
Kpm	Half-activation constant for PMCA pump	0.076 μM
φ	Stimulation-dependent influx	0.0024 s ⁻¹
Ctot	Total Calcium concentration	2 μM
k2	Calcium leak	0.014 s ⁻¹
Ki	Calcium binding to inhibiting site	0.469 μM
Tr	Characteristic time of IP3r inactivation	7 s
k3k	IP3 phosphorylation rate constant	0
Kplc	Half-activation constant of PLC	0.213 μM
Vserca	Maximal SERCA pump rate	0.27 μM s ⁻¹

Vpm	Maximal PMCA pump rate	0.014 $\mu\text{M s}^{-1}$
v0	Basal calcium flux	0.0001 $\mu\text{M s}^{-1}$
ϵ	Calcium flux strength	5
k1	Maximal rate of calcium release	0.85 s^{-1}
Ka	Calcium binding to activating site	0.059 μM
Kp	IP3 binding	0.13 μM
basal	Basal IP3 production rate by PLC	0.3 $\mu\text{M s}^{-1}$
k1L	Ligand-receptor association rate constant	2.3 $\mu\text{M}^{-1} \text{s}^{-1}$
k2L	Ligand-receptor dissociation rate constant	0.07 s^{-1}
k3	Basal exchange rate of GTP for GDP on G α subunit	0.008 s^{-1}
k4	Rate constant for hydrolysis of G α GTP to G α GDP	2 s^{-1}
k5	Encounter rate constant for ligand-receptor complex and G-protein	2*10 ⁻⁵ s^{-1}
k6	Encounter rate constant for PLC and G α GTP	2*10 ⁻⁵ s^{-1}
k7	Encounter rate constant for $\beta\gamma$ and G α GDP	1*10 ⁻⁵ s^{-1}
Rtot	Receptor total	0.068 μM
Gtot	G-protein total	0.2 μM
PLCtot	PLC total	0.1 μM
kgrk1f	GRK-mediated receptor phosphorylation rate constant	0.0324 s^{-1}
kgrk1r	Receptor dephosphorylation rate constant	6*10 ⁻⁴ s^{-1}
kgrk2f	Ligand dissociation rate constant with phosphorylated receptor	0.0919 s^{-1}
kgrk2r	Ligand association rate constant with phosphorylated receptor	1*10 ⁻⁴ s^{-1}
kgrk3r	Receptor dephosphorylation rate constant without ligand	0.007 s^{-1}

Model Schematic:

