Electronic Supplementary Information

Table S1. Potential parameters used in this work.

Charges (e)			Core-shell interaction			
			$(eVÅ^{-2})$			
Ion	Core	Shell				
Si	+4.00000					
0	+0.84819	-2.84819	74.92038			
Li	+1.00000					
K	+1.00000					
Rb	+1.00000					
Cs	+1.00000					
	Buckingh	am Potential				
Inter-molecular	A (eV)	ρ (Å)	$C (eVÅ^6)$			
Si^{4+} - O^{2-} [ref 20]	1283.91	0.32052	10.66158			
$O^{2-} - O^{2-}$ [ref 20]	22764.0	0.14900	27.88			
$Li^{+} - O^{2-}$ [ref 24]	262.54	0.3476	0.0			
$Na^{+} - O^{2-} [ref 24]$	1266.84	0.3065	0.0			
$K^{+} - O^{2-}$ [ref 24]	680.4384	0.3798	0.0			
$Rb^{+} - O^{2-} [ref 24]$	919.38	0.3772	0.0			
$Cs^{+} - O^{2-} [ref 24]$	649.60	0.4142	64.3395			
Three-body Potential						
	K (eV	rad ⁻²)	Θ_0			
O_{shell}^{2} - Si - O_{shell}^{2}	2.09	109.470000				
[ref 20]						

Based on Li ₈ Si ₈ O ₂₀									
Content of guest ions %	0	0.12	0.25	0.37	0.5	0.62	0.75	0.87	1
Number of configurations	1	1	7	7	14	7	7	1	1
Based on K ₄ Li ₄ Si ₈ O ₂₀ *									
Content of guest ions %		0	0.2	5	0.5		0.75		1.0
Number of configurations	1		1 3			1		1	
Based on M ₄ Li ₄ Si ₈ O ₂₀ or K ₄ M ₄ Si ₈ O ₂₀									
Content of guest ions %		0	0.2	5	0.5		0.75		1.0
Number of configurations	22	2	14		10		2		1

Table S2. Number of non-identical configurations for each composition of the different solid solutions.

* Guest ions replace K or Li where the other host ion is kept in situ.

Table S3. Ionic radii of alkali ions in this study.

Ion	Li ⁺	Na ⁺	K^+	Rb^+	Cs^+
Ionic radius (Å) [ref 31]	0.68	0.97	1.33	1.47	1.67

Table S4. Comparison of lattice parameters of optimized $KLi_{(1-x)}M_xSi_2O_5$ or $K_{(1-x)}M_xLiSi_2O_5$ structures with those of a pure $KLiSi_2O_5$.

(a) The lattice parameters of optimized K₄Li₄Si₈O₂₀

Compound	Lattice parameters (Å)						
Compound	а	b	С	α	β	γ	
$K_4Li_4Si_8O_{20}$	6.44	4.99	16.94	90.00°	94.83°	90.00°	

(b) Replace Li by a guest ion

Compound	Lattice parameters (Å)					
Compound	а	b	С	α	β	γ
$K_4Li_3Na_1Si_8O_{20}$	6.56	5.01	17.06	90.43°	93.93	88.73°
$K_4Li_2Na_2Si_8O_{20}$	6.69	5.01	17.21	90.78°	93.55	87.06°
$K_4Li_1Na_3Si_8O_{20}$	6.77	5.03	17.19	90.24°	90.87	88.50°
Na ₄ K ₄ Si ₈ O ₂₀	6.87	5.05	17.27	90.00	89.00	90.00°
$K_4Li_3Rb_1Si_8O_{20}$	6.68	5.10	17.02	90.84°	91.57	88.25°
$K_4Li_2Rb_2Si_8O_{20}$	7.26	5.13	16.86	90.00°	80.92	90.00°
K4LiRb3Si8O20	7.89	5.13	17.66	90.88°	98.43	110.00°
$K_4Rb_4Si_8O_{20}$	8.26	5.14	17.80	90.00°	100.3°	108.12°
K4Li3CsSi8O20	6.70	5.02	17.43	91.21°	101.38°	90.82°
$K_4Li_2Cs_2Si_8O_{20}$	7.44	5.02	17.39	90.00°	90.01°	90.00°
K4LiCs3Si8O20	8.12	5.14	17.35	90.72°	78.48°	89.14°
$K_4Cs_4Si_8O_{20}$	8.32	5.16	17.86	90.00°	100.3	71.90°

(c) Replace K by a guest ion

Compound	Lattice parameters (Å)						
Compound	а	b	С	α	β	γ	
K ₃ Na Li ₄ Si ₈ O ₂₀	6.42	4.95	16.87	89.97°	95.43°	89.30°	
K ₂ Na ₂ Li ₄ Si ₈ O ₂₀	6.42	4.91	16.83	89.95°	96.58°	88.18°	
KNa ₃ Li ₄ Si ₈ O ₂₀	6.36	4.85	16.76	90.10°	95.60°	88.81°	
Na ₄ Li ₄ Si ₈ O ₂₀	6.23	4.82	17.17	90.00°	99.39°	90.00°	
K ₃ RbLi ₄ Si ₈ O ₂₀	6.46	5.01	16.99	90.04°	95.28°	90.18°	
K ₂ Rb ₂ Li ₄ Si ₈ O ₂₀	6.48	5.02	16.99	90.00°	95.19°	90.00°	
KRb ₃ Li ₄ Si ₈ O ₂₀	6.51	5.04	17.04	90.04°	95.72°	90.18°	
Rb ₄ Li ₄ Si ₈ O ₂₀	6.53	5.05	17.04	90.00°	95.72°	90.00°	

K ₃ CsLi ₄ Si ₈ O ₂₀	6.48	5.02	17.00	90.06°	95.37°	90.23°
$K_2Cs_2Li_4Si_8O_{20}$	6.52	5.04	17.00	90.00°	95.42°	90.00°
KCs3Li4Si8O20	6.56	5.06	17.06	90.06°	95.89°	90.23°
Cs4Li4Si8O20	6.59	5.07	17.07	90.00°	95.94°	90.00°