

# Restriction of CaCO<sub>3</sub> polymorph by NH $\cdots$ O hydrogen-bonded poly(methacryloylaminocarboxylate) ligands; induced polymorph change by strength and/or formation manner of hydrogen bond

*Kazuyuki Takahashi, Atsuko Kobayashi, Mototsugu Doi, Seizi Adachi, Takahisa Taguchi, Taka-aki Okamura, Hitoshi Yamamoto, and Norikazu Ueyama*

## Experimental Section

**Materials.** Triphenylacetic acid was obtained from Sigma-Aldrich Co. Other reagents were commercially obtained and solvents were used after distillation. All synthetic procedures were performed under Ar atmosphere.

**3-Methyl-2-(methacryloylamino)-butyric Acid 2-Oxo-2-phenyl-ethyl Ester (MA-Val-OPac).** H-Val-OPac $\cdot$ HCl (3.0 g, 11 mmol) and triethylamine (3.06 mL, 22 mmol) in 40 mL of CH<sub>2</sub>Cl<sub>2</sub> was added methacryloyl chloride (1.08 mL, 11 mmol) dropwise on ice-water bath with shade and stirred at room temperature. After 12 hours, the solution was washed with pure water (1 time), 3.5% HCl aqueous solution (1 time), pure water (1 time) and 4% NaHCO<sub>3</sub> aqueous solution (3 times), respectively. The organic layer was dried over Na<sub>2</sub>SO<sub>4</sub> and concentrated to give an orange powder. Yield, 51%. m.p. = 334 K ~ 336 K. <sup>1</sup>H NMR (303 K, chloroform-*d*);  $\delta$  7.91 (2H, d, *o*-CH), 7.62 (1H, t, *p*-CH), 7.50 (2H, t, *m*-CH), 6.29 (1H, d, NH), 5.76 (1H, t, *trans*-CH), 5.53 (1H, d, CH<sub>2</sub>), 5.39 (1H, m, *cis*-CH), 5.28 (1H, d, CH<sub>2</sub>), 4.80 (1H, d, Val  $\alpha$ -CH), 2.41 (1H, m, Val  $\beta$ -CH), 2.00 (3H, d, CH<sub>3</sub>), 1.08 (6H, d, Val CH<sub>3</sub>). Anal Calcd for C<sub>17</sub>H<sub>21</sub>N<sub>1</sub>O<sub>4</sub>: C, 67.31; H, 6.98; N, 4.62. Found: C, 67.14; H, 6.98; N, 4.61.

**Poly(MA-Val-OPac).** <sup>1</sup>H NMR (303 K, chloroform-*d*);  $\delta$  7.85 (2H, br, *o*-CH), 7.57 (1H, br, *p*-CH), 7.45 (2H, br, *m*-CH), 6.39 (1H, br, NH), 5.48 (1H, br, Pac-CH<sub>2</sub>), 5.10 (1H, br, Pac-CH<sub>2</sub>), 4.40 (1H, br, Val  $\alpha$ -CH), 2.17 (1H, br, Val  $\beta$ -CH), 1.74 (2H, br, CH<sub>2</sub>), 0.95 (9H, br, Val CH<sub>3</sub> and CH<sub>3</sub>).

**Poly(MA-Val-OH) (1H).** <sup>1</sup>H NMR (303 K, Me<sub>2</sub>SO-*d*<sub>6</sub>); δ 12.8 (1H, br, COOH), 5.40 (1H, br, NH), 4.05 (1H, br, Val α-CH), 1.90 (1H, br, Val β-CH), 1.23 (2H, br, CH<sub>2</sub>), 0.87 (9H, br, CH<sub>3</sub>).

**3-(Methacryloylamino)-propionic Acid Benzyl Ester (MA-β-Ala-OBzl).** H-β-Ala-OBzl•*p*-tosylate (5.00 g, 14 mmol) and triethylamine (3.96 mL, 28 mmol) in 100 mL of CH<sub>2</sub>Cl<sub>2</sub> was added methacryloyl chloride (1.39 mL, 14 mmol) dropwise on an ice-water bath and stirred at room temperature and kept out of direct sunlight. After 12 hours, the solution was washed with 3.5% HCl aqueous solution (1 time), pure water (1 time) and 4% NaHCO<sub>3</sub> aqueous solution (3 times), respectively. The organic layer was dried over Na<sub>2</sub>SO<sub>4</sub> and concentrated to give a yellow solution. Yield, 2.48 g (71%). <sup>1</sup>H NMR (303 K, chloroform-*d*): δ 7.39-7.31 (5H, m, phenyl), 6.39 (1H, br, NH), 5.63 (1H, t, *trans*-CH), 5.30 (1H, m, *cis*-CH), 5.15 (2H, s, CH<sub>2</sub>), 3.60 (2H, q, H<sup>β</sup>), 2.63 (2H, t, H<sup>α</sup>), 1.92 (3H, t, CH<sub>3</sub>).

**Poly(MA-β-Ala-OBzl).** <sup>1</sup>H NMR (303 K, chloroform-*d*): δ 7.30 (5H, br, phenyl), 6.36 (1H, br, NH), 5.09 (2H, br, CH<sub>2</sub>), 3.34 (2H, br, H<sup>β</sup>), 2.52 (2H, br, H<sup>α</sup>), 1.79-1.65 (2H, br, CH<sub>2</sub>), 0.92 (3H, br, CH<sub>3</sub>). <sup>1</sup>H NMR (303 K, Me<sub>2</sub>SO-*d*<sub>6</sub>): δ 7.29 (6H, br, Ar and NH), 5.03 (2H, br, Bzl-CH<sub>2</sub>), 3.18 (2H, br, H<sup>β</sup>), 2.49 (2H, br, H<sup>α</sup>), 1.61 (2H, br, CH<sub>2</sub>), 0.89-0.75 (3H, br, CH<sub>3</sub>).

**Poly(MA-β-Ala-OH) (2H).** <sup>1</sup>H NMR (303 K, Me<sub>2</sub>SO-*d*<sub>6</sub>): δ 12.1 (1H, br, COOH), 7.40 (1H, br, NH), 3.15 (2H, br, H<sup>β</sup>), 2.44 (2H, br, H<sup>α</sup>), 1.55 (2H, br, CH<sub>2</sub>), 0.88-0.72 (3H, br, CH<sub>3</sub>).

**4-(Methacryloylamino)-butyric Acid Benzyl Ester (MA-γ-Abu-O'Bu).** H-γ-Abu-O'Bu•HCl (1.00 g, 3.8 mmol) and triethylamine (1.06 mL, 7.6 mmol) in 100 mL of CH<sub>2</sub>Cl<sub>2</sub> was added methacryloyl chloride (0.370 mL, 3.8 mmol) dropwise on an ice-water bath and stirred at room temperature and kept out of direct sunlight. After 12 hours, the solution was washed with 3.5% HCl aqueous solution (1 time), pure water (1 time) and 4% NaHCO<sub>3</sub> aqueous solution (3 times), respectively. The organic layer was dried over Na<sub>2</sub>SO<sub>4</sub> and concentrated to give a yellow solution. Yield, 830 mg (71%). <sup>1</sup>H NMR (303 K, chloroform-*d*): δ 6.75 (1H, br, NH), 5.62 (1H, s, *trans*-CH), 5.22 (1H, s, *cis*-CH), 3.25 (2H, q, H<sup>γ</sup>), 2.21 (2H, t, H<sup>α</sup>), 1.67 (3H, s, CH<sub>3</sub>), 1.76 (2H, m, H<sup>β</sup>), 1.36 (9H, s, <sup>t</sup>Bu).

**Poly(MA- $\gamma$ -Abu-O'Bu).**  $^1\text{H}$  NMR (303 K, chloroform-*d*):  $\delta$  6.13 (1H, br, NH), 3.14 (2H, br, H $^\gamma$ ), 2.27 (2H, br, H $^\alpha$ ), 1.77 (2H, br, H $^\beta$ ), 1.45 (9H, br,  $^t\text{Bu}$ ), 1.53 (2H, br, CH $_2$ ), 1.2-0.9 (3H, br, CH $_3$ ).  $^1\text{H}$  NMR (303 K, Me $_2\text{SO}-d_6$ ):  $\delta$  7.24 (1H, br, NH), 3.26 (2H, br, H $^\gamma$ ), 2.92 (2H, br, H $^\alpha$ ), 2.15 (2H, br, H $^\beta$ ), 1.59 (2H, br, CH $_2$ ), 1.39 (9H, s,  $^t\text{Bu}-\text{CH}_3$ ), 0.91-0.76 (3H, br, CH $_3$ ).

**Poly(MA- $\gamma$ -Abu-OH) (3H).**  $^1\text{H}$  NMR (303 K, Me $_2\text{SO}-d_6$ ):  $\delta$  12.0 (1H, br, COOH), 7.28 (1H, br, NH), 3.58 (2H, br, H $^\gamma$ ), 2.93 (2H, br, H $^\alpha$ ), 2.18 (2H, br, H $^\beta$ ), 1.61 (2H, br, CH $_2$ ), 0.91-0.77 (3H, br, CH $_3$ ).

**Isotactic-rich Poly(MA- $\beta$ -Ala-OBzl).**  $^1\text{H}$  NMR (303 K, chloroform-*d*):  $\delta$  7.35-7.26 (5H, br, phenyl), 6.90 (1H, br, NH), 5.09 (2H, br, CH $_2$ ), 3.34 (2H, br, H $^\beta$ ), 2.52 (2H, br, H $^\alpha$ ), 1.8-1.6 (2H, br, CH $_2$ ), 1.3-0.8 (3H, br, CH $_3$ ).

**Isotactic-rich Poly(MA- $\beta$ -Ala-OH) ( $2^{iso}\text{H}$ ).**  $^1\text{H}$  NMR (303 K, Me $_2\text{SO}-d_6$ ):  $\delta$  12.1 (1H, br, COOH), 7.30 (1H, br, NH), 3.14 (2H, br, H $^\beta$ ), 2.38 (2H, br, H $^\alpha$ ), 1.87-1.74 (2H, br, CH $_2$ ), 1.50-0.86 (3H, br, CH $_3$ ).

**Triphenylacetyl chloride.** Triphenylacetic acid (5.0 g, 17.3 mmol) in 4.1 mL of thionyl chloride (51.9 mmol) was stirred at 363 K. After 2 hours, the solution was concentrated to give yellow powder. Yield, 5.3 g (~ 100%).  $^1\text{H}$  NMR (303 K, chloroform-*d*):  $\delta$  7.37-7.26 (15H, m, Ar).

**3-Methyl-2-(2,2,2-triphenyl-acetylamino)-butyric Acid Benzyl Ester (Ph $_3\text{CCO}-\text{Val}-\text{OBzl}$ ).** H-Val-OBzl $\cdot\text{HCl}$  (795 mg, 3.3 mmol) in 10 mL of CH $_2\text{Cl}_2$  was added triethylamine (0.90 mL, 6.6 mmol) and the solution was stirred. The solution was added triphenylacetyl chloride (1.0 g, 3.3 mmol) in 10 mL of CH $_2\text{Cl}_2$  on an ice-water bath and stirred at room temperature. After 12 hours, the solution was washed with pure water, 3.5% HCl *aq.*, 4% NaHCO $_3$  *aq.* and conc. NaCl *aq.*, respectively, and dried with Na $_2\text{SO}_4$ . The organic layer was concentrated to give a yellow powder and the obtained powder was dried over P $_2\text{O}_5$  under reduced pressure. Yield, 635 mg (40%).  $^1\text{H}$  NMR (303 K, chloroform-*d*):  $\delta$  7.34-7.23 (20H, m, Ar), 6.18 (1H, d, NH), 5.14 (2H, dd, Bzl-CH $_2$ ), 4.65 (1H, dd, H $^\alpha$ ), 2.15 (1H, m, H $^\beta$ ), 0.81 and 0.63 (6H, d, H $^\gamma$ ).

**3-Methyl-2-(2,2,2-triphenyl-acetylamino)-butyric Acid (4H).** Ph<sub>3</sub>CCO-Val-OBzl (635 mg, 1.33 mmol) in 50 mL of MeOH was stirred under Ar atmosphere during 30 minutes, and the solution was added Pd-C (64 mg) and stirred under Ar atmosphere. After 30 minutes, H<sub>2</sub> gas was bubbled to the solution for 4 hours and the solution was filtrated to remove Pd. The mother liquor was concentrated and the residue was suspended to ether. The solution was concentrated and added *n*-hexane to give white powder. The powder was collected by filtration and dried over P<sub>2</sub>O<sub>5</sub> under reduced pressure. Yield, 222 mg (43%). M.p. = 399 ~ 401 K. <sup>1</sup>H NMR (303 K, chloroform-*d*): δ 7.30-7.23 (15H, m, Ar), 6.22 (1H, d, NH), 4.45 (1H, d, H<sup>α</sup>), 2.17 (1H, m, H<sup>β</sup>), 0.88 and 0.69 (6H, d, H<sup>γ</sup>). FT-IR (10 mM, in chloroform-*d*, at r.t.): ν(NH) = 3435 cm<sup>-1</sup>, ν(CO) = 1755 and 1672 cm<sup>-1</sup> (COOH and CONH, respectively). Anal. Calcd for C<sub>25</sub>H<sub>25</sub>NO<sub>3</sub>: C, 77.49; H, 6.50; N, 3.61. Found: C, 76.66; H, 6.51; N, 3.63.

**Tetramethylammonium 3-Methyl-2-(2,2,2-triphenyl-acetylamino)-butyrate (4NMe<sub>4</sub>).** 4H (100 mg, 258 μmol) in 5 mL of MeOH was added 25 % NMe<sub>4</sub>OH methanol solution (108.8 μL, 258 μmol) and the mixed solution was stirred for several minutes. The solution was concentrated and the residue was washed with ether to give a white powder. <sup>1</sup>H NMR (303 K, chloroform-*d*): δ 7.37-7.20 (15H, m, Ar), 6.64 (1H, d, NH), 4.26 (1H, d, H<sup>α</sup>), 2.26 (1H, m, H<sup>β</sup>), 0.93 and 0.77 (6H, d, H<sup>γ</sup>). FT-IR (10 mM, in chloroform-*d*, at r.t.): ν(NH) = 3377 cm<sup>-1</sup>, ν(CO) = 1597 and 1652 cm<sup>-1</sup> (COO<sup>-</sup> and CONH, respectively).

**3-(2,2,2-Triphenyl-acetylamino)-propionic Acid Benzyl Ester (Ph<sub>3</sub>CCO-β-Ala-OBzl).** H-β-Ala-OBzl•*p*-tosylate (573 mg, 1.63 mmol) in 10 mL of CH<sub>2</sub>Cl<sub>2</sub> was added triethylamine (0.454 mL, 3.26 mmol) and the mixed solution was stirred. The solution was added triphenylacetyl chloride (500 mg, 1.63 mmol) in 10 mL of CH<sub>2</sub>Cl<sub>2</sub> on an ice-water bath and stirred at room temperature. After 12 hours, the solution was washed with pure water, 3.5% HCl *aq.*, 4% NaHCO<sub>3</sub> *aq.* and conc. NaCl *aq.*, respectively, and dried with Na<sub>2</sub>SO<sub>4</sub>. The organic layer was concentrated and the residue was suspended to ether. The solution was concentrated and added *n*-hexane to give a white powder. The

obtained powder was collected by filtration and dried over P<sub>2</sub>O<sub>5</sub> under reduced pressure. Yield, 281 mg (38%). <sup>1</sup>H NMR (303 K, chloroform-*d*): δ 7.34-7.20 (20H, m, Ar), 6.26 (1H, br, NH), 5.03 (2H, s, Bzl-CH<sub>2</sub>), 3.59 (2H, q, H<sup>β</sup>), 2.58 (2H, t, H<sup>α</sup>).

**3-(2,2,2-Triphenyl-acetylamino)-propionic Acid (5H).** Ph<sub>3</sub>CCO-β-Ala-OBzl (281 mg, 647 μmol) in 5 mL of hot EtOH was added NaOH (40.0 mg, 1.00 mmol) in 2 mL aqueous solution. The solution was stirred at 353 K during a day and concentrated to remove EtOH. The residue was suspended to a pure water and the solution was stirred at 353 K. After a day, 3.5% HCl *aq.* was added to the solution to give white powder, and the powder was collected by filtration and dried over P<sub>2</sub>O<sub>5</sub> under reduced pressure. Yield, 200 mg (86%). M.p. = 441 ~ 443 K. <sup>1</sup>H NMR (303 K, chloroform-*d*): δ 7.31-7.22 (15H, m, Ar), 6.31 (1H, br, NH), 3.59 (2H, m, H<sup>β</sup>), 2.60 (2H, t, H<sup>α</sup>). FT-IR (10 mM, in chloroform-*d*, at r.t.): ν(NH) = 3437 cm<sup>-1</sup>, ν(CO) = 1749 and 1663 cm<sup>-1</sup> (COOH and CONH, respectively). Anal. Calcd for C<sub>23</sub>H<sub>21</sub>NO<sub>3</sub>: C, 76.86; H, 5.89; N, 3.90. Found: C, 75.67; H, 5.81; N, 3.92.

**Tetramethylammonium 3-(2,2,2-Triphenyl-acetylamino)-propionate (5NMe<sub>4</sub>).** 5H (100 mg, 278 μmol) in 5 mL of MeOH was added 25% NMe<sub>4</sub>OH methanol solution (117.2 μL, 278 μmol) and the mixed solution was stirred for several minutes. The solution was concentrated and the residue was washed with ether to give a white powder. The powder was crystallized with the mixed solution of MeCN and ether. <sup>1</sup>H NMR (303 K, chloroform-*d*): δ 7.32-7.18 (15H, m, Ar), 7.07 (1H, br, NH), 3.57 (2H, m, H<sup>β</sup>), 2.32 (2H, t, H<sup>α</sup>). FT-IR (10 mM, in chloroform-*d*, at r.t.): ν(NH) = 3019 cm<sup>-1</sup>, ν(CO) = 1578 and 1653 cm<sup>-1</sup> (COO<sup>-</sup> and CONH, respectively).

**4-(2,2,2-Triphenyl-acetylamino)-butyric Acid Benzyl Ester (Ph<sub>3</sub>CCO-γ-Abu-OBzl).** H-γ-Val-OBzl•*p*-tosylate (1.00 g, 3.26 mmol) in 10 mL of CH<sub>2</sub>Cl<sub>2</sub> was added triethylamine (0.91 mL, 6.52 mmol) and the solution was stirred. The solution was added triphenylacetyl chloride (1.19 g, 3.26 mmol) in 10 mL of CH<sub>2</sub>Cl<sub>2</sub> on an ice-water bath and stirred at room temperature. After 12 hours, the solution was washed with pure water, 3.5% HCl *aq.*, 4 % NaHCO<sub>3</sub> *aq.* and conc. NaCl *aq.*, respectively, and dried with Na<sub>2</sub>SO<sub>4</sub>. The organic layer was concentrated to give a white powder and the obtained

powder was dried over P<sub>2</sub>O<sub>5</sub> under reduced pressure. Yield, 536 mg (35%). <sup>1</sup>H NMR (303 K, chloroform-*d*): δ 7.29-7.14 (20H, m, Ar), 5.80 (1H, br, NH), 4.99 (2H, s, Bzl-CH<sub>2</sub>), 3.28 (2H, m, H<sup>γ</sup>), 2.21 (2H, t, H<sup>α</sup>), 1.73 (2H, m, H<sup>β</sup>).

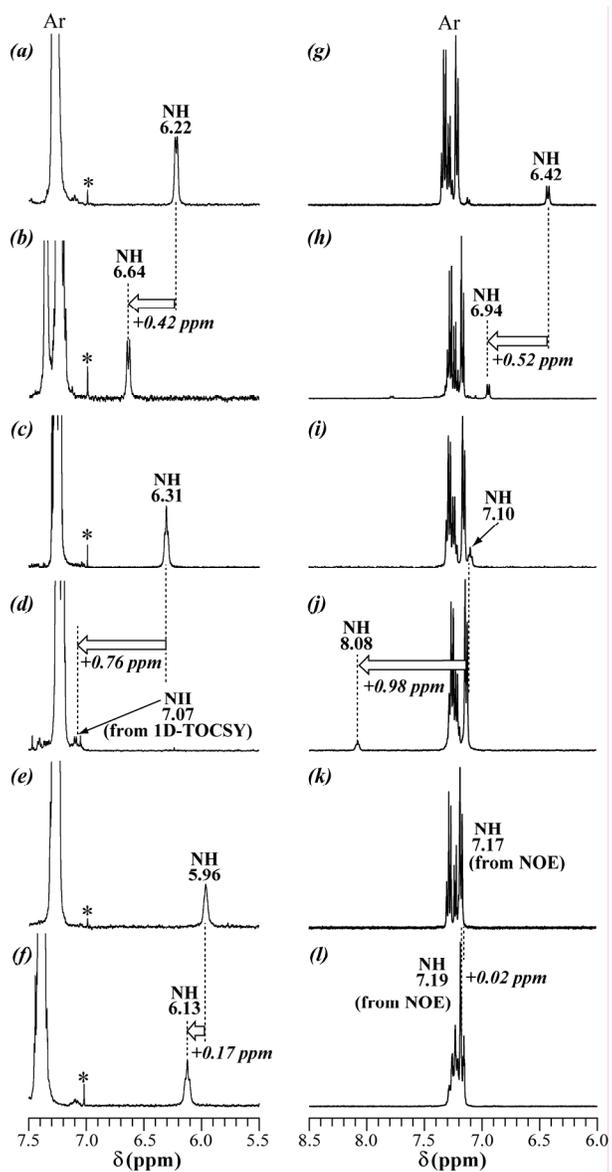
**4-(2,2,2-Triphenyl-acetylamino)-butyric Acid (6H).** Ph<sub>3</sub>CCO-γ-Abu-OBzl (528 mg, 1.14 mmol) in 10 mL of MeOH was added 1 M NaOH *aq.* (1.2 mL, 1.20 mmol) and the solution was stirred at 313 K. After 12 hours, the solution was concentrated to remove MeOH and the residue was added 3.5% HCl *aq.* to give a white powder. The white powder was collected by filtration and washed with pure water, and dried over P<sub>2</sub>O<sub>5</sub> under reduced pressure. Yield, 381 mg (89%). M.p. = 433 ~ 437 K. <sup>1</sup>H NMR spectra (303 K, chloroform-*d*): δ 9.62 (1H, br, COOH), 7.32-7.23 (15H, m, Ar), 5.94 (1H, br, NH), 3.39 (2H, m, H<sup>γ</sup>), 2.27 (2H, t, H<sup>α</sup>), 1.79 (2H, m, H<sup>β</sup>). FT-IR (10 mM, in chloroform-*d*, at r.t.): ν(NH) = 3435 cm<sup>-1</sup>, ν(CO) = 1746 and 1664 cm<sup>-1</sup> (COOH and CONH, respectively). Anal. Calcd for C<sub>24</sub>H<sub>23</sub>NO<sub>3</sub>: C, 77.19; H, 6.21; N, 3.75. Found: C, 77.26; H, 6.11; N, 3.48.

**Tetramethylammonium 4-(2,2,2-Triphenyl-acetylamino)-butyrate (6NMe<sub>4</sub>).** **6H** (100 mg, 268 μmol) in 5 mL of MeOH was added 25% NMe<sub>4</sub>OH methanol solution (112.8 μL, 268 μmol) and the mixed solution was stirred for several minutes. The solution was concentrated and the residue was washed with ether to give a white powder. <sup>1</sup>H NMR spectra (303 K, chloroform-*d*): δ 7.46-7.34 (15H, m, Ar), 6.13 (1H, br, NH), 2.30 (2H, m, H<sup>γ</sup>), 1.89 (2H, t, H<sup>α</sup>), 1.03 (2H, m, H<sup>β</sup>). FT-IR (10 mM, in chloroform-*d*, at r.t.): ν(NH) = 3011 cm<sup>-1</sup>, ν(CO) = 1570 and 1656 cm<sup>-1</sup> (COO<sup>-</sup> and CONH, respectively).

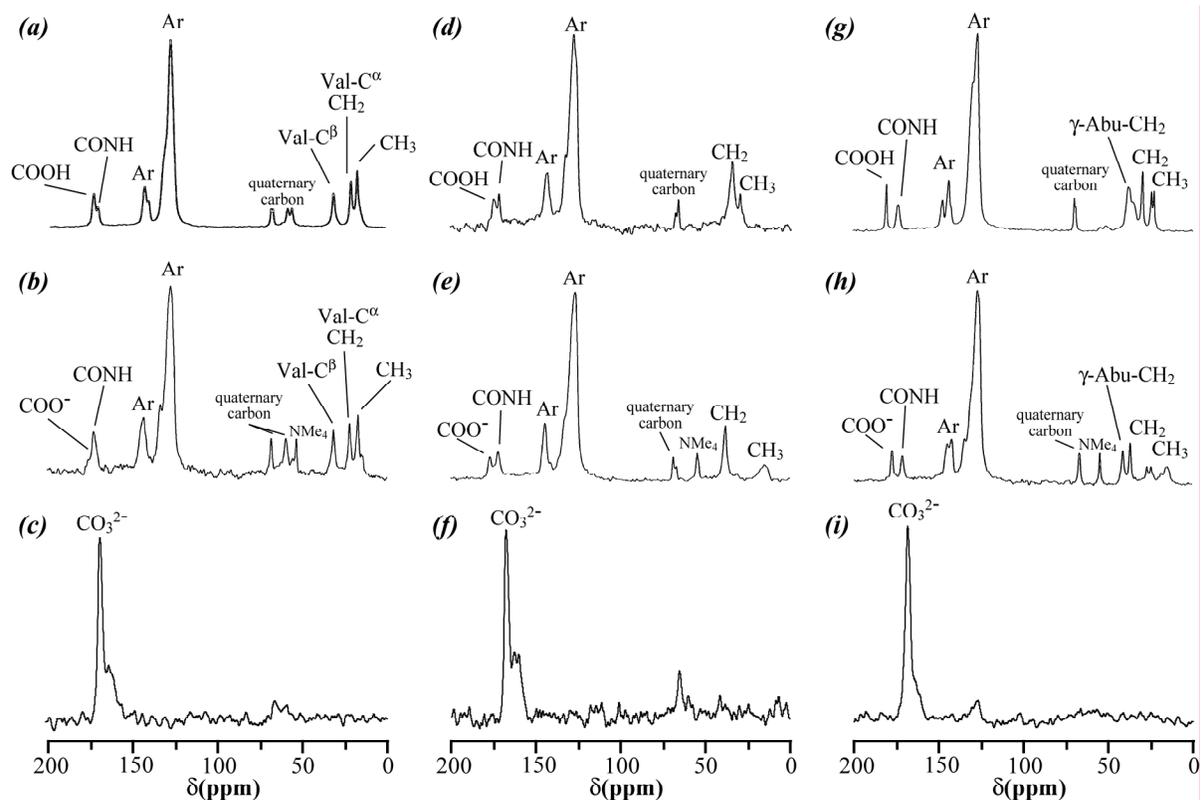
**Deuteration of Amide Proton of 5NMe<sub>4</sub> and 6NMe<sub>4</sub> (7 and 8, respectively).** The deuteration of the amide NH of **5NMe<sub>4</sub>** was performed by an exchange reaction with methanol-*d*<sub>1</sub> (CH<sub>3</sub>OD). Tetramethylammonium 3-(2,2,2-triphenyl-*N*-deuterium-acetylamino)-propionate (**7**) was obtained as white powder by concentration of the CH<sub>3</sub>OD solution of **6NMe<sub>4</sub>**. Tetramethylammonium 4-(2,2,2-triphenyl-*N*-deuterium-acetylamino)-butyrate (**8**) was prepared by the same procedure.

### **Crystallization of CaCO<sub>3</sub> Composites in the Presence of Model Carboxylate Ligands.**

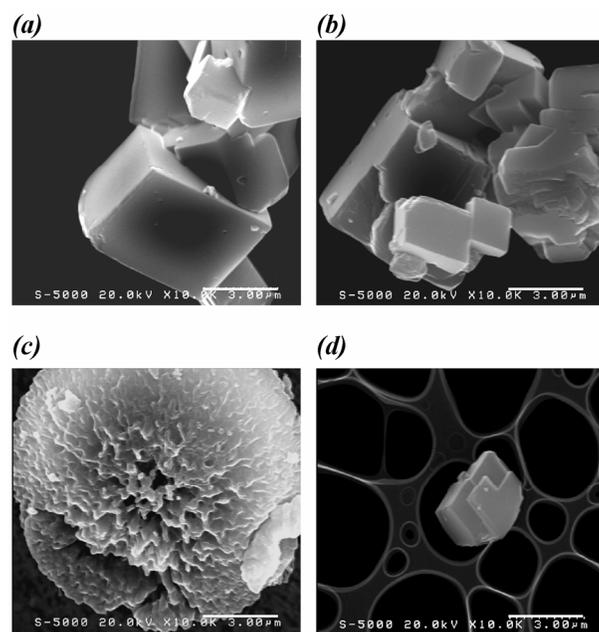
Crystalline model ligand–CaCO<sub>3</sub> composites were obtained by the same procedures in the case of polymer ligands.



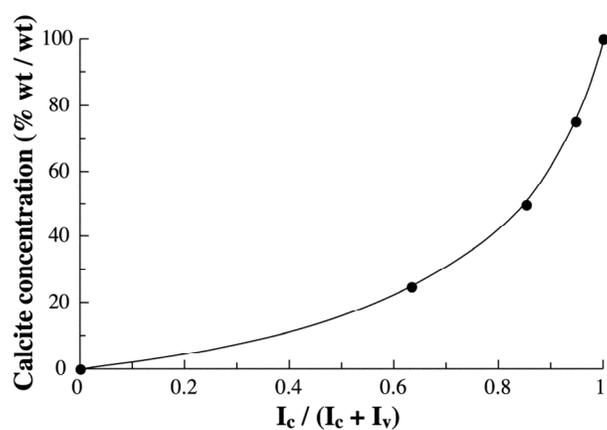
**Fig. S1.** <sup>1</sup>H NMR spectra of (a) 4H, (b) 4NMe<sub>4</sub>, (c) 5H, (d) 5NMe<sub>4</sub>, (e) 6H, and (f) 6NMe<sub>4</sub> (303 K, chloroform-*d*), and (g) 4H, (h) 4NMe<sub>4</sub>, (i) 5H, (j) 5NMe<sub>4</sub>, (k) 6H, and (l) 6NMe<sub>4</sub> (303 K, Me<sub>2</sub>SO-*d*<sub>6</sub>).



**Fig. S2.** Solid-state  $^{13}\text{C}$  CP/MAS NMR spectra of (a) **4H**, (b) **4NMe<sub>4</sub>**, (c)  $\text{CaCO}_3$  composite in the presence of **4**, (d) **5H**, (e) **5NMe<sub>4</sub>**, (f)  $\text{CaCO}_3$  composite in the presence of **5**, (g) **6H**, (h) **6NMe<sub>4</sub>**, and (i)  $\text{CaCO}_3$  composite in the presence of **6**. The model ligands were easily dislodged from  $\text{CaCO}_3$  crystal during the washing process. The spectra in (c), (f), and (i) were obtained after the washing process.



**Fig. S3.** FE/SEM images of (a)  $\text{CaCO}_3$  composite in the presence of **4**, (b)  $\text{CaCO}_3$  composite in the presence of **5**, (c)  $\text{CaCO}_3$  composite in the presence of **6**, and (d)  $\text{CaCO}_3$  composite in the absence of model ligands. The model ligands were easily dislodged from  $\text{CaCO}_3$  crystal during the washing process. These images were obtained after the washing process (20 kV acceleration voltage,  $\times 10,000$ ). The scale bars in these images show 3  $\mu\text{m}$ .



**Fig. S4.** A calibration curve for determining the component ratio of calcite and vaterite by the XRD analysis. The calcite content is plotted as a function of the relative intensity  $I_c/(I_c + I_v)$  between the (104) calcite peak,  $I_c$ , and the (101) vaterite peak,  $I_v$ .